

RBE474X/595-B01-ST: Deep Learning For Perception

Class 10: Generative Models: VAEs, GANs,
Attacking GANs

Prof. Wei Xiao

Image Compression



1MB

Image Compression



1MB

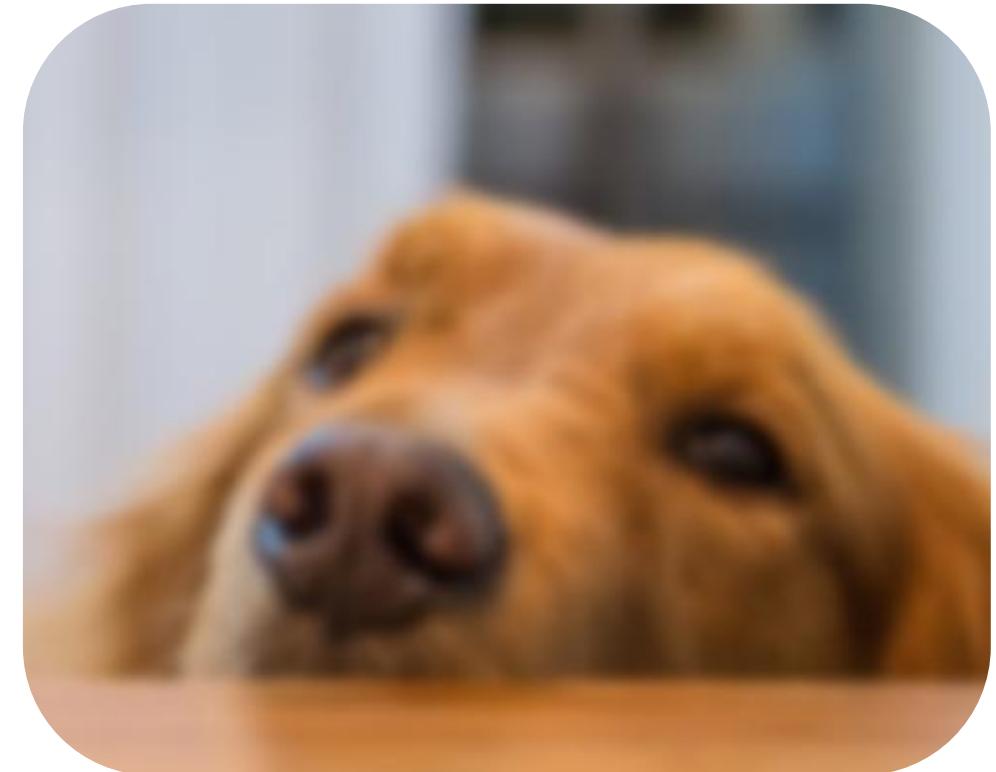


0.1MB

Image Compression



1MB



0.1MB

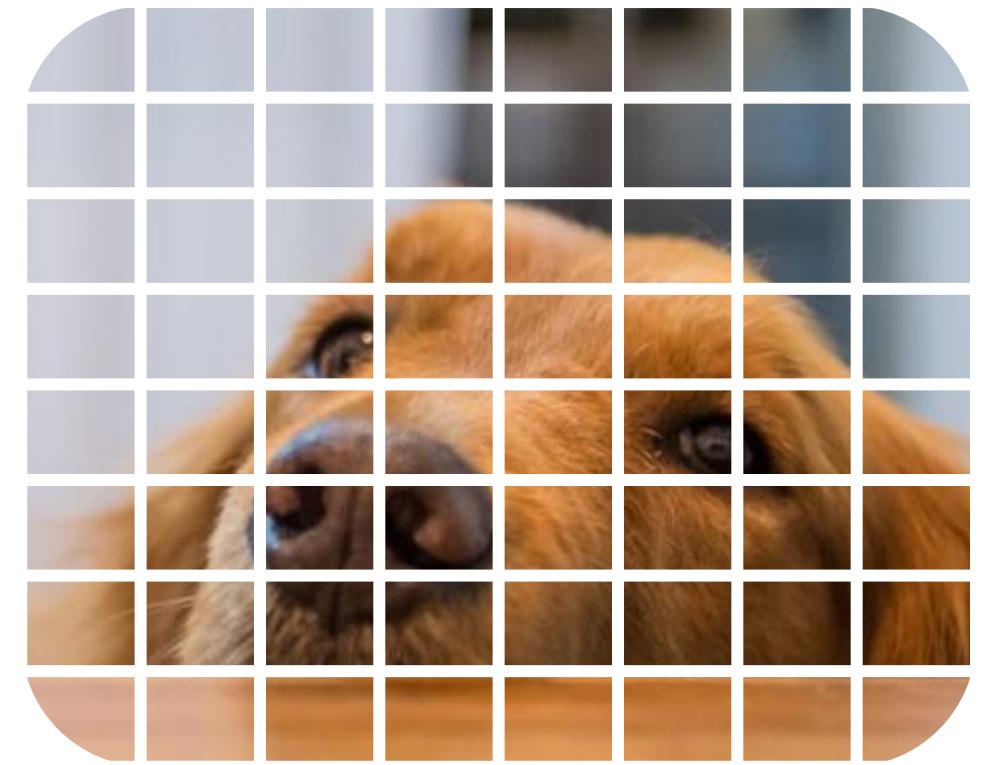
We Don't Want To Lose Details



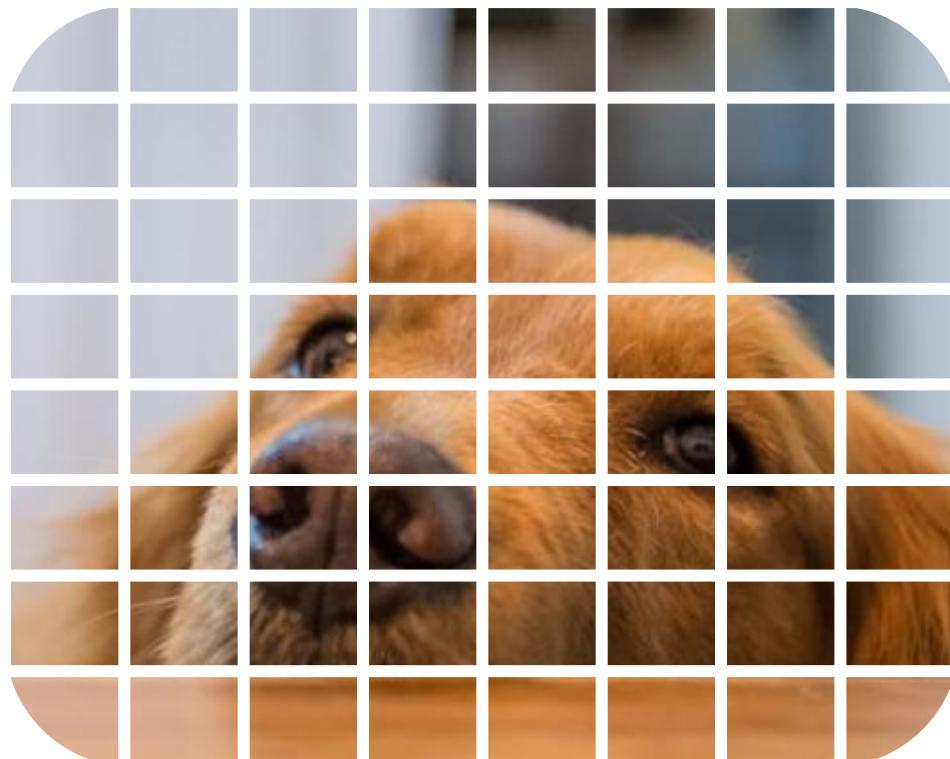
$$\begin{bmatrix} 0.37 \\ -40 \\ 250 \\ 0.74 \\ 0.11 \\ -0.35 \\ \vdots \\ 0.01 \end{bmatrix}$$
$$\mathbb{R}^{D \times 1}$$

$$D \ll MNK$$

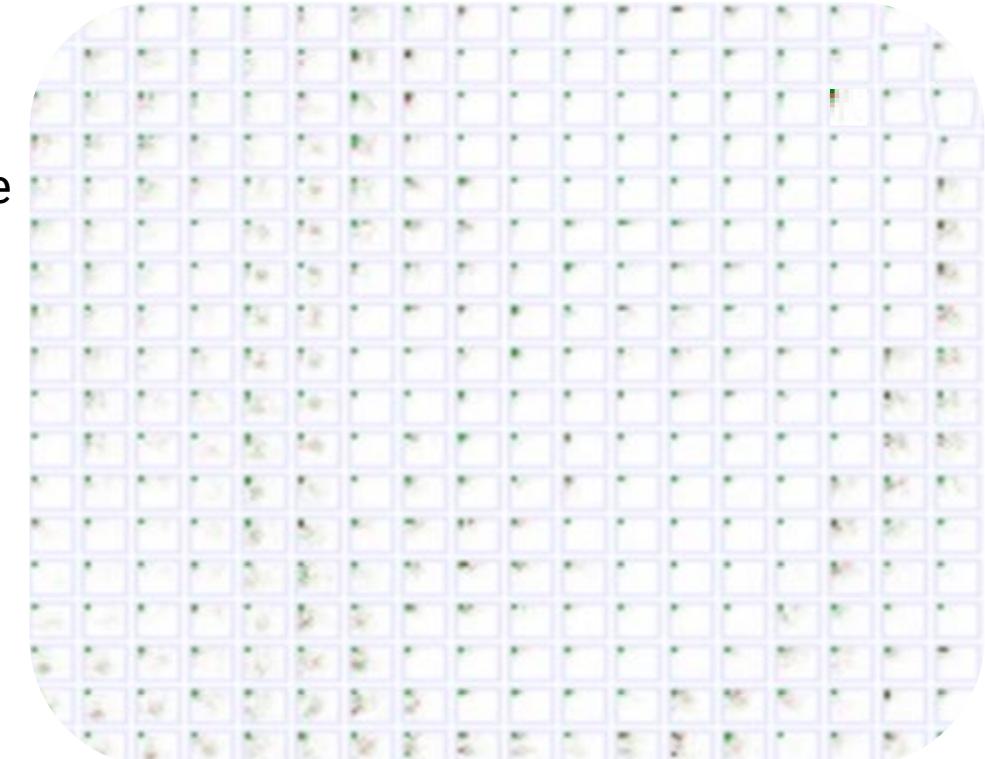
We Don't Want To Lose Details



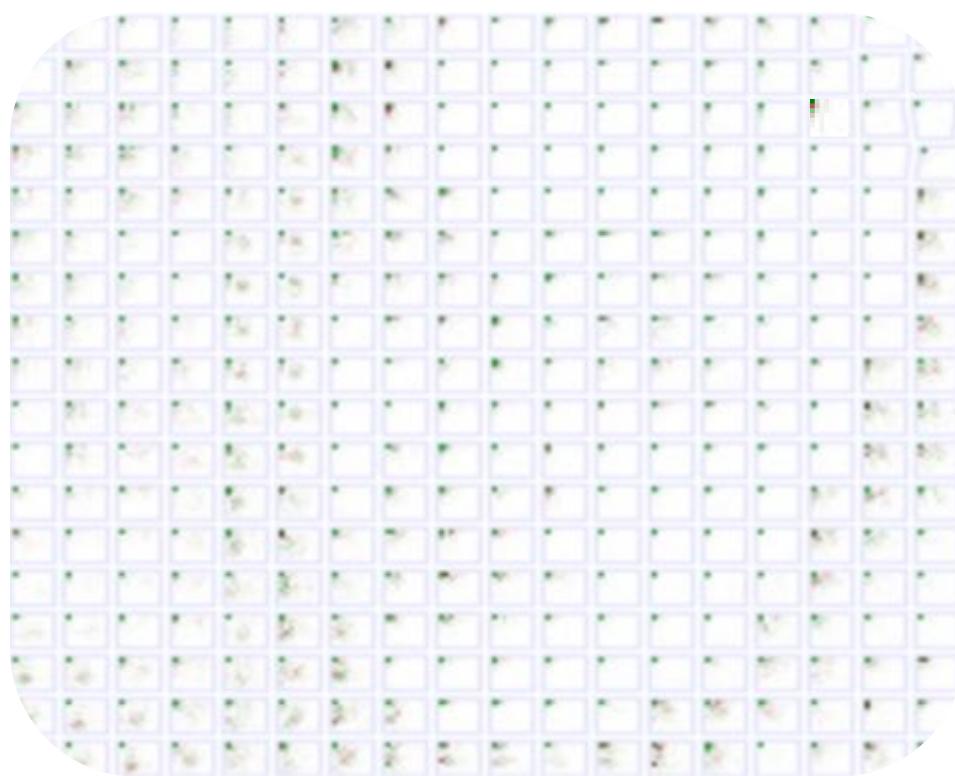
We Don't Want To Lose Details



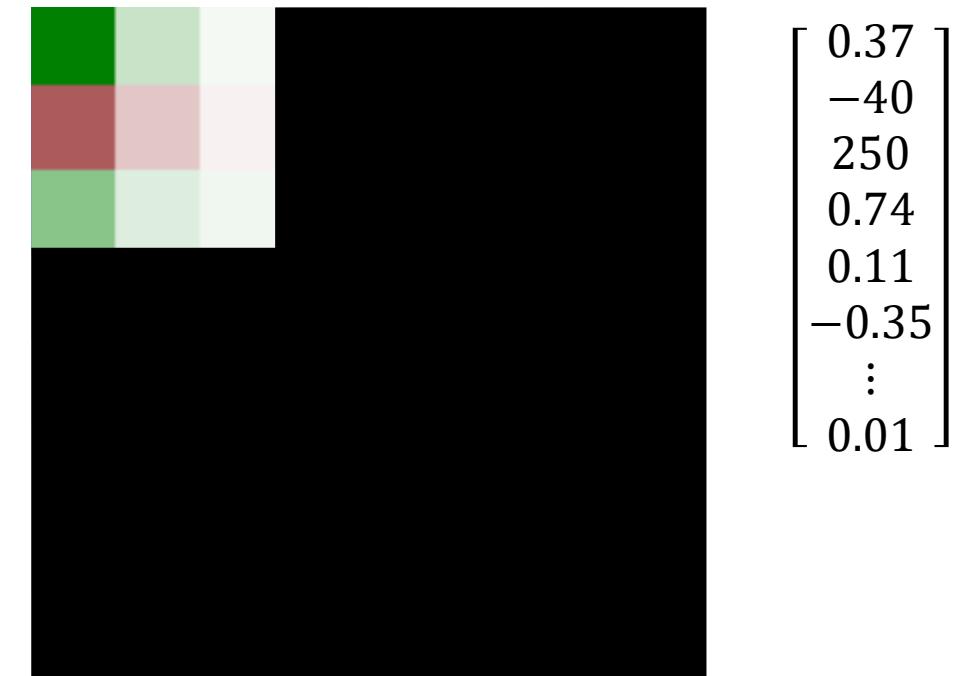
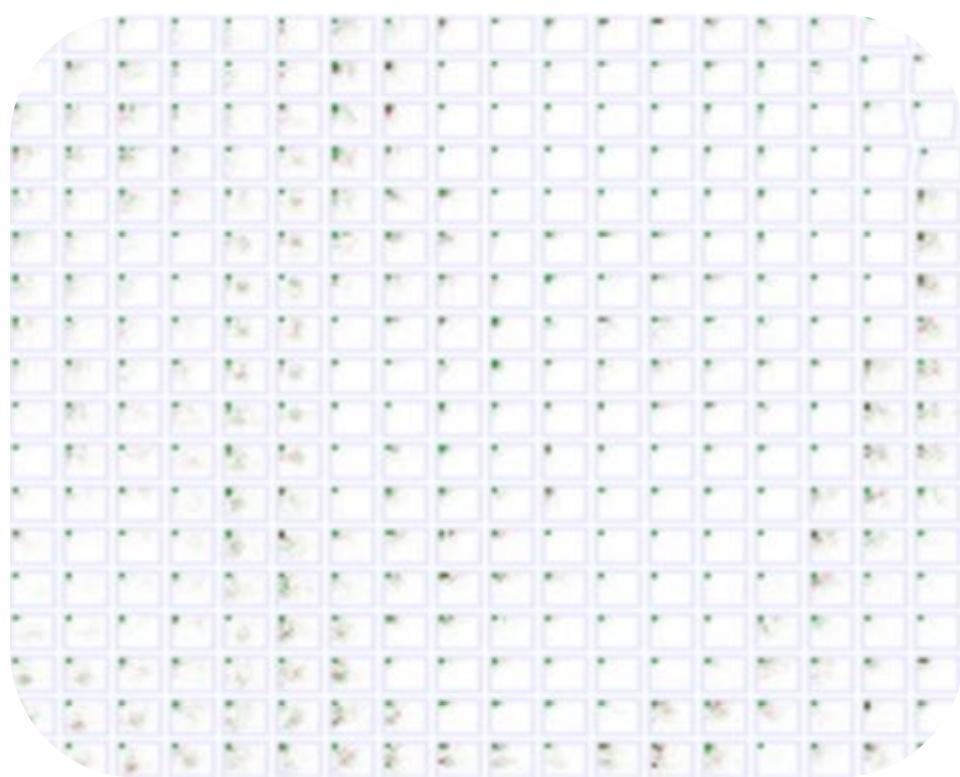
DCT(discrete cosine transform)



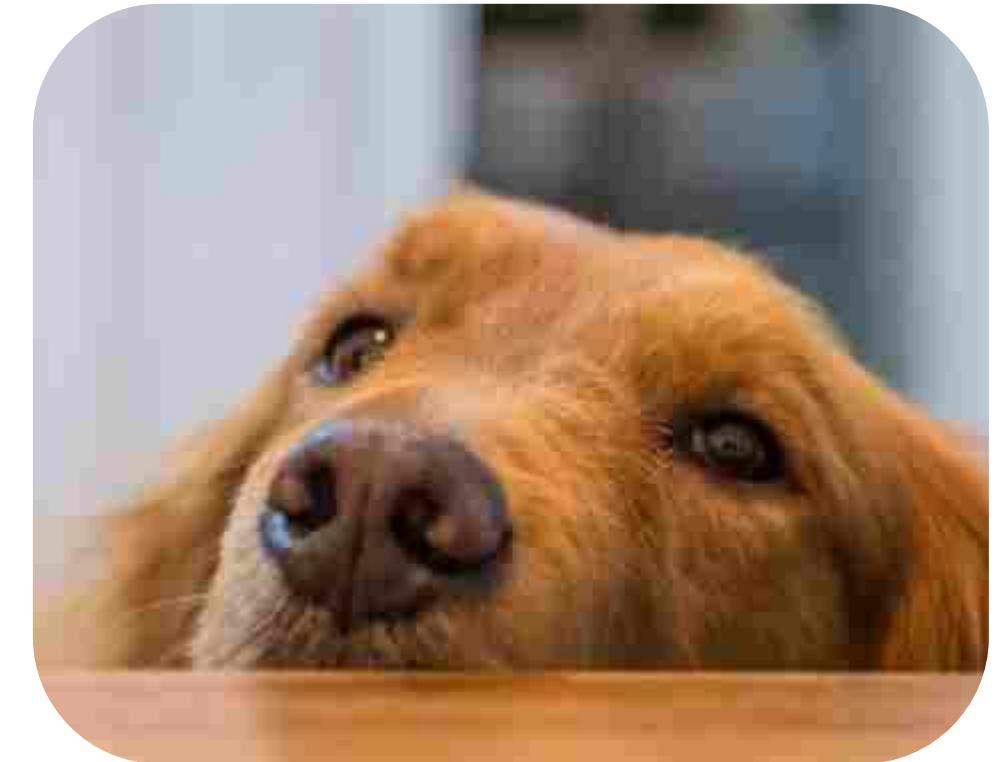
We Don't Want To Lose Details



We Don't Want To Lose Details

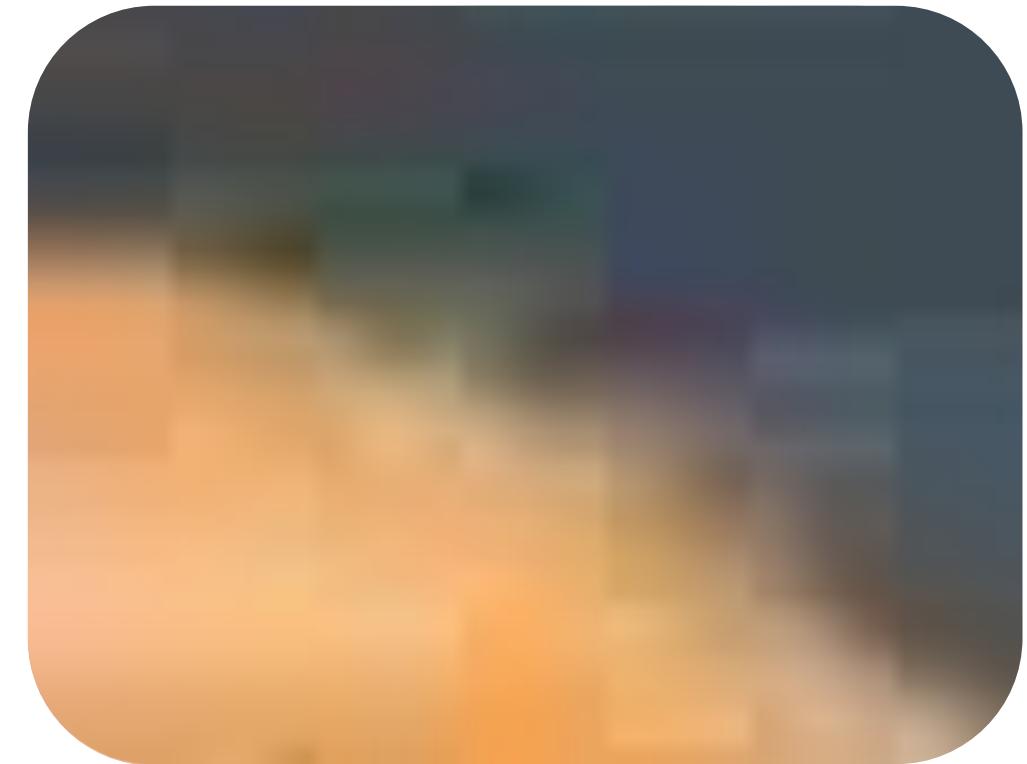


We Don't Want To Lose Details

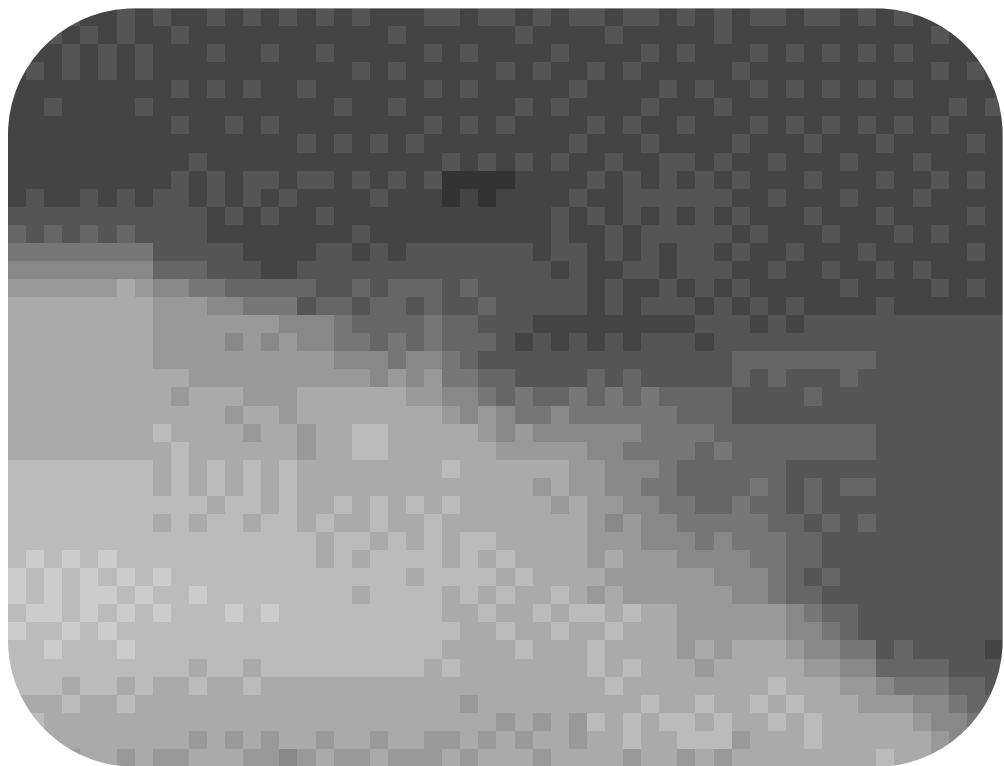


68× compression!

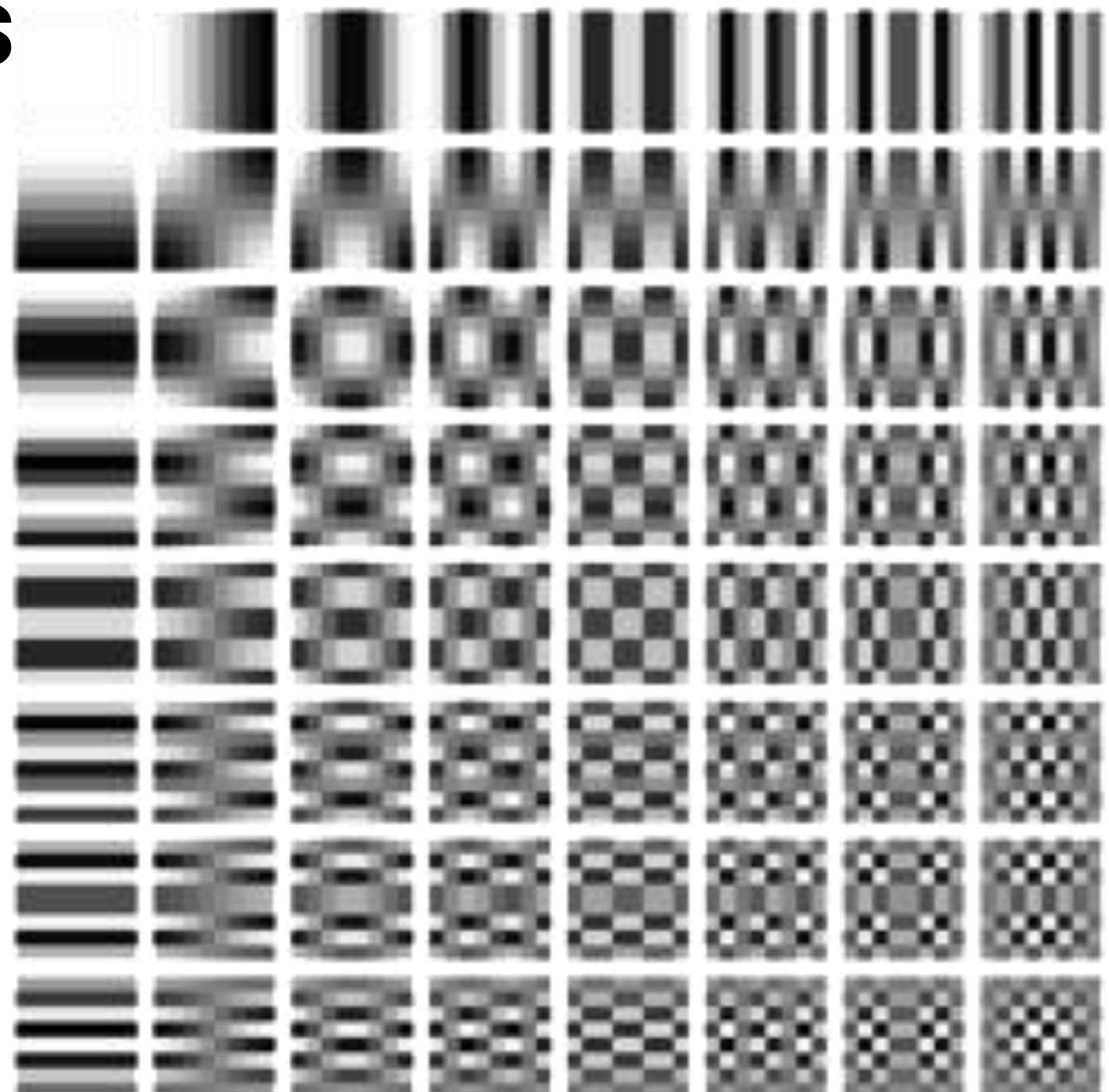
JPEG



DCT Basis Functions

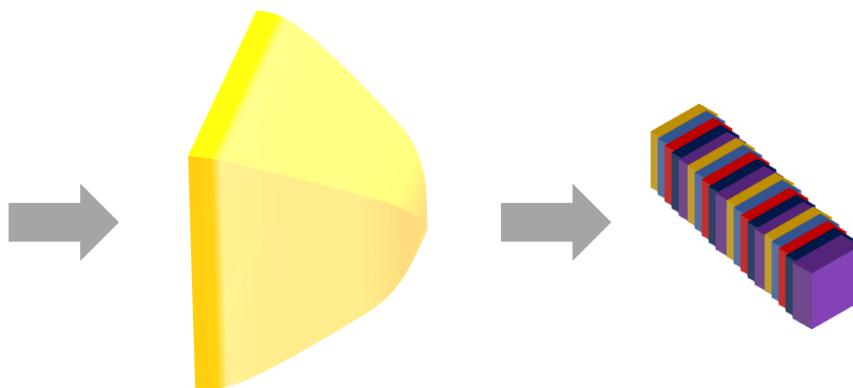


A **discrete cosine transform (DCT)** expresses a finite sequence of **data points** in terms of a sum of **cosine** functions oscillating at different **frequencies**



Era Of Deep Learning

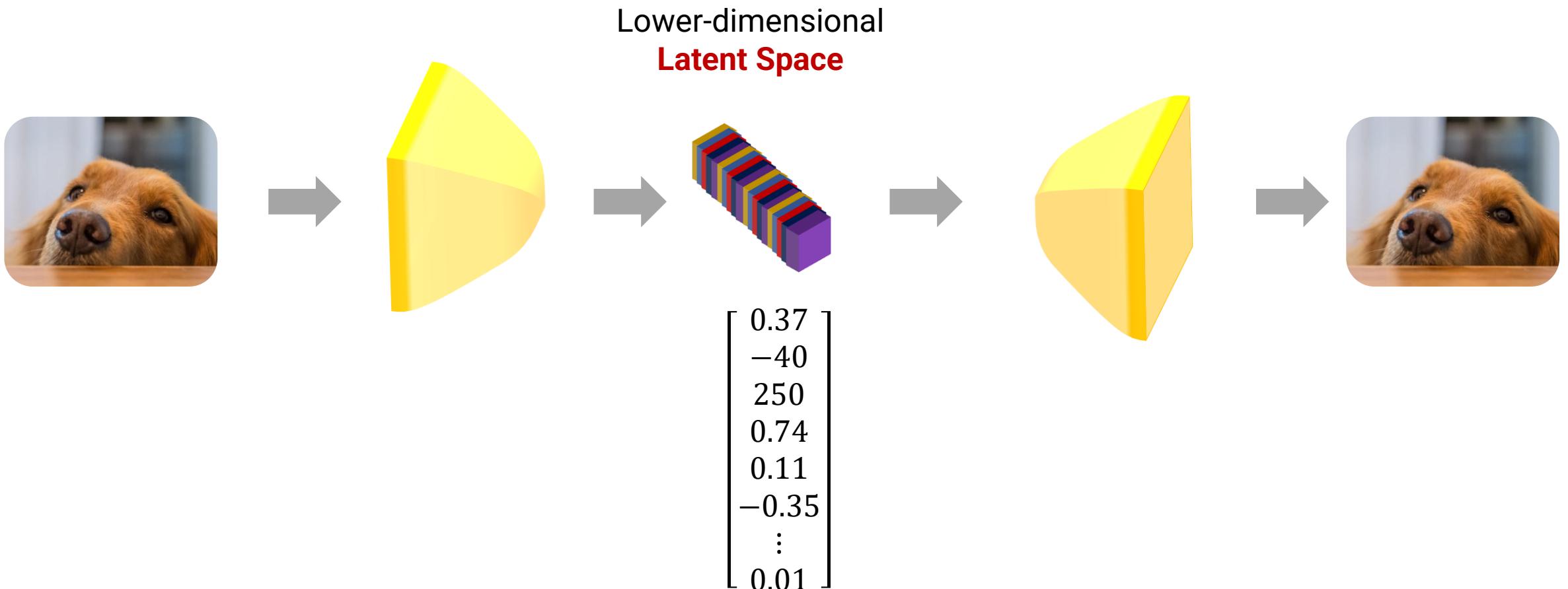
Let's Do This With A Neural Network



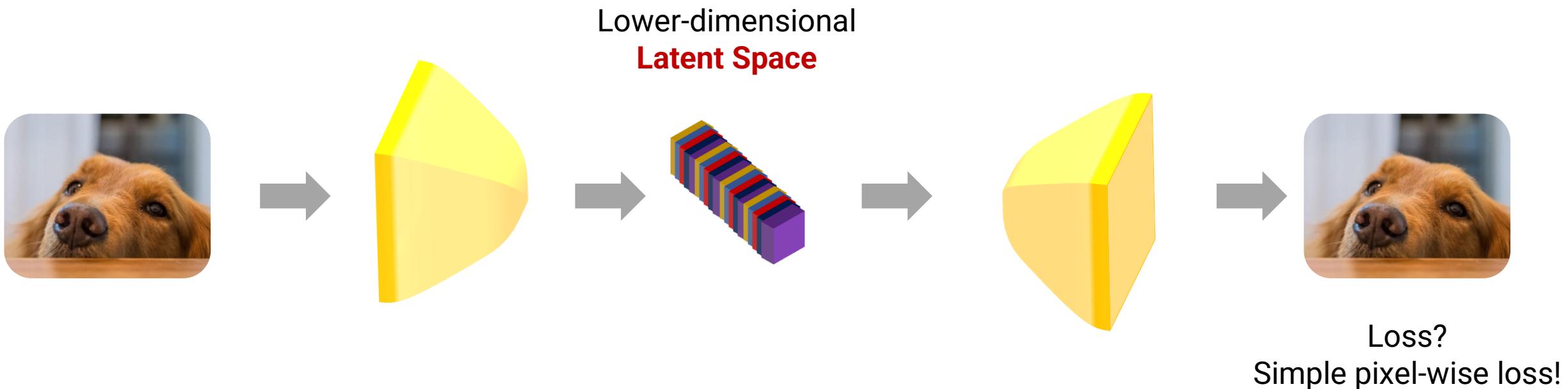
$$\begin{bmatrix} 0.37 \\ -40 \\ 250 \\ 0.74 \\ 0.11 \\ -0.35 \\ \vdots \\ 0.01 \end{bmatrix}$$

Era Of Deep Learning

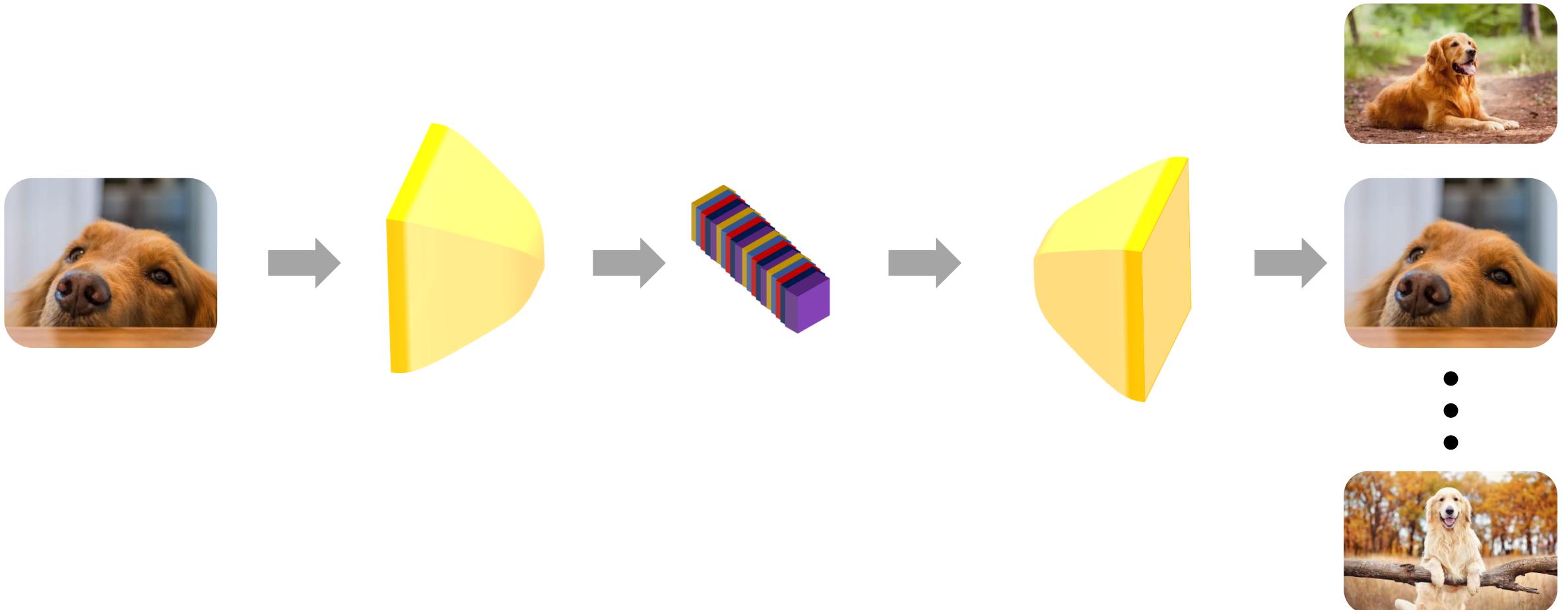
Let's Do This With A Neural Network



Autoencoder

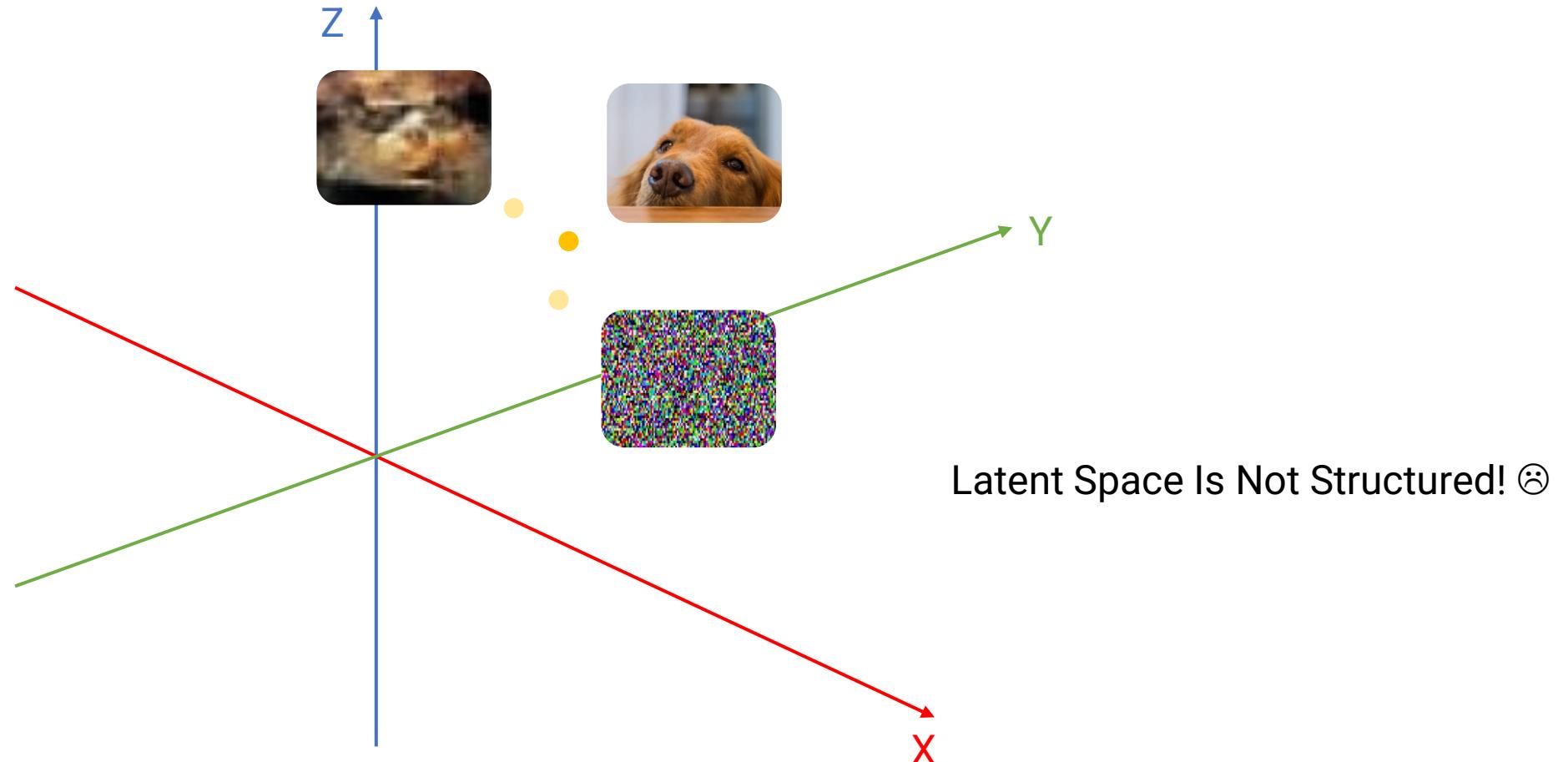


I Want All Doggo Images!

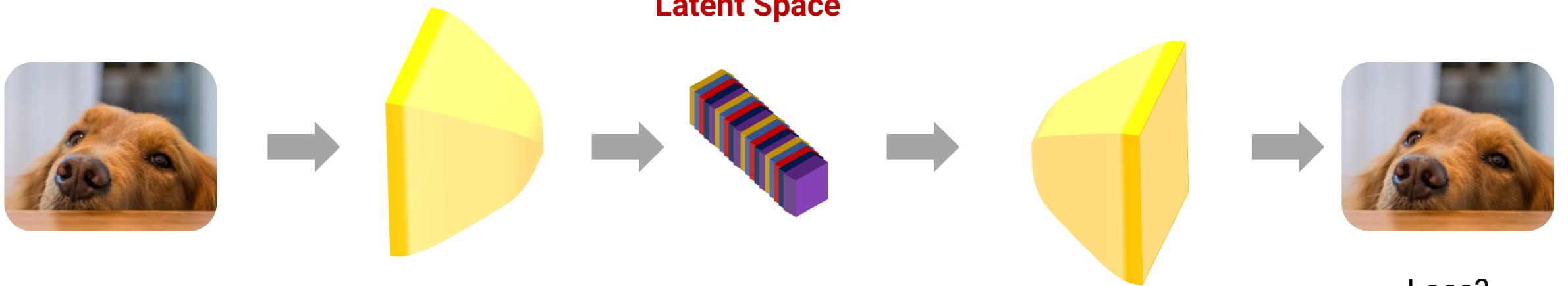


Can't I Use Latent Space Tricks?

From Before?



Autoencoder



Lower-dimensional
Latent Space

Can only **generate** one image!
So, one NN per image ☹

Loss?
Simple pixel-wise loss!



Data Is The Key!

Moore's Law for Machine Learning

"The amount of training data doubles every eighteen months."

- Danny Lange, Unity

IMPLAUSIBLE



EXPENSIVE



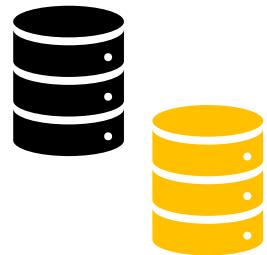
DESTRUCTIVE



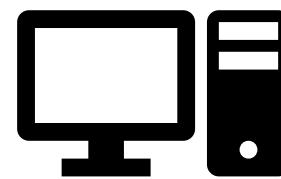
ARDUOUS



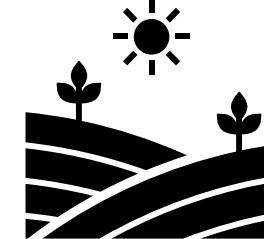
Ways To Increase Data



Augmentation



Simulation

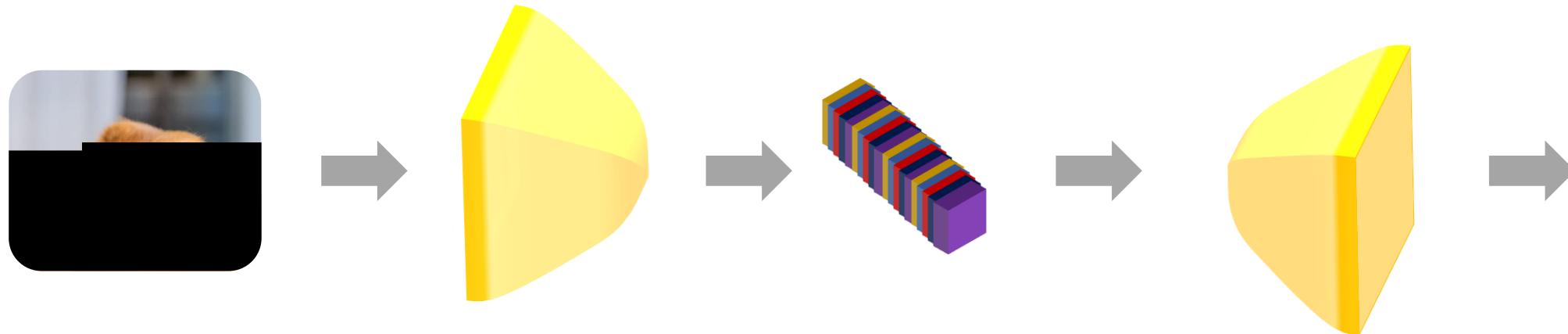


Field Collection

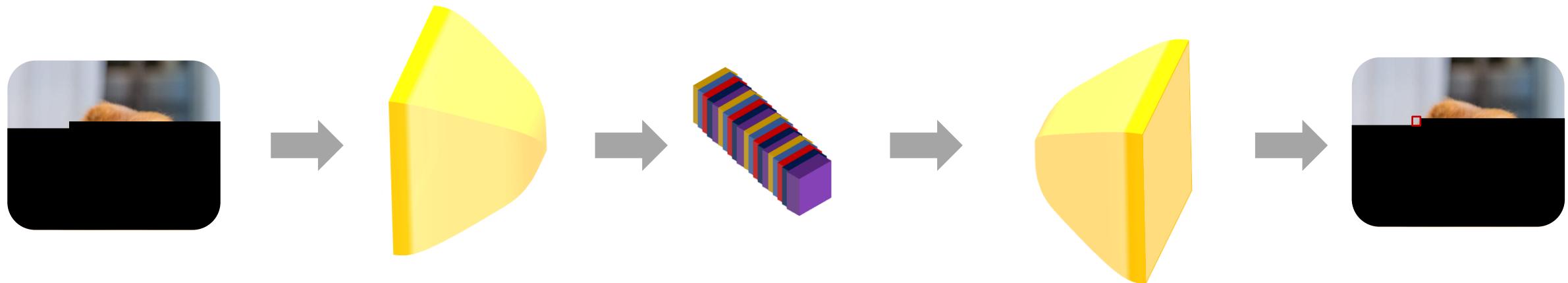


Crowd-source Data

I Want All Doggo Images!

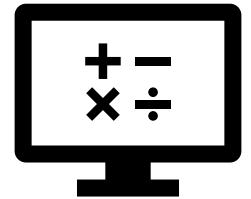


I Want All Doggo Images!



Make up an image **pixel-by-pixel**

Van den Oord, Aaron, et al. "Conditional image generation with pixelcnn decoders." Advances in neural information processing systems 29 (2016).



PixelRNN

Simplified
Mathematical Model

Called a Fully Visible Belief Network

$$p(\mathbf{x}) = \prod_{i=1}^n p(\mathbf{x}_i | \mathbf{x}_1, \dots, \mathbf{x}_{i-1})$$

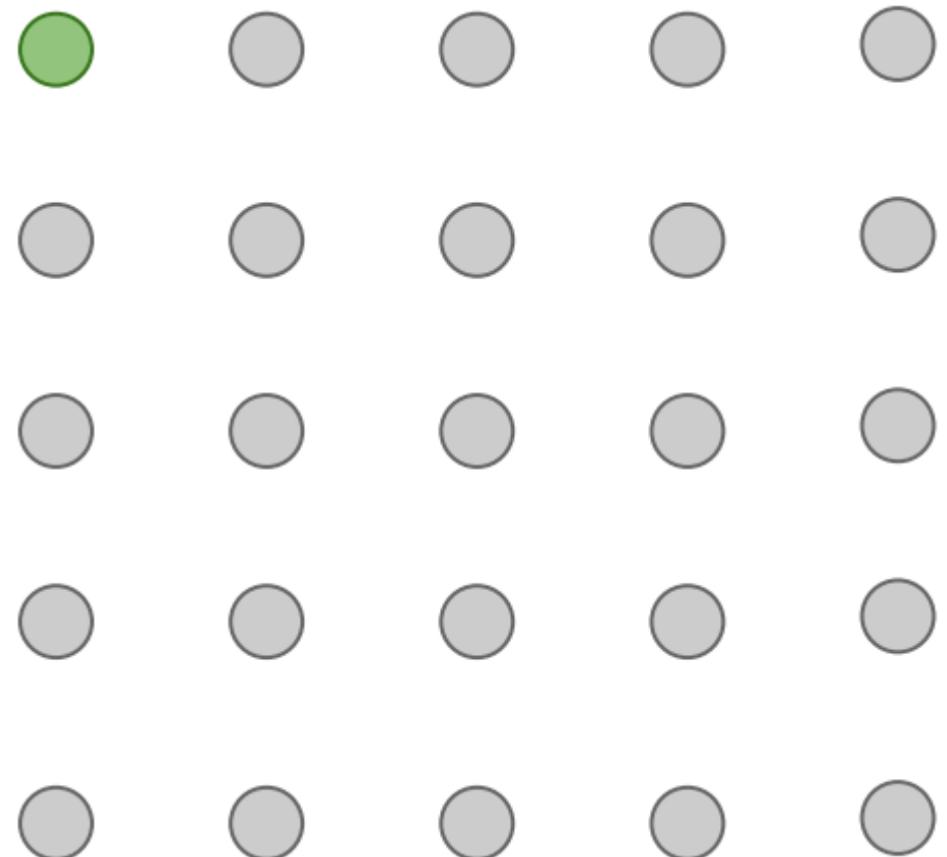
Likelihood of image \mathbf{x}

Probability of i^{th} pixel value given all previous values

Maximize the likelihood of training data!

PixelRNN

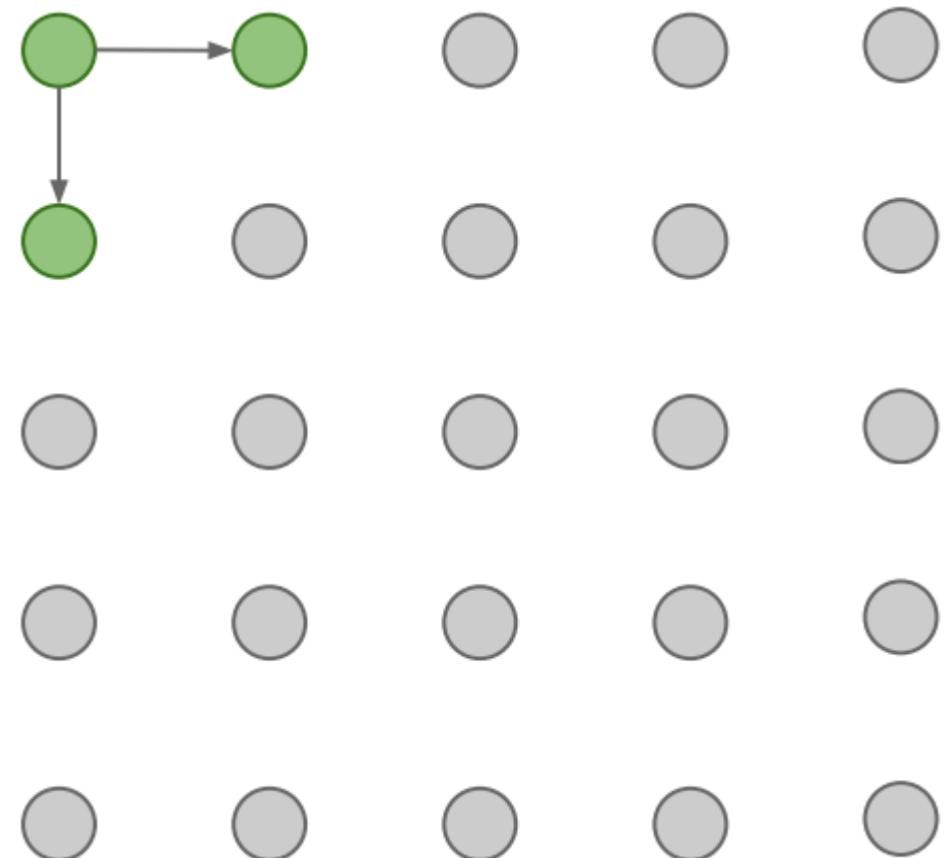
Image generation starts from corner



PixelRNN

Image generation starts from corner

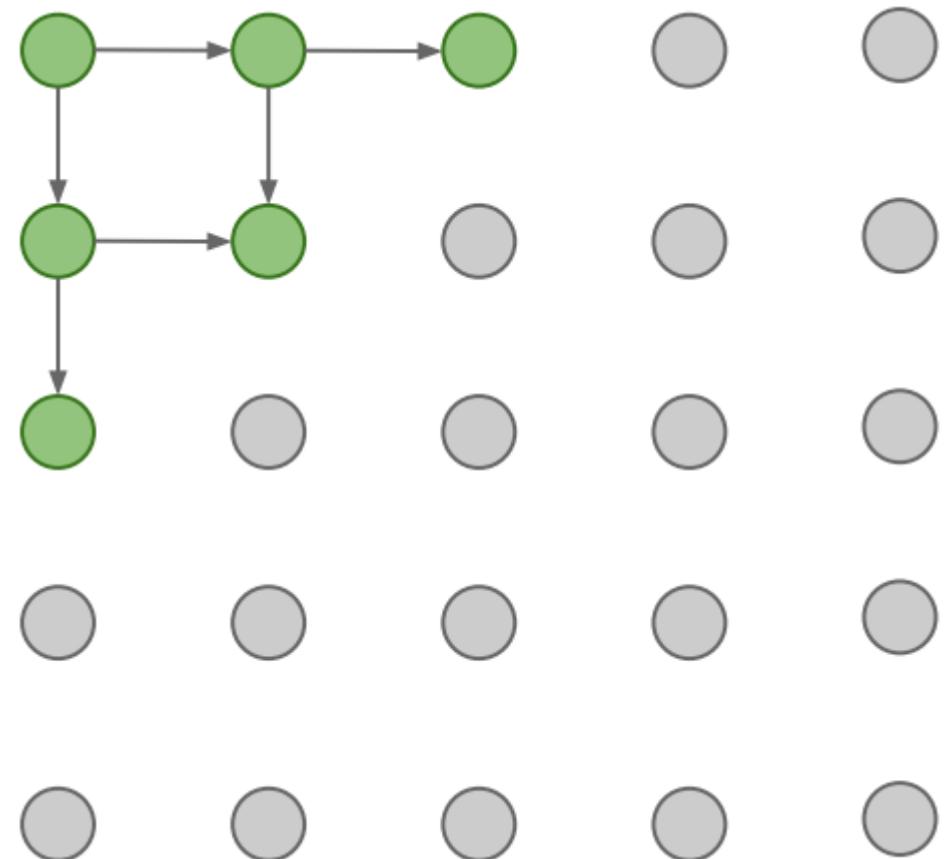
Dependency on previous pixels
modeled using an RNN (LSTM)



PixelRNN

Image generation starts from corner

Dependency on previous pixels
modeled using an RNN (LSTM)



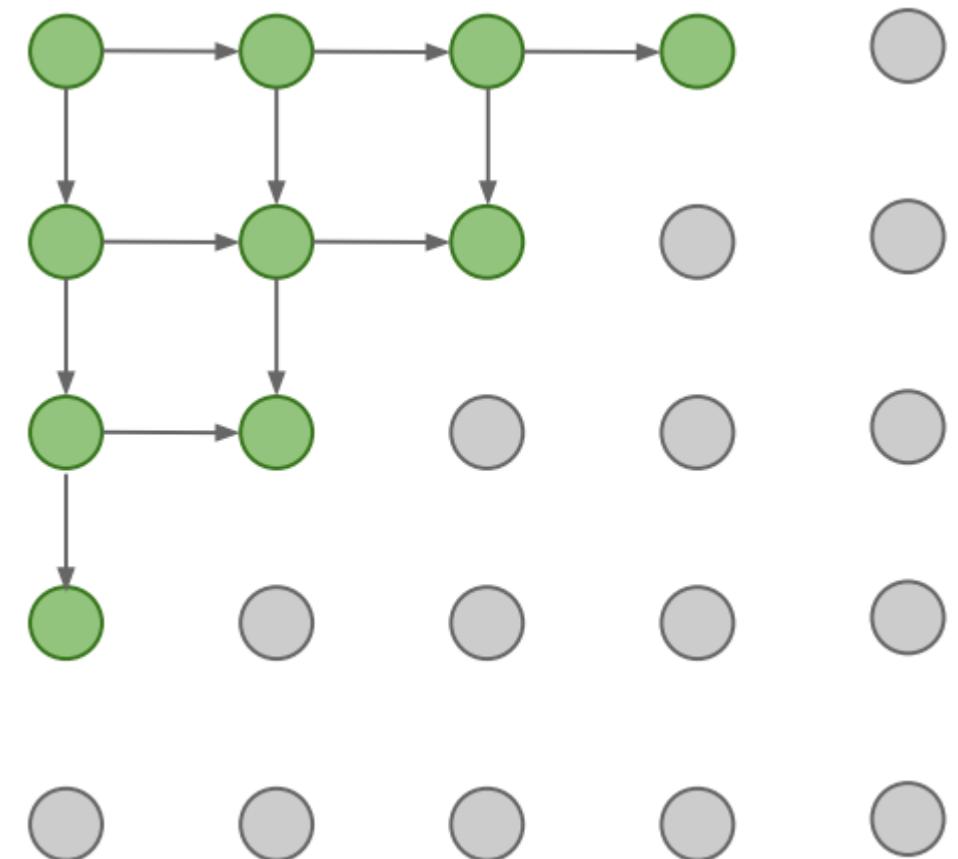
PixelRNN

Image generation starts from corner

Dependency on previous pixels
modeled using an RNN (LSTM)

Issue?

Very Very Slow 😞



PixelCNN

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

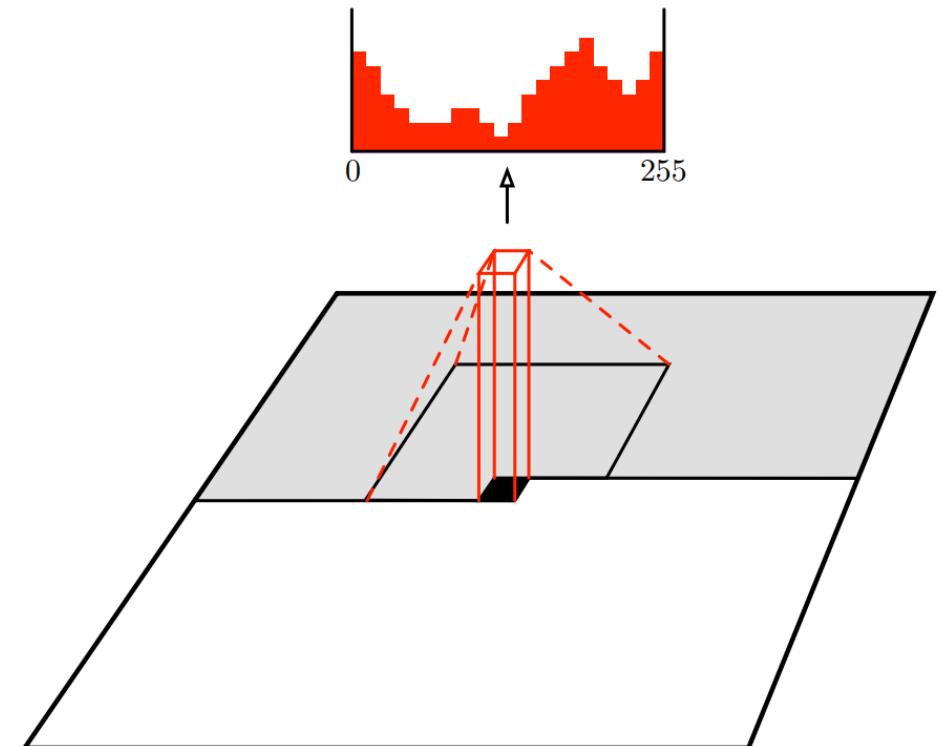
Trained using Maximum Likelihood

$$p(\mathbf{x}) = \prod_{i=1}^n p(\mathbf{x}_i | \mathbf{x}_1, \dots, \mathbf{x}_{i-1})$$

Much faster than PixelRNN: Can parallelize

Issue?

Still pixel by pixel, so slow 😞



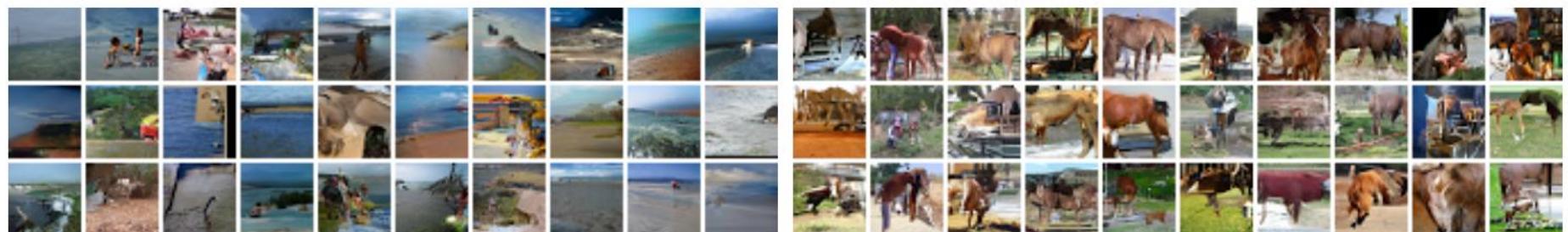
Works?



African elephant



Coral Reef



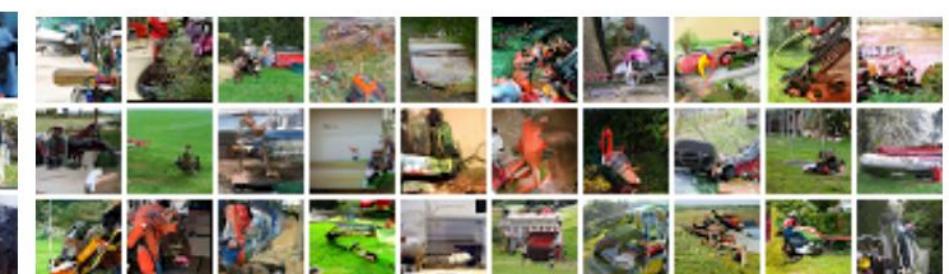
Sandbar



Sorrel horse

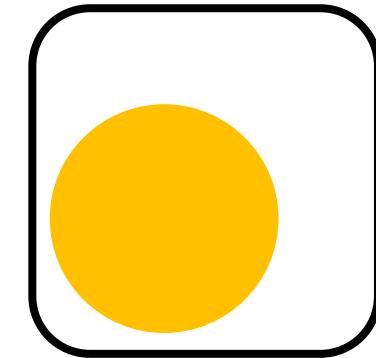
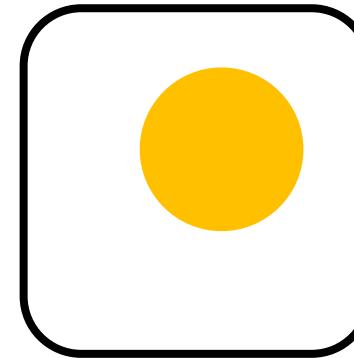
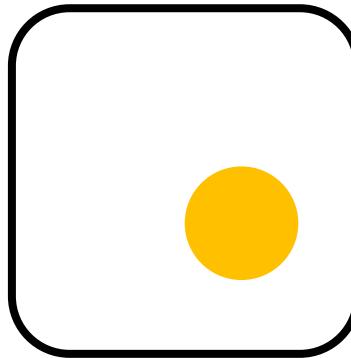
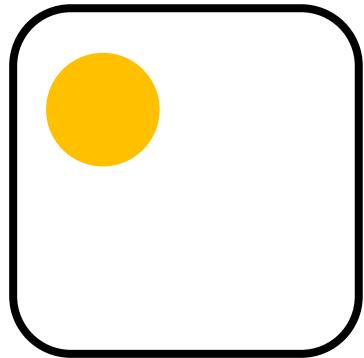


Lhasa Apso (dog)



Lawn mower

Toy Example

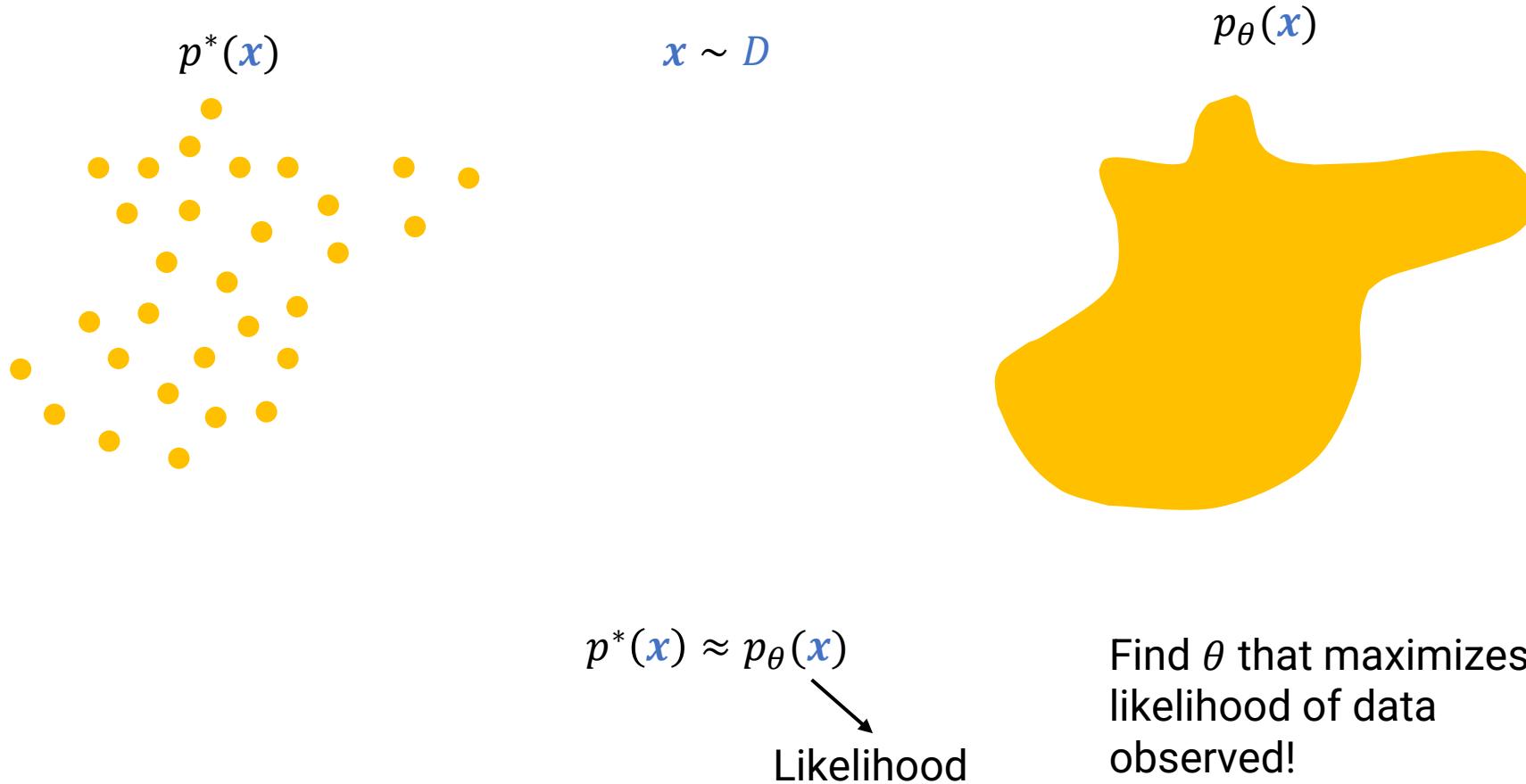


Circles!

- Same color
- Always fully enclosed
- Only variables:
 - Size
 - Location

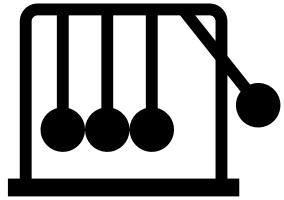
Slides inspired from: [Understanding Variational Autoencoders \(VAEs\) | Deep Learning \(youtube.com\)](https://www.youtube.com/watch?v=UgXWzqfjyJY)

What Do We Actually Have?



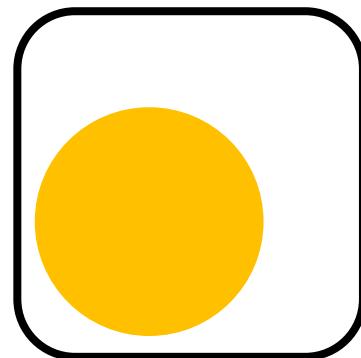
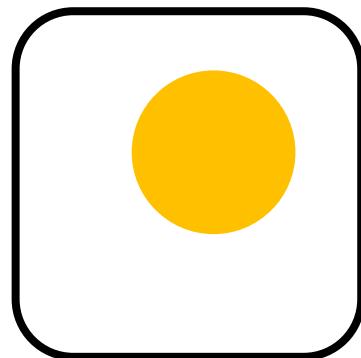
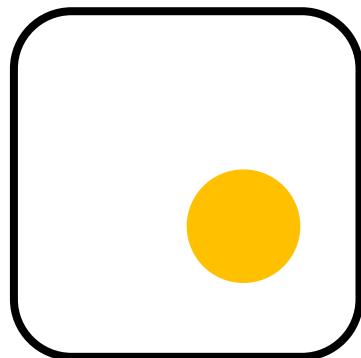
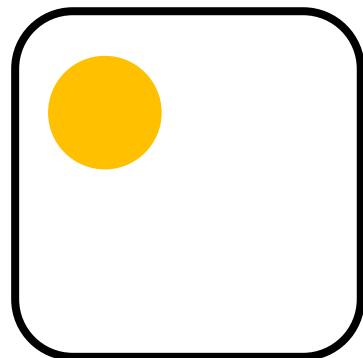
Toy Example

How would you get more data?



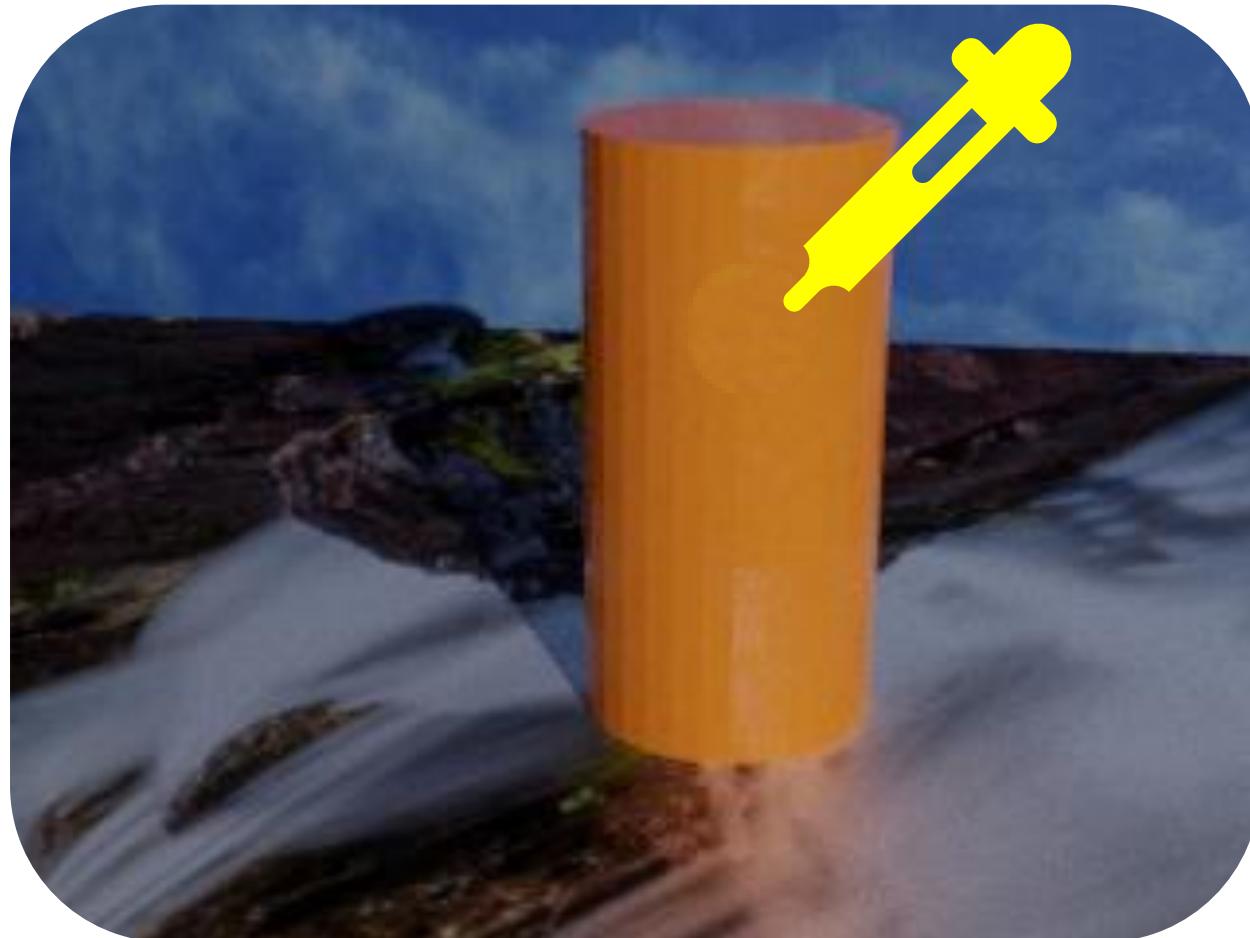
Simplified
Mathematical/Physical
Model

Data x

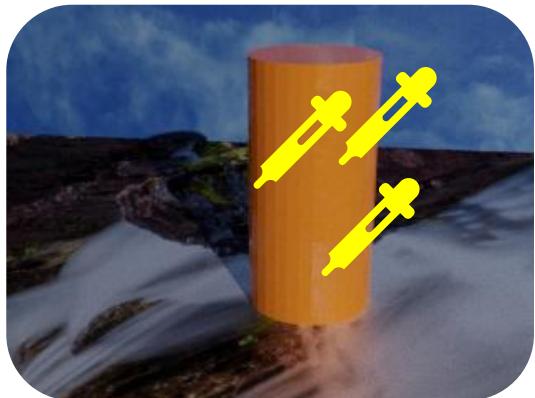


Latent Variables $z = [r, p]^T$

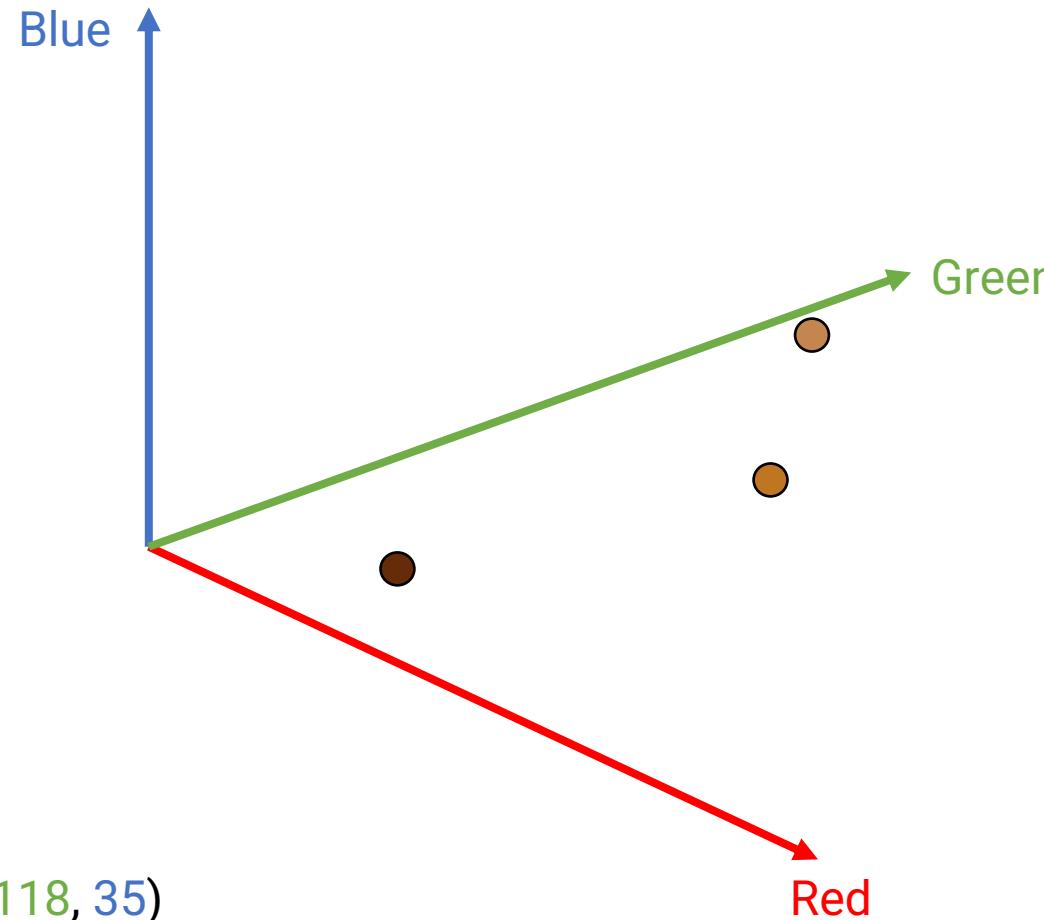
Is The Shape Actually Complex?



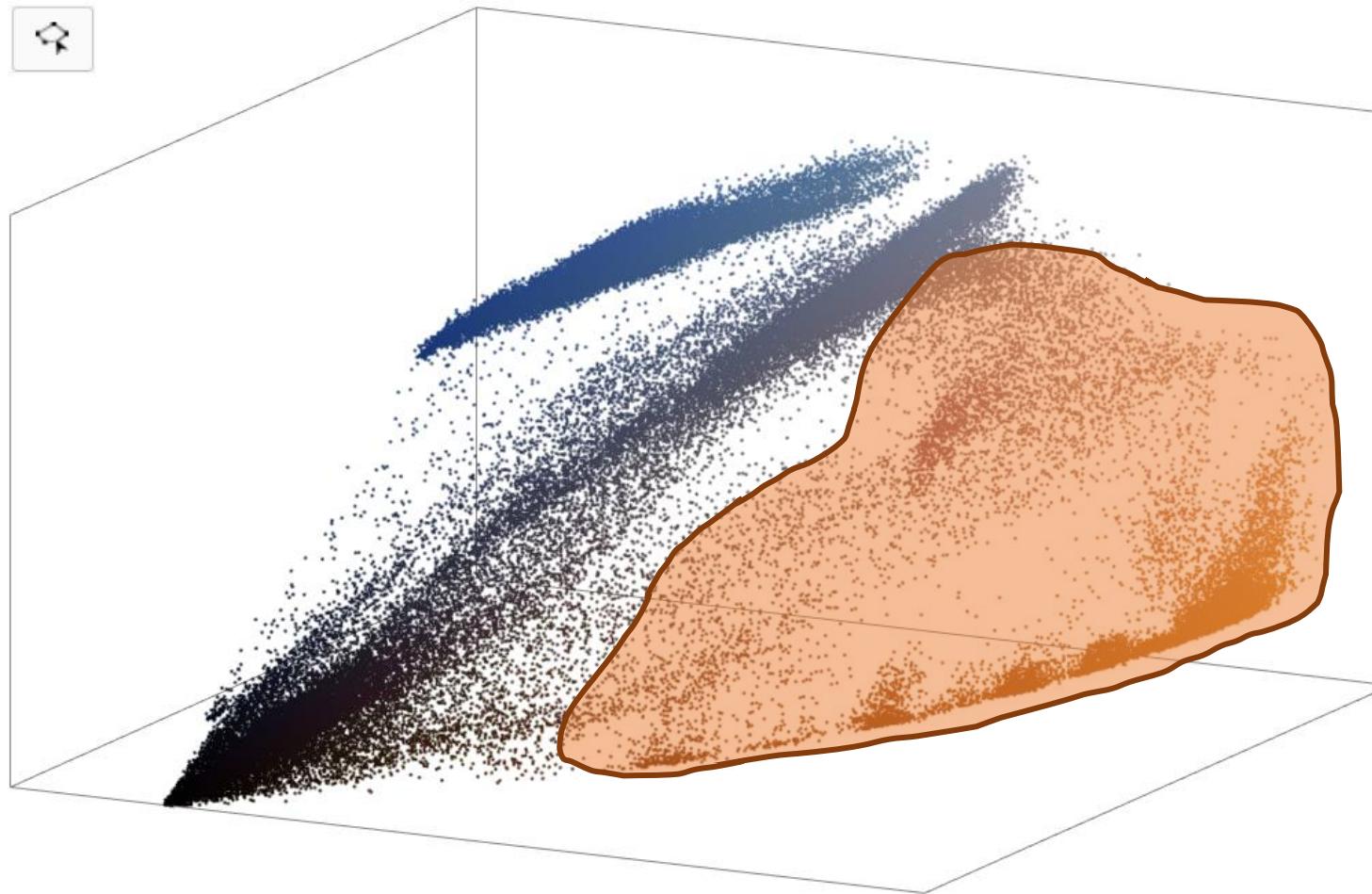
Is The Shape Actually Complex?



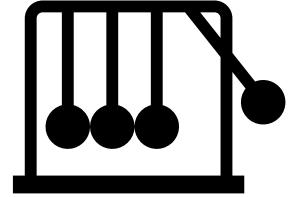
(192, 118, 35)



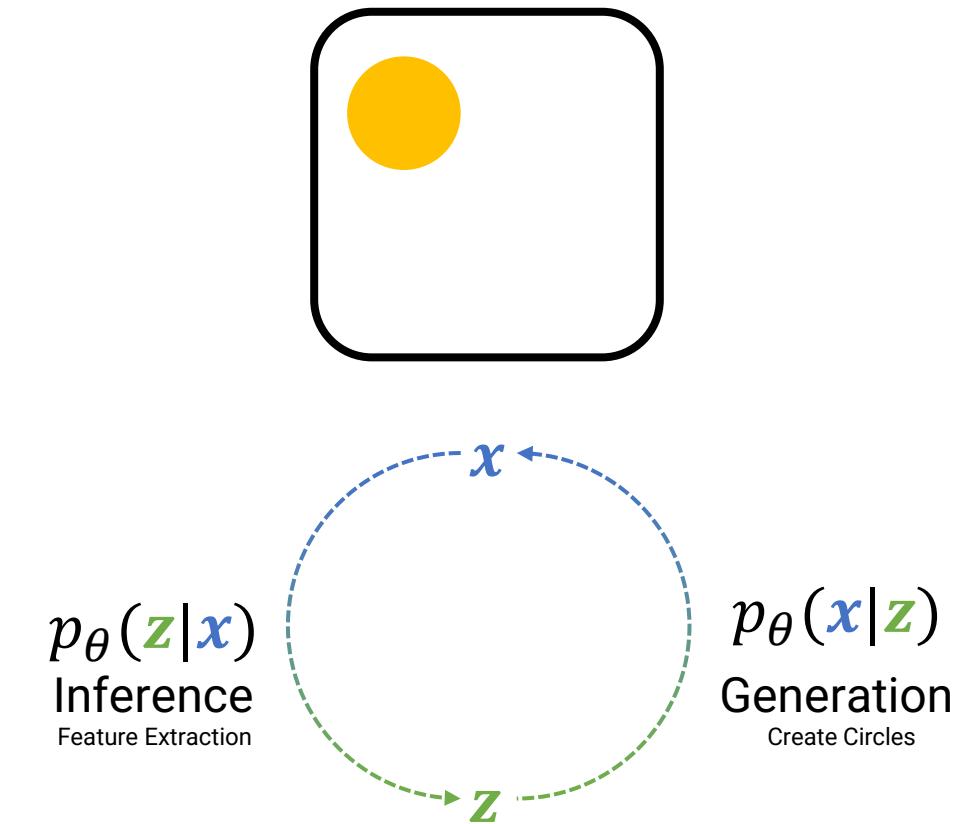
Is The Shape Actually Complex?



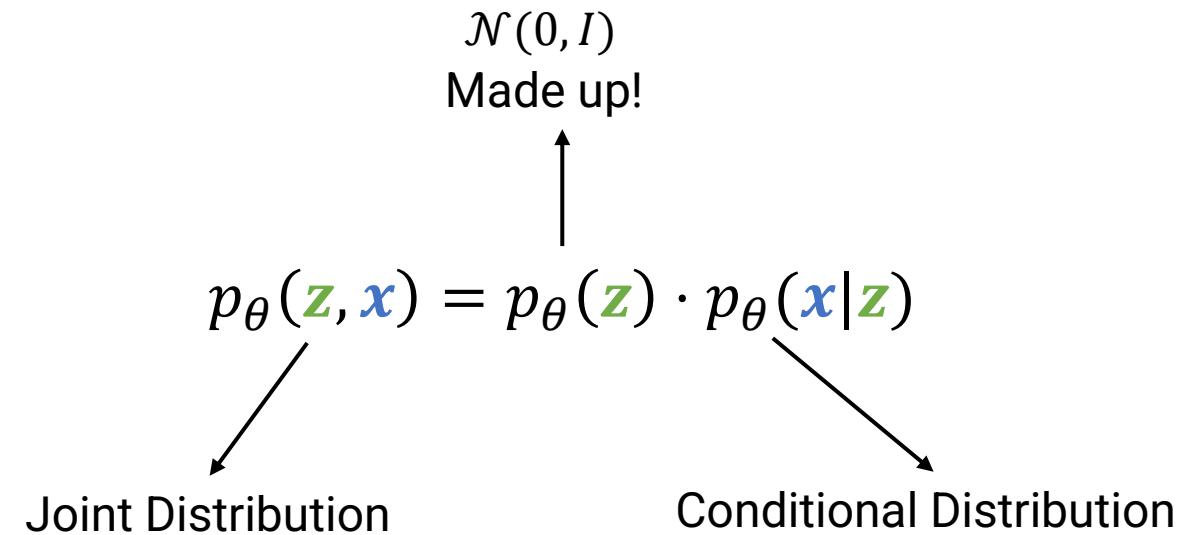
We Can Do Cool Stuff!



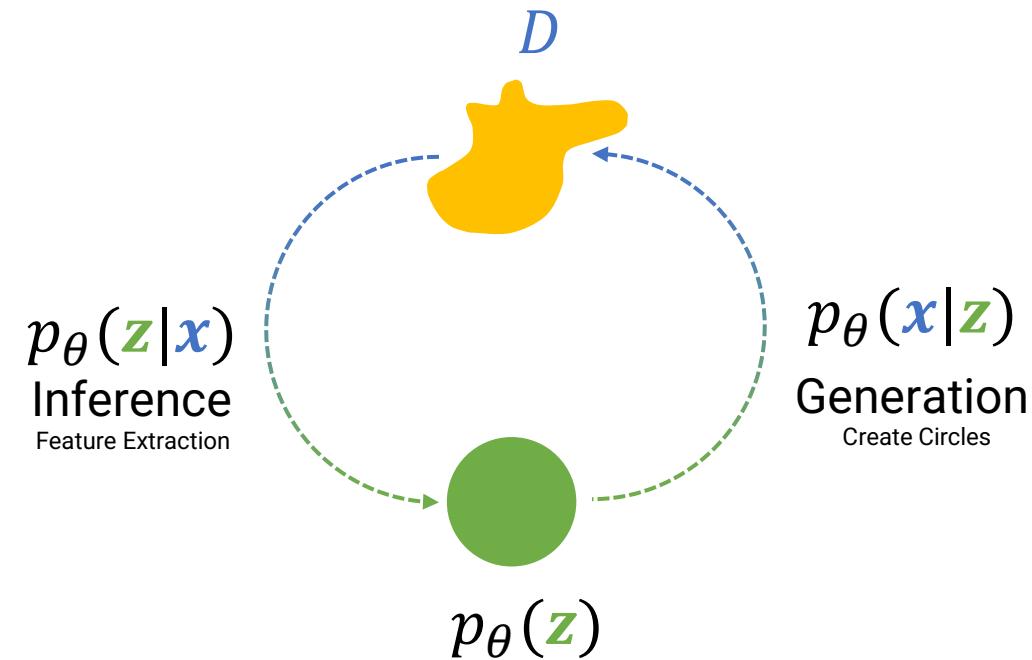
Simplified
Mathematical/Physical
Model



Time To Warm Up Probabilities!



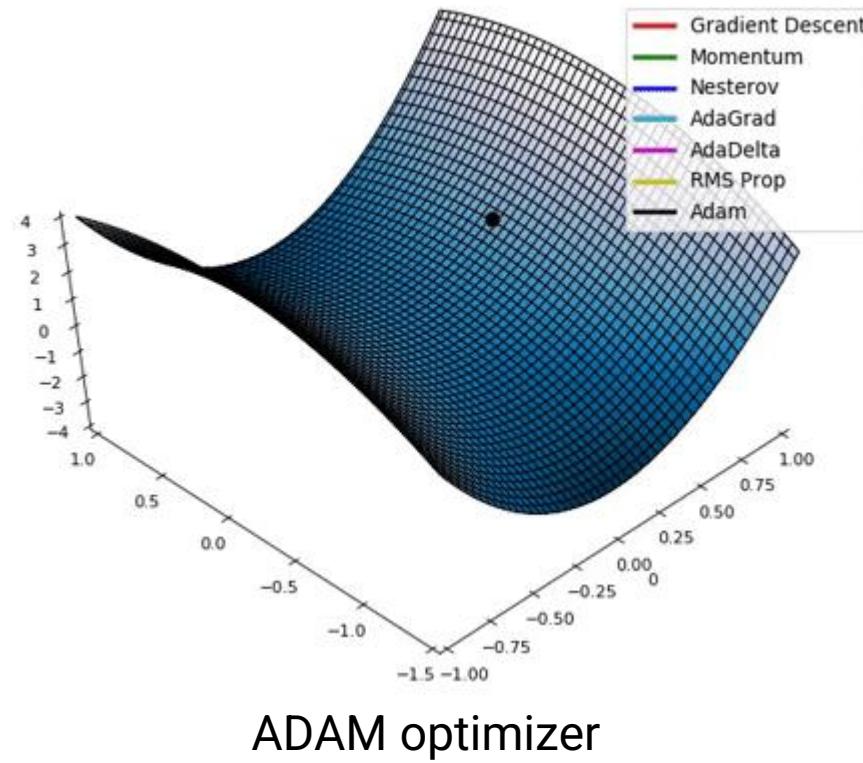
Esentially



Story Time



Diederik P. Kingma



Kingma, Diederik P. "Auto-encoding variational bayes." arXiv preprint arXiv:1312.6114 (2013).

Marginal Likelihood

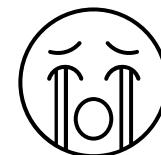
Marginal Likelihood

$$p_{\theta}(\mathbf{x}) = \int_{\mathbf{z}} p_{\theta}(\mathbf{z}, \mathbf{x})$$

Want it high for
data point $\mathbf{x} \in D$

$$= \int_{\mathbf{z}} p_{\theta}(\mathbf{z}) \cdot p_{\theta}(\mathbf{x}|\mathbf{z}) d\mathbf{z}$$

Intractable



Bayes' Rule

$$p(H|E) = \frac{p(H) \cdot p(E|H)}{p(E)}$$

The diagram illustrates the components of Bayes' Theorem. At the top, 'Prior' and 'Likelihood' are shown with arrows pointing towards the central formula. An arrow points from the formula down to 'Posterior' at the bottom left. Another arrow points from the formula down to 'Marginal Likelihood' and 'Model Evidence' at the bottom right.

$$p(\mathbf{z}|\mathbf{x}) = \frac{p(\mathbf{z}) \cdot p(\mathbf{x}|\mathbf{z})}{p(\mathbf{x})}$$

We want to find θ to maximize:

$$p_{\theta}(\mathbf{x}) = \frac{p_{\theta}(\mathbf{z}, \mathbf{x})}{p(\mathbf{z}|\mathbf{x})}$$

Intractable 😞



Variational Inference

$$q_{\phi}(\mathbf{z}|\mathbf{x}) \approx p_{\theta}(\mathbf{z}|\mathbf{x})$$

Approximation Target

If p is Bayesian \Rightarrow Variational Bayes

For same ϕ over all data \Rightarrow Amortized VI

We want to push the two distributions to be similar!

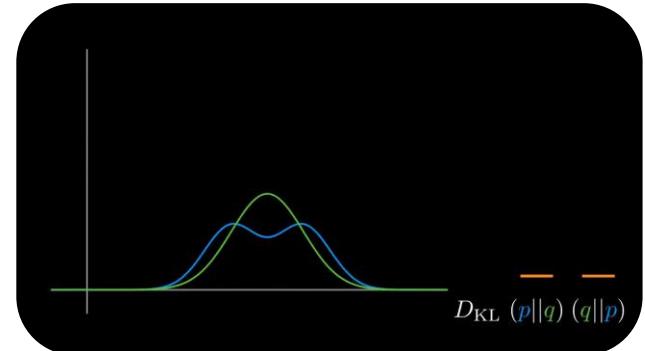
Kullback-Leibler (KL) Divergence

We need to measure how “close” two distributions are

$$D_{KL}(Q \parallel P) = \int_{\mathbf{z}} Q(\mathbf{z}) \log \left(\frac{Q(\mathbf{z})}{P(\mathbf{z})} \right) d\mathbf{z} \geq 0$$

Expected Information Loss due to approximation

⋮



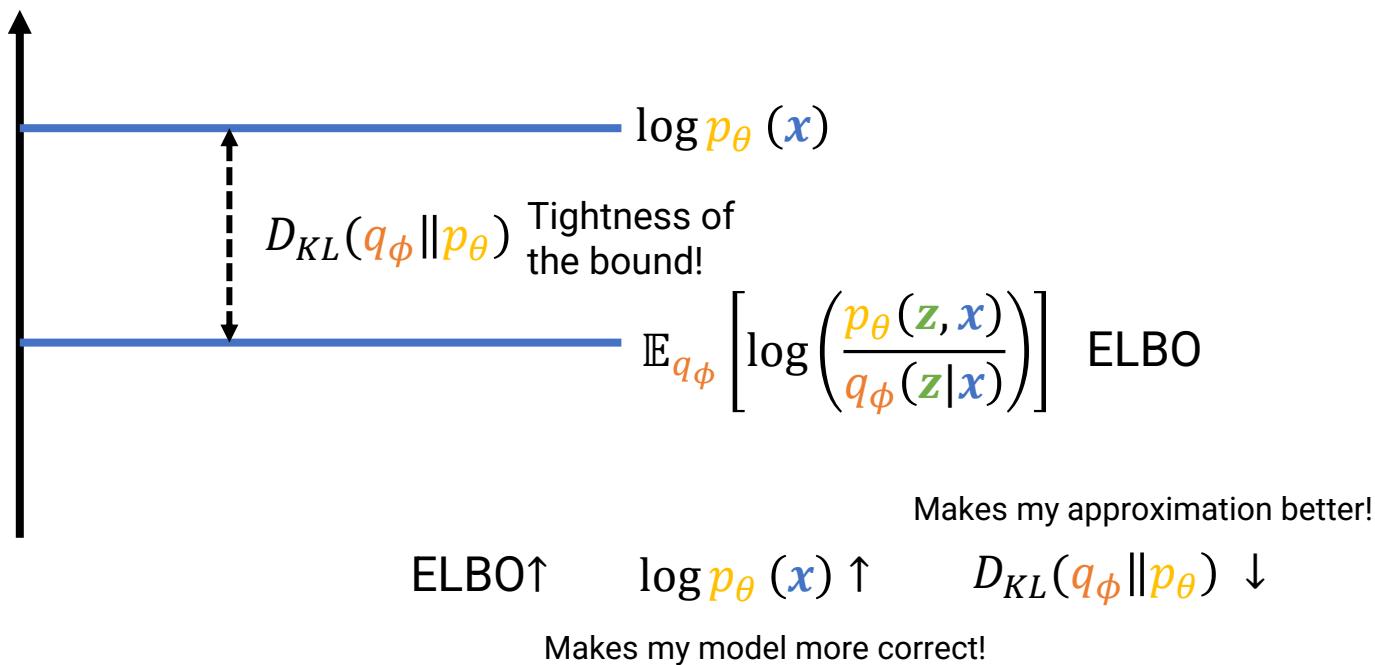
$$D_{KL}(q_\phi \parallel p_\theta) = \log p_\theta(\mathbf{x}) - \mathbb{E}_{q_\phi} [\log p_\theta(\mathbf{z}, \mathbf{x}) - \log q_\phi]$$

$$\log p_\theta(\mathbf{x}) = D_{KL}(q_\phi \parallel p_\theta) + \mathbb{E}_{q_\phi} [\log p_\theta(\mathbf{z}, \mathbf{x}) - \log q_\phi]$$

ELBO

$$\log p_{\theta}(\mathbf{x}) = D_{KL}(q_{\phi} \| p_{\theta}) + \mathbb{E}_{q_{\phi}}[\log p_{\theta}(\mathbf{z}, \mathbf{x}) - \log q_{\phi}]$$

$$\log p_{\theta}(\mathbf{x}) \geq \mathbb{E}_{q_{\phi}}[\log p_{\theta}(\mathbf{z}, \mathbf{x}) - \log q_{\phi}] \quad \text{Evidence Lower Bound (ELBO)}$$



Maximize ELBO!

Should be easy right?

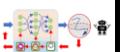
No 😞

We can't compute gradients easily!

No $\nabla_{\phi} q_{\phi}$ 😞

What can we do?

Approximate!



Reparametrization Trick

$\mathbf{z} = \mathbf{g}(\phi, \mathbf{x}, \epsilon)$ Trick is to make all stochasticity to come from ϵ
 $\epsilon \sim p(\epsilon)$ And maintain everything else to be deterministic ☺

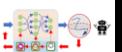
$$\mathcal{L}(\mathbf{x}) = \mathbb{E}_{p(\epsilon)} [\log p_\theta (\mathbf{z}, \mathbf{x}) - \log q_\phi (\mathbf{z}|\mathbf{x})]$$

$$\nabla_{\theta, \phi} \mathcal{L}(\mathbf{x}) \approx -\frac{1}{L} \sum_{i=1}^L \nabla_{\theta, \phi} [\log p_\theta (\mathbf{z}, \mathbf{x}) - \log q_\phi (\mathbf{z}|\mathbf{x})] \quad \text{Monte Carlo Sampling}$$

Stochastic Gradient Variational Bayes (SGVB)

$$\text{ELBO} = \mathbb{E}_{p(\epsilon)} \left[\log \left(\frac{p_\theta (\mathbf{z}, \mathbf{x})}{q_\phi (\mathbf{z}|\mathbf{x})} \right) \right]$$

$$\text{ELBO} \approx \left[\frac{1}{L} \sum_{i=1}^L \log p_\theta (\mathbf{x}|\mathbf{z}) \right] - D_{KL}(q_\phi (\mathbf{z}|\mathbf{x}) \| p_\theta (\mathbf{z})) \quad \text{Slow to compute! ☹}$$



All Hail The Gaussian!

$$q_{\phi}(\mathbf{z}|\mathbf{x}) = g(\phi, \mathbf{x}, \epsilon) = \mathcal{N}(\mu, \sigma)$$

$\epsilon \sim p(\epsilon)$ Sampling

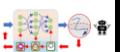
$$p_{\theta}(\mathbf{z}) = \mathcal{N}(0, I)$$

$\mu, \sigma = f(\mathbf{x})$ Deterministic

$$\text{ELBO} \approx \left[\frac{1}{L} \sum_{i=1}^L \log p_{\theta}(\mathbf{x}|\mathbf{z}) \right] - D_{KL}(q_{\phi}(\mathbf{z}|\mathbf{x}) \| p_{\theta}(\mathbf{z}))$$

$$\approx \left[\frac{1}{L} \sum_{i=1}^L \log p_{\theta}(\mathbf{x}|\mathbf{z}) \right] + \frac{1}{2} [\log \sigma^2 - \mu^2 - \sigma^2 + 1]$$

Done over Mini batch
Called Single Sample Monte Carlo



How Do You Compute $p_{\theta}(\mathbf{x}|\mathbf{z})$?

$$\mathbf{y} \sim p_{\theta}(\mathbf{x}|\mathbf{z})$$



V7 Chairs (Real-valued)

$$p_{\theta}(\mathbf{x}|\mathbf{z}) = \mathcal{N}(y_{\mu}, y_{\sigma})$$

Gaussian!



Binarized MNIST (Binary-valued)

$$p_{\theta}(\mathbf{x}|\mathbf{z}) = \text{Bernoulli}(y)$$

Bernoulli!

Practically

$$\log p_{\theta}(\mathbf{x}|\mathbf{z}) = \mathcal{N}(\mathbf{y}_{\mu}, \mathbf{y}_{\sigma})$$

$$\log p_{\theta}(\mathbf{x}|\mathbf{z}) = -\log y_{\sigma} - \log \sqrt{2\pi} - \frac{1}{2y_{\sigma}^2} (\mathbf{x} - \mathbf{y}_{\mu})^2$$

$\log p_{\theta}(\mathbf{x}|\mathbf{z}) \uparrow \quad (\mathbf{x} - \mathbf{y}_{\mu}) \downarrow \quad y_{\sigma} \downarrow$ Numerical Instability

Focus on some data variables

Only work well on some pixels

Set $y_{\sigma} = 1$

Becomes MSE ☺

$$\log p_{\theta}(\mathbf{x}|\mathbf{z}) = \text{Bernoulli}(y)$$

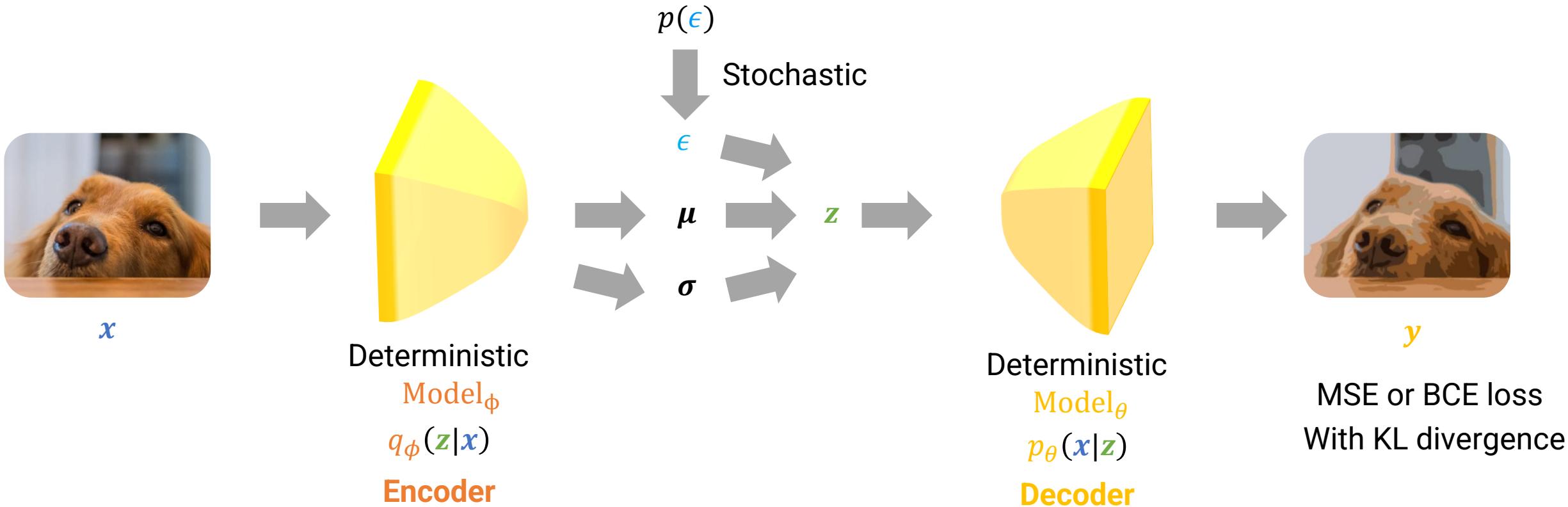
$$\text{Bernoulli}(\mathbf{x}; p) = p^{\mathbf{x}} (1-p)^{1-\mathbf{x}}; \mathbf{x} \in \{0,1\}$$

$$\log p_{\theta}(\mathbf{x}|\mathbf{z}) = \sum_{i=1}^D \mathbf{x}_i \log y_i + (1 - \mathbf{x}_i) \log(1 - y_i)$$

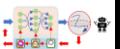
Becomes BCE (Binary Cross Entropy) ☺



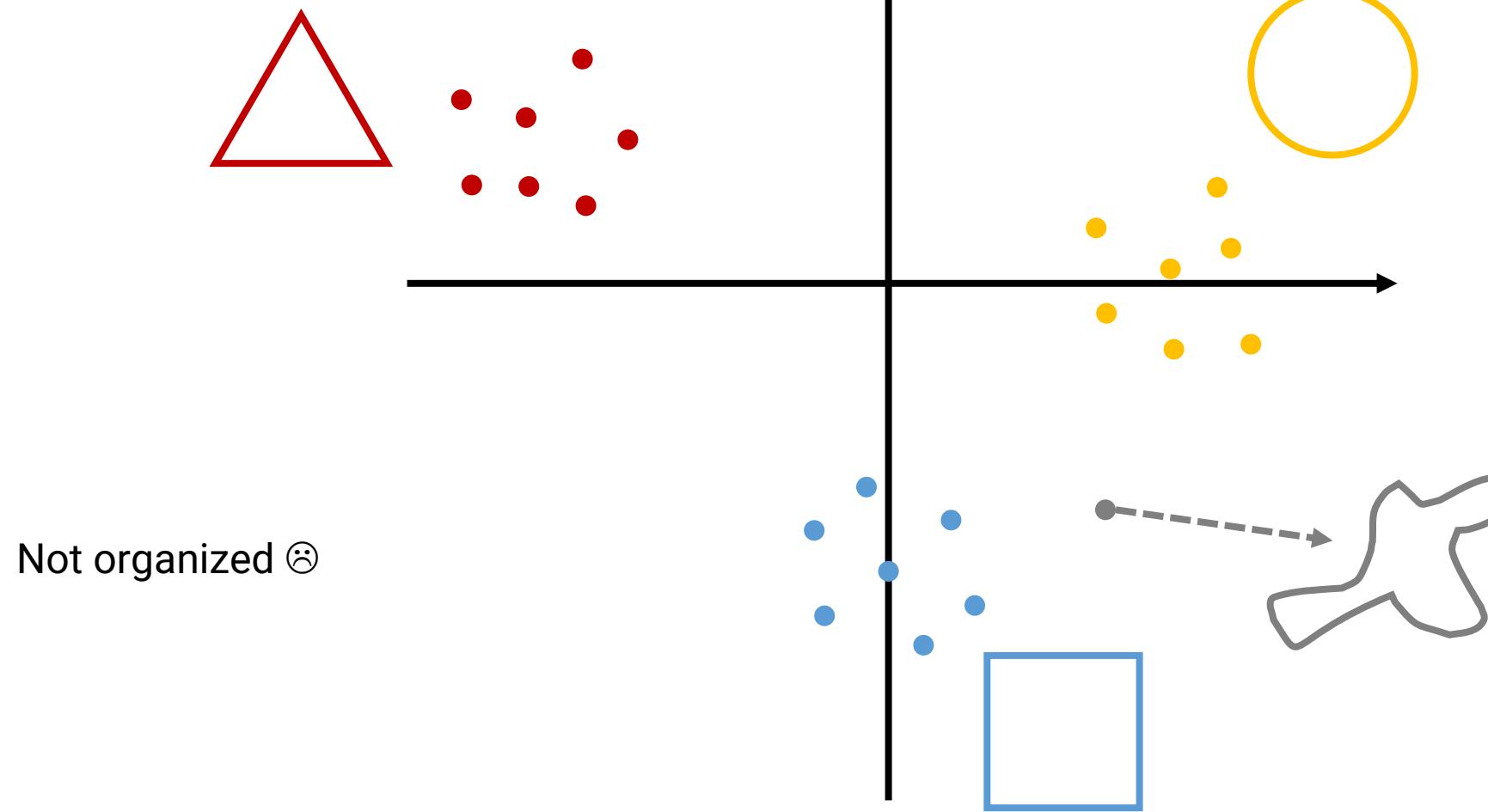
Variational Auto Encoder



Kingma, Diederik P. "Auto-encoding variational bayes." arXiv preprint arXiv:1312.6114 (2013).

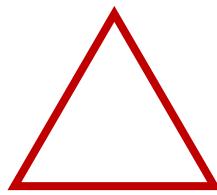


Latent Space

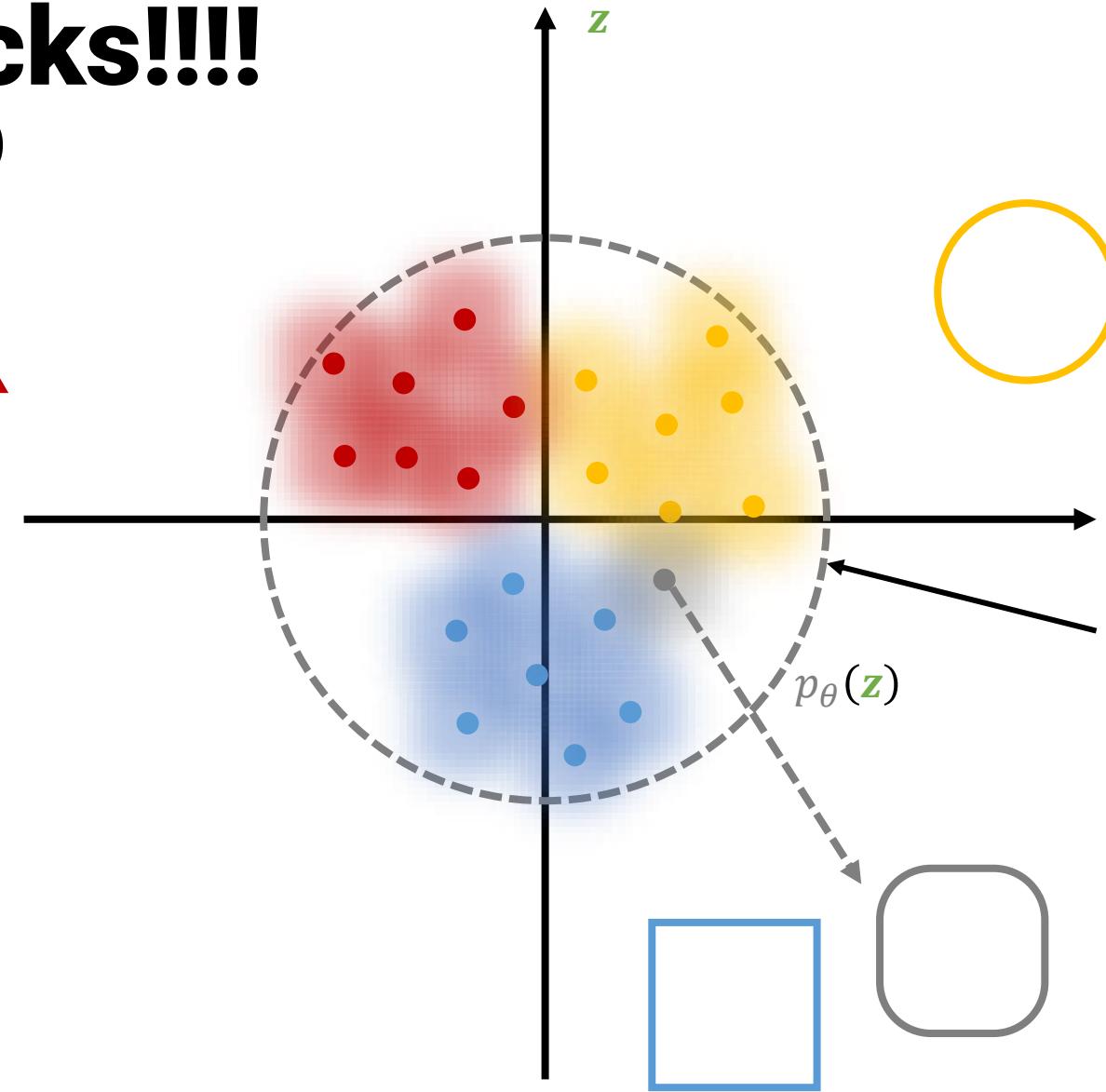


VAE Rocks!!!!

$$D_{KL}(q_\phi(\mathbf{z}|\mathbf{x})\|p_\theta(\mathbf{z}))$$

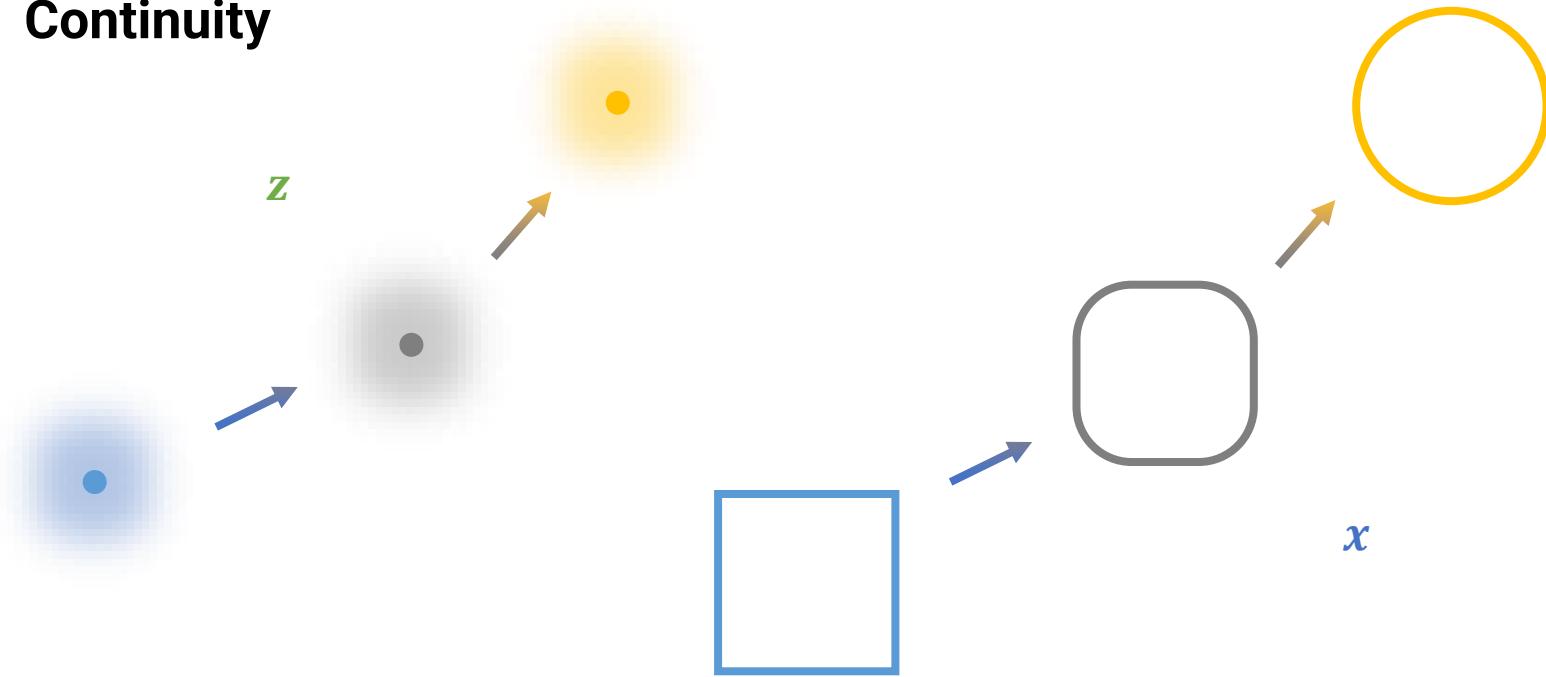


Well organized 😊



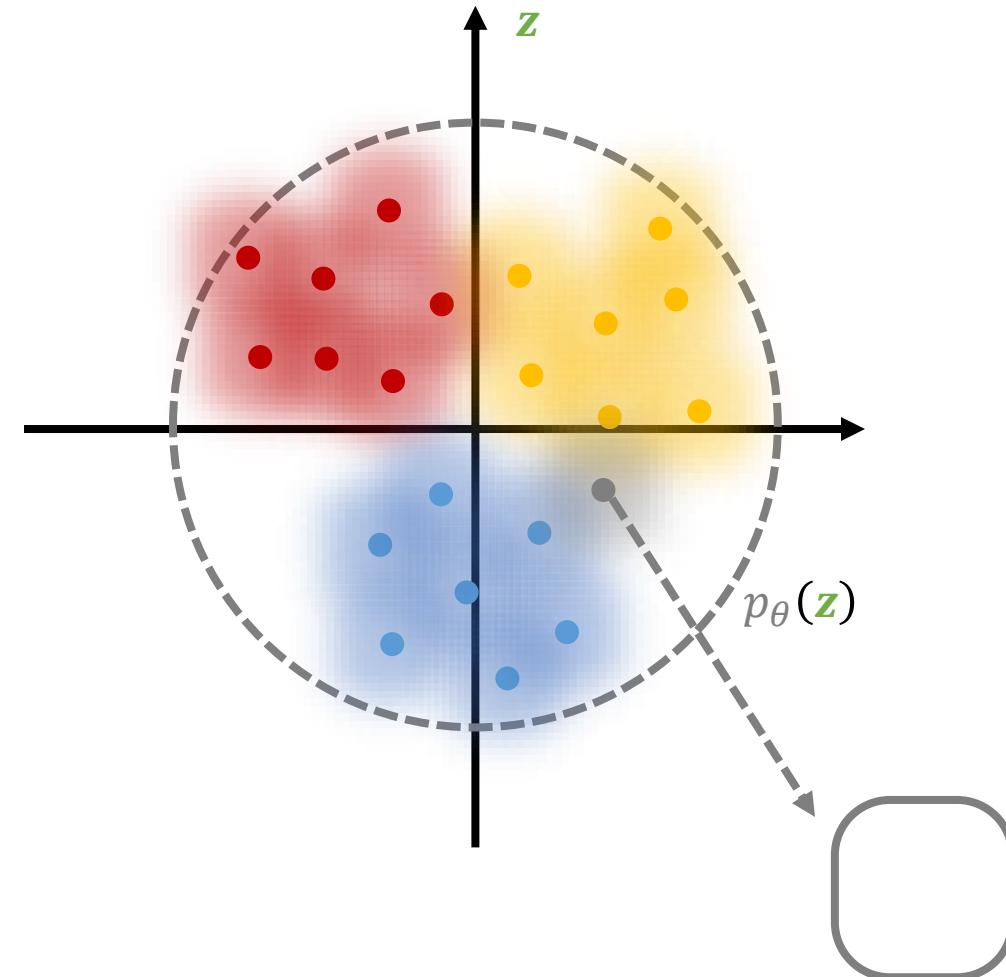
Awesome Latent Space!

Continuity



Awesome Latent Space!

Completeness



Beta VAE

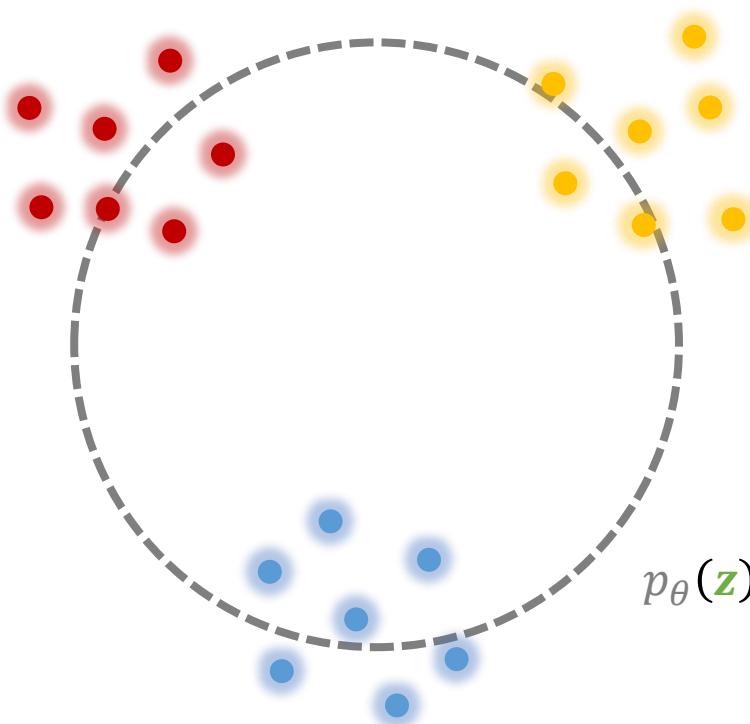
VAE

$$\mathcal{L} = \mathcal{L}_{\text{recons}} + \mathcal{L}_{\text{KL}}$$

Weighted Loss

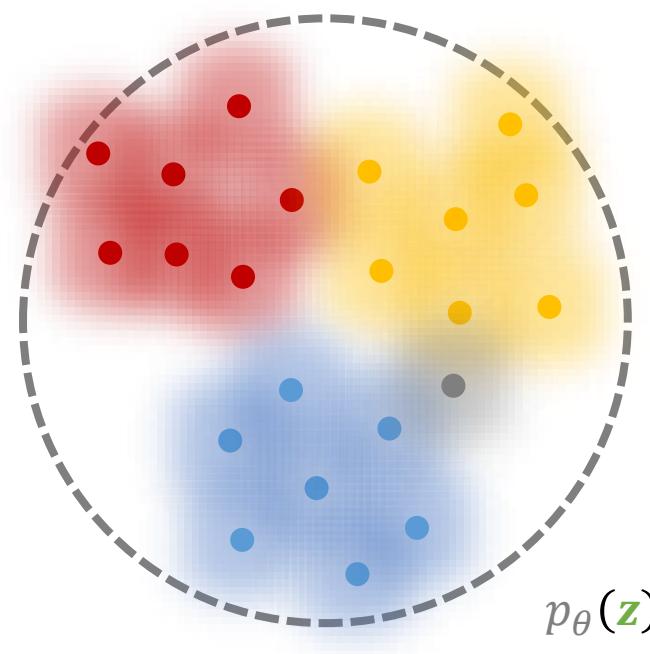
$$\mathcal{L} = \alpha \mathcal{L}_{\text{recons}} + \beta \mathcal{L}_{\text{KL}}$$

$$\alpha \gg \beta$$



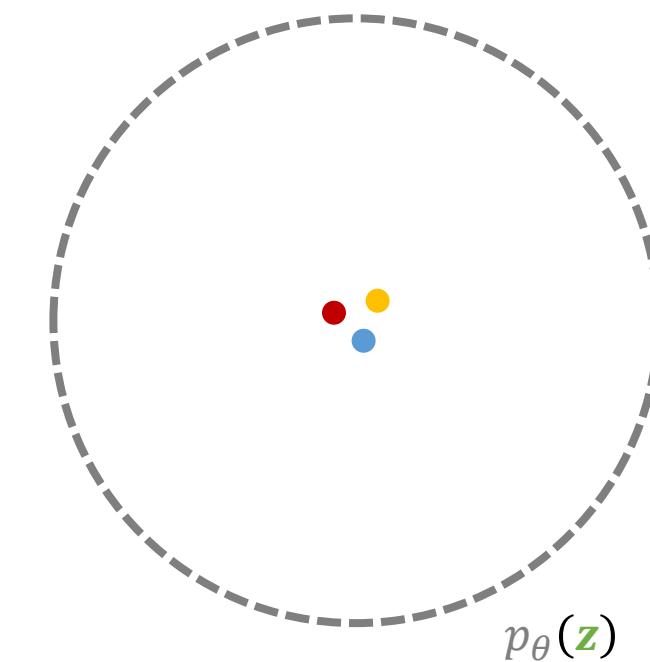
Discontinuity like Autoencoder

Doesn't mean $\beta = \alpha$

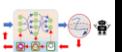


Balanced

$$\beta \gg \alpha$$



No reconstructive capacity

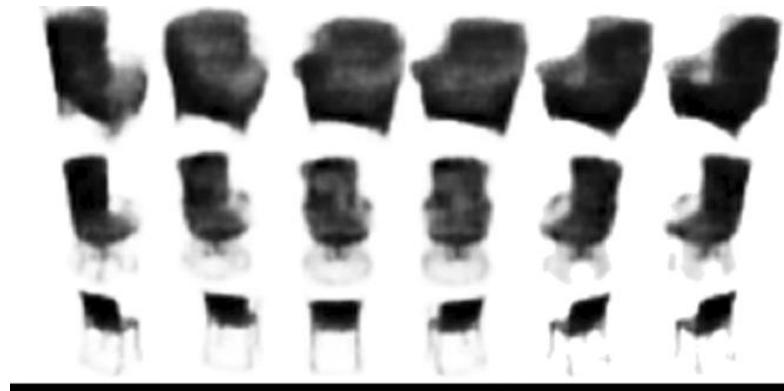


Beta VAE

$$\mathcal{L} = \mathcal{L}_{\text{recons}} + \beta \mathcal{L}_{\text{KL}}$$

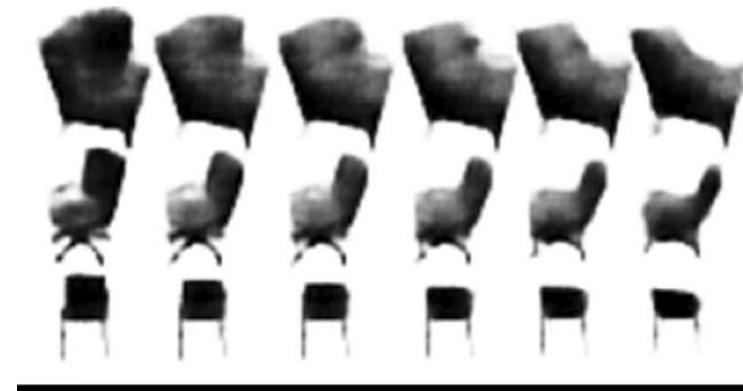
$$\beta > 1$$

Rotation

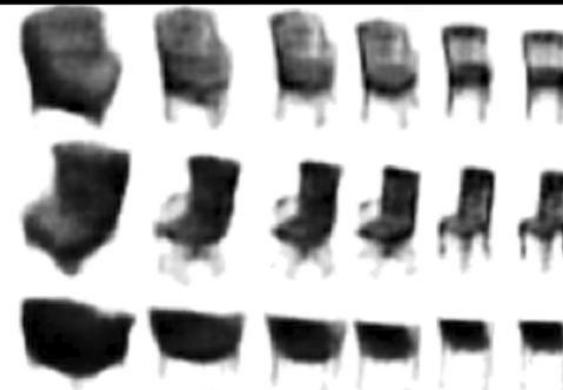


$$\beta = 1$$

Rotation/Size



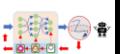
Size



Rotation/Size

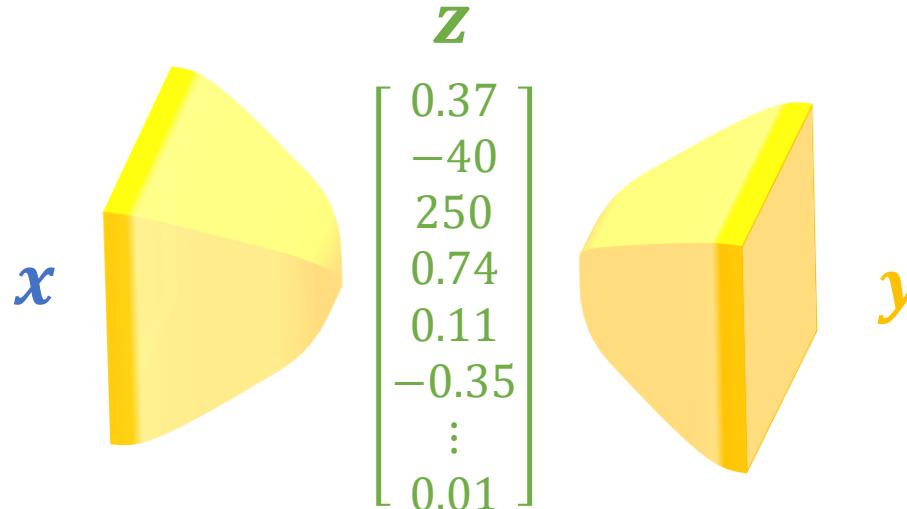
VAE Recap

$$\mathcal{L}(\theta, \phi, \mathbf{x}, \mathbf{z}) = \underbrace{-\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})}[\log p_\theta(\mathbf{x}|\mathbf{z})]}_{l_2 \text{ Loss}} + \overbrace{D_{KL}(q_\phi(\mathbf{z}|\mathbf{x}) \| p_\theta(\mathbf{z}))}^{\text{Latent Space Regularization Distribution (KL) Loss}}$$

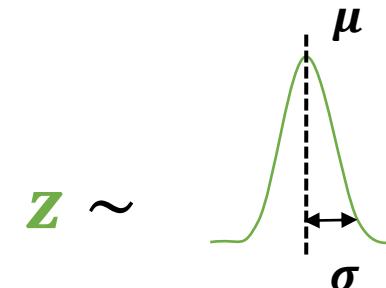


VAE Recap

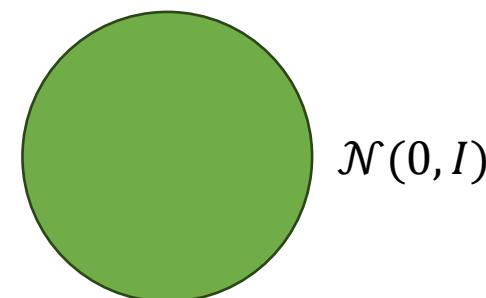
1. Continuous Latent Space



2. Gaussian $q_{\phi}(\mathbf{z}|\mathbf{x})$



3. Pre-defined $p_{\theta}(\mathbf{z})$



4. Loss function

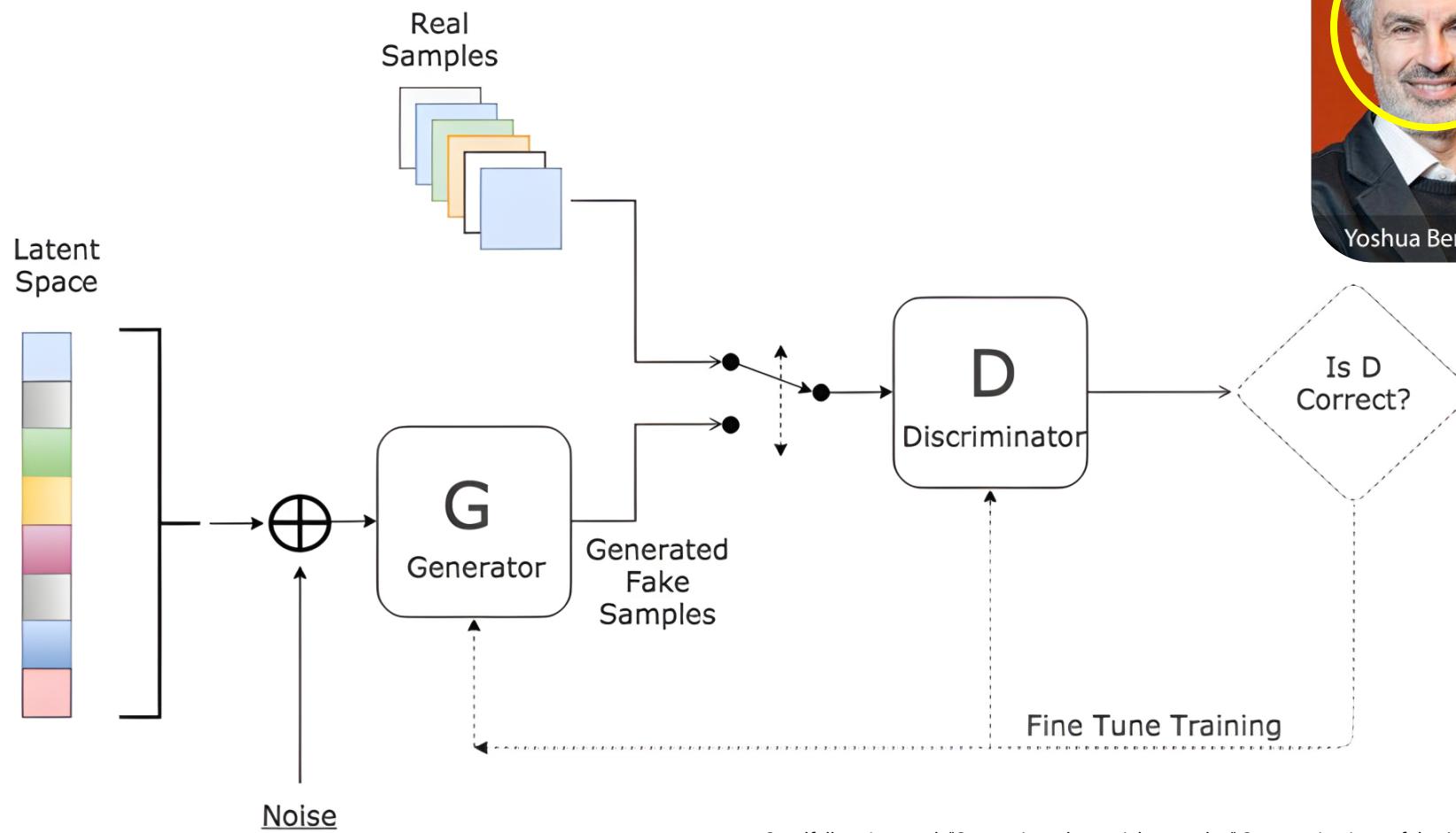
$$\mathcal{L}(\theta, \phi, \mathbf{x}, \mathbf{z}) = -\mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})}[\log p_{\theta}(\mathbf{x}|\mathbf{z})] + D_{KL}(q_{\phi}(\mathbf{z}|\mathbf{x}) \| p_{\theta}(\mathbf{z}))$$



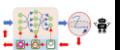
Deep Fakes

Generative Adversarial Networks

Let's Not Model Explicit Density Function

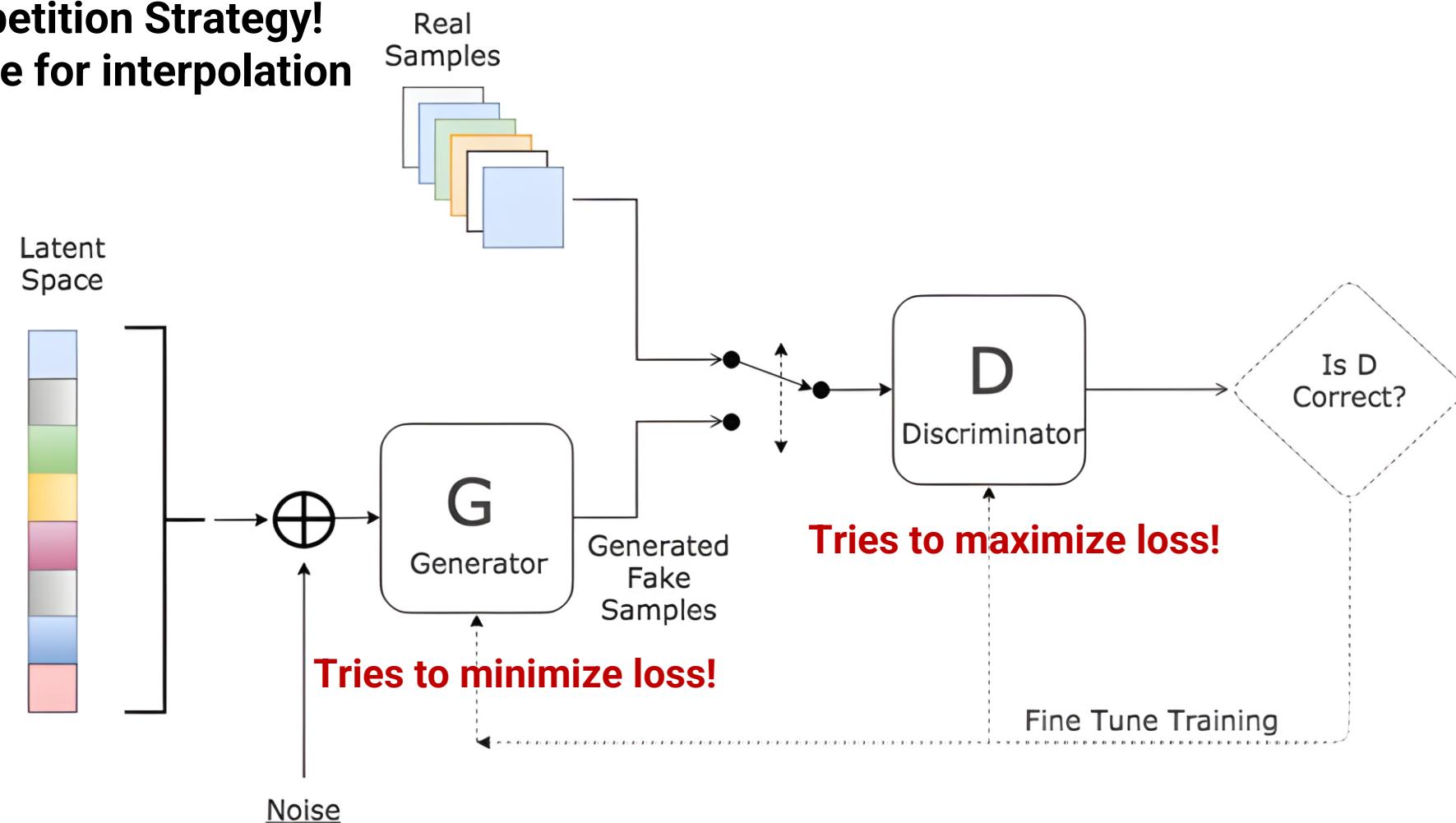


Goodfellow, Ian, et al. "Generative adversarial networks." Communications of the ACM 63.11 (2020): 139-144. [CVPR 2018 Tutorial on GANs \(google.com\)](https://www.cvpr2018.org/tutorials/gans/)



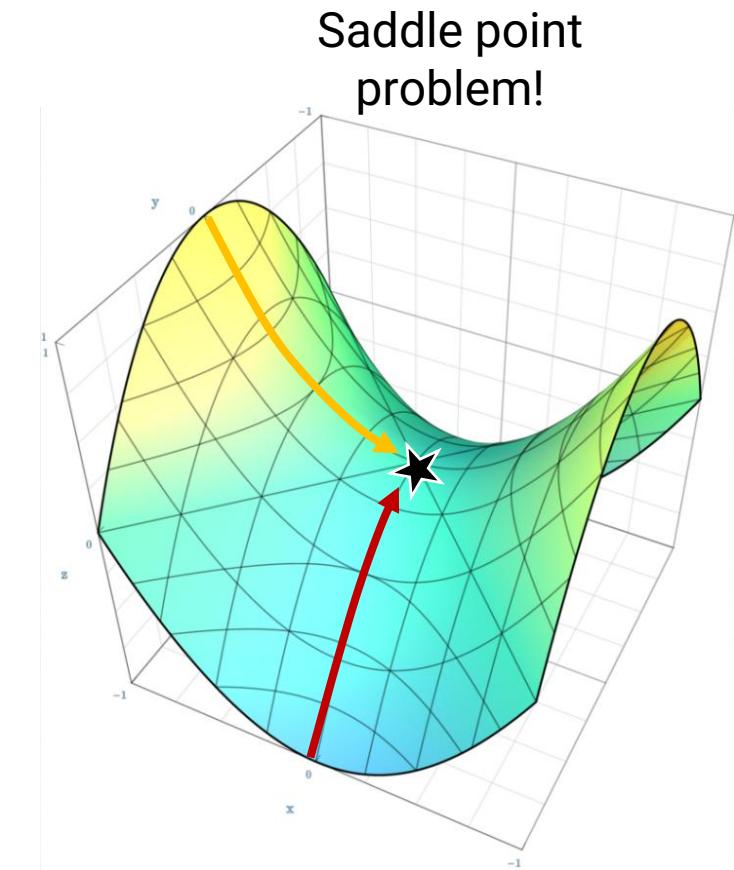
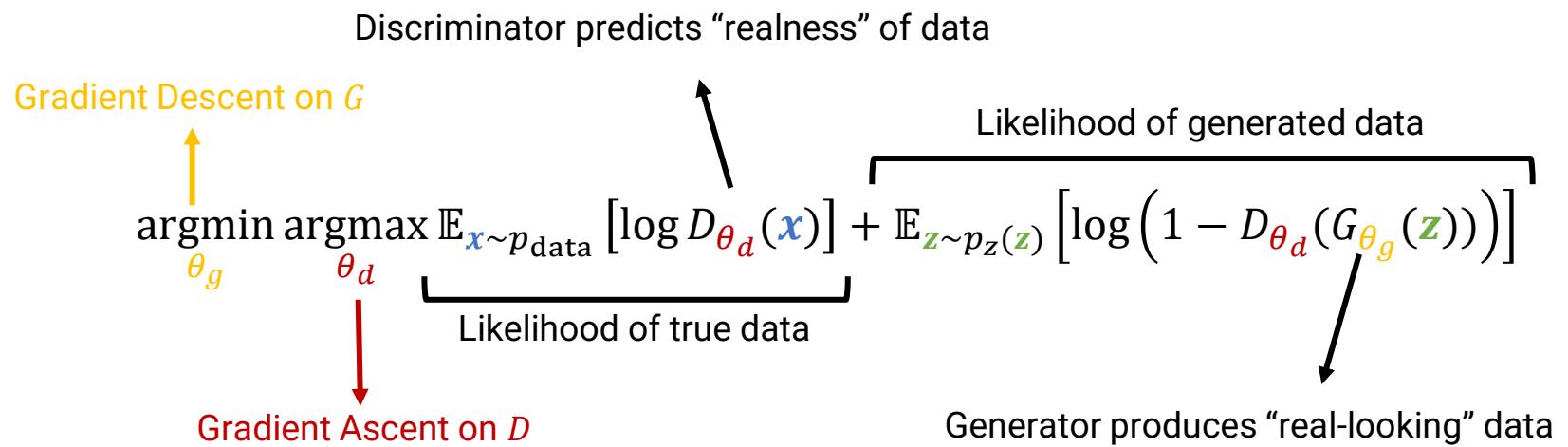
Generative Adversarial Networks

Use A Competition Strategy!
Latent Space for interpolation



Loss Function

Two-player min-max game



GAN Gremlins!



Inherently unstable to train 😞

Vanishing Gradients

D becomes “too good” faster and G gradients become 0

Non-Convergence

D and G oscillate without reaching equilibrium

Mode Collapse

G will only generate a small set of examples (low diversity)

Mode Dropping

G does not cover the data distribution

GAN Gremlins!

Vanishing Gradients



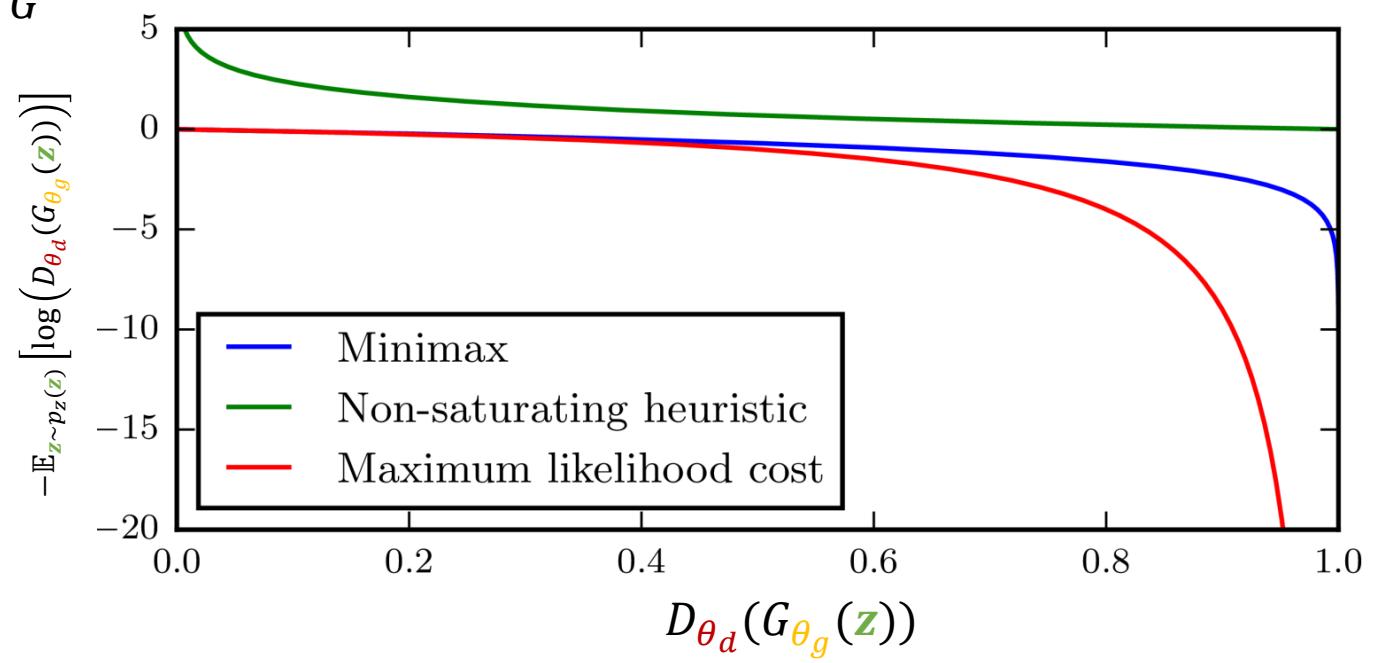
$$\operatorname{argmin}_{\theta_g} \operatorname{argmax}_{\theta_d} \mathbb{E}_{x \sim p_{\text{data}}} [\log D_{\theta_d}(x)] + \mathbb{E}_{z \sim p_z(z)} [\log (1 - D_{\theta_d}(G_{\theta_g}(z)))]$$

Use a non-saturating heuristic objective for G

$$-\mathbb{E}_{z \sim p_z(z)} [\log (D_{\theta_d}(G_{\theta_g}(z)))]$$

Limit D capacity

Schedule learning between G and D



GAN Gremlins!

Non-Convergence



Generally, hacks with not much mathematical backing

Use soft and Noisy Labels

Use DCGAN and Hybrid Models

Use stability tricks from Reinforcement Learning

Use ADAM optimizer

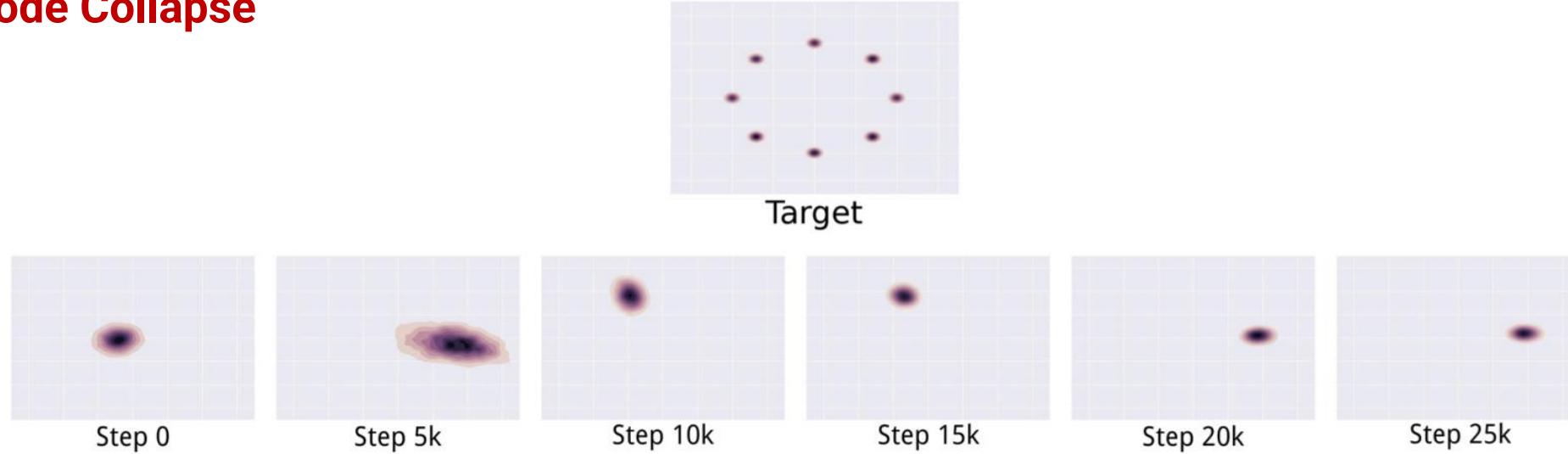
[soumith/ganhacks: starter from "How to Train a GAN?" at NIPS2016 \(github.com\)](https://github.com/soumith/ganhacks)



GAN Gremlins!



Mode Collapse



Use divergence measures like KL (Recall VAE) Check f-GAN

Use Integral Probability metrics like Earth Movers Distance Check Wasserstein GAN, Fisher GAN and Sobolev GAN

GANs Work Well....

VAE



VAE_{Dis_l}



VAE/GAN

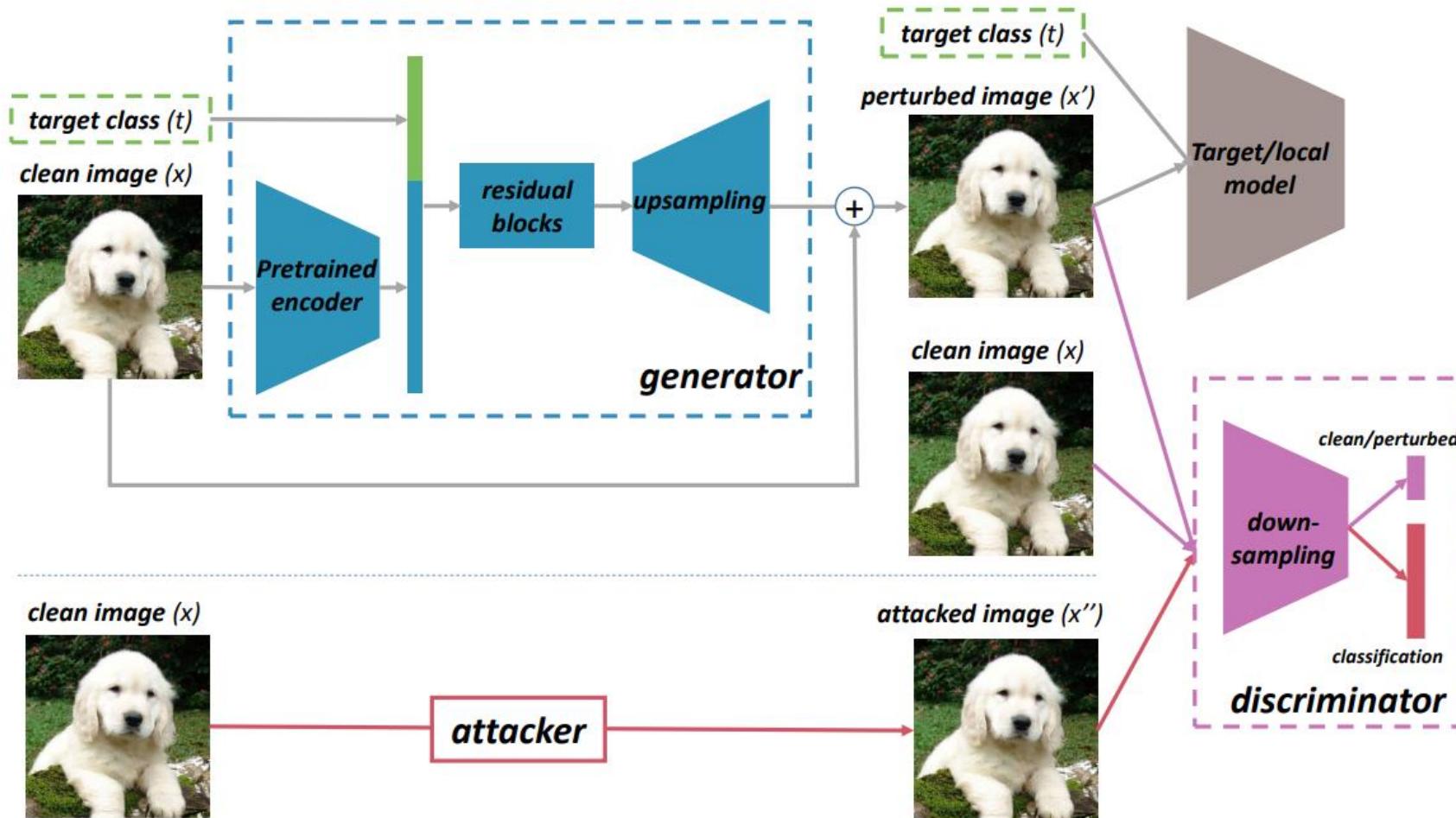


GAN



Well almost well....

AI-GAN



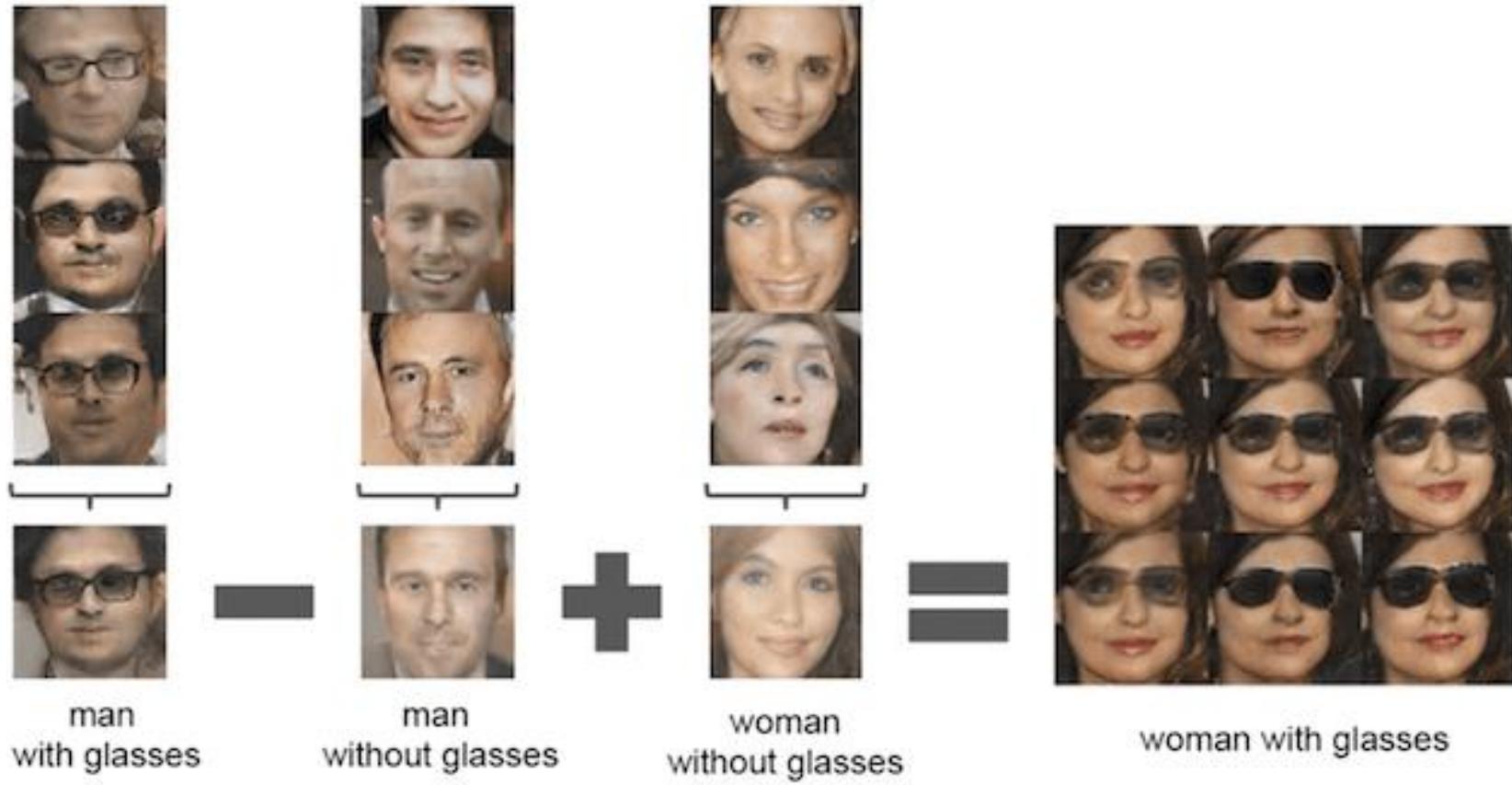
Bai, Tao, et al. "Ai-gan: Attack-inspired generation of adversarial examples." 2021 IEEE International Conference on Image Processing (ICIP). IEEE, 2021.

AI-GAN



Generative Models Can Do Cool Stuff!

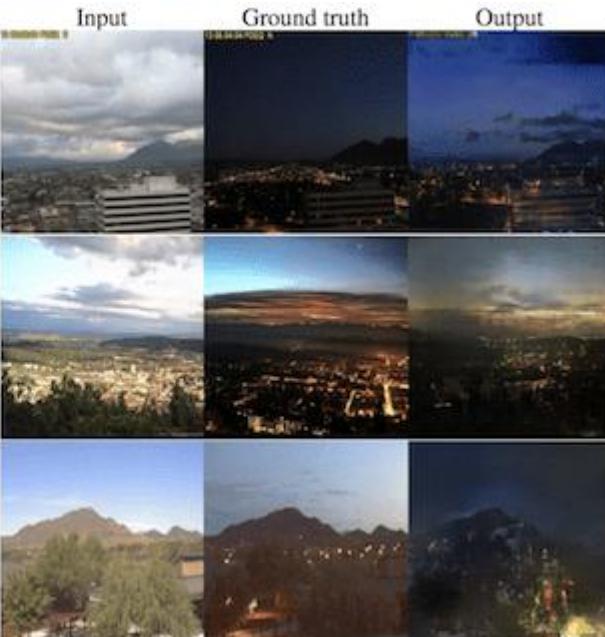
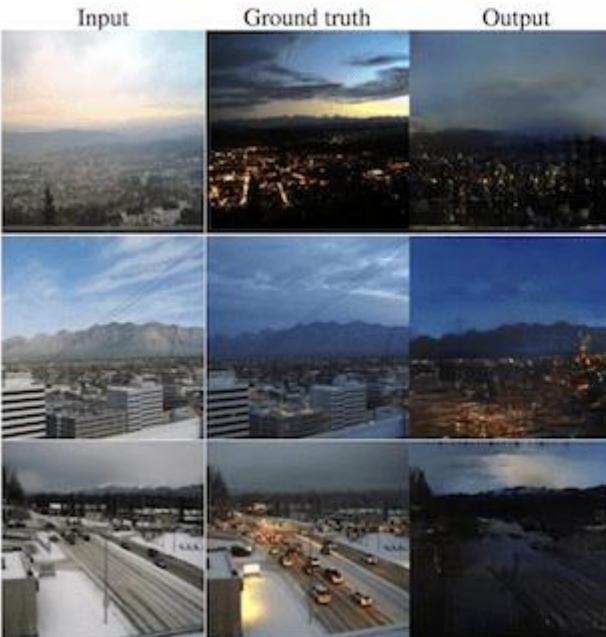
Generation with Latent Space Arithmetic



18 Impressive Applications of Generative Adversarial Networks (GANs) - MachineLearningMastery.com

Generative Models Can Do Cool Stuff!

Image To Image Translation AKA pix2pix



Generative Models Can Do Cool Stuff!

Text2Image

The small bird has a red head with feathers that fade from red to gray from head to tail

Stage-I
images



Stage-II
images

This bird is black with green and has a very short beak

Stage-I
images



Stage-II
images

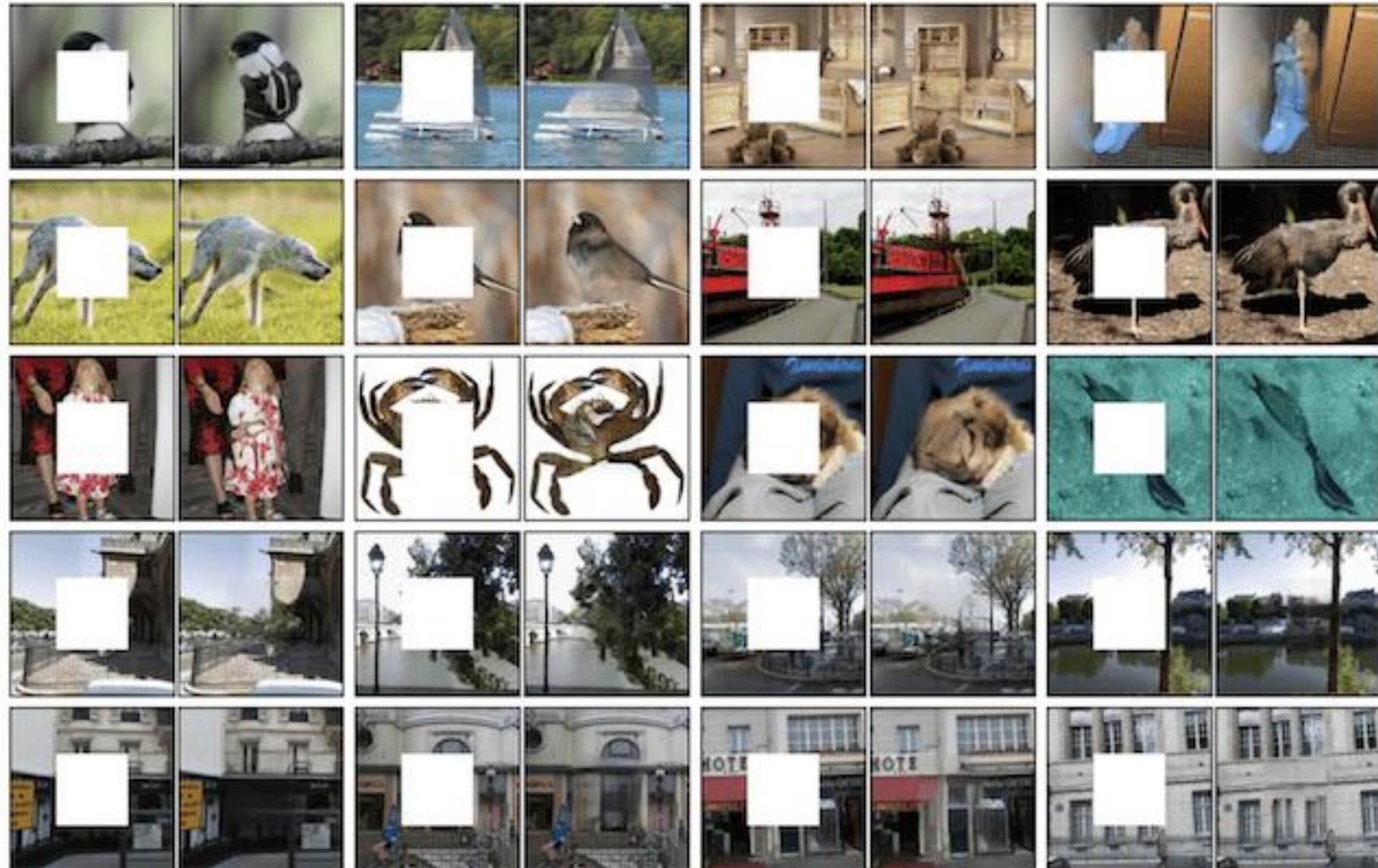
Generative Models Can Do Cool Stuff!

Super Resolution



Generative Models Can Do Cool Stuff!

Inpainting

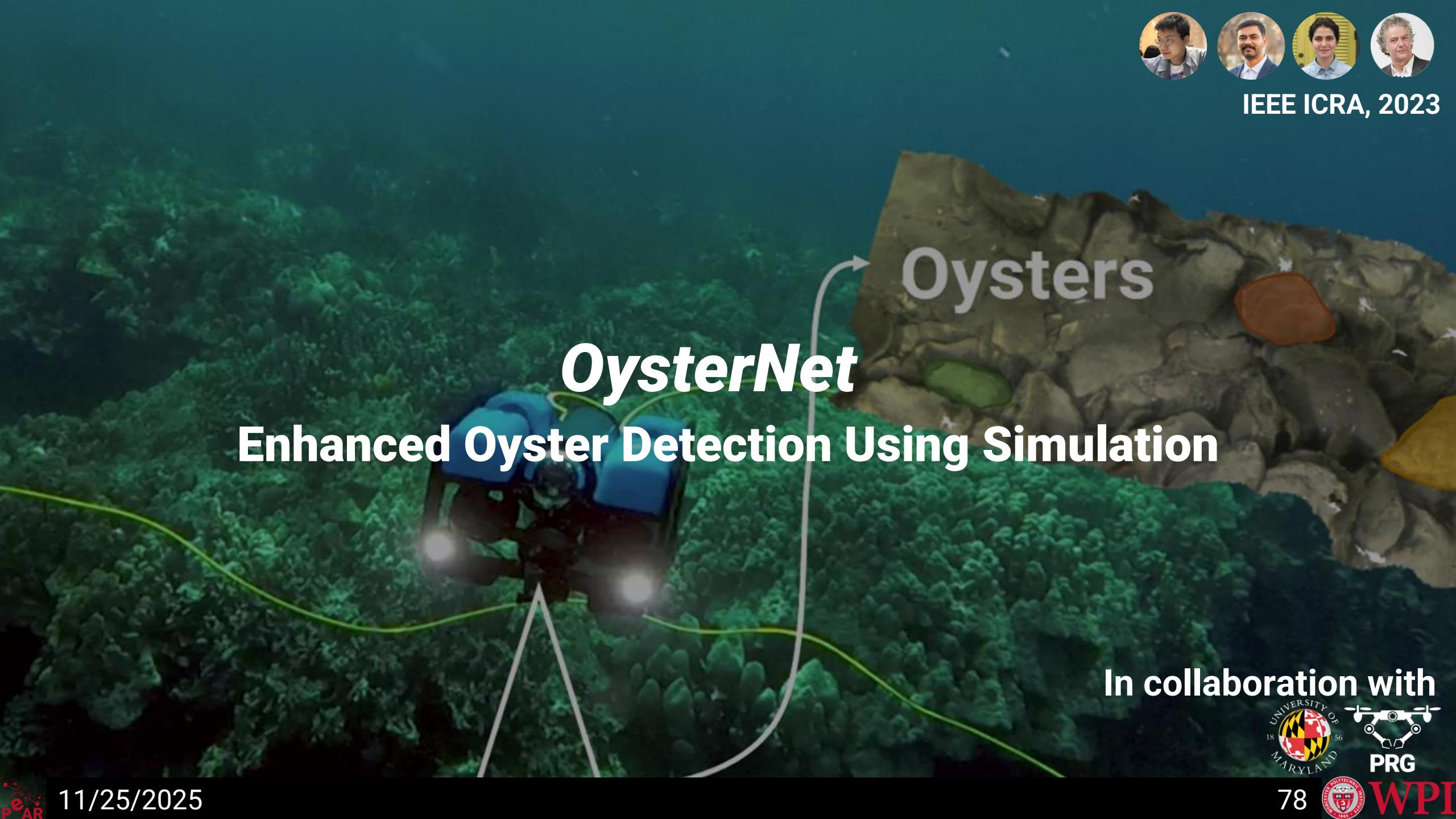




Generate A LOT Of Data



IEEE ICRA, 2023



OysterNet

Enhanced Oyster Detection Using Simulation

In collaboration with



PRG

WPI

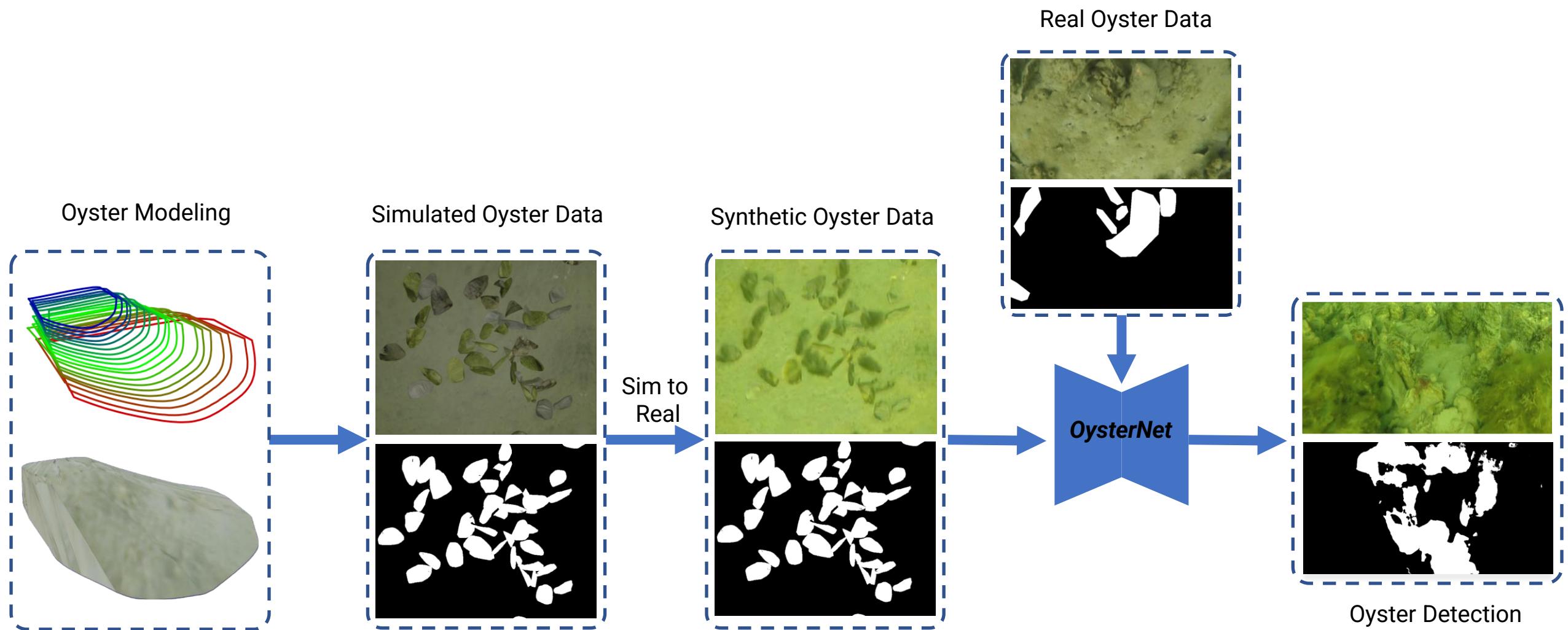
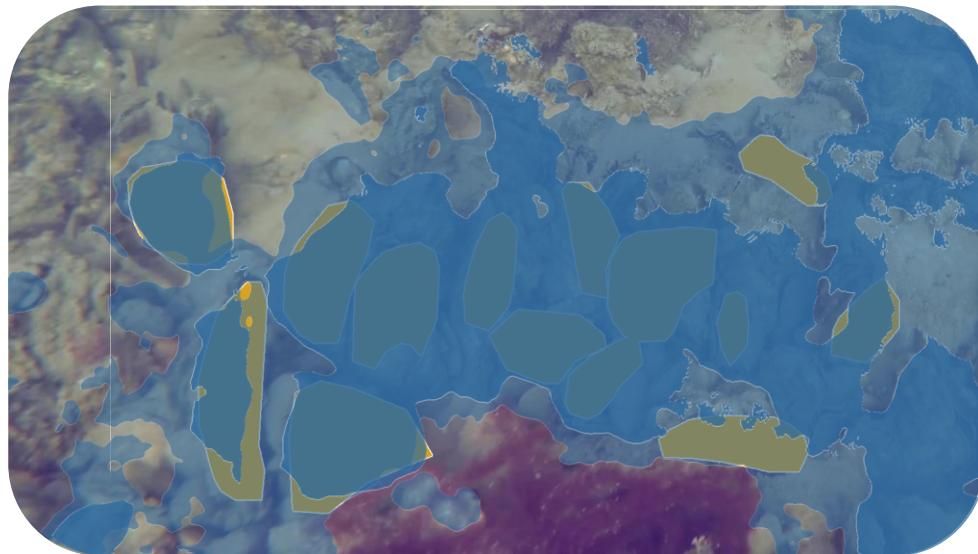
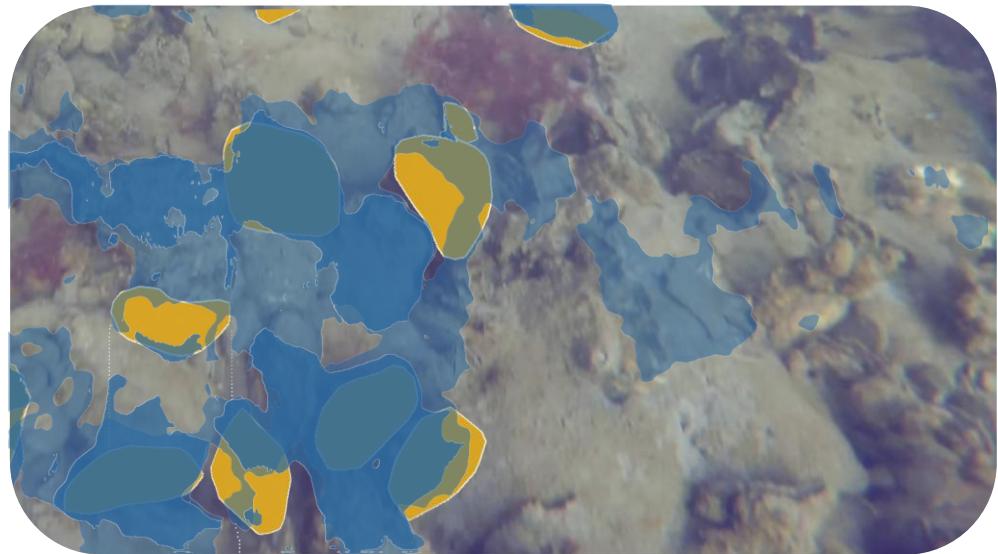


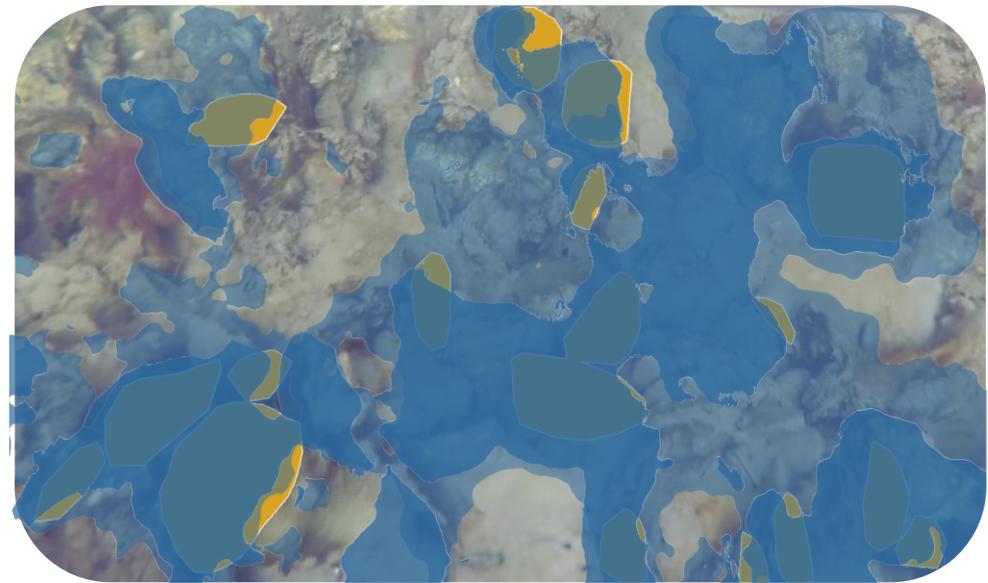
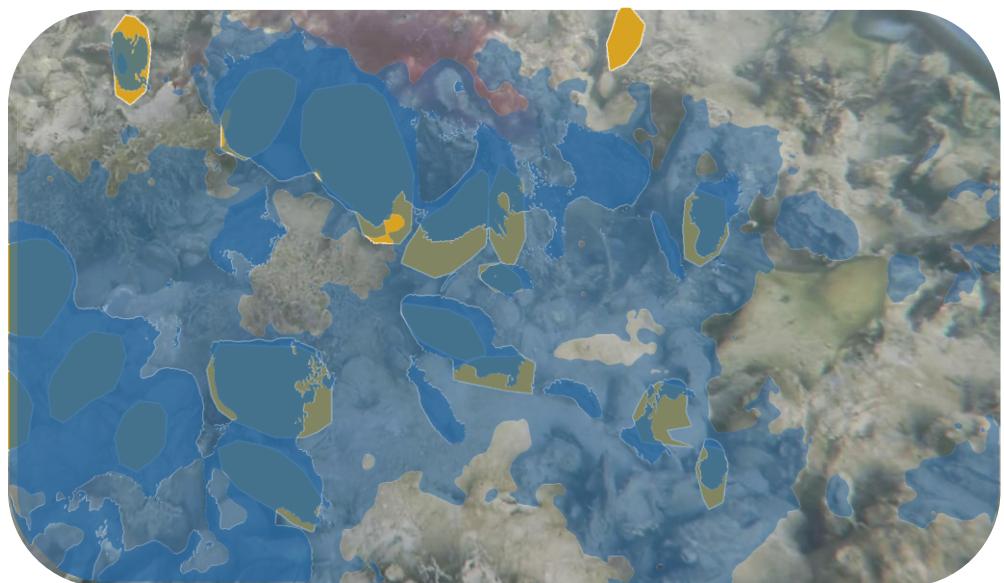


Photo-Sensitization in the image





Detections results with the synthetic data





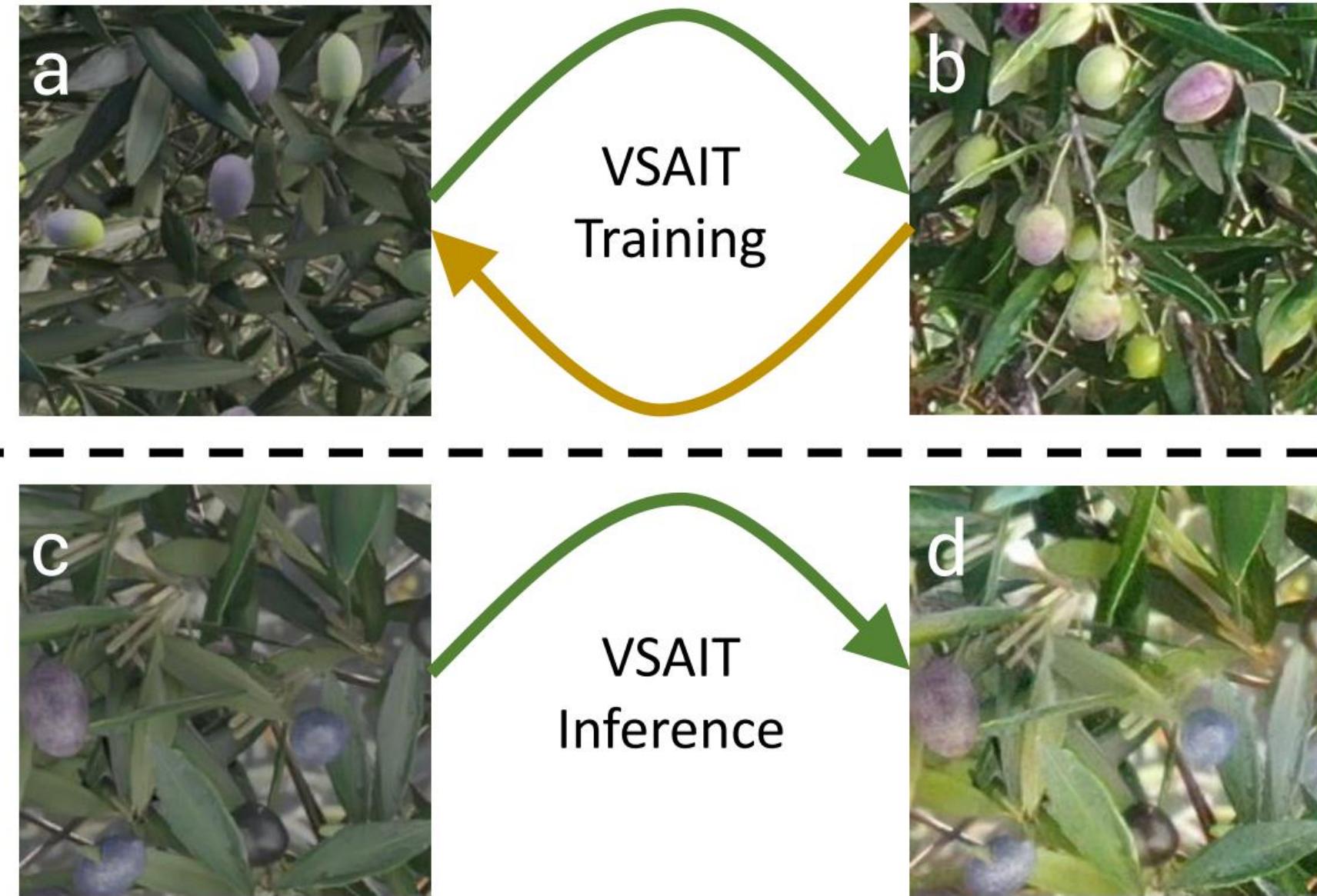
IEEE IROS, 2023

Olive the Above

Detecting Olives with Synthetic or Real Data?

In collaboration with





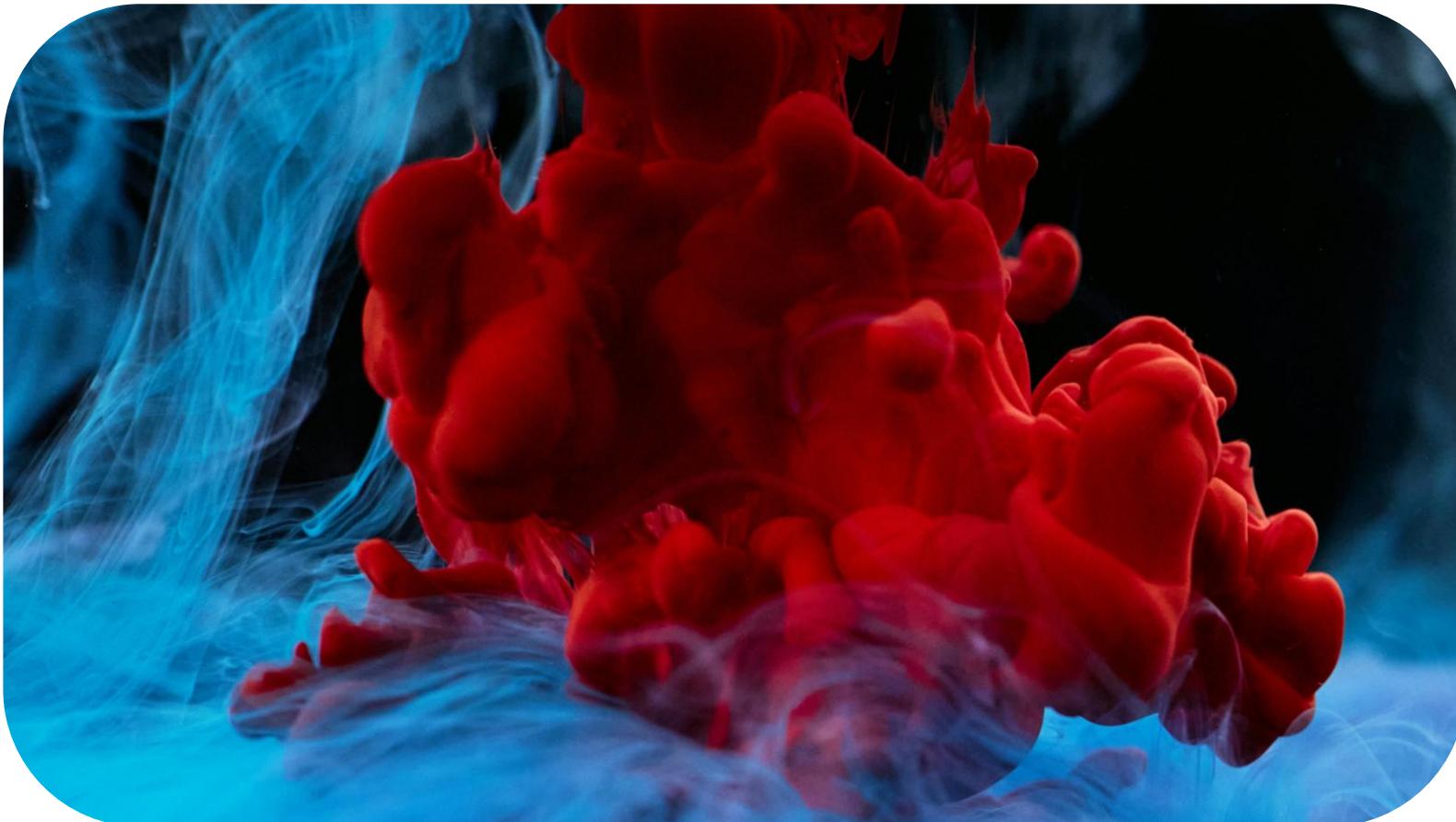




Better Deep Fakes

DEEP FAKE S

Next Class!



Advanced Generative Models: Diffusion Models