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Introduction

In 1993, Cboe Global Markets, Incorporated® (Cboe®) introduced the Cboe Volatility Index® (VIX® Index), which was originally designed to measure the market's expectation of 30-day volatility implied by at-the-money S&P 100® Index (OEX® Index) option prices. The VIX Index soon became the premier benchmark for U.S. stock market volatility. It is regularly featured in the Wall Street Journal, Barron's and other leading financial publications, as well as business news shows on CNBC, Bloomberg TV and CNN/Money, where the VIX Index is often referred to as the "fear gauge."

Ten years later in 2003, Cboe together with Goldman Sachs, updated the VIX Index to reflect a new way to measure expected volatility, one that continues to be widely used by financial theorists, risk managers and volatility traders alike. The new VIX Index is based on the S&P 500® Index (SPXSM), the core index for U.S. equities, and estimates expected volatility by aggregating the weighted prices of SPX puts and calls over a wide range of strike prices. By supplying a script for replicating volatility exposure with a portfolio of SPX options, this new methodology transformed the VIX Index from an abstract concept into a practical standard for trading and hedging volatility.

In 2014, Cboe enhanced the VIX Index to include series of SPX WeeklysSM. First introduced by Cboe in 2005, weekly options are now available on hundreds of indexes, equities, ETFs and ETNs and have become a very popular and actively-traded risk management tool. Today, SPX Weeklys account for one-third of all SPX options traded, and average close to 350,000 contracts traded per day¹.

The inclusion of SPX Weeklys allows the VIX Index to be calculated with S&P 500 Index option series that most precisely match the 30-day target timeframe for expected volatility that the VIX Index is intended to represent. Using SPX options with more than 23 days and less than 37 days to expiration ensures that the VIX Index will always reflect an interpolation of two points along the S&P 500 volatility term structure.

Cboe began dissemination of the VIX Index outside of U.S. trading hours in April 2016. The VIX index is now available during "extended trading hours" between 3 a.m. and 9:15 a.m ET, as well as during regular trading hours between 9:30 a.m. and 4:15 p.m. ET. As part of the VIX Index expansion, Cboe implemented a smoothing algorithm for VIX Index values disseminated during both extended and regular market hours.

Volatility as a tradable asset: VIX Futures & Options

On March 24, 2004, Cboe introduced the first exchange-traded VIX futures contract on its new, all-electronic Cboe Futures ExchangeSM (CFE®). Two years later in February 2006, Cboe launched VIX options, the most successful new product in Cboe history. In 2015, combined trading activity in VIX options and futures grew to nearly 800,000 contracts per day.

The negative correlation of volatility to stock market returns is well documented and suggests a diversification benefit to including volatility in an investment portfolio. VIX futures and options are designed to deliver pure volatility exposure in a single, efficient package. Cboe/CFE provides a continuous, liquid and transparent market for VIX products that are available to all investors from the smallest retail trader to the largest institutional money managers and hedge funds.



¹ Based on 2015 Volume.

Beyond the VIX Index

In addition to the VIX Index, Cboe calculates several other broad market volatility indexes including the Cboe Short-Term Volatility Index (VIX9DSM), which reflects 9-day expected volatility of the S&P 500 Index, the Cboe S&P 500® 3-Month Volatility Index (VIX3MSM), Cboe S&P 500® 6-Month Volatility Index (VIX6MSM) and the Cboe S&P 500 1-Year Volatility Index (VIX1YSM). Cboe also calculates the Nasdaq-100® Volatility Index (VXNSM), Cboe DJIA® Volatility Index (VXDSM) and the Cboe Russell 2000® Volatility Index (RVXSM).

Historical Prices: The VIX Index and Other Volatility Indexes

Perhaps one of the most valuable features of the VIX Index is the existence of more than 25 years of historical prices. This extensive data set provides investors with a useful perspective of how option prices have behaved in response to a variety of market conditions. Price history for the original Cboe Volatility Index (VXO) based on OEX options is available from 1986 to the present. Cboe has created a similar historical record for the new VIX Index dating back to 1990 so that investors can compare the new VIX Index with VXO, which reflects information about the volatility "skew" or "smile."

The VIX Index Calculation: Step-by-Step

Stock indexes, such as the S&P 500, are calculated using the prices of their component stocks. Each index employs rules that govern the selection of component securities and a formula to calculate index values.

The VIX Index is a volatility index comprised of options rather than stocks, with the price of each option reflecting the market's expectation of future volatility. Like conventional indexes, the VIX Index calculation employs rules for selecting component options and a formula to calculate index values. Some different rules and procedures apply when calculating the VIX Index value to be used for the final settlement value of VIX futures and options. For more information about those differences, refer to the section below titled "The Calculation of the Final Settlement Value for VIX Derivatives."

The generalized formula used in the VIX Index calculation§ is:

$$\sigma^{2} = \frac{2}{T} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{RT} Q(K_{i}) - \frac{1}{T} \left[\frac{F}{K_{0}} - 1 \right]^{2}$$
 (1)

Where

$$\sigma VIX/100 \Rightarrow VIX = \sigma \times 100$$

T Time to expiration

 $\,F\,\,$ Forward index level derived from index option prices

 $K_0\,$ First strike below the forward index level, F

 K_i Strike price of i^{th} out-of-the-money option; a call if Ki > Ko and a put if Ki < Ko; both put and call if Ki=Ko.

 ΔK_i Interval between strike prices – half the difference between the strike on either side of Ki:

$$\Delta \mathbf{K}_{i} = \frac{K_{i+1} - K_{i-1}}{2}$$

R Risk-free interest rate to expiration

 $Q(K_i)$ The midpoint of the bid-ask spread for each option with strike Ki.



[§] Please see "More than you ever wanted to know about volatility swaps" by Kresimir Demeterfi, Emanuel Derman, Michael Kamal and Joseph Zou, Goldman Sachs Quantitative Strategies Research Notes, March 1999.

Getting Started

The VIX Index measures 30-day expected volatility of the S&P 500 Index. The components of the VIX Index are near- and next-term put and call options with more than 23 days and less than 37 days to expiration. These include SPX options with "standard" 3rd Friday expiration dates and "weekly" SPX options that expire every Friday, except the 3rd Friday of each month. Once each week, the SPX options used to calculate the VIX Index "roll" to new contract maturities. For example, on the second Tuesday in October, the VIX Index would be calculated using SPX options expiring 24 days later (i.e., "near-term") and 31 days later (i.e., "next-term"). On the following day, the SPX options that expire in 30 calendar days would become the "near-term" options and SPX options that expire in 37 calendar days would be the "next-term" options.

In this hypothetical example, the near-term options are "standard" SPX options with 25 days to expiration, the next-term options are P.M.-settled SPX Weeklys with 32 days to expiration; and the calculation reflects prices observed at 9:46 a.m. ET. For the purpose of calculating time to expiration, "standard" SPX options are deemed to expire at the open of trading on SPX settlement day - the third Friday of the month, and "weekly" SPX options are deemed to expire at the close of trading (i.e., 4:00 p.m. ET).

The VIX Index calculation measures time to expiration, T, in calendar days and divides each day into minutes in order to replicate the precision that is commonly used by professional option and volatility traders. The time to expiration is given by the following expression:

$$T = \{ M_{Current day} + M_{Settlement day} + M_{Other days} \} / Minutes in a year$$

Where

M _{Current day}	minutes remaining until midnight of the current day
M _{Settlement day}	minutes from midnight until 9:30 a.m. ET for "standard" SPX expirations; or minutes from midnight until 4:00 p.m. ET for "weekly" SPX expirations
M _{Other days}	total minutes in the days between current day and expiration day

Using 9:46 a.m. ET as the time of the calculation, T for the near-term and next-term options, T1 and T2, respectively, is:

$$T_1 = \{854 + 510 + 34,560\} / 525,600 = 0.0683486$$

$$T_2 = \{854 + 900 + 44,640\} / 525,600 = 0.0882686$$

The risk-free interest rates, R_1 and R_2 , are yields based on U.S. Treasury yield curve rates (commonly referred to as "Constant Maturity Treasury" rates or CMTs), to which a cubic spline is applied to derive yields on the expiration dates of relevant SPX options. As such, the VIX Index calculation may use different risk-free interest rates for near- and next-term options. In this example, assume that R_1 = 0.0305% for the near-term options and that R_2 = 0.0286% for the next-term options. Note in this example, T_2 uses a value of 900 for Msettlement day, which reflects the 4:00 p.m. ET expiration time of the next-term SPX Weeklys options. Since many of the interim calculations are repetitive, only representative samples appear below. The complete set of SPX option data and calculations may be found in *Appendix 1*.



Step 1: Select the options to be used in the VIX Index calculation

The selected options are out-of-the-money SPX calls and out-of-the-money SPX puts centered around an at-the-money strike price, Ko. Only SPX options quoted with non-zero bid prices are used in the VIX Index calculation.

One important note: as volatility rises and falls, the strike price range of options with non-zero bids tends to expand and contract. As a result, the number of options used in the VIX Index calculation may vary from month-to-month, day-to-day and possibly, even minute-to-minute.

For each contract month:

> Determine the forward SPX level, F, by identifying the strike price at which the absolute difference between the call and put prices is smallest. The call and put prices in the following table reflect the midpoint of each option's bid / ask quotation. As shown below, the difference between the call and put prices is smallest at the 1965 strike for the near- and the 1960 strike for the next-term options.

Near Term Options				
Strike Price	Call	Put	Difference	
1940	38.45	15.25	23.20	
1945	34.70	16.55	18.15	
1950	31.10	18.25	12.85	
1955	27.60	19.75	7.85	
1960	24.25	21.30	2.95	
1965	21.05	23.15	2.10	
1970	18.10	25.05	6.95	
1975	15.25	27.30	12.05	
1980	12.75	29.75	17.00	

	Next Term Options				
	Next Territ Options				
Strike Price	Call	Put	Difference		
1940	41.05	18.80	22.25		
1945	37.45	20.20	17.25		
1950	34.05	21.60	12.45		
1955	30.60	23.20	7.40		
1960	27.30	24.90	2.40		
1965	24.15	26.90	2.75		
1970	21.10	28.95	7.85		
1975	18.30	31.05	12.75		
1980	15.70	33.50	17.80		

Using the 1965 call and put in the near-term, and the 1960 call and put in the next-term contract applied to the formula:

$$F = Strike Price + e^{RT} x (Call Price - Put Price)$$

the forward index prices, F1 and F2, for the near- and next-term options, respectively, are:

$$F_1 = 1965 + e^{(0.000305 \times 0.0683486)} \times (21.05 - 23.15) = 1962.89996$$

$$F_2 = 1960 + e^{(0.000286 \times 0.0882686)} \times (27.30 - 24.90) = 1962.40006$$

- Next, determine K_0 the strike price equal to or otherwise immediately below the forward index level, F for the near- and next-term options. In this example, $K_{0,1} = 1960$ and $K_{0,2} = 1960$.
- > Select out-of-the-money put options with strike prices < Ko. Start with the put strike immediately lower than Ko and move to successively lower strike prices. Exclude any put option that has a bid price equal to zero (i.e., no bid). As shown below, once two puts with consecutive strike prices are found to have zero bid prices, no puts with lower strikes are considered for inclusion. (Note that the 1350 and 1355 put options are not included despite having non-zero bid prices.)



Put Strike	Bid	Ask	Include?
1345	0	0.15	
1350	0.05	0.15	Not considered following two zero bids
1355	0.05	0.35	5103
1360	0	0.35	No
1365	0	0.35	No
1370	0.05	0.35	Yes
1375	0.1	0.15	Yes
1380	0.1	0.2	Yes

Next, select out-of-the-money call options with strike prices > Ko. Start with the call strike immediately higher than Ko and move to successively higher strike prices, excluding call options that have a bid price of zero. As with the puts, once two consecutive call options are found to have zero bid prices, no calls with higher strikes are considered. (Note that the 2225 call option is not included despite having a non-zero bid price.)

Call Strike	Bid	Ask	Include?
2095	0.05	0.35	Yes
2100	0.05	0.15	Yes
2120	0	0.15	No
2125	0.05	0.15	Yes
2150	0	0.1	No
2175	0	0.05	No
2200	0	0.05	
2225	0.05	0.1	Not considered following two zero bids
2250	0	0.05	2.03

- > Finally, select **both** the put and call with strike price Ko. Notice that two options are selected at Ko, while a single option, either a put or a call, is used for every other strike price.
- > The following table contains the options used to calculate the VIX Index in this example. The VIX Index uses the midpoint of quoted bid and ask prices for each option selected. The K₀ put and call prices are averaged to produce a single value. The price used for the 1960 strike in the near-term is, therefore, (24.25 + 21.30)/2 = 22.775; and the price used in the next-term is (27.30 + 24.90)/2 = 26.10.

Near term Strike	Option Type	Midpoint Price
1370	Put	0.2
1375	Put	0.125
1380	Put	0.15
1950	Put	18.25
1955	Put	19.75
1960	Put/Call Average	22.775
1965	Call	21.05
1970	Call	18.1
	•	•
2095	Call	0.2
2100	Call	0.1
2125	Call	0.1

Next term Strike	Option Type	Midpoint Price
1275	Put	0.075
1325	Put	0.15
1350	Put	0.15
1950	Put	21.60
1955	Put	23.20
1960	Put/Call Average	26.10
1965	Call	24.15
1970	Call	21.10
	•	•
2125	Call	0.1
2150	Call	0.1
2200	Call	0.08



Step 2: Calculate volatility for both near-term and next-term options

Applying the VIX formula (1) to the near-term and next-term options with time to expiration of T_1 and T_2 , respectively, yields:

$$\sigma^{2}_{I} = \frac{2}{T_{1}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{1}T_{1}} Q(K_{i}) - \frac{1}{T_{1}} \left[\frac{F_{1}}{K_{0}} - 1 \right]^{2}$$

$$\sigma^{2}_{2} = \frac{2}{T_{2}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{2}T_{2}} Q(K_{i}) - \frac{1}{T_{2}} \left[\frac{F_{2}}{K_{0}} - 1 \right]^{2}$$

The VIX Index is an amalgam of the information reflected in the prices of all of the selected options. The contribution of a single option to the VIX Index value is proportional to ΔK and the price of that option, and inversely proportional to the square of the option's strike price.

Generally, Δ Ki is half the difference between the strike prices on either side of Ki. For example, the Δ K for the next-term 1325 Put is 37.5: Δ K1325 Put = (1350 – 1275)/2. At the upper and lower edges of any given strip of options, Δ Ki is simply the difference between Ki and the adjacent strike price. In this example, the 1370 Put is the lowest strike in the strip of near-term options and 1375 is the adjacent strike. Therefore, Δ K1370 Put = 5 (i.e., 1375 – 1370).

The contribution of the near-term 1370 Put is given by:

$$\frac{\Delta K_{1370Put}}{K_{1370Put}^2} e^{R_1 T_1} Q(1370Put)$$

$$\frac{\Delta K_{1370Put}}{K_{1370Put}^2} e^{R_1 T_1} Q(1370Put) = \frac{5}{1370^2} e^{.000305 (0.0683486)} (0.20) = 0.0000005328$$

A similar calculation is performed for each option. The resulting values for the near-term options are then summed and multiplied by $2/T_1$. Likewise, the resulting values for the next-term options are summed and multiplied by $2/T_2$. The table below summarizes the results for each strip of options.

Near term Strike	Option Type	Midpoint Price	Contribution by Strike
1370	Put	0.2	0.0000005328
1375	Put	0.125	0.0000003306
1380	Put	0.15	0.0000003938
1950	Put	18.25	0.0000239979
1955	Put	19.75	0.0000258376
1960	Put/Call Average	22.775	0.0000296432
1965	Call	21.05	0.0000272588
1970	Call	18.1	0.0000233198
2095	Call	0.2	0.0000002278
2100	Call	0.1	0.0000003401
2125	Call	0.1	0.0000005536
	0.018495		

Near term Strike	Option Type	Midpoint Price	Contribution by Strike
1275	Put	0.075	0.0000023069
1325	Put	0.15	0.0000032041
1350	Put	0.15	0.0000020577
1950	Put	21.6	0.0000284031
1955	Put	23.2	0.0000303512
1960	Put/Call Average	26.1	0.0000339711
1965	Call	24.15	0.0000312732
1970	Call	21.1	0.0000271851
2125	Call	0.1	0.0000005536
2150	Call	0.1	0.0000008113
2200	Call	0.075	0.0000007748
$\frac{2}{T_2}$	$\sum_{i} \frac{\Delta K_i}{K_i^2} e^{R_2 T_2} Q(K_i)$	(C_i)	0.018838



Next, calculate
$$\frac{1}{T} \left[\frac{F}{K_0} - 1 \right]^2$$
 for the near-term (T1) and next-term (T2):

$$\frac{1}{T_1} \left[\frac{F_1}{K_0} - 1 \right]^2 = \frac{1}{0.0683486} \left[\frac{1962.89996}{1960} - 1 \right]^2 = 0.00003203$$

$$\frac{1}{T_2} \left[\frac{F_2}{K_0} - 1 \right]^2 = \frac{1}{0.0882686} \left[\frac{1962.40006}{1960} - 1 \right]^2 = 0.00001699$$

Now calculate σ^2 1 and σ^2 2:

$$\sigma^{2}_{1} = \frac{2}{T_{1}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{1}T_{1}} Q(K_{i}) - \frac{1}{T_{1}} \left[\frac{F_{1}}{K_{0}} - 1 \right]^{2} = 0.018495 - 0.00003203 = 0.01846292$$

$$\sigma^{2}_{2} = \frac{2}{T_{2}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{2}T_{2}} Q(K_{i}) - \frac{1}{T_{2}} \left[\frac{F_{2}}{K_{0}} - 1 \right]^{2} = 0.018838 - 0.00001699 = 0.01882101$$

Step 3

Calculate the 30-day weighted average of σ^2 1 and σ^2 2. Then take the square root of that value and multiply by 100 to get the VIX Index value.

$$\text{VIX} = \textbf{100} \times \sqrt{ \left\{ T_1 \sigma_1^2 \left[\frac{N_{T_2} - N_{30}}{N_{T_2} - N_{T_1}} \right] + T_2 \sigma_2^2 \left[\frac{N_{30} - N_{T_1}}{N_{T_2} - N_{T_1}} \right] \right\} \times \frac{N_{365}}{N_{30}} }$$

The inclusion of SPX Weeklys in the VIX Index calculation means that the near-term options will always have more than 23 days to expiration and the next-term options always have less than 37 days to expiration, so the resulting VIX Index value will always reflect an interpolation of σ^2 and σ^2 ; i.e., each individual weight is less than or equal to 1 and the sum of the weights equals 1.

Returning to the example...

NT1 = number of minutes to settlement of the near-term options (35,924)

 N_{T2} = number of minutes to settlement of the next-term options (46,394)

 N_{30} = number of minutes in 30 days (30 x 1,440 = 43,200)

 N_{365} = number of minutes in a 365-day year (365 x 1,440 = 525,600)

$$VIX = 100 \times \sqrt{\left\{0.0683486 \times 0.0184629 \times \left[\frac{46,394 - 43,200}{46,394 - 35,924}\right] + 0.0882686 \times 0.018821 \times \left[\frac{43,200 - 35,924}{46,394 - 35,924}\right]\right\} \times \frac{525,600}{43,200}}$$

$$VIX = 100 \times 0.13685821 = 13.69$$



VIX Index Filtering Algorithm

As described above, "spot" VIX Index values are based on the average of SPX option bid/ask quotes ("mid-quote" prices), and only options that have a non-zero bid price are included. The bid-ask spread is generally accepted as a current indication of market price, and the average of the bid and ask quotes can be thought of as an indication of "fair" value. Spot VIX Index values are calculated using mid-quote option prices.

From time to time, option price quotations widen due to changing market conditions, technology failures or other reasons. When this occurs, options that were previously included in a VIX Index value calculation might be excluded due to them now having a zero-bid price. In other instances, the mid-quote prices of one or more SPX options might materially change. This can result in a VIX Index value that, while accurately reflecting SPX option quotes at the time, may not reflect the expected volatility of the S&P 500 Index. Cboe uses a filtering algorithm to address this circumstance.

The VIX Index Filtering Algorithm operates as follows:

- 1. The first VIX Index spot value calculated during the Cboe RTH session or the Cboe GTH session is deemed to be the "baseline" VIX Index spot value.
- 2. Any VIX Index spot value calculated after and within two (2) minutes of the baseline that is higher than the baseline value or lower than the baseline value by .49 volatility points or less becomes the new baseline value.
- 3. If VIX Index spot values calculated after and within two (2) minutes of a baseline are lower than the baseline by 0.50 volatility points or more, then the baseline VIX Index spot value will be republished as the VIX Index spot value. Calculated values above the baseline are not filtered.
- 4. If the published VIX Index spot values remain the same for a period of two (2) minutes because the calculated values are 0.50 or more volatility points lower than the baseline, the first VIX Index spot value calculated after the two-minute period becomes the new baseline VIX Index spot value.
- 5. The filtering algorithm does not apply to the first VIX Index spot value calculated during the Cboe RTH session (approximately 9:30 a.m. ET) or the first VIX Index spot value calculated during the Cboe GTH session (approximately 3:15 a.m. ET). All other VIX Index spot values calculated during Cboe RTH and Cboe GTH are subject to the filtering process.

The Calculation of the Final Settlement Value for VIX Derivatives

The final settlement value for VIX futures and options is determined on the morning of their expiration date (usually a Wednesday) through a Special Opening Quotation ("SOQ") of the VIX Index. There are several ways in which the calculation of the SOQ of the VIX Index differs from the calculation of the VIX Index at all other times.

• The SOQ calculation uses SPX, or SPXW, options from a single expiration 30 calendar days from the subject settlement day. Unlike the VIX Index calculation at other times, the SOQ calculation does not involve the interpolation of volatility calculated with near-term and next-term options.



- Unlike the VIX Index calculation at other times, the determination of the strike range used for the SOQ calculation does not depend on whether options with consecutive strikes have zero bid prices. Cboe determines and announces the strike range to be used in the SOQ calculation. It does so by using an algorithm to determine the call with the highest strike and the put with the lowest strike to be used in that calculation. The strike prices used in the SOQ calculation include all put options within the strike range that have a strike price > K₀, and both the put and call options that have a strike price equal to K₀. Importantly, options within the Cboe-determined strike range with a zero bid price are eligible to be included in the SOQ calculation, which also differs from the calculation of the VIX index at other times.
- The SOQ calculation uses the "opening trade price" of each of the selected options, as determined pursuant to Cboe's rules during the special opening auction that Cboe conducts on days when VIX derivatives settle. This approach is different from the mid-quote prices that are used to calculate the VIX Index at all other times. Cboe uses the mid-quote price in the SOQ calculation only if a selected option does not have an opening price, in which case Cboe uses the midpoint price of the highest bid and lowest offer at the time of the opening.

For more information about Volatility Derivatives settlement, visit http://www.cboe.com/products/vix-index-volatility/vix-options-and-futures/vix-index/vix-faqs.

Related VIX Index Values

In addition to the VIX Index, Cboe publishes the Cboe VIX Indicative Bid Index ("VWB"), a VIX Index value based on SPX bid quotations, and the Cboe VIX Indicative Ask Index ("VWA"), a VIX Index value based on SPX option ask quotations. These values provide a market estimate of SPX option bid-ask "spreads" expressed in volatility terms. Cboe also publishes volatility information related to the near-term and next-term VIX "components", σ_1 and σ_2 , under ticker symbols "VIN" (Cboe Near-Term VIX Index) and "VIF" (Cboe Far-Term VIX Index) every 15 seconds during each Cboe trading day.



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Appendix 1: Complete SPX Option Data Used in Sample VIX Index Calculation

Option Series included in the VIX Index calculation are highlighted.

Near-Term Options				
Strike	Calls		Pι	ıts
Strike	Bid	Ask	Bid	Ask
800	1160.90	1164.40	0.00	0.10
900	1060.90	1064.50	0.00	0.10
1000	961.00	964.50	0.00	0.10
1050	911.00	914.50	0.00	0.10
1100	861.00	864.60	0.00	0.05
1125	836.00	839.60	0.00	0.05
1150	811.00	814.60	0.00	0.05
1175	786.10	789.60	0.00	0.05
1200	761.10	764.60	0.00	0.05
1220	741.10	744.60	0.00	0.10
1225	736.10	739.60	0.00	0.05
1240	721.10	724.60	0.00	0.10
1250	711.10	714.60	0.00	0.05
1260	701.10	704.60	0.00	0.10
1270	691.10	694.60	0.00	0.10
1275	686.10	689.60	0.00	0.10
1280	681.10	684.60	0.00	0.10
1290	671.10	674.70	0.00	0.10
1300	661.10	664.70	0.05	0.10
1305	656.10	659.70	0.00	0.10
1310	651.10	654.70	0.00	0.10
1315	646.10	649.70	0.00	0.10
1320	641.20	644.70	0.00	0.10
1325	636.20	639.70	0.05	0.10
1330	631.20	634.70	0.00	0.10
1335	626.20	629.70	0.00	0.15
1340	621.20	624.70	0.00	0.15
1345	616.20	619.70	0.00	0.15
1350	611.20	614.70	0.05	0.15
1355	606.20	609.70	0.05	0.35
1360	601.20	604.70	0.00	0.35
1365	596.20	599.70	0.00	0.35
1370	591.20	594.70	0.05	0.35
1375	586.20	589.70	0.10	0.15
1380	581.20	584.70	0.10	0.20
1385	576.20 571.20	579.70 574.70	0.10	0.35
1390	566.20	569.70	0.10	0.35
1400	561.20	564.80	0.10	0.15
1400	556.20	559.80	0.00	0.15
1410	551.20	554.80	0.00	0.35
1410	546.20	549.80	0.00	0.40
1415	541.20	544.80	0.00	0.40
1425	536.30	539.80	0.15	0.20

	Next-Term Options				
Ctrileo	Strike Calls		Puts		
Strike	Bid	Ask	Bid	Ask	
1225	735.90	738.80	0.00	0.10	
1250	710.80	713.80	0.00	0.10	
1275	686.00	688.70	0.05	0.10	
1300	660.90	663.80	0.00	0.10	
1325	635.90	638.60	0.10	0.20	
1350	610.90	613.60	0.10	0.20	
1375	585.90	588.70	0.10	0.25	
1400	561.00	563.70	0.15	0.25	
1425	536.00	538.80	0.20	0.30	
1450	511.10	513.80	0.25	0.35	
1500	486.10 461.20	488.90 464.00	0.30	0.40	
1510	451.30	454.00	0.35	0.45	
1520	441.30	444.00	0.40	0.50	
1525	436.30	439.10	0.40	0.55	
1530	431.30	434.10	0.45	0.55	
1540	421.40	424.10	0.45	0.60	
1550	411.40	414.20	0.50	0.60	
1555	406.40	409.20	0.50	0.65	
1560	401.40	404.20	0.55	0.65	
1565	396.50	399.20	0.55	0.70	
1570	391.20	394.00	0.60	0.70	
1575	386.50	389.30	0.60	0.75	
1580	381.50	384.30	0.60	0.75	
1585	376.60	379.30	0.65	0.75	
1590	371.30	374.10	0.65	0.80	
1595	366.60	369.40	0.70	0.80	
1600	361.60	364.40	0.70	0.85	
1605	356.70	359.40	0.75	0.85	
1610	351.70	354.50	0.75	0.90	
1615	346.70	349.50	0.80	0.90	
1620	341.80	344.50	0.80	0.95	
1625	336.80	339.50	0.85	0.95	
1630	331.80	334.60	0.90	1.00	



Near-Term Options (cont.)				
G1 11	Ca	ills	Pu	ıts
Strike	Bid	Ask	Bid	Ask
1430	531.30	534.80	0.05	0.40
1435	526.30	529.80	0.15	0.40
1440	521.30	524.80	0.05	0.30
1445	516.30	519.80	0.05	0.40
1450	511.30	514.80	0.15	0.25
1455	506.30	509.80	0.05	0.45
1460	501.30	504.80	0.05	0.45
1465	496.30	499.80	0.05	0.45
1470	491.30	494.80	0.05	0.45
1475	486.30	489.90	0.15	0.25
1480	481.30	484.90	0.05	0.45
1485	476.30	479.90	0.20	0.50
1490	471.30	474.90	0.05	0.30
1495	466.40	469.90	0.05	0.50
1500	461.40	464.90	0.25	0.40
1505	456.40	459.90	0.30	0.35
1510	451.40	454.90	0.05	0.55
1515	446.40	449.90	0.05	0.55
1520	441.40	445.00	0.10	0.60
1525	436.40	440.00	0.30	0.40
1530	431.40	435.00	0.05	0.60
1535	426.40	430.00	0.10	0.65
1540	421.40	425.00	0.10	0.65
1545	416.50	420.00	0.10	0.65
1550	411.50	415.00	0.30	0.70
1555	406.50	410.10	0.15	0.70
1560	401.50	405.10	0.15	0.70
1565	396.50	400.10	0.15	0.70
1570	391.50	395.10	0.20	0.75
1575	386.50	390.10	0.35	0.75
1580	381.50	385.10	0.25	0.80
1585	376.60	380.20	0.25	0.80
1590	371.60	375.20	0.25	0.80
1595	366.60	370.20	0.25	0.80
1600	361.60	365.20	0.50	0.85
1605	356.60	360.30	0.30	0.85
1610	351.60	355.30	0.35	0.90
1615	346.70	350.30	0.35	0.90
1620	341.70	345.30	0.35	0.90
1625	336.70	340.40	0.40	0.95
1630	331.70	335.40	0.40	0.95
1635	326.70	330.40	0.45	1.00
1640	321.80	325.40	0.45	1.00
1645	316.80	320.50	0.50	1.05
1650	311.80	315.50	0.50	0.85
1655	306.80	310.50	0.55	1.10
1660	301.90	305.60	0.55	1.10
1665	296.90	300.60	0.60	1.15

Next-Term Options (cont.)				
Chailea	Ca	lls	Pu	its
Strike	Bid	Ask	Bid	Ask
1635	326.90	329.60	0.90	1.05
1640	321.90	324.70	0.95	1.05
1645	316.90	319.70	0.95	1.10
1650	312.00	314.70	1.00	1.15
1655	307.00	309.80	1.05	1.15
1660	302.10	304.80	1.10	1.20
1665	297.10	299.90	1.15	1.25
1670	292.20	294.90	1.15	1.30
1675	287.20	289.90	1.20	1.35
1680	282.30	285.00	1.25	1.40
1685	277.30	280.10	1.30	1.45
1690	272.40	275.10	1.35	1.50
1695	267.40	270.20	1.40	1.55
1700	262.50	265.20	1.45	1.60
1705	257.50	260.30	1.50	1.70
1710	252.60	255.30	1.60	1.75
1715	247.70	250.40	1.65	1.80
1720	242.70	245.50	1.70	1.90
1725	237.80	240.60	1.75	1.95
1730	232.90	235.60	1.85	2.00
1735	228.00	230.70	1.90	2.10
1740	223.40	225.30	2.00	2.20
1745	218.50	220.40	2.10	2.25
1750	213.60	215.50	2.20	2.35
1755	208.70	210.60	2.30	2.45
1760	203.80	205.70	2.40	2.55
1765	198.90	200.80	2.50	2.65
1770	194.00	195.90	2.65	2.80
1775	189.20	191.10	2.75	2.90
1780	184.30	185.80	2.90	3.10
1785	179.40	180.90	3.00	3.20
1790	174.60	176.10	3.10	3.40
1795	169.70	171.20	3.30	3.60
1800	164.90	166.40	3.50	3.70
1805	160.10	161.60	3.70	3.90
1810	155.30	156.70	3.80	4.10
1815	150.50	152.00	4.10	4.30
1820	145.70	147.20	4.30	4.50
1825	140.90	142.40	4.50	4.80
1830	136.20	137.70	4.80	5.00
1835	131.50	132.90	5.00	5.30
1840	126.80	128.20	5.30	5.60
1845	122.10	123.50	5.60	5.90
1850	117.40	118.80	5.90	6.20
1855	112.80	114.20	6.30	6.60
1860	108.20	109.60	6.60	6.90
1865	103.60	105.00	7.00	7.30
1870	99.00	100.40	7.50	7.80
	I			



Near-Term Options (cont.)				
G1 11	Ca	ills	Pu	ıts
Strike	Bid	Ask	Bid	Ask
1670	291.90	295.70	0.60	1.15
1675	287.00	290.70	0.65	1.20
1680	282.00	285.70	0.70	1.25
1685	277.00	280.80	0.75	1.30
1690	272.10	275.80	0.75	1.30
1695	267.10	270.90	0.80	1.35
1700	262.10	265.90	0.85	1.40
1705	257.20	261.00	0.85	1.40
1710	252.20	256.00	0.90	1.45
1715	247.30	251.10	0.95	1.50
1720	242.30	246.10	1.00	1.55
1725	237.40	241.20	1.05	1.60
1730	232.40	236.30	1.10	1.65
1735	227.50	231.30	1.15	1.70
1740	222.50	226.40	1.20	1.75
1745	217.60	221.50	1.25	1.85
1750	212.60	216.60	1.30	1.90
1755	207.70	211.60	1.40	1.95
1760	202.80	206.70	1.45	2.05
1765	197.80	201.80	1.50	2.15
1770	192.90	196.90	1.60	2.20
1775	188.00	192.00	1.65	2.35
1780	183.10	187.10	1.75	2.40
1785	178.20	182.20	1.85	2.50
1790	173.30	177.30	1.90	2.60
1795	168.40	172.40	2.00	2.75
1800	163.50	167.50	2.15	2.90
1805	158.60	162.60	2.25	3.00
1810	153.80	157.80	2.35	3.20
1815	148.90	152.90	2.50	3.40
1820	144.10	148.10	2.65	3.50
1825	139.20	143.30	3.00	3.60
1830	134.40	138.40	3.00	3.90
1835	129.60	133.60	3.20	4.10
1840	124.80	128.80	3.40	4.40
1845	120.10	124.10	3.60	4.60
1850	115.40	119.30	3.80	4.90
1855	110.60	114.60	4.10	5.20
1860	105.90	109.90	4.40	5.50
1865	101.30	105.20	4.70	5.80
1870	96.60	100.50	5.00	6.20
1875	92.00	95.90	5.40	6.60
1880	87.40	91.30	5.80	7.00
1885	82.90	86.70	6.20	7.50
1890	78.40	82.20	6.70	8.00
1895	74.00	77.70	7.20	8.60
1900	69.60	73.20	7.80	8.80
1905	66.00	68.50	8.50	9.50

Next-Term Options (cont.)					
Ct :1	Ca	ılls	Puts		
Strike	Bid	Ask	Bid	Ask	
1875	94.50	95.90	8.00	8.30	
1880	90.00	91.40	8.40	8.80	
1885	85.50	86.90	9.00	9.40	
1890	81.10	82.50	9.50	10.00	
1895	76.80	78.10	10.20	10.60	
1900	72.40	73.70	10.90	11.30	
1905	68.20	69.40	11.60	12.00	
1910	64.00	65.20	12.40	12.80	
1915	59.80	61.10	13.20	13.70	
1920	55.70	57.00	14.20	14.60	
1925	51.70	53.00	15.20	15.60	
1930	47.80	49.10	16.20	16.60	
1935	44.60	45.10	17.40	17.80	
1940	40.80	41.30	18.60	19.00	
1945	37.20	37.70	20.00	20.40	
1950	33.70	34.40	21.40	21.80	
1955	30.30	30.90	23.00	23.40	
1960	27.00	27.60	24.70	25.10	
1965	23.80	24.50	26.50	27.30	
1970	20.80	21.40	28.50	29.40	
1975	18.00	18.60	30.50	31.60	
1980	15.50	15.90	33.00	34.00	
1985	13.10	13.50	35.50	36.60	
1990	10.90	11.30	38.40	39.50	
1995	9.00	9.30	41.30	42.50	
2000	7.20	7.60	44.50	45.80	
2005	5.70	6.00	48.10	49.30	
2010	4.50	4.80	51.70	53.00	
2015	3.40	3.70	55.80	57.00	
2020	2.60	2.80	59.90	61.70	
2025	1.95	2.15	64.10	66.10	
2030	1.45	1.65	68.60	70.60	
2035	1.05	1.25	73.30	75.20	
2040	0.80	0.95	78.00	80.00	
2045	0.60	0.75	82.00	84.80	
2050	0.50	0.65	86.90	89.60	
2060	0.30	0.40	96.60	99.40	
2070	0.20	0.30	106.70	109.50	
2075	0.15	0.25	111.70	114.50	
2100	0.10	0.20	136.30	139.10	
2125	0.05	0.15	161.50	164.30	
2150	0.05	0.15	186.30	189.00	
2175	0.00	0.10	211.30	214.00	
2200	0.05	0.10	236.30	239.00	
2225	0.00	0.10	261.30	264.00	
2250	0.00	0.10	286.30	289.00	



Near-Term Options (cont.)				
		ılls	Pu	tc
Strike	Bid	Ask	Bid	Ask
1910	61.60	64.10	9.10	10.20
		59.80		
1915	57.40		9.90	11.30
1920	53.30	55.60	10.70	12.10
1925	49.10	51.20	11.60	12.60
1930	45.20	47.30	12.50	14.00
1935	41.20	43.40	13.60	14.70
1940	37.40	39.50	14.70	15.80
1945	33.70	35.70	15.90	17.20
1950	30.10	32.10	17.70	18.80
1955	26.70	28.50	19.00	20.50
1960	23.40	25.10	20.60	22.00
1965	20.30	21.80	22.30	24.00
1970	17.40	18.80	24.30	25.80
1975	14.60	15.90	26.50	28.10
1980	12.20	13.30	28.90	30.60
1985	9.90	11.00	31.40	33.20
1990	7.90	9.00	34.30	36.50
1995	6.20	7.10	37.40	39.70
2000	4.70	5.20	40.70	43.20
2005	3.40	4.20	44.00	47.70
2010	2.65	3.10	48.00	51.40
2015	1.75	2.30	52.20	56.00
2020	1.20	1.70	56.60	60.40
2025	1.00	1.25	61.20	65.00
2030	0.45	1.00	65.90	69.70
2035	0.25	0.80	70.70	74.40
2040	0.35	0.65	75.60	79.30
2045	0.20	0.60	80.50	84.10
2050	0.20	0.30	85.40	89.00
2055	0.15	0.50	90.40	94.00
2060	0.15	0.30	95.30	98.90
2065	0.15	0.20	100.30	103.90
2070	0.10	0.20	105.30	108.90
2075	0.10	0.20	110.30	113.80
2080	0.05	0.45	115.30	118.80
2085	0.05	0.40	120.30	123.80
2090	0.05	0.15	125.30	128.80
2095	0.05	0.35	130.30	133.80
2100	0.05	0.15	135.30	138.80
2120	0.00	0.15	155.30	158.80
2125	0.05	0.15	160.30	163.80
2150	0.00	0.10	185.20	188.80
2175	0.00	0.05	210.20	213.70
2200	0.00	0.05	235.20	238.70
2225	0.05	0.10	260.20	263.70
2250	0.00	0.05	285.20	288.70



Appendix 2: Individual Contributions — K₀ = 1960

Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1370	Put	0.200	5	0.0000005328
1375	Put	0.125	5	0.0000003306
1380	Put	0.150	5	0.0000003938
1385	Put	0.225	5	0.0000005865
1390	Put	0.225	5	0.0000005823
1395	Put	0.125	5	0.0000003212
1400	Put	0.125	7.5	0.0000004783
1410	Put	0.225	10	0.0000011318
1420	Put	0.225	7.5	0.0000008369
1425	Put	0.175	5	0.0000004309
1430	Put	0.225	5	0.0000005502
1435	Put	0.275	5	0.0000006677
1440	Put	0.175	5	0.0000004220
1445	Put	0.225	5	0.0000005388
1450	Put	0.200	5	0.0000004756
1455	Put	0.250	5	0.0000005905
1460	Put	0.250	5	0.0000005864
1465	Put	0.250	5	0.0000005824
1470	Put	0.250	5	0.0000005785
1475	Put	0.200	5	0.0000004596
1480	Put	0.250	5	0.0000005707
1485	Put	0.350	5	0.0000007936
1490	Put	0.175	5	0.0000003941
1495	Put	0.275	5	0.0000006152
1500	Put	0.325	5	0.0000007222
1505	Put	0.325	5	0.0000007174
1510	Put	0.300	5	0.0000006579
1515	Put	0.300	5	0.0000006535
1520	Put	0.350	5	0.0000007575
1525	Put	0.350	5	0.0000007525
1530	Put	0.325	5	0.0000006942
1535	Put	0.375	5	0.0000007958
1540	Put	0.375	5	0.0000007906
1545	Put	0.375	5	0.0000007855
1550	Put	0.500	5	0.0000010406
1555	Put	0.425	5	0.0000008788
1560	Put	0.425	5	0.0000008732
1565	Put	0.425	5	0.0000008676
1570	Put	0.475	5	0.0000009635
1575	Put	0.550	5	0.0000011086
1580	Put	0.525	5	0.0000011505
1585	Put	0.525	5	0.0000010313
1590	Put	0.525	5	0.0000010443
1595	Put	0.525	5	0.0000010384
1600	Put	0.525	5	0.0000010319
1605	Put	0.675	5	0.0000013184
1610	Put	0.625	5	0.0000011161
1010	ΓUL	0.025	J	0.0000012036

Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1275	Put	0.075	50	0.0000023069
1325	Put	0.150	37.5	0.0000032041
1350	Put	0.150	25	0.0000020577
1375	Put	0.175	25	0.0000023141
1400	Put	0.200	25	0.0000025511
1425	Put	0.250	25	0.0000030779
1450	Put	0.300	25	0.0000035673
1475	Put	0.350	25	0.0000040219
1500	Put	0.400	17.5	0.0000031112
1510	Put	0.425	10	0.0000018640
1520	Put	0.450	7.5	0.0000014608
1525	Put	0.475	5	0.0000010213
1530	Put	0.500	7.5	0.0000016020
1540	Put	0.525	10	0.0000022138
1550	Put	0.550	7.5	0.0000017170
1555	Put	0.575	5	0.0000011890
1560	Put	0.600	5	0.0000012328
1565	Put	0.625	5	0.0000012759
1570	Put	0.650	5	0.0000013185
1575	Put	0.675	5	0.0000013606
1580	Put	0.675	5	0.0000013520
1585	Put	0.700	5	0.0000013932
1590	Put	0.725	5	0.0000014339
1595	Put	0.750	5	0.0000014741
1600	Put	0.775	5	0.0000015137
1605	Put	0.800	5	0.0000015528
1610	Put	0.825	5	0.0000015914
1615	Put	0.850	5	0.0000016295
1620	Put	0.875	5	0.0000016671
1625	Put	0.900	5	0.0000017042
1630	Put	0.950	5	0.0000017878
1635	Put	0.975	5	0.0000018237
1640	Put	1.000	5	0.0000018591
1645	Put	1.025	5	0.0000018940
1650	Put	1.075	5	0.0000019743
1655	Put	1.100	5	0.0000020081
1660	Put	1.150	5	0.0000020867
1665	Put	1.200	5	0.0000021644
1670	Put	1.225	5	0.0000021963
1675	Put	1.275	5	0.0000022723
1680	Put	1.325	5	0.0000023474
1685	Put	1.375	5	0.0000024215
1690	Put	1.425	5	0.0000024947
1695	Put	1.475	5	0.0000025670
1700	Put	1.525	5	0.0000026385
1705	Put	1.600	5	0.0000027520
1710	Put	1.675	5	0.0000028642
1715	Put	1.725	5	0.0000029325



Individual Contributions (Cont.)				
Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1620	Put	0.625	5	0.0000011908
1625	Put	0.675	5	0.0000012781
1630	Put	0.675	5	0.0000012703
1635	Put	0.725	5	0.0000013561
1640	Put	0.725	5	0.0000013478
1645	Put	0.775	5	0.0000014320
1650	Put	0.675	5	0.0000012397
1655	Put	0.825	5	0.0000015060
1660	Put	0.825	5	0.0000014970
1665	Put	0.875	5	0.0000015782
1670	Put	0.875	5	0.0000015688
1675	Put	0.925	5	0.0000016485
1680	Put	0.975	5	0.0000017273
1685	Put	1.025	5	0.0000018051
1690	Put	1.025	5	0.0000017944
1695	Put	1.075	5	0.0000018709
1700	Put	1.125	5	0.0000019464
1705	Put	1.125	5	0.0000019350
1710	Put	1.175	5	0.0000020092
1715	Put	1.225	5	0.0000020825
1720	Put	1.275	5	0.0000021549
1725	Put	1.325	5	0.0000022265
1730	Put	1.375	5	0.0000022972
1735	Put	1.425	5	0.0000023670
1740	Put	1.475	5	0.0000024360
1745	Put	1.550	5	0.0000025452
1750	Put	1.600	5	0.0000026123
1755	Put	1.675	5	0.0000027192
1760	Put	1.750	5	0.0000028248
1765	Put	1.825	5	0.0000029292
1770	Put	1.900	5	0.0000030324
1775	Put	2.000	5	0.0000031740
1780	Put	2.075	5	0.0000032746
1785	Put	2.175	5	0.0000034132
1790	Put	2.250	5	0.0000035112
1795	Put	2.375	5	0.0000036856
1800	Put	2.525	5	0.0000038967
1805	Put	2.625	5	0.0000040286
1810	Put	2.775	5	0.0000042353
1815	Put	2.950	5	0.0000044776
1820	Put	3.075	5	0.0000046417
1825	Put	3.300	5	0.0000040411
1830	Put	3.450	5	0.0000051511
1835	Put	3.650	5	0.0000051311
1840	Put	3.900	5	0.0000057598
1845	Put	4.100	5	0.0000037338
1850	Put	4.350	5	0.0000003551
1855	Put	4.650	5	0.0000067568
1860	Put	4.950	5	0.0000071542
1000	Tut	7.550		0.0000011342

Individual Contributions (Cont.)				
Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1720	Put	1.800	5	0.0000030423
1725	Put	1.850	5	0.0000031087
1730	Put	1.925	5	0.0000032160
1735	Put	2.000	5	0.0000033221
1740	Put	2.100	5	0.0000034682
1745	Put	2.175	5	0.0000035715
1750	Put	2.275	5	0.0000037144
1755	Put	2.375	5	0.0000038556
1760	Put	2.475	5	0.0000039951
1765	Put	2.575	5	0.0000041330
1770	Put	2.725	5	0.0000043491
1775	Put	2.825	5	0.0000044834
1780	Put	3.000	5	0.0000047344
1785	Put	3.100	5	0.0000048648
1790	Put	3.250	5	0.0000050718
1795	Put	3.450	5	0.0000053539
1800	Put	3.600	5	0.0000055557
1805	Put	3.800	5	0.0000058319
1810	Put	3.950	5	0.0000060287
1815	Put	4.200	5	0.0000063750
1820	Put	4.400	5	0.0000066419
1825	Put	4.650	5	0.0000069808
1830	Put	4.900	5	0.0000073160
1835	Put	5.150	5	0.0000076474
1840	Put	5.450	5	0.0000080490
1845	Put	5.750	5	0.0000084461
1850	Put	6.050	5	0.0000088388
1855	Put	6.450	5	0.0000093724
1860	Put	6.750	5	0.0000097557
1865	Put	7.150	5	0.0000102785
1870	Put	7.650	5	0.0000102103
1875	Put	8.150	5	0.0000115914
1880	Put	8.600	5	0.0000123664
1885	Put	9.200	5	0.0000129463
1890	Put	9.750	5	0.0000136478
1895	Put	10.400	5	0.0000133110
1900	Put	11.100	5	0.0000111003
1905	Put	11.800	5	0.0000153743
1910	Put	12.600	5	0.0000102502
1915	Put	13.450	5	0.0000172037
1920	Put	14.400	5	0.0000185386
1925	Put	15.400	5	0.0000193317
1930	Put	16.400	5	0.0000207797
1935	Put	17.600	5	0.0000220146
1935	Put	18.800	5	0.0000235035
			5	
1945	Put	20.200		0.0000266989
1950	Put	21.600	5	0.0000284031
1955	Put /Call Average	23.200	5	0.0000303512
1960	Put/Call Average	26.100	5	0.0000339711



	Individual Contributions (Cont.)				
Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike	
1865	Put	5.250	5	0.0000075471	
1870	Put	5.600	5	0.0000080073	
1875	Put	6.000	5	0.0000085335	
1880	Put	6.400	5	0.0000090541	
1885	Put	6.850	5	0.0000096393	
1890	Put	7.350	5	0.0000102883	
1895	Put	7.900	5	0.0000109999	
1900	Put	8.300	5	0.0000114961	
1905	Put	9.000	5	0.0000124003	
1910	Put	9.650	5	0.0000132263	
1915	Put	10.600	5	0.0000144526	
1920	Put	11.400	5	0.0000154626	
1925	Put	12.100	5	0.0000163269	
1930	Put	13.250	5	0.0000177861	
1935	Put	14.150	5	0.0000188962	
1940	Put	15.250	5	0.0000202603	
1945	Put	16.550	5	0.0000218745	
1950	Put	18.250	5	0.0000239979	
1955	Put	19.750	5	0.0000258376	
1960	Put/Call Average	24.250	5	0.0000296432	
1965	Call	21.050	5	0.0000272588	
1970	Call	18.100	5	0.0000233198	
1975	Call	15.250	5	0.0000195486	
1980	Call	12.750	5	0.0000162614	
1985	Call	10.450	5	0.0000132609	
1990	Call	8.450	5	0.0000106691	
1995	Call	6.650	5	0.0000083544	
2000	Call	4.950	5	0.0000061876	
2005	Call	3.800	5	0.0000047264	
2010	Call	2.875	5	0.0000035582	
2015	Call	2.025	5	0.0000033332	
2020	Call	1.450	5	0.0000017768	
2025	Call	1.125	5	0.0000017700	
2030	Call	0.725	5	0.0000013710	
2035	Call	0.525	5	0.0000006339	
2040	Call	0.523	5	0.0000006333	
2045	Call	0.400	5	0.000000007	
2050	Call	0.400	5		
2055	Call	0.250	5	0.0000002974	
	Call		5	0.0000003848	
2060		0.225			
2065	Call	0.175	5	0.0000002052	
2070	Call	0.150	5	0.0000001750	
2075	Call	0.150	5	0.0000001742	
2080	Call	0.250	5	0.0000002889	
2085	Call	0.225	5	0.0000002588	
2090	Call	0.100	5	0.0000001145	
2095	Call	0.200	5	0.0000002278	
2100	Call	0.100	15	0.0000003401	
2125	Call	0.100	25	0.0000005536	

Individual Contributions (Cont.)				
Near term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1965	Call	24.150	5	0.0000312732
1970	Call	21.100	5	0.0000271851
1975	Call	18.300	5	0.0000234584
1980	Call	15.700	5	0.0000200240
1985	Call	13.300	5	0.0000168776
1990	Call	11.100	5	0.0000140152
1995	Call	9.150	5	0.0000114952
2000	Call	7.400	5	0.0000092502
2005	Call	5.850	5	0.0000072763
2010	Call	4.650	5	0.0000057550
2015	Call	3.550	5	0.0000043718
2020	Call	2.700	5	0.0000033086
2025	Call	2.050	5	0.0000024997
2030	Call	1.550	5	0.0000018807
2035	Call	1.150	5	0.0000013885
2040	Call	0.875	5	0.0000010513
2045	Call	0.675	5	0.0000008070
2050	Call	0.575	7.5	0.0000010262
2060	Call	0.350	10	0.0000008248
2070	Call	0.250	7.5	0.0000004376
2075	Call	0.200	15	0.0000006968
2100	Call	0.150	25	0.0000008504
2125	Call	0.100	25	0.0000005536
2150	Call	0.100	37.5	0.0000008113
2200	Call	0.075	50	0.0000007748



Sum of Individual Contributions 0.000831402

 $\frac{2}{T} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{RT} Q(K_{i})$ 0.018838

$$\frac{2}{T} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{RT} Q(K_{i})$$

Sum of Individual Contributions 0.0006320516 $\frac{2}{T} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{RT} Q(K_{i})$ 0.018494953



