Homework 4, due 5/8/2019, 10am, FRE-6971

Problem 1 (50 ponts):

Read Diebold & Li paper on Dynamic Nelson-Siegel model (DNS).

Dataset: CMT rates, sample: 2011-2015

Carry out estimation of DNS parameters in the following way:

- 1. Step 1: Assume a value of  $\lambda$ , and fit  $\beta_1(t)$ ,  $\beta_2(t)$ ,  $\beta_3(t)$  to a set of yields observed on day t (repeat for all days in the dataset)
- 2. Step 2: Find  $\lambda$  that bests fits the whole dataset (Step1 needs to be repeated on each iteration, as you search for optimal  $\lambda$ ). You can use an optimization package, or write your own code

Problem 2 (50 ponts):

Use results of DNS estimation you carried out in Problem 1.

Estimated model: DNS (optimal  $\lambda$ +time series of  $\beta_1(t), \beta_2(t), \beta_3(t)$ )

Perform the following analysis of results:

- 1. Step 1: Compute RMSE for each day in the sample and pick 20 days with largest RMSE
- 2. Step 2: Use 6m of data prior to each of the 20 days to fit AR(1) to each of  $\beta_1(t)$ ,  $\beta_2(t)$ ,  $\beta_3(t)$  time series and compute half-lives (HL). Generate t+5d. t+10d, t+1m forecast for each of the 20 days, using the corresponding model for each forecast. Total of 3 forecasts for each of the 20 days.
- 3. Step 3. Do these forecasts perform better than those generated under a random walk assumption?