Homework 5, FRE-6971, due 5/16/2019, 10am

Problem 1 (20 points)

1-Factor Affine model:

$$d\mathbf{r}(t) = \{\mu - \kappa r(t)\}d\mathbf{t} + \sqrt{\gamma r(t) + \sigma} d\mathbf{W}(\mathbf{t})$$

- 1. Initially assume  $\gamma = 0$ , and derive the expressions for Eurodollar futures rate in the above model
- 2. Build a Jupyter Notebook to demonstrate your calculations using  $\mu=0.005,$  r(0)=0.015, k=0.1,  $\sigma=0.008,$   $\gamma=0.0$
- 3. What changes if  $\gamma \neq 0$ ? Reason through this case. We will cover this topic more fully at the end of the semester
- 4. How would your calculation change if the above model was a 2-factor model?

Problem 2 (80 ponts):

Data: Settle prices of first 20 rolling Eurodollar futures on 11/27/2017 (1 day of data)

- 1. Compute IMM dates for all the futures either manually or using a QuantLib python package (I will email instructions). Explain why you need to know the IMM dates
- 2. Consider 2 models: ModelA: model from Problem 1.1 & ModelB: DNS model from HW4
- 3. Carry out a fit of all parameters for Models A & B
- 4. Check for collinearity and apply collinearity remedies (PCA rank reduction or Ridge regression) if your problems are collinear
- 5. Explain your work