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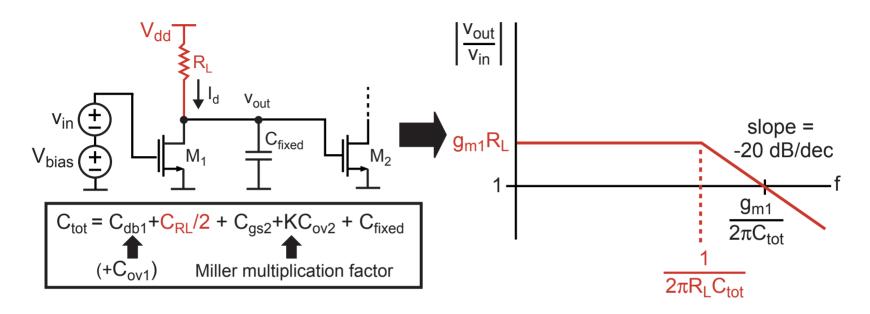
6.976
High Speed Communication Circuits and Systems
Lecture 6
Enhancement Techniques for Broadband Amplifiers,
Narrowband Amplifiers

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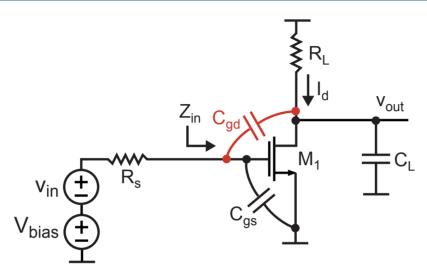
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Resistor Loaded Amplifier (Unsilicided Poly)



- We decided this was the fastest non-enhanced amplifier
 - Can we go faster? (i.e., can we enhance its bandwidth?)
- We will look at the following
 - Reduction of Miller effect on C_{gd}
 - Shunt, series, and zero peaking
 - Distributed amplification

Miller Effect on C_{ad} Is Significant



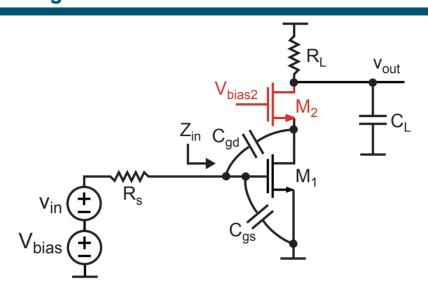
- C_{gd} is quite significant compared to C_{gs}
 - In 0.18 μ CMOS, C_{gd} is about 45% the value of C_{gs}
- Input capacitance calculation

$$Z_{in} \approx \frac{1}{s(C_{gs} + C_{gd}(1 - A_v))} = \frac{1}{sC_{gs}(1 + C_{gd}/C_{gs}(1 + g_m R_L))}$$

For 0.18 μ CMOS, gain of 3, input cap is almost tripled over C_{gs}! 1 1

 $Z_{in} \approx \frac{1}{sC_{gs}(1+0.45(4))} = \frac{1}{sC_{gs}2.8}$

Reduction of C_{ad} Impact Using a Cascode Device



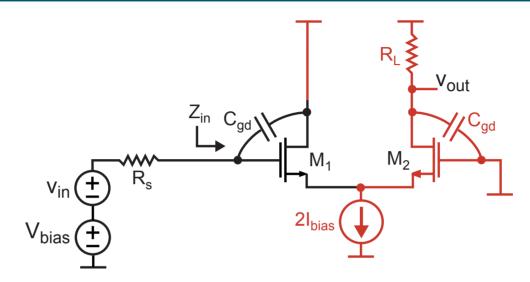
The cascode device lowers the gain seen by
$$C_{gd}$$
 of M_1 $A_v \to g_{m1} \frac{1}{g_{m2}} \approx 1 \ \Rightarrow \ Z_{in} \approx \frac{1}{sC_{gs}(1+C_{gd}/C_{gs}(2))}$

For 0.18m CMOS and gain of 3, impact of C_{qd} is reduced by 30%:

$$Z_{in} pprox rac{1}{sC_{qs}1.9}$$

Issue: cascoding lowers achievable voltage swing

Source-Coupled Amplifier



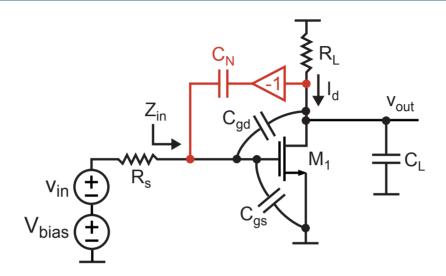
- Remove impact of Miller effect by sending signal through source node rather than drain node
 - C_{gd} not Miller multiplied AND impact of C_{gs} cut in half!

$$Z_{in} pprox rac{1}{s(C_{gs}/2 + C_{gd})} \Rightarrow Z_{in} pprox rac{1}{sC_{gs}0.95}$$
 (0.18 μ CMOS)

- The bad news
 - Signal has to go through source node (C_{sb} significant)
 - Power consumption doubled

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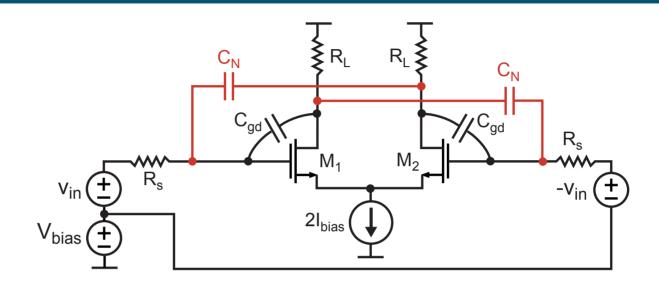
Neutralization



- Consider canceling the effect of C_{ad}
 - Choose $C_N = C_{gd}$
 - $\overline{}$ Charging of C_{gd} now provided by C_{N}
- Benefit: Impact of C_{gd} removed $\Rightarrow Z_{in} \approx \frac{1}{sC_{as}}$
- Issues:
 - How do we create the inverting amplifier?
 - What happens if C_N is not precisely matched to C_{gd} ?

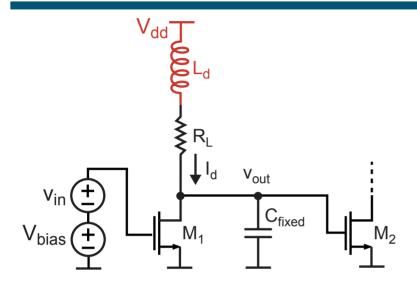
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Practical Implementation of Neutralization



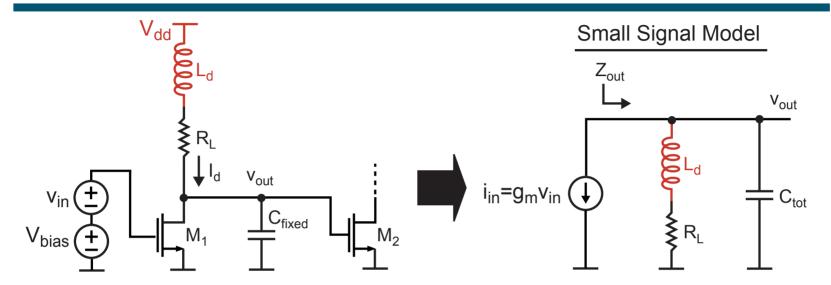
- Leverage differential signaling to create an inverted signal
- Only issue left is matching C_N to C_{gd}
 - Often use lateral metal caps for C_N (or CMOS transistor)
 - If C_N too low, residual influence of C_{gd}
 - If C_N too high, input impedance has inductive component
 - Causes peaking in frequency response
 - Often evaluate acceptable level of peaking using eye diagrams

Shunt-peaked Amplifier



- Use inductor in load to extend bandwidth
 - Often implemented as a spiral inductor
- We can view impact of inductor in both time and frequency
 - In frequency: peaking of frequency response
 - In time: delay of changing current in R_L
- Issue can we extend bandwidth without significant peaking?

Shunt-peaked Amplifier - Analysis



Expression for gain

$$A_v = g_m Z_{out} = g_m [(sL_d + R_L)||1/(sC_{tot})]$$

Parameterize with

$$= g_m R_L \frac{s(L_d/R_L) + 1}{s^2 L_d C_{tot} + s R_L C_{tot} + 1}$$

$$m = \frac{R_L C_{tot}}{ au}$$
, where $au = \frac{L_d}{R_L}$

Corresponds to ratio of RC to LR time constants

The Impact of Choosing Different Values of m – Part 1

Parameterized gain expression

$$A_v = g_m R_L \frac{\tau s + 1}{s^2 \tau^2 m + s \tau m + 1}$$

Small Signal Model

$$|A_v| = g_m R_L \left| \frac{jw/(w_1 m) + 1}{-(w/(w_1 m))^2 m + jw/(w_1 m)m + 1} \right|$$

define w_2 as new 3 dB frequency, note that w_1 is old one

$$\Rightarrow \left| \frac{jw_2/(w_1m) + 1}{-(w_2/(w_1m))^2m + jw_2/w_1 + 1} \right| = \frac{1}{\sqrt{2}}$$

Want to solve for w₂/w₄

The Impact of Choosing Different Values of m – Part 2

From previous slide, we have

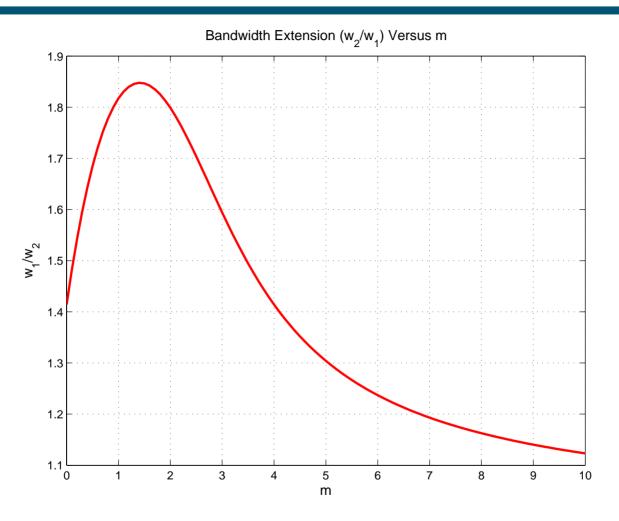
$$\left| \frac{jw_2/(w_1m) + 1}{-(w_2/(w_1m))^2m + jw_2/w_1 + 1} \right| = \frac{1}{\sqrt{2}}$$

After much algebra

$$\frac{w_2}{w_1} = \sqrt{\left(-\frac{m^2}{2} + m + 1\right) + \sqrt{\left(-\left(\frac{m^2}{2} + m + 1\right)^2 + m^2\right)^2}}$$

- We see that m directly sets the amount of bandwidth extension!
 - Once m is chosen, inductor value is $L_d = \frac{R_L^2 C_{tot}}{m}$

Plot of Bandwidth Extension Versus m



- Highest extension: $w_2/w_1 = 1.85$ at m ≈ 1.41
 - However, peaking occurs!

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Plot of Transfer Function Versus m

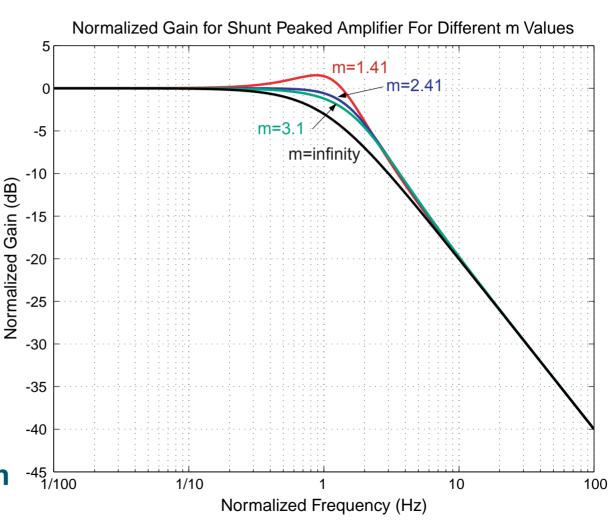
Maximum bandwidth: m = 1.41 (extension = 1.85)

Maximally flat response:m = 2.41 (extension = 1.72)

Best phase response:m = 3.1 (extension = 1.6)

No peaking:m = infinity

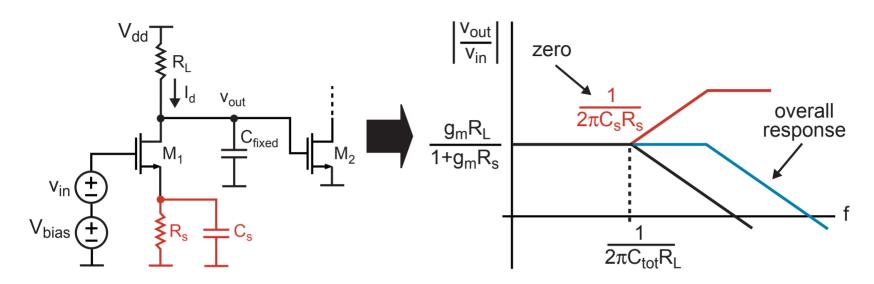
Eye diagrams often used to evaluate best m



To Do

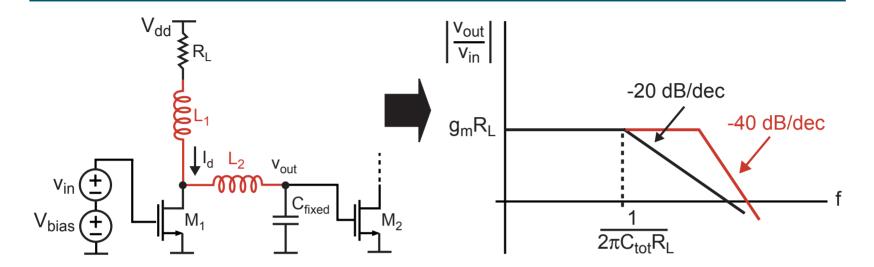
Add eye diagrams

Zero-peaked Common Source Amplifier



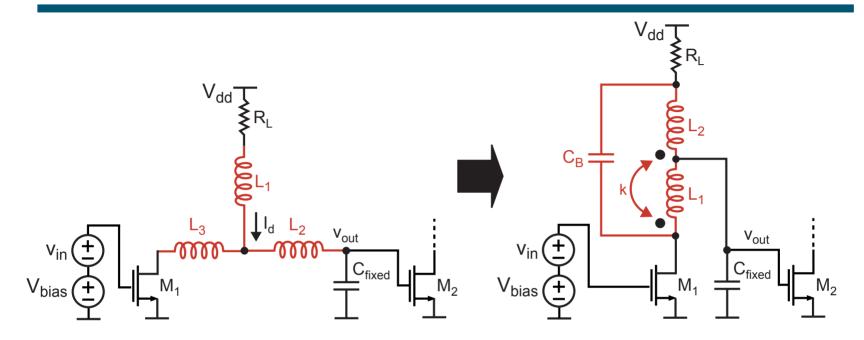
- Inductors are expensive with respect to die area
- We can instead achieve bandwidth extension with capacitor
 - Idea: degenerate gain at low frequencies, remove degeneration at higher frequencies (i.e., create a zero)
- Issues:
 - Must increase R₁ to keep same gain (lowers pole)
 - Lowers achievable gate voltage bias (lowers device f,)

Back to Inductors – Shunt and Series Peaking



- Combine shunt peaking with a series inductor
 - Bandwidth extension by converting to a second order filter response
 - Can be designed for proper peaking
- Increases delay of amplifier

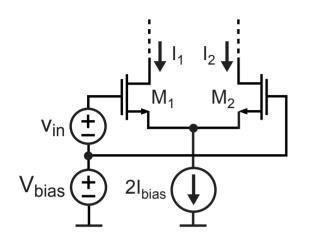
T-Coil Bandwidth Enhancement



- Uses coupled inductors to realize T inductor network
 - Works best if capacitance at drain of M₁ is much less than the capacitance being driven at the output load
- See Chap. 8 of Tom Lee's book (pp 187-191) for analysis
- See S. Galal, B. Ravazi, "10 Gb/s Limiting Amplifier and Laser/Modulator Driver in 0.18u CMOS", ISSCC 2003, pp 188-189 and "Broadband ESD Protection ...", pp. 182-183

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Bandwidth Enhancement With f, Doublers



A MOS transistor has f_t calculated as

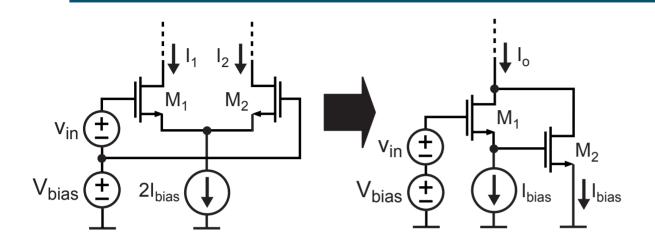
$$2\pi f_t = \frac{g_m}{C_{gs} + C_{gd}} \approx \frac{g_m}{C_{gs}}$$

- f_t doubler amplifiers attempt to increase the ratio of transconductance to capacitance
- We can make the argument that differential amplifiers are f₁ doublers
 - lacktriangle Capacitance seen by $f V_{in}$ for single-ended input: $C_{gs}/2$
 - Difference in current:

$$i_2 - i_1 = \frac{v_{in}}{2}g_m - \left(-\frac{v_{in}}{2}\right)g_m = v_{in}g_m$$

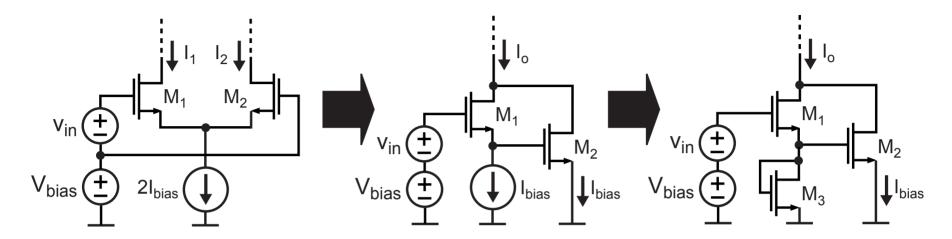
lacksquare Transconductance to Cap ratio is doubled: $rac{2g_m}{C_{as}}$

Creating a Single-Ended Output



- Input voltage is again dropped across two transistors
 - Ratio given by voltage divider in capacitance
 - Ideally is ½ of input voltage on C_{qs} of each device
- Input voltage source sees the series combination of the capacitances of each device
 - Ideally sees $\frac{1}{2}$ of the C_{gs} of M_1
- Currents of each device add to ideally yield ratio: $\frac{2g}{C}$

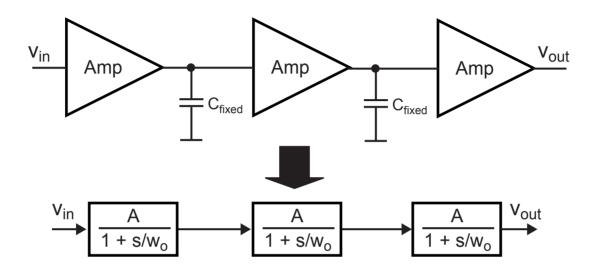
Creating the Bias for M₂



- Use current mirror for bias
 - Inspired by bipolar circuits (see Tom Lee's book, page 198)
- Need to set V_{bias} such that current through M₁ has the desired current of I_{bias}
 - The current through M₂ will ideally match that of M₁
- Problem: achievable bias voltage across M₁ (and M₂) is severely reduced (thereby reducing effective f₁ of device)

■ Do f, doublers have an advantage in CMOS?

Increasing Gain-Bandwidth Product Through Cascading



We can significantly increase the gain of an amplifier by cascading n stages

$$\Rightarrow \frac{v_{out}}{v_{in}} = \left(\frac{A}{1 + s/w_o}\right)^n = A^n \frac{1}{(1 + s/w_o)^n}$$

Issue – bandwidth degrades, but by how much?

Analytical Derivation of Overall Bandwidth

The overall 3-db bandwidth of the amplifier is where

$$\left|\frac{v_{out}}{v_{in}}\right| = \left|\frac{A}{1 + jw_1/w_o}\right|^n = \frac{A^n}{\sqrt{2}}$$

- w₁ is the overall bandwidth
- A and w_o are the gain and bandwidth of each section

$$\Rightarrow \left(\frac{A}{\sqrt{1 + (w_1/w_o)^2}}\right)^n = \frac{A^n}{\sqrt{2}}$$

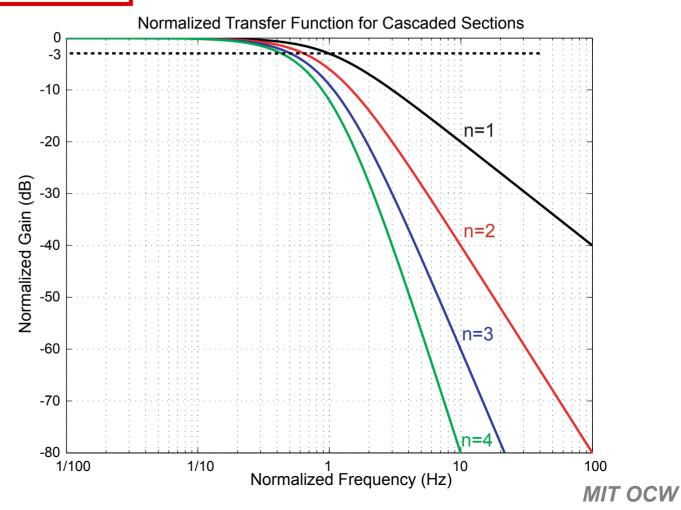
$$\Rightarrow \left(1 + (w_1/w_o)^2\right)^n = 2$$

$$\Rightarrow w_1 = w_o\sqrt{2^{1/n} - 1}$$

- Bandwidth decreases much slower than gain increases!
 - Overall gain bandwidth product of amp can be increased!

Transfer Function for Cascaded Sections

$$H(f) = \left| \frac{1}{1 + j2\pi f} \right|^n$$



Choosing the Optimal Number of Stages

To first order, there is a constant gain-bandwidth product for each stage

$$\Rightarrow Aw_o = w_t \Rightarrow w_o = w_t/A$$

- Increasing the bandwidth of each stage requires that we lower its gain
- Can make up for lost gain by cascading more stages
- We found that the overall bandwidth is calculated as

$$w_1 = w_o \sqrt{2^{1/n} - 1} = \frac{w_t}{A} \sqrt{2^{1/n} - 1}$$

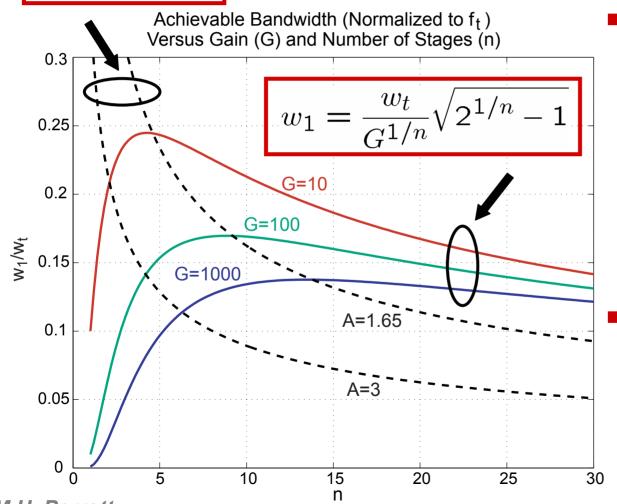
Assume that we want to achieve gain G with n stages

$$\Rightarrow A = G^{1/n} \Rightarrow w_1 = \frac{w_t}{G^{1/n}} \sqrt{2^{1/n} - 1}$$

- From this, Tom Lee finds optimum gain \approx 1.65
 - See Tom Lee's book, pp 207-211

Achievable Bandwidth Versus G and n

$$\frac{w_t}{A}\sqrt{2^{1/n}-1}$$

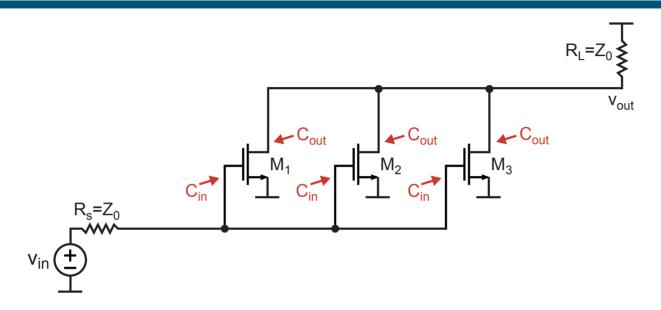


- Optimum gain per stage is about 1.65
 - Note than gain per stage derived from plot as

$$A = G^{1/n}$$

- Maximum is fairly soft, though
- Can dramatically lower power (and improve noise) by using larger gain per stage

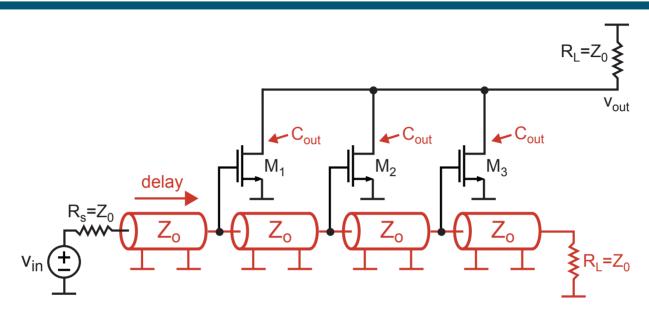
Motivation for Distributed Amplifiers



- We achieve higher gain for a given load resistance by increasing the device size (i.e., increase g_m)
 - Increased capacitance lowers bandwidth
 - We therefore get a relatively constant gain-bandwidth product
- We know that transmission lines have (ideally) infinite bandwidth, but can be modeled as LC networks

Can we lump device capacitances into transmission line?

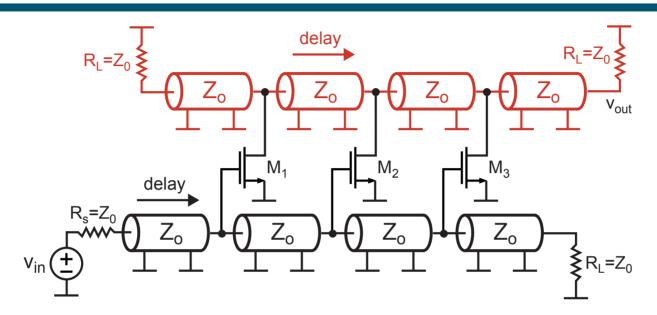
Distributing the Input Capacitance



- Lump input capacitance into LC network corresponding to a transmission line
 - Signal ideally sees a real impedance rather than an RC lowpass
 - Often implemented as lumped networks such as T-coils
 - We can now trade delay (rather than bandwidth) for gain

Issue: outputs are delayed from each other

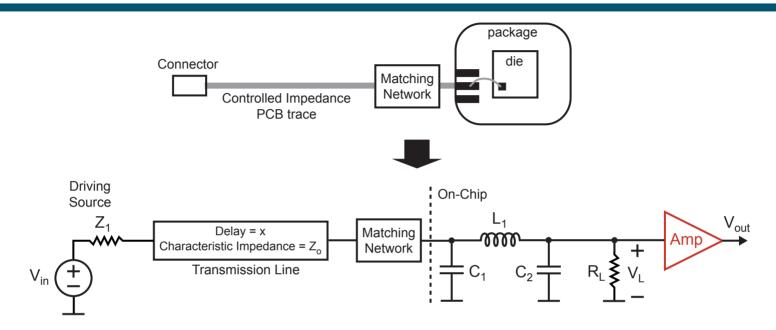
Distributing the Output Capacitance



- Delay the outputs same amount as the inputs
 - Now the signals match up
 - We have also distributed the output capacitance!
- Benefit high bandwidth
- Negatives high power, poorer noise performance, expensive in terms of chip area

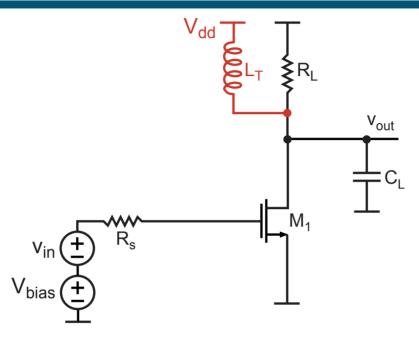
Each transistor gain is adding rather than multiplying!

Narrowband Amplifiers



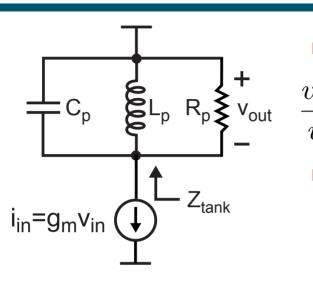
- For wireless systems, we are interested in conditioning and amplifying the signal over a narrow frequency range centered at a high frequency
 - Allows us to apply narrowband transformers to create matching networks
- Can we take advantage of this fact when designing the amplifier?

Tuned Amplifiers



- Put inductor in parallel across R_L to create bandpass filter
 - It will turn out that the gain-bandwidth product is roughly conserved regardless of the center frequency!
 - Assumes that center frequency (in Hz) << f_t
- To see this and other design issues, we must look closer at the parallel resonant circuit

Tuned Amp Transfer Function About Resonance



Amplifier transfer function

Note that conductances add in parallel

$$Y_{tank}(s) = \frac{1}{R_n} + \frac{1}{sL_n} + sC_p$$

Evaluate at s = jw

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$$Y_{tank}(w) = \frac{1}{R_p} - \frac{j}{wL_p} + jwC_p = \frac{1}{R_p} + \frac{j}{wL_p} \left(-1 + w^2L_pC_p\right)$$

■ Look at frequencies about resonance: $w = w_o + \Delta w$

$$\Rightarrow Y_{tank}(\Delta w) = \frac{1}{R_p} + \frac{j}{(w_o + \Delta w)L_p} \left(-1 + (w_o + \Delta w)^2 L_p C_p \right)$$
$$\approx \frac{1}{R_p} + \frac{j}{w_o L_p} \left(-1 + w_o^2 L_p C_p + 2w_o \Delta w L_p C_p \right)$$

Tuned Amp Transfer Function About Resonance (Cont.)

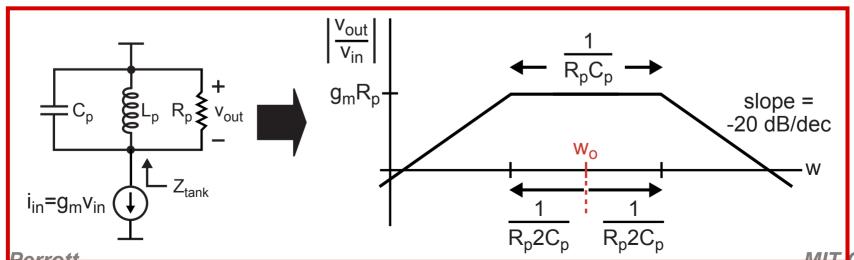
From previous slide

$$Y_{tank}(\Delta w) \approx \frac{1}{R_p} + \frac{j}{w_o L_p} \left(-\frac{1 + w_o^2 L_p C_p}{= \mathbf{0}} + 2w_o \Delta w L_p C_p \right)$$

$$\approx \frac{1}{R_p} + \frac{j}{w_o L_p} \left(2w_o \Delta w L_p C_p \right) = \frac{1}{R_p} + j \Delta w 2C_p$$

Simplifies to RC circuit for bandwidth calculation!

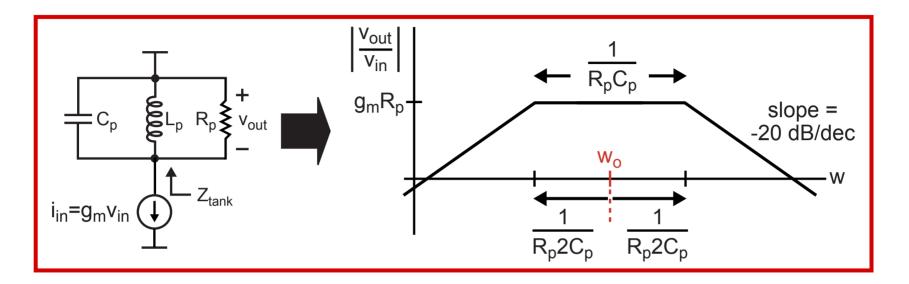
$$|Z_{tank}(\Delta w) \approx R_p || \frac{1}{j\Delta w 2C_p}|$$



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Gain-Bandwidth Product for Tuned Amplifiers

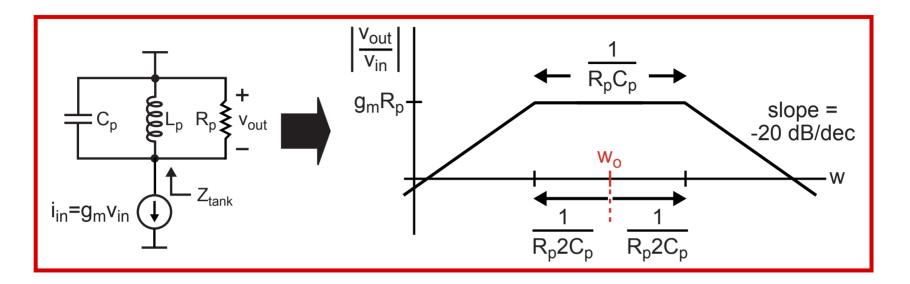


The gain-bandwidth product:

$$G \cdot BW = g_m R_p \frac{1}{R_p C_p} = \frac{g_m}{C_p}$$

- The above expression is independent of center frequency!
 - In practice, we need to operate at a frequency less than the f_t of the device

The Issue of Q

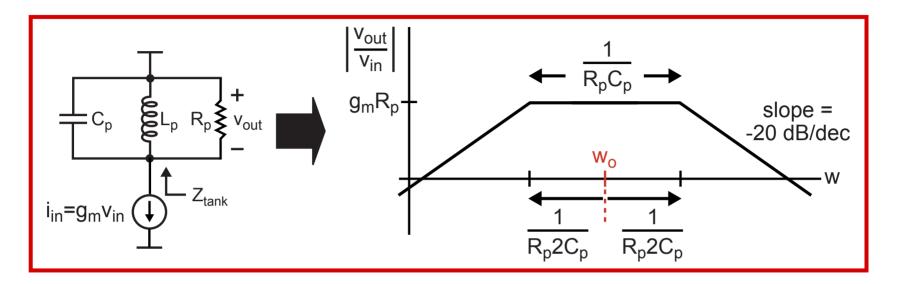


- **By definition** $Q = w \frac{\text{energy stored}}{\text{average power dissipated}}$
- For parallel tank (see Tom Lee's book, pp 88-89)

at resonance:
$$Q = \frac{R_p}{w_o L_p} = w_o R_p C_p$$

Comparing to above: $Q = w_o R_p C_p = \frac{w_o}{1/(R_p C_p)} = \frac{w_o}{BW}$

Design of Tuned Amplifiers



Three key parameters

- **Gain** = $g_m R_p$
- Center frequency = w_o
- $\mathbf{Q} = \mathbf{W}_0 / \mathbf{B} \mathbf{W}$
- Impact of high Q
 - Benefit: allows achievement of high gain with low power
 - Problem: makes circuit sensitive to process/temp variations

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Issue: Cad Can Cause Undesired Oscillation

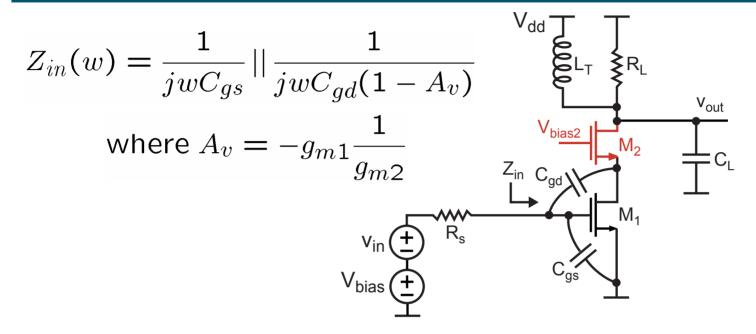
$$Z_{in}(w) = \frac{1}{jwC_{gs}} || \frac{1}{jwC_{gd}(1-A_v)}$$
 where $A_v = -g_m Z_{tank}(w)$
$$V_{\text{bias}} \underbrace{+}_{\text{V}}$$

At frequencies below resonance, tank looks inductive

$$A_v pprox -g_m(jwL) \ \Rightarrow \ Z_{in}(w) pprox rac{1}{jwC_{gs}} || rac{1}{jwC_{gd}(1+g_m(jwL))}$$
 $\Rightarrow \ Z_{in}(w) pprox rac{1}{jwC_{gs}} || rac{1}{jwC_{gd} - w^2 g_m C_{gd} L}$
 $\Rightarrow \ Z_{in}(w) pprox rac{1}{jwC_{gs}} || rac{1}{jwC_{gd}} || rac{-1}{w^2 g_m C_{gd} L}$
Resistance!

Resistance!

Use Cascode Device to Remove Impact of C_{gd}

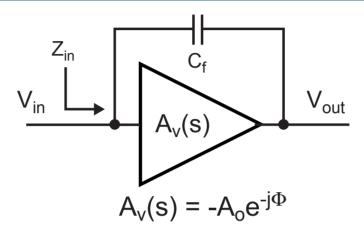


At frequencies above and below resonance

$$Z_{in}(w) = \frac{1}{jwC_{gs}} || \frac{1}{jwC_{qd}(1 + g_{m1}/g_{m2})}|$$

Purely Capacitive!

Active Real Impedance Generator



Input impedance:

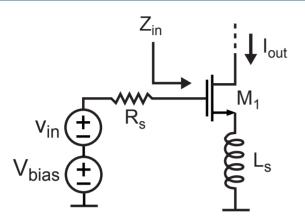
$$Z_{in}(w) = \frac{1}{jwC_f(1 - A_v)} = \frac{1}{jwC_f(1 + A_o e^{-j\Phi})}$$

$$= \frac{1}{jwC_f(1 + A_o \cos \Phi) + A_o wC \sin \Phi}$$

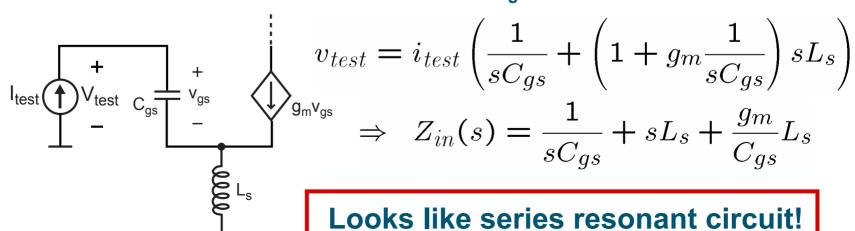
$$= \frac{1}{jwC_f(1 + A_o \cos \Phi)} || \frac{1}{A_o wC \sin \Phi}$$

Resistive component!

This Principle Can Be Applied To Impedance Matching

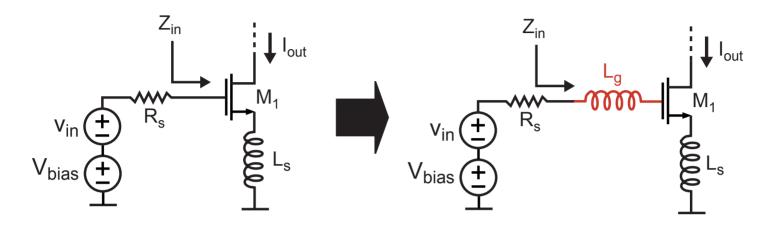


- We will see that it's advantageous to make Z_{in} real without using resistors
 - For the above circuit (ignoring C_{qd})



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Use A Series Inductor to Tune Resonant Frequency



Calculate input impedance with added inductor

$$Z_{in}(s) = \frac{1}{sC_{gs}} + s(L_s + L_g) + \frac{g_m}{C_{gs}}L_s$$

- Often want purely resistive component at frequency w_o
 - Choose L_q such that resonant frequency = w_o

i.e., want
$$\frac{1}{\sqrt{(L_s + L_g)C_{gs}}} = w_o$$