

ENV 790.30 - Time Series Analysis for Energy Data | Spring 2023

Assignment 6 - Due date 03/06/23

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Directions

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github. And to do so you will need to fork our repository and link it to your RStudio.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., “LuanaLima_TSA_A06_Sp23.Rmd”). Then change “Student Name” on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

R packages needed for this assignment: “xlsx” or “readxl”, “ggplot2”, “forecast”, “tseries”, and “Kendall”. Install these packages, if you haven’t done yet. Do not forget to load them before running your script, since they are NOT default packages.

Questions

This assignment has general questions about ARIMA Models.

Packages needed for this assignment: “forecast”, “tseries”. Do not forget to load them before running your script, since they are NOT default packages.\

```
#Load/install required package here
library(forecast)
```

```
## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo

library(tseries)
```

Q1

Describe the important characteristics of the sample autocorrelation function (ACF) plot and the partial sample autocorrelation function (PACF) plot for the following models:

- AR(2)

Answer: The AR(2) shows a strong autocorrelation and a gradual decay of autocorrelation with increasing lag in the acf of the model. The pacf of AR(2) will identify the order of the AR model ($p=2$), which shows significant spikes in the first two lags and cutoff after the lag 2.

- MA(1)

Answer: The acf of MA(1) will identify the order of the model ($q=1$), meaning that there is a significant spike at lag=1 and cutoff after lag 1. The pacf of MA(1) will decay exponentially.

Q2

Recall that the non-seasonal ARIMA is described by three parameters $ARIMA(p, d, q)$ where p is the order of the autoregressive component, d is the number of times the series need to be differenced to obtain stationarity and q is the order of the moving average component. If we don't need to difference the series, we don't need to specify the "I" part and we can use the short version, i.e., the $ARMA(p, q)$. Consider three models: $ARMA(1,0)$, $ARMA(0,1)$ and $ARMA(1,1)$ with parameters $\phi = 0.6$ and $\theta = 0.9$. The ϕ refers to the AR coefficient and the θ refers to the MA coefficient. Use R to generate $n = 100$ observations from each of these three models

```
#ARMA(1,0)
ARMAModel_1<- arima.sim(model=list(ar=0.6), n=100) #the AR coefficient is 0.6
ARMAModel_1

## Time Series:
## Start = 1
## End = 100
## Frequency = 1
## [1] 0.01549904 -0.07088119 -0.34782126 -0.61436954 0.28331676 -0.33946546
## [7] 0.48596117 1.99047884 2.61765370 1.33231524 2.08473431 2.07392094
## [13] 1.69112502 0.08556690 -0.06747913 -1.12299997 -0.30456470 0.38875833
## [19] 0.54925523 1.47319859 1.08977130 -0.06230389 1.25036228 0.69395542
## [25] -0.69536152 -1.04711404 -2.15968405 0.09528470 -1.06246664 0.47627875
## [31] -0.57900816 -0.65897253 -0.16256863 -0.00801316 -0.71894681 0.30045056
## [37] 0.18204594 1.71072085 0.93175311 -1.24777211 -1.30120793 -0.74708613
## [43] 0.41827115 2.40220130 -1.16195203 -1.44698211 -0.60187424 0.44868888
## [49] 0.59177633 0.49072489 -1.67298270 -0.11886158 0.13395503 -0.13516206
## [55] -1.08529030 -0.29969447 1.17972291 1.57062904 -0.65882984 0.74553681
## [61] 1.57377819 1.39112809 0.48346359 -0.54189665 -1.24632865 -1.32177578
## [67] -0.56216376 0.04502444 -1.99015883 -0.46430497 0.12739144 -1.39034435
## [73] -2.62331825 -1.31938819 0.17143733 1.31204404 2.84222455 2.45455744
## [79] 0.50178736 0.29342366 2.66070833 1.99898692 0.86891956 2.03539457
## [85] 1.51605462 2.14527993 0.98283323 0.30983802 -0.18416896 -0.19625864
## [91] 0.43911781 -0.94206202 -1.30852587 0.60669073 -0.64690201 1.35454137
## [97] 0.25656244 0.12711458 1.11905363 -0.56771207

#ARMA(0,1)
ARMAModel_2<- arima.sim(model=list(ma=0.9), n=100) #the MA coefficient is 0.9
ARMAModel_2

## Time Series:
## Start = 1
## End = 100
## Frequency = 1
## [1] -1.91005461 -1.98897203 -0.67173670 -1.64301019 -0.83368116 0.87793626
## [7] 2.61321087 2.58528532 0.95942995 1.21512651 2.82848545 1.57686004
## [13] -1.33657053 -1.19549484 -0.37483624 0.77734207 2.05897190 0.60844052
## [19] 0.46831852 0.97193687 -0.85695375 -1.37461610 -0.39304790 -0.19636459
## [25] -0.51690240 -0.25952791 0.73351200 -1.09417289 -1.10354585 0.37071345
## [31] 0.38057718 0.12526454 -0.77433586 -1.89894270 -1.48080945 -1.32672595
## [37] -2.29986648 -0.84699703 -1.26600992 -0.81508859 0.38758601 -0.40631188
## [43] 0.18058657 1.49204085 2.24414307 0.89304737 -0.68853642 1.10174121
## [49] 0.86763430 -0.34519028 -0.38219628 -0.66035043 0.87631008 0.77210235
```

```
## [55] 1.94512972 2.48548129 0.44568216 0.88149285 1.53505595 0.22452248
## [61] -2.41729749 -4.61457641 0.07241557 3.23401473 0.32110693 -0.64238344
## [67] -0.48823575 0.21861824 -0.37060154 1.02737754 1.97296182 1.04752660
## [73] 0.63402713 -1.05889890 -2.85666171 -3.29949197 -1.36837377 0.20468565
## [79] 0.38295016 -0.25779681 -0.95662340 -0.86500853 -0.48992799 -0.69726615
## [85] -0.71469426 -0.49332406 0.57632305 0.82783073 0.39678275 1.72533689
## [91] 1.24091003 -1.81824307 -1.40480708 1.18694364 2.48417763 0.30858354
## [97] -0.67109389 1.78302549 1.49573961 -0.37625701
```

```
#ARMA(1,1)
```

```
ARMAmodel_3 <- arima.sim(model=list(ar=0.6, ma=0.9), n=100)
```

```
ARMAmodel_3
```

```
## Time Series:
```

```
## Start = 1
```

```
## End = 100
```

```
## Frequency = 1
```

```
## [1] 1.51561120 3.57472785 2.87144566 1.91816244 2.22388314 2.21916656
## [7] 2.17448199 1.75489140 1.79871775 1.65805470 0.05667639 -2.15064601
## [13] -2.17190531 -0.23648987 1.20544397 2.12312492 1.63561018 1.22291081
## [19] 2.51216802 1.75802584 -1.91749154 -3.07177215 -2.45800117 -3.58991781
## [25] -3.70243379 -1.13968793 -0.92139114 -3.29636301 -4.93362999 -4.00936363
## [31] -0.78428436 0.26629307 -1.43447247 -0.92613314 -0.14798161 0.32302051
## [37] 1.03124457 0.92165661 -0.63191108 -1.81532335 -0.76647599 -0.01456510
## [43] -0.18868673 2.02176227 3.49731976 0.71703184 -1.50724706 -0.79457700
## [49] -0.87336677 -2.21528139 0.08734520 1.79757504 0.03880806 0.13722641
## [55] 2.09963144 0.75424170 -0.65759903 1.82278628 3.53629801 2.59249105
## [61] 2.29600925 1.93191745 -0.69095225 -1.88058380 -2.56926399 -4.60471469
## [67] -4.65776531 -2.37620137 -0.44198558 0.97651304 1.96450133 0.69401513
## [73] 0.13525138 0.62432905 -0.12469865 -0.97086768 -1.26910163 -0.38807277
## [79] -0.44841087 0.17638917 2.26957649 2.43627154 3.15645752 4.54536506
## [85] 3.69005841 1.63530536 0.11169785 -0.25078480 -0.56875643 0.32758411
## [91] 3.37911630 4.46115707 2.67484898 -0.57573165 -1.71598793 -0.68938941
## [97] -0.43632141 -1.38506194 -1.95352520 -1.82790728
```

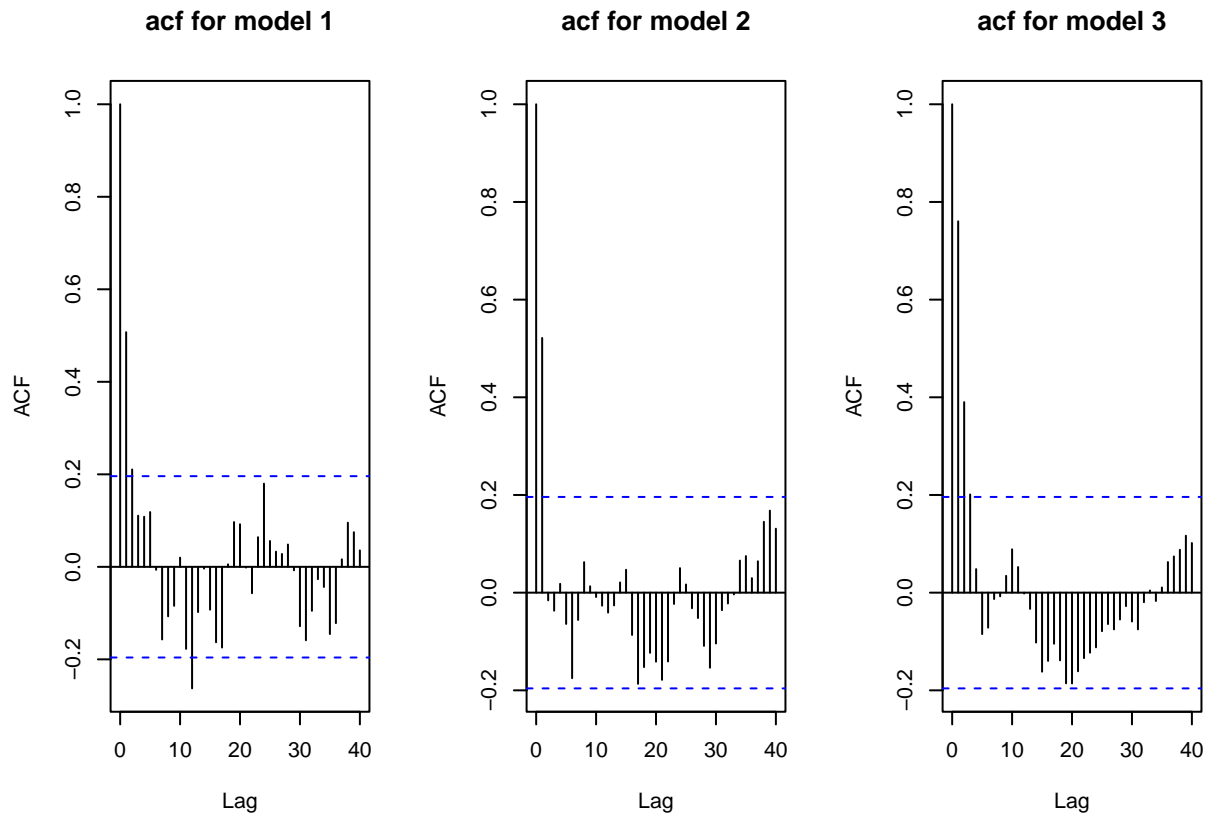
- (a) Plot the sample ACF for each of these models in one window to facilitate comparison (Hint: use command `par(mfrow = c(1,3))` that divides the plotting window in three columns).

```
par(mfrow=c(1,3))
```

```
acf(ARMAmodel_1, lag.max = 40, main = "acf for model 1")
```

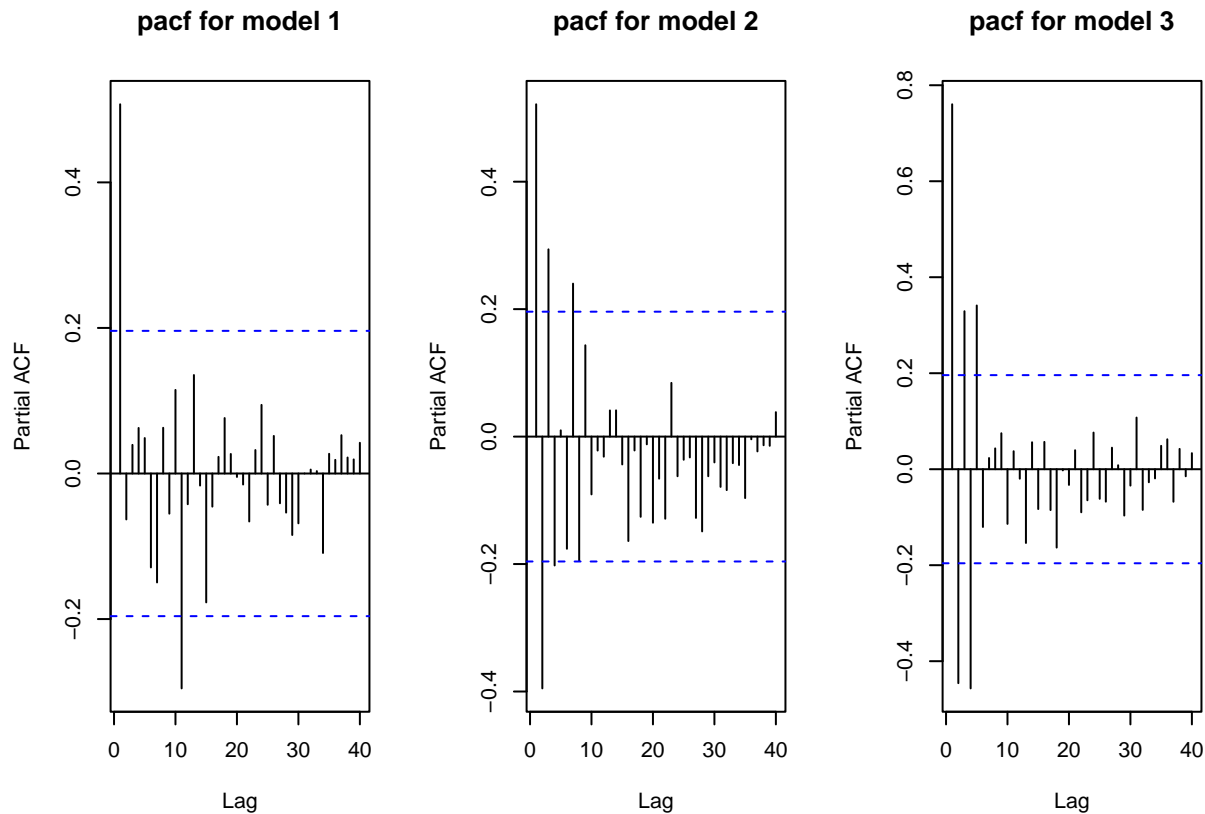
```
acf(ARMAmodel_2, lag.max = 40, main = "acf for model 2")
```

```
acf(ARMAmodel_3, lag.max = 40, main = "acf for model 3")
```



(b) Plot the sample PACF for each of these models in one window to facilitate comparison.

```
par(mfrow=c(1,3))
pacf(ARMAModel_1, lag.max = 40, main = "pacf for model 1")
pacf(ARMAModel_2, lag.max = 40, main = "pacf for model 2")
pacf(ARMAModel_3, lag.max = 40, main = "pacf for model 3")
```



- (c) Look at the ACFs and PACFs. Imagine you had these plots for a data set and you were asked to identify the model, i.e., is it AR, MA or ARMA and the order of each component. Would you be identify them correctly? Explain your answer.

Answer: Model 1 is AR, model 2 is MA, model 3 is ARMA. Model 1 is AR model because ACF will decay exponentially with time, and we found that it is decaying with lags in the ACF of model 1. Model 2 is MA model because pacf has slow decay, while it is not obvious in the above graph. Model 3 is ARMA model because in the PACF initial values dependent on the AR followed by the decay due to the MA part.

- (d) Compare the ACF and PACF values R computed with the theoretical values you provided for the coefficients. Do they match? Explain your answer.

Answer: The AR model somewhat matches with the theoretical value. We set $\phi=0.6$, meaning that the coefficient of AR should be 0.6. However, sometimes we can find that the pacf of lag 1 is 0.6 for model 1, but pacf of lag 1 is not 0.6 when we rerun the ARMA again. It didn't match with the theoretical value for MA model since we didn't find 0.9 at lag 1. For the ARMA model, ar coefficient at lag 1 in pacf didn't match with the theoretical value (0.6), but ma coefficient at lag 1 in acf matches with the theoretical value (0.9).

- (e) Increase number of observations to $n = 1000$ and repeat parts (a)-(d).

```
#ARMA(1,0)
ARMAModel_1_new<- arima.sim(model=list(ar=0.6), n=1000) #the AR coefficient is 0.6
ARMAModel_1_new

## Time Series:
## Start = 1
## End = 1000
## Frequency = 1
##      [1] -0.488958669  0.128683733  0.897218546  0.619568285 -0.194988460
```

```

##      [6] -0.607982694 -1.516425161 -1.865441957 -1.071599916 -2.167007423
##     [11] -2.555360865 -1.056007094 -0.715460399 -0.399182184 -0.029208792
##     [16] -0.464644186 -2.209202169 -1.512207736 -0.918252377 -0.482506122
##     [21] -0.552609391  1.055056942  0.420315711 -0.202570437  1.063899169
##     [26]  0.983922748 -1.197979225  0.164828529 -0.520446045  1.925831002
##     [31]  2.044451674  1.820121736  2.233760383  1.244021145 -1.305458656
##     [36] -0.691668838 -1.152443633  0.854965188  0.428169742 -0.874485959
##     [41] -1.407566951 -1.913985527  0.538464626 -0.209388913 -0.903381478
##     [46] -0.907048122  0.520822819  0.600640478 -0.324469946 -0.297567801
##     [51] -0.374639119 -0.941265543 -0.937966902  0.086405166 -0.713029681
##     [56]  0.098330167  0.294153432  0.050482034  0.709622017  1.481991373
##     [61] -0.016554641 -1.469338772 -1.143844915 -1.590646659 -0.388811641
##     [66] -0.466310150 -0.254038780  1.733968699  1.112334468  0.873455957
##     [71]  1.525760496  1.481662942  1.481418633  1.258076223  0.723597465
##     [76] -0.198077126  1.980348979  0.676173797  0.559088609  2.837493212
##     [81]  1.000014489 -0.964122674 -0.526745100 -1.446525453 -0.930774476
##     [86]  0.268751830  0.362526628 -0.416807829 -0.789457100 -0.660865542
##     [91]  0.459628501  1.119803752  2.732304333  1.914585226  1.317469482
##     [96] -0.135560389 -1.129422206 -1.171908231 -0.391755105 -1.060384266
##    [101] -1.971197316 -0.600146050 -0.294854327  0.618901822  0.534990192
##    [106]  1.384674804  1.662531490  1.351393027  1.743002345  0.096682062
##    [111] -1.682333358 -1.571775842  0.061476436 -0.840650950 -2.805156681
##    [116] -1.619211736 -1.735877183  1.092242083  2.846777369  0.017450642
##    [121]  1.251588704  1.275006747  1.358525483  1.563456719  0.802017400
##    [126]  1.350499065  0.049182905  0.123777274  0.606577338 -0.043036690
##    [131] -0.054633743  0.406802435 -0.875313714 -0.856840742  0.168255559
##    [136]  1.179716862  1.051129950  0.631037774  1.017722660  1.337654377
##    [141]  0.357754719  0.504698176  1.635624540  1.527541469 -0.833153816
##    [146] -0.883583596 -3.100965723 -2.876751305 -2.023612360 -2.808092507
##    [151] -0.267271887  1.321691841  2.693108050  0.258476505  0.060431138
##    [156] -0.290126366 -0.119935579 -0.722056963 -0.996430913 -2.246723202
##    [161] -2.875302775 -2.293585520 -0.976814674  0.242385742  0.088695083
##    [166] -0.983143415 -1.554424692 -1.667406012  0.427355647  0.736419665
##    [171]  0.530627502 -0.245319630 -0.523778529 -0.500453944 -1.282777634
##    [176] -0.537122721 -0.230462369  0.449677035 -0.331493143 -0.937395512
##    [181]  0.768208082 -0.306662871  1.489838302  2.137190931  2.106106133
##    [186]  0.376249342 -2.585645032 -0.551732071  0.590372429  0.194840680
##    [191]  0.817039347  0.139175753  1.335117107  1.597360198  0.824897216
##    [196] -0.232720930  0.890686983 -0.208221967  0.644431643  0.599855593
##    [201] -0.607238480 -2.051377858 -1.662814445 -0.886590859  0.307746068
##    [206]  1.918367191  0.845644793  1.409322867  1.947083613  2.055598594
##    [211]  1.283094116  0.786281014  0.427161939 -0.090882080  0.317232922
##    [216]  0.395138053  0.183216593 -0.528052765  1.117210284  1.011310642
##    [221] -0.490551077 -0.968876404 -1.274098832 -2.014610602 -3.162963932
##    [226] -2.474281075 -0.558647794  0.753356539  1.081982160 -1.148450019
##    [231]  0.512589898 -0.566956209 -0.232583017  1.703370271  0.984180049
##    [236]  1.645782798  1.632483702  1.335205281  0.234421187  1.402223011
##    [241]  1.798823048  1.167556973 -0.072769615  0.999464698  1.513300828
##    [246]  1.059075046  1.314511375 -0.080020093  0.959414490  0.058081138
##    [251] -0.358274835 -0.521991279 -1.295898900 -1.359889845 -0.091715241
##    [256] -0.774150715 -0.955755178 -2.040416531 -1.007260548 -0.173280506
##    [261]  0.263503550 -0.357726809  1.068083676  2.001454077  1.159165946
##    [266] -0.666217998 -1.879095270  0.470808371  0.588919353  0.490873828
##    [271]  0.130536006  0.754688402  1.402889504  0.689764348  0.953325060

```

```

## [276] 0.527256805 0.359429738 -0.204097675 0.509859488 0.361382810
## [281] -0.215895510 0.091353481 0.283282050 -0.940034953 -0.100677553
## [286] -0.189549425 -0.220673481 0.820986152 0.111697347 -0.931342253
## [291] -1.197737147 -2.563836021 -1.191599784 0.056594464 0.669330326
## [296] 0.828101817 1.110116918 -1.010658259 -1.125001398 -0.468550482
## [301] -0.047761298 -1.210288582 0.096686091 -0.425174890 -2.276953334
## [306] -2.574420680 -0.080872993 0.455070867 0.651166642 -0.185085329
## [311] 0.306290751 -0.521750288 -0.572454451 0.437275445 -0.888064771
## [316] -1.743121431 0.176174793 -0.031817205 0.383264035 -1.643166425
## [321] -1.117841093 -2.234528557 -0.728734744 -1.133532138 0.413513068
## [326] 0.512961573 -0.648155772 0.599898440 0.143330290 -1.090048647
## [331] -0.163463441 -0.272834525 0.146357404 -0.466527683 -0.599891460
## [336] -1.587613143 -1.401157365 0.372364040 -0.460105558 1.067540512
## [341] 1.312075844 1.328624702 1.259249864 1.055771075 0.017287292
## [346] -0.257807384 -0.032738580 1.694788735 0.157987078 0.189591773
## [351] -0.384906093 -0.501299964 -0.411454657 -0.393525448 -1.396445130
## [356] -1.236263632 -1.555137386 -1.815000219 -1.398748721 -2.179327620
## [361] -1.047775497 -1.314642995 -0.691471432 1.204240236 1.272231810
## [366] 0.421579420 -0.137267501 -0.400632415 -0.275022142 -0.684116614
## [371] -0.935209964 -0.763378259 -0.484882957 -1.769804427 -0.050349363
## [376] 1.079417653 0.944889389 1.172067101 1.799884220 0.036751909
## [381] 1.030204979 -0.412452635 -0.078159020 0.503553665 1.114564744
## [386] 0.086790370 -0.418566670 0.637845072 0.053186796 -0.636284976
## [391] 0.330896952 0.787502523 0.361852822 -0.241318376 -1.232460280
## [396] -0.427082099 -0.351342542 1.137696634 1.392235631 -0.922692718
## [401] -0.641118766 -1.424708926 0.505299668 0.538081081 -0.913826950
## [406] -1.024731067 0.032150667 -0.463527038 -0.263657751 -0.427817126
## [411] -1.143523675 -2.204943458 -1.821692268 -0.947044694 1.247905863
## [416] 1.769758308 0.167248606 -0.055790565 -1.003241916 0.761972911
## [421] 1.139473273 0.416322427 1.829855608 0.858535377 -0.556246530
## [426] -1.958543952 -2.826937740 -0.777527294 0.573800007 2.251843975
## [431] 1.663870482 -0.292183454 -2.025293554 -1.895161894 -0.374911930
## [436] -2.001642598 -2.967104879 -2.468764738 -2.989102328 -1.701960611
## [441] -0.731781927 -0.734345962 -1.473061776 -1.440223131 -0.628030337
## [446] -1.425296434 -0.915273927 0.136969615 1.429213013 2.540370654
## [451] 0.139705240 -1.316363958 -1.615595724 -2.134434591 -1.267555168
## [456] -2.307917186 -1.799995733 -1.480713953 1.537528175 0.662679135
## [461] 2.084341994 -0.145868476 0.245808497 1.304449004 1.602329733
## [466] 2.893699927 2.496298893 1.943517828 1.184656442 0.871609000
## [471] -0.983562828 0.502454038 1.569251420 0.340032764 1.355220433
## [476] -0.191939268 -1.443066614 0.081270834 -1.157889939 -2.167177557
## [481] -2.332703433 1.469304913 0.498026311 1.510553066 -0.288472630
## [486] 0.316376907 -0.305587793 1.637677506 0.191787629 -0.586793744
## [491] -1.248457779 0.575575098 0.272058774 0.249445458 -0.367261079
## [496] -0.628932102 -0.804499764 -0.853437439 -0.349221302 -1.013636343
## [501] 0.274864538 0.866009199 -0.293214855 0.722125142 0.995026678
## [506] 2.125299000 2.476049263 0.747642980 1.299044375 0.404404652
## [511] 1.551212798 0.792515256 -0.545330455 -1.438128832 0.429048137
## [516] 0.060227600 -0.895122492 1.250901326 -0.304090230 -0.536476600
## [521] -1.034631793 -1.553837472 -0.304983490 -1.117700509 -0.710809171
## [526] -2.074043396 0.196945363 -1.325404667 -0.817854948 -1.126489725
## [531] -1.143471423 -0.370089885 -0.208881672 0.459703613 -1.629977890
## [536] -0.066552480 0.692045836 -0.837138477 0.654349131 -0.174845661
## [541] 0.312218197 0.534662606 0.952581667 0.972230835 2.462397176

```

```

## [546] 1.820274133 0.383827604 -1.629063170 -2.028613582 -1.932256165
## [551] -0.148832004 -1.642653185 -0.664407954 0.090768397 -0.082930293
## [556] -1.093764703 0.337255747 0.411607438 -0.255305218 0.624477179
## [561] 0.633103151 2.737806818 2.112632215 1.402102046 1.181294803
## [566] 0.633109099 -0.673959620 0.357609927 -0.062351776 0.300063313
## [571] 0.038074259 1.437302880 1.509078520 -0.968410032 -0.786151424
## [576] 0.059856673 1.604655717 -0.257130582 1.058508187 0.433134897
## [581] -0.833062339 1.253928197 1.042015250 -1.174232958 -1.311795313
## [586] -1.193627340 -1.549292049 -1.149935199 -2.308699115 -0.478343407
## [591] 0.348974614 0.445744743 0.812254688 2.067861485 1.503460390
## [596] 1.667609496 0.412088707 0.503770088 0.735100695 -2.149741496
## [601] -0.471593220 -0.300050905 -0.280594534 -0.482289486 -0.159725166
## [606] 0.723752251 1.327746703 0.450966286 0.913489948 2.170595089
## [611] 0.973068696 0.860895585 -0.193674411 -1.882187306 -1.462166949
## [616] 0.014138003 -0.437480182 0.303820532 -1.105766202 -0.818201903
## [621] -0.305177504 -1.205070000 -0.695757235 -0.305764773 -0.008614009
## [626] 0.884829917 -0.382198851 -0.842802358 -0.122665858 0.064120135
## [631] -0.714586585 -0.826567460 0.620332923 1.397985693 1.779525061
## [636] -1.149733675 -1.169755147 0.782535487 -0.426421173 -0.407763414
## [641] -0.586113114 -1.076188169 -0.841138760 -0.368181937 0.966635981
## [646] 1.559989625 1.710068692 0.016420781 -0.231548829 -0.665872539
## [651] -0.726290541 0.581292070 0.838360555 2.628618826 2.629096456
## [656] 1.936379645 2.849289484 1.711810864 2.229815777 -0.527265993
## [661] -0.140210295 -0.343397472 -0.002496108 -0.232971472 -1.535371030
## [666] -2.850005194 -0.070822269 0.443386393 -0.101263278 0.572615815
## [671] 1.273343710 2.475530478 0.999289908 0.434983267 1.807659796
## [676] -0.447790641 1.623050945 1.549695021 0.556790125 0.507196354
## [681] -1.014453886 -1.446691706 -0.204543486 -0.190771944 0.332505717
## [686] 0.873459815 1.542870656 2.298439643 1.374357113 1.813205824
## [691] 0.938591675 0.007975598 1.069399723 1.046042689 0.909014493
## [696] 1.666486394 1.272466333 0.613570285 -1.015508117 -0.406229696
## [701] -0.247092310 -0.822426276 -1.227652233 -0.952649462 0.991587298
## [706] 2.241690829 2.308278995 0.569284094 -0.894132587 -2.563419821
## [711] -2.003859876 -0.172232029 -0.583109551 -0.387295255 0.863562188
## [716] 2.083213570 0.543272900 -1.835345560 -1.360921746 0.068474494
## [721] -1.647917683 -2.298409705 -1.493639348 -1.319307601 -0.432838066
## [726] -1.029925922 -1.008311994 -0.298058063 -0.001179363 -0.138010696
## [731] 1.722686102 2.297786724 -1.098423080 -0.857304262 0.697692475
## [736] 1.094178278 2.723650197 1.153496382 0.620721842 -0.087537474
## [741] -0.585968641 -1.561279771 0.208462516 0.806407408 0.482664612
## [746] 1.146118450 1.387607741 3.294084501 1.162382028 0.174088961
## [751] -1.084616629 -0.094467883 0.159783039 1.504705761 -0.525176458
## [756] -0.907849474 -0.224978852 0.086182308 -1.450818688 1.050466751
## [761] -0.131321155 -0.574142932 -0.319981396 0.156316703 -0.975977850
## [766] -1.018071979 0.604058285 0.148407087 -1.042277458 -0.452547347
## [771] -1.131700188 0.144160722 1.438542659 -0.570705002 0.752180868
## [776] 0.290496563 0.006830768 -0.455474432 0.729998610 3.328711368
## [781] 2.803678092 2.507300914 0.330574756 -0.508214472 -0.126546769
## [786] 0.123987039 0.584558883 -0.788252781 -0.597522077 -1.080072488
## [791] 2.335641530 2.027453869 1.683188456 1.832599624 0.814815902
## [796] 0.546078634 1.201461518 0.272636994 0.334762070 0.930782524
## [801] -0.510874397 0.030213807 -0.246601819 -0.455580057 -1.755403216
## [806] 0.981677883 -0.079218540 0.789605427 0.362685886 -0.660959843
## [811] -1.025148137 -1.286709718 -1.666739443 -0.777308741 -0.349693911

```



```
## [816] -1.218026452 -1.169596214 1.047309718 2.850333302 2.229817197
## [821] 0.498552875 1.890568634 0.754249372 1.075441411 -0.818795730
## [826] -0.450648564 0.207843816 1.060332762 2.179489306 1.753997111
## [831] 2.250307230 2.008920859 1.946271039 -0.399025930 -0.969887562
## [836] 1.413818296 0.447583310 0.909767815 -0.276107851 -0.879860565
## [841] -0.779196101 -1.789079867 1.002395926 2.937467205 2.127800064
## [846] 1.024924033 0.145529031 1.401074729 0.499781311 1.572954811
## [851] -0.643884123 2.109070271 1.604312631 0.905496656 0.368056250
## [856] 0.425671149 -0.344099421 0.981115079 0.742805853 1.036281719
## [861] 1.742592977 1.883625886 1.234425284 2.644697198 0.935222046
## [866] 0.728958374 0.965799512 1.014452993 0.116614198 1.631913871
## [871] 0.765593946 1.247163883 0.755835639 0.698276218 0.365883280
## [876] -1.623713138 -0.300271135 0.049835564 1.368240004 -0.102928806
## [881] 0.672573664 -0.134967542 -0.563238014 1.230978252 0.629060658
## [886] -0.457308592 -1.165605593 -0.552855512 0.498972696 -0.066356491
## [891] -0.501723389 -0.835626206 0.079131301 0.289013629 -1.631724192
## [896] -0.054137646 -0.898934185 -0.607896013 -0.233416259 1.075878954
## [901] 1.056093544 -0.119628722 -0.363133517 -2.117013376 -2.226529242
## [906] -0.891739505 1.178922400 2.471440621 1.557801343 -0.684069718
## [911] -1.829039988 -0.910628128 0.993956163 1.465961433 1.897945612
## [916] -0.271400257 0.592506376 0.569605473 0.554884654 -0.523736002
## [921] 0.005857625 1.113970563 0.662422405 -0.400166928 -0.639520684
## [926] 0.077413379 -0.688965229 -0.216699361 0.503291188 -0.660016476
## [931] -0.005911302 0.929616876 -2.330120993 -1.795528635 -0.737655120
## [936] -0.312444066 0.457305177 1.221030515 0.502625106 -0.515056230
## [941] 1.372522169 1.122486126 -0.085992374 -0.066878797 0.645325257
## [946] 1.183860815 0.177037317 1.291948624 -0.701795048 -1.474350762
## [951] 0.603062988 2.178690656 1.976996821 0.914321880 0.100181558
## [956] -1.052849930 1.421160853 0.680031998 1.109974219 0.431391949
## [961] -0.319309048 0.475516209 1.947544229 3.417663807 2.143516306
## [966] 1.208228827 1.386953111 -0.081470736 -0.589017016 1.666735032
## [971] -0.009175304 -1.106446599 1.949954433 2.628046560 1.881629243
## [976] 0.218936457 -0.280166410 -1.196775323 -1.322859820 0.127535727
## [981] 0.024523397 0.384232329 -0.046344120 -1.626622182 -2.273502184
## [986] -2.236112655 -2.983324302 1.085607554 0.935816512 0.584955346
## [991] 0.605705412 1.397656310 -0.010386224 -1.494341374 -2.935726479
## [996] -1.494996268 -0.963731584 -1.450405033 -0.500906979 -0.008219860
```

```
#ARMA(0,1)
```

```
ARMAmodel_2_new<- arima.sim(model=list(ma=0.9), n=1000) #the MA coefficient is 0.9
```

```
ARMAmodel_2_new
```

```
## Time Series:
```

```
## Start = 1
```

```
## End = 1000
```

```
## Frequency = 1
```

```
## [1] -1.404578112 -2.118869455 -0.810877185 0.357346001 -0.674597267
## [6] 1.131971329 0.709501015 -0.794464617 1.569798368 0.807878444
## [11] -2.180101485 0.331217887 0.156780954 -1.439101524 0.385919517
## [16] -1.255540477 -4.121854502 -1.514365753 1.343029853 1.062176586
## [21] -0.365158669 -2.031975341 -1.325717571 0.131072248 -0.367374868
## [26] -0.053007902 -0.359103445 -0.053146198 -0.326032461 -0.747494411
## [31] -0.722689856 -1.970760161 -3.526795149 -3.320871740 -1.675020180
## [36] -0.919167785 -0.226725185 -1.186676225 -1.579215094 -1.901432259
## [41] -2.046046932 -0.744922564 -0.664447625 1.715135255 0.491514137
```

```

## [46] -1.682699281 -1.837772903 -1.116636711 0.924457792 -0.306227772
## [51] -1.725882613 -0.274405887 -1.060587208 -1.791386291 0.061860282
## [56] 0.152791968 0.123305701 -1.291652981 -1.356828754 1.843344801
## [61] 3.084270690 -0.561453509 -2.924523059 -0.913222804 -0.729479284
## [66] -1.898255907 -1.275764564 -0.513463899 1.751664335 2.908063913
## [71] 0.374080366 0.389077188 1.016451974 0.027919342 0.484422515
## [76] -0.319977777 -0.810314272 1.780136069 -0.195425178 -3.331209048
## [81] -2.193397278 0.004340358 0.205306756 1.058368473 0.928991548
## [86] -1.825224038 -0.999771255 0.833685878 1.396970735 0.631795882
## [91] 0.299668332 -0.470108331 -0.551330061 0.917019282 0.693033577
## [96] -1.265258951 -2.271017545 -0.890678238 0.341624847 0.095402363
## [101] -0.744557082 -1.206349593 0.220115069 1.785706115 -0.285719567
## [106] -2.623829358 -1.536504481 0.628582234 0.186863253 0.538953449
## [111] 1.231180728 -1.314379467 -0.851091664 0.567069771 0.279781884
## [116] 1.642978509 0.804273623 -0.928092357 -1.678804864 -2.402778014
## [121] -2.332036661 -0.958975944 -1.607438316 -2.071759904 -2.421944878
## [126] -1.647053163 1.129215437 -0.111699152 -2.383982899 1.083807567
## [131] 3.541971938 1.072772681 0.778046965 1.902842668 0.314544307
## [136] 0.573015985 1.082669597 -1.359866426 -1.509161358 -0.247055481
## [141] -0.590424306 -1.124856973 0.532162736 -0.945758061 -0.860745051
## [146] 0.970185619 1.504497950 1.350300284 0.975843114 1.875960018
## [151] 0.283448060 -2.605915092 -3.595197258 -3.304887125 0.429857774
## [156] 0.151984942 0.014397133 1.514929203 0.160662937 -2.216588278
## [161] -1.094052117 -0.415709303 -1.778865378 -1.519490090 -0.181924548
## [166] 0.828847553 0.507011815 1.825489979 2.158671647 -0.695888056
## [171] -2.810341404 -0.064963020 1.820375202 -1.419478975 -0.558646604
## [176] 2.399577048 0.722760000 -0.974455529 2.237633699 1.935845244
## [181] -0.048727736 -0.305575885 -1.946664540 -0.279702677 1.397986180
## [186] 0.098863188 -1.247079369 0.263040306 -0.649444315 -2.308338740
## [191] 0.169879859 0.388419390 1.134608504 1.695731279 0.176222278
## [196] 0.853410720 0.551416531 -1.773719924 -0.782575952 0.194535738
## [201] 0.854167674 0.995440768 -0.054435852 1.091325712 2.431370227
## [206] -0.589223210 -2.642771302 -1.039173306 0.909613882 1.152536204
## [211] -0.686705509 -1.133988116 0.114298621 1.008988272 0.257059425
## [216] 0.151903858 0.151829607 -0.749728482 -1.404853099 0.031345279
## [221] 1.694185646 -0.246289701 -0.784659787 -1.192353235 -1.204218998
## [226] 0.658296075 -0.022773347 1.311913915 0.855975506 -1.048631976
## [231] -0.354589087 -1.270883365 -1.842636365 -3.030333090 -2.585307227
## [236] -1.244631167 -2.611634766 -2.232815296 -0.830544596 -0.142344266
## [241] 0.508018348 -0.126435300 -0.085974203 0.947104745 0.986638114
## [246] 0.155925410 1.330127658 0.700659425 -0.019043784 1.507795640
## [251] 1.483091856 0.433095244 -0.041118196 -0.354991970 -1.145835680
## [256] -1.067702245 0.494714335 -0.690295459 -0.103401453 0.886041040
## [261] -0.583729699 1.128241249 1.591536735 2.428955228 4.296490300
## [266] 1.692566877 0.262259291 0.416800446 0.265424104 -0.097684365
## [271] 0.607943207 2.308430225 0.593236030 0.136235555 0.739349652
## [276] 0.635906140 0.056490608 -0.274250322 1.820942021 1.082727141
## [281] 0.062995553 -1.131267371 -2.882759616 -0.318915034 3.056306056
## [286] 1.676781375 1.886077659 2.530540802 0.832818691 1.508996807
## [291] 1.586203627 -0.685470266 -1.967767089 -0.620780610 0.376155365
## [296] 0.091622753 -1.891218513 0.412466860 1.008459592 -1.394044074
## [301] 1.712663451 0.671252869 -1.782209962 -0.566893627 1.699288261
## [306] 1.584612156 -1.110516249 -1.313772433 -0.580633655 0.469827246
## [311] 1.205786289 1.395496803 -0.103962852 -1.336499758 -0.278301402

```

```

## [316] 1.357317523 0.685181808 -0.411490801 1.279841509 1.705410976
## [321] 1.449019289 -0.050959837 -1.452249239 -0.169008785 -0.935066094
## [326] -1.054843608 -0.037627464 -1.187919754 -1.181202922 -0.772618967
## [331] 0.390577565 0.778159137 -0.001541372 -0.289234749 -0.486760493
## [336] 0.217088122 -0.992665164 -1.595835299 0.225098591 0.458366366
## [341] 0.222819609 0.323139934 -0.036324201 -1.226770128 -0.347896295
## [346] 2.077037832 1.699285475 -0.056515835 -0.876855902 -0.376229842
## [351] -0.598172329 -0.603725059 0.432292737 -0.670582686 -1.258749135
## [356] -0.510588254 0.280586618 -0.042109815 -0.355250029 2.659638576
## [361] 2.164175865 -2.148201382 -1.746144329 1.165627635 0.147844408
## [366] -1.413054948 -0.171723732 1.096714530 -0.480947845 -1.229087095
## [371] 0.181497554 0.539881149 0.838847109 0.179337632 -1.554847531
## [376] -1.217667192 -0.424321084 0.427562898 1.306329086 0.244733907
## [381] -0.018319974 0.482629490 -0.689041073 -1.667116304 -0.346319356
## [386] 0.064570777 -1.574264567 -2.207440506 -1.051945280 -1.111121411
## [391] 0.167807696 0.201134378 0.683058687 -0.664759479 -1.212830635
## [396] 0.696734970 0.158828102 1.583942327 1.791372021 0.465377020
## [401] -0.363091916 -1.104795969 -0.164717842 2.522524612 1.169984651
## [406] -1.372610986 0.081996579 0.398115809 -2.003742795 -1.994834948
## [411] -0.373964865 0.373148876 3.117540208 1.343549843 0.188719874
## [416] 2.568912048 -0.371158417 -2.189283626 0.152828339 0.827949663
## [421] -1.042314055 0.184793628 0.017973245 0.524704647 0.311107670
## [426] -0.273845822 0.744176584 -0.573672955 -0.861115223 -0.911375372
## [431] -0.541780258 0.437496710 -0.754191975 -1.203015983 -0.185069528
## [436] 1.535955730 3.527300695 2.016039842 -1.081232177 -1.809879892
## [441] -1.498765164 -0.953016973 0.413470579 1.111714419 0.789372683
## [446] 0.072918144 0.736765955 2.562611901 1.836293966 0.917861686
## [451] 1.881562860 1.393737833 2.583824241 0.755098410 -1.660852137
## [456] 0.468562471 -0.998536703 -3.168271897 -1.277768552 0.324566612
## [461] -0.003663940 0.093115907 0.377134664 0.583357198 1.437986467
## [466] 1.393354158 2.126828448 1.147804663 -0.078685685 0.865687682
## [471] 0.753046555 2.047492939 0.437474211 -1.838813403 -0.762289951
## [476] 0.134168511 -0.885294385 -0.505405161 -0.493840511 -1.057834450
## [481] -0.559922670 -0.702724120 -1.570278413 -2.560255320 -3.628889625
## [486] -1.727296752 0.833344561 -0.745084817 0.042634048 0.262861573
## [491] -0.644089229 0.990125147 1.596641535 -1.130352719 -3.445546100
## [496] -2.183566181 1.566385317 2.260174538 -0.096599064 1.302802047
## [501] 1.375947306 -0.589994233 0.288432191 0.544375794 -1.129854081
## [506] -1.433315135 0.162614327 1.012131173 -1.460079214 -1.238326908
## [511] 0.088601795 -0.098459313 -0.308925648 0.982919538 0.732791749
## [516] -1.596193548 -1.249977806 0.217930734 -1.192207980 -1.633116811
## [521] 0.150441047 0.886872315 0.933184593 1.356049727 -0.083941390
## [526] -0.875949978 0.246058196 1.556363814 0.949774708 -1.232525770
## [531] -1.605253476 0.155922434 3.201660617 1.079067401 -1.382909175
## [536] 0.710039063 3.244282387 0.738267915 -1.093850887 2.111679744
## [541] 0.797110758 -0.088390595 0.768355994 -0.739508348 -2.358387242
## [546] -0.958121428 0.869862130 -0.292111128 -0.284069123 0.305448080
## [551] -0.722874198 -0.131913282 -0.968391621 -0.534947434 0.279385194
## [556] -0.397542110 1.430931174 2.562702623 1.430667067 1.766922085
## [561] 0.245960711 -0.105916915 -0.474119380 0.150180051 0.896794352
## [566] -0.257731455 0.393101117 -0.106567107 0.353601296 -0.478827686
## [571] -1.222779340 0.262214771 -0.222632164 -1.131732609 -0.970708803
## [576] -0.539874750 0.493472596 1.299419200 1.091529920 1.332658567
## [581] -0.102004746 -1.514629252 -2.528029567 -2.649271782 -1.459547395

```

```

## [586] -0.427625848 -2.313588909 -0.189292576 0.410061001 -1.685680213
## [591] -0.360502202 -0.626706196 -0.227125464 0.473723536 -0.424210463
## [596] -1.060918570 -0.077038442 1.095763356 -0.127839352 -0.062912565
## [601] -0.647808748 -1.674099353 0.115686528 2.221674333 1.121893281
## [606] -0.094070635 0.556723978 1.796641898 1.481627470 0.253949151
## [611] 0.029720508 0.938488257 0.182794240 -0.712815478 -0.367382585
## [616] -0.365942827 1.308113010 0.370827956 -1.479579808 -0.524550493
## [621] -0.023980918 -1.461644526 -2.494439630 0.065405603 1.123178045
## [626] -0.082537169 -1.317902444 -2.672175356 -1.243457550 0.803047253
## [631] 0.978964053 -0.884330249 -1.881034997 0.180990121 -0.674662903
## [636] -1.080913052 -0.146192267 -0.299167459 0.109919749 0.369838774
## [641] 0.966974358 0.987377287 1.979792886 1.893587089 1.632274905
## [646] 0.616170934 -0.775339869 -0.178968760 0.788946563 1.839985928
## [651] 1.290939797 -0.986242356 -2.947435624 -1.164197338 1.186969239
## [656] 0.725342792 0.977574232 1.380209038 0.993193394 -0.859979327
## [661] -0.649999368 1.358084307 0.499835841 1.615429126 2.220823617
## [666] 0.710627451 1.687220325 0.670563094 1.033032426 3.147858568
## [671] 2.196639981 0.351092011 0.571860040 1.265579840 1.371072189
## [676] -0.114854480 -0.030860624 0.087055039 -1.658517366 -0.756610029
## [681] -0.313550581 1.333344113 2.051852760 -0.073640494 0.283348995
## [686] 2.052851554 1.736164854 0.285703520 -0.322315369 -0.088310899
## [691] 0.945630547 0.058956154 -0.957299011 1.633132383 1.911995845
## [696] 0.809981905 0.617490331 1.067489156 -0.150273061 -0.204059137
## [701] 2.626407343 1.585802984 -1.219429156 -2.072393841 -0.987930028
## [706] 0.596315047 1.179359853 1.924825837 0.641511515 -0.293137389
## [711] 0.303392598 1.114616043 2.412098893 0.760157338 1.447960526
## [716] 2.700262078 0.979196885 0.879946325 0.518859236 1.463058219
## [721] 0.455866802 -1.568248115 -1.654978003 -2.263899346 -1.298781147
## [726] -1.523631010 -1.663673338 -1.598250251 0.219052011 1.565375881
## [731] 1.760806092 3.158576671 2.849055880 1.324653092 -1.317354617
## [736] -1.779687889 -0.537544568 0.772979678 1.429869970 0.879636539
## [741] 2.435904215 0.314641305 -1.488887945 -2.088648571 -1.625725972
## [746] 0.137394969 -0.609716380 0.224641487 0.309227351 -2.865208164
## [751] -2.678008599 0.429749106 0.905643654 0.821394116 1.289795575
## [756] 1.261335696 0.439204503 -0.857015593 0.636601250 1.039166544
## [761] 0.124514545 3.201932454 2.425935570 -0.360411123 -0.501775508
## [766] 0.377020552 0.991528524 -0.373010133 -0.544240173 0.253701214
## [771] 1.762842564 -0.273983127 -1.442255356 0.972266561 -0.030961236
## [776] -0.121392209 1.622288626 1.803740373 0.940973351 0.439664479
## [781] -0.226383040 -0.872574919 -0.644593720 -0.259719224 -1.243859860
## [786] -0.726800754 -0.733622516 -1.988299400 -0.394761974 -1.228273264
## [791] -2.191344636 -1.295991456 -0.020401517 -0.654810940 -2.077720638
## [796] -2.467005846 -2.169718385 -0.106832334 0.328733591 1.546735033
## [801] 2.554551551 -0.950023176 -2.882325141 0.325908702 -0.159328649
## [806] -2.710888772 0.153559411 0.984237104 0.749527002 0.798860547
## [811] -1.105532392 -0.944097642 -1.346922720 -1.114978287 -1.566493208
## [816] -0.765671398 1.089521741 -1.593316337 -1.844139787 -0.802971137
## [821] -2.185265613 0.008062368 1.434836288 1.605610993 2.130660277
## [826] 2.665341611 2.750437372 0.699293546 -0.025119238 0.176459764
## [831] 0.215624528 -0.599601604 -1.011672289 -0.524179899 0.015952599
## [836] 0.376521080 -0.735631567 -2.562352364 -2.863248089 -2.231739448
## [841] -2.939089905 -2.060484146 0.676709346 2.258986069 0.954583295
## [846] -1.062200402 -1.069301245 -1.031455253 0.078538706 0.580977720
## [851] 1.544680653 1.408998984 -1.837327343 -1.449430905 1.185767925

```

```
## [856] 2.026594864 0.284800603 0.337341283 -0.998100584 -1.816317270
## [861] 0.468176654 0.569613984 -1.063358690 -1.576206521 -1.872934144
## [866] -0.878103289 1.366991243 2.238912373 -0.144539433 0.011698514
## [871] 1.710708322 0.335272702 -0.614540110 -0.866466534 -0.085092149
## [876] -0.895966641 -1.953916617 0.117952375 0.387956332 0.440123738
## [881] 0.570658799 -0.607399658 0.828129165 -0.570141684 0.173142944
## [886] 1.311126611 0.482020522 0.674719811 1.072667194 0.165265798
## [891] -1.009057496 -0.187242921 -0.340034275 0.224723499 -1.137168200
## [896] -3.097778129 -1.044968432 1.416071367 1.284054706 -1.419480378
## [901] -3.280823120 -1.925712141 0.021813953 1.435488855 1.373501946
## [906] -0.629175038 0.805533183 2.430420702 -0.013809401 -1.474077934
## [911] 0.050516920 0.179900014 0.164581809 0.241986413 -0.903460536
## [916] -1.375153732 -0.629014741 1.009262555 1.337586028 -0.767865282
## [921] -2.519126212 -0.893155861 0.709908650 0.957061970 -1.130204173
## [926] 0.099320229 0.800245334 -0.723231839 -0.625653125 -1.207330296
## [931] -2.223709089 -0.953298595 1.818973997 0.128307162 -1.034103442
## [936] 0.736003851 2.267940360 1.987313891 -0.266541671 -2.565120220
## [941] -2.865006572 -0.885745368 -0.486756413 -0.953919499 0.391345164
## [946] -0.570908838 -0.887154856 0.771115014 0.327591104 -1.357616493
## [951] -1.303619613 -1.316209842 0.218706792 0.624056268 0.894531136
## [956] 2.512656912 1.400315610 1.928802999 1.321162345 -0.659519300
## [961] -1.631974164 -1.843428563 -1.210878923 -1.263139251 -0.691504035
## [966] -0.599111462 0.640323473 2.248080768 0.921221080 -0.457844939
## [971] 0.554698931 0.629737289 0.589199387 1.199885902 1.676870839
## [976] 0.657040078 1.360165083 0.796105283 -1.481220113 -2.019272261
## [981] -1.948077913 -1.430294428 -2.352498561 -0.048109040 1.757689519
## [986] 0.921427703 1.937198961 -0.009188981 -1.453195705 0.406044275
## [991] 1.251633234 -0.414418852 -0.610268521 1.675758652 2.654464485
## [996] 2.037013920 -0.189169389 2.024726586 3.980263160 0.636753598
```

```
#ARMA(1,1)
```

```
ARMAmodel_3_new<- arima.sim(model=list(ar=0.6, ma=0.9), n=1000)
```

```
ARMAmodel_3_new
```

```
## Time Series:
```

```
## Start = 1
```

```
## End = 1000
```

```
## Frequency = 1
```

```
## [1] 3.849216538 2.065263403 0.435336213 -1.458578973 -1.541657777
## [6] -2.670068911 -2.358997206 -0.526474612 -0.753657236 -0.370252032
## [11] -0.211940584 0.705584050 1.614575014 0.320468195 -0.542136072
## [16] -0.006704159 1.855650501 2.855615469 2.926865699 3.932652752
## [21] 3.027143609 1.124068612 -0.414676166 -1.363656056 -3.098298043
## [26] -2.985945201 -1.927637188 -3.612328127 -2.304669531 -0.106139277
## [31] -0.618385058 -1.526382701 -0.371441767 0.195813417 -1.270757711
## [36] -0.272996311 1.639534516 1.720336991 2.055064510 3.559866667
## [41] 4.251436924 3.461977608 1.838639977 -0.670073458 -3.019099472
## [46] -3.386308250 -1.680848905 -0.597414932 -0.176872775 0.569103593
## [51] 0.589480488 0.774706128 2.038185157 2.058371249 0.689551199
## [56] -1.433585657 -1.880940294 -1.937687884 -3.593108727 -2.582743570
## [61] 0.308424508 1.467380907 -0.248115119 -3.953417588 -3.277222721
## [66] -2.238283628 -2.531548710 -0.346354747 1.152901515 1.872968965
## [71] 2.009743409 1.341414035 1.006265974 1.379193830 1.529793542
## [76] 1.885670345 0.906667765 -0.045173900 -1.531872782 -2.401708324
## [81] -0.809691325 0.239414376 1.615196011 0.521510681 -3.581228134
```

```

## [86] -3.120649130 1.546663296 2.720892519 2.101732844 1.938683228
## [91] -0.540803776 -0.313042925 1.589925303 0.091194617 -2.403089608
## [96] -3.434084262 -1.388128198 0.129952914 -0.198407422 -0.228261680
## [101] 0.218636234 1.185444043 -0.194656305 -0.521243981 0.672496406
## [106] 0.982710826 0.589462626 -0.190499954 -0.723788218 -0.319574681
## [111] 0.818200759 1.814088884 0.665189463 -0.342422165 -0.131674110
## [116] -0.200959836 -1.019803381 -0.271595401 0.278574373 -0.387856018
## [121] -1.037836832 -0.166993991 0.641297481 -0.797357461 -0.754717291
## [126] 1.009734870 0.892066499 0.752147554 2.426044404 3.181938606
## [131] 3.072749735 1.846766437 -1.088876375 -2.640474045 -1.727666748
## [136] -0.867867343 0.007411384 1.605476404 2.858560432 2.411488096
## [141] 1.939473255 3.968542914 2.999000686 -0.388419243 -0.544820368
## [146] 1.066074213 1.376115286 2.021608366 1.498656518 -0.028477730
## [151] -0.134844297 -0.718692078 -2.082941615 -3.689363702 -1.891904300
## [156] -0.262936415 -2.031197080 -2.133378844 -0.241315554 0.628526035
## [161] -0.412538030 -1.914290741 -1.808873935 -0.209759307 -0.223877448
## [166] 1.203738614 5.077991954 6.141884364 5.090165450 3.153581453
## [171] -0.224015061 -2.875754995 -0.584163559 2.465560600 1.296419472
## [176] 0.753794312 1.310396031 -1.715341500 -4.751430960 -3.890152820
## [181] -1.596171752 0.431841442 2.272479927 3.251931844 1.324415429
## [186] 1.321070604 0.734446282 -2.164981456 -3.127283666 -1.749546404
## [191] -0.920412412 -1.623856738 -0.830103091 -0.171939828 0.003906364
## [196] 0.978495075 -0.508931259 -2.327265265 -2.467302975 -1.129500321
## [201] -2.815245413 -4.105443209 -2.947439580 -0.586740418 1.204473857
## [206] 0.131940887 0.704737514 1.034991705 0.409494814 -0.543190867
## [211] -0.581053242 0.062989994 0.179162404 -1.729025915 -4.760439619
## [216] -2.815717883 0.773944576 3.489679987 3.134674460 1.898166163
## [221] 1.051862476 -0.670687246 -0.948272055 -0.947759720 0.004331805
## [226] 1.119210769 0.676727986 0.306941459 1.919839415 2.647475465
## [231] 2.006774833 0.663363192 1.740399983 2.303789644 0.138772161
## [236] 0.098417122 -0.167399332 -3.138080051 -4.269322660 -1.941725558
## [241] -0.179856736 -2.337871458 -5.123298696 -6.109955605 -4.548068508
## [246] -1.246096868 0.926665714 3.169643866 3.357851001 1.327946754
## [251] 1.412794504 -0.486937745 -2.874249049 -3.083263371 -2.030941705
## [256] -1.510866999 -2.375786759 -2.190798059 -1.288910697 -1.300748117
## [261] -3.356377236 -4.742806857 -4.392199794 -2.720154404 -1.305780478
## [266] -0.743542018 0.610261596 0.280618450 -1.239116777 -1.011307954
## [271] -1.331942049 -1.947243463 0.765028371 3.741220139 3.541444040
## [276] 3.151108193 3.062207853 4.037461846 3.062567392 0.432705448
## [281] -1.403761993 -2.470289892 -2.836777510 -2.627692823 -3.050462180
## [286] -3.233322575 -4.299873599 -4.543919007 -3.495874666 -2.031476576
## [291] -0.392907550 2.680554915 3.320975700 1.520918312 1.770703404
## [296] 3.941415097 3.519579075 0.136139109 -0.907729983 0.923678788
## [301] 3.010699369 1.952955251 0.783512531 0.780940207 1.460103705
## [306] 3.242859384 3.137970521 2.074085924 1.318490638 0.020562063
## [311] -0.060174717 -0.365348406 0.008728750 0.409820868 -1.082225137
## [316] -1.778639911 -0.746494876 2.088218199 1.525325115 0.548578193
## [321] -0.560656211 -2.288572791 -2.843728842 -3.305446868 -2.594918729
## [326] -3.015660718 -3.119953386 -0.692861325 1.934556511 3.969847581
## [331] 2.483944795 -0.109664970 -0.672583727 -1.220707884 -1.936636186
## [336] -1.423055771 -0.649723357 0.617829824 -0.240132811 -3.778383512
## [341] -5.096110957 -2.668506838 -0.894253171 -0.087856890 -0.124787538
## [346] -0.666064399 0.722025738 0.115534045 -0.007245667 0.987857645
## [351] -1.243473528 -1.564987236 -0.787580153 -0.303263726 2.073515198

```

##	[356]	3.360640392	4.339107141	5.918056692	5.749873196	4.515066736
##	[361]	3.786701916	3.081017370	3.837750121	6.389559435	6.734504653
##	[366]	5.290003225	4.877847100	3.504792038	2.073990413	1.926694234
##	[371]	2.977559520	3.947034140	2.969375387	3.238574886	2.886167744
##	[376]	0.705334865	0.065234516	1.421152380	2.149672891	-0.540000232
##	[381]	-2.604176258	-1.899538019	0.650991371	2.555332531	3.399904593
##	[386]	2.827380604	3.177438385	3.016155941	-0.755378002	-4.635847197
##	[391]	-4.345513482	-0.676400040	2.083130606	3.956312235	2.813034372
##	[396]	1.776630023	2.275614465	0.208607426	-2.548866482	-3.329123988
##	[401]	-2.317591491	-2.580657134	-3.571467345	-6.138717721	-7.727590111
##	[406]	-6.937192096	-4.736896725	-2.691195026	-2.039817396	-1.309198149
##	[411]	-0.979583206	-1.175954298	-1.323301295	-2.077290436	-2.390585970
##	[416]	-1.934316925	-0.714520055	2.457274327	3.797259629	1.690792224
##	[421]	-1.590568733	-3.446019740	-2.093368598	-0.378453383	-2.263871043
##	[426]	-3.723213850	-2.719111667	-1.878448758	-2.433953177	-4.487843757
##	[431]	-5.232554015	-5.604460755	-5.010623673	-4.770870804	-3.489378898
##	[436]	-1.009504094	-0.449530081	0.261297331	1.122571639	0.931439082
##	[441]	-0.587868391	-1.768070260	-2.691182939	-1.936649421	-1.661281520
##	[446]	-2.036363965	-1.262184595	-0.560398486	-0.920157474	-0.290560195
##	[451]	0.739220445	0.599096304	0.165742881	-1.018678225	-1.757780396
##	[456]	-1.470987885	-1.855792770	-3.288302245	-5.155436951	-3.354020120
##	[461]	-1.067212518	-1.549690511	-0.845183902	-0.063459152	1.606515635
##	[466]	2.749837207	1.390478371	0.063384555	-0.570714516	-0.399878788
##	[471]	0.355352696	0.469802264	-0.272609583	-0.241632121	0.455830367
##	[476]	0.747659384	0.863118907	1.064097052	0.026735053	-0.022113307
##	[481]	0.006045923	-1.383011896	-2.475211827	-4.258458797	-4.103106643
##	[486]	-2.215901349	-1.533864279	-0.896937950	-0.998018185	-1.098750885
##	[491]	-1.071525030	-2.283224794	-2.056500646	-2.513820655	-2.900530216
##	[496]	-0.347203127	-1.121474008	-2.520014405	-1.522977048	-1.059125668
##	[501]	-1.270439910	-1.656140673	-1.323306610	-0.849463394	-1.927655169
##	[506]	-2.954000971	-2.021956262	-2.151333764	-2.516609711	-1.800219242
##	[511]	-0.312369930	1.803656451	2.010640095	0.388484235	-0.936837630
##	[516]	0.485113084	1.792662652	1.180836847	-0.123355772	-0.751074968
##	[521]	-1.478289382	-0.517654534	2.103283584	1.211241918	0.618793823
##	[526]	1.798541046	1.985923122	3.002151206	3.339167014	1.248319666
##	[531]	-0.985512079	-1.213527362	1.259900663	2.670308744	2.026937454
##	[536]	2.257349789	2.026899330	1.626591594	0.941962296	-0.326683165
##	[541]	-1.389348948	-0.418014606	0.311250145	-0.192286198	-0.613790841
##	[546]	-0.777572611	-1.007628371	-0.766682910	1.327469466	2.398831807
##	[551]	0.946913477	-0.188685455	0.791879985	1.911208885	2.510563559
##	[556]	2.128482401	0.526001926	-1.270140682	-0.725144396	0.141159782
##	[561]	0.998428270	1.608560220	1.376785367	1.525225198	3.710466484
##	[566]	4.591333521	3.492204147	1.212028424	-0.044699614	0.714414999
##	[571]	0.188805719	0.782544417	1.811726752	-0.289491323	-2.778333517
##	[576]	-1.795480101	-0.602615389	0.023953291	-0.425937126	-0.808492232
##	[581]	0.043400535	0.497528555	-0.592769067	-0.835299502	0.203118455
##	[586]	2.043686875	3.456428678	2.362594205	1.686333793	0.696416391
##	[591]	-0.680179511	-0.629385435	0.895398381	2.439956207	1.629828283
##	[596]	0.861444954	-1.168049108	-3.272739461	-3.624396278	-3.697210186
##	[601]	-0.879715745	0.773270202	-0.996569827	-3.205647349	-3.569571553
##	[606]	-1.771372252	0.104770957	0.504299305	0.251168473	-0.102583860
##	[611]	-0.061184009	0.518218367	0.342538059	0.371653665	0.208049694
##	[616]	0.271135410	0.656292123	1.900280911	3.153391335	4.512263312
##	[621]	3.959176733	1.531922402	-0.439860636	-0.644362038	1.391737299

```

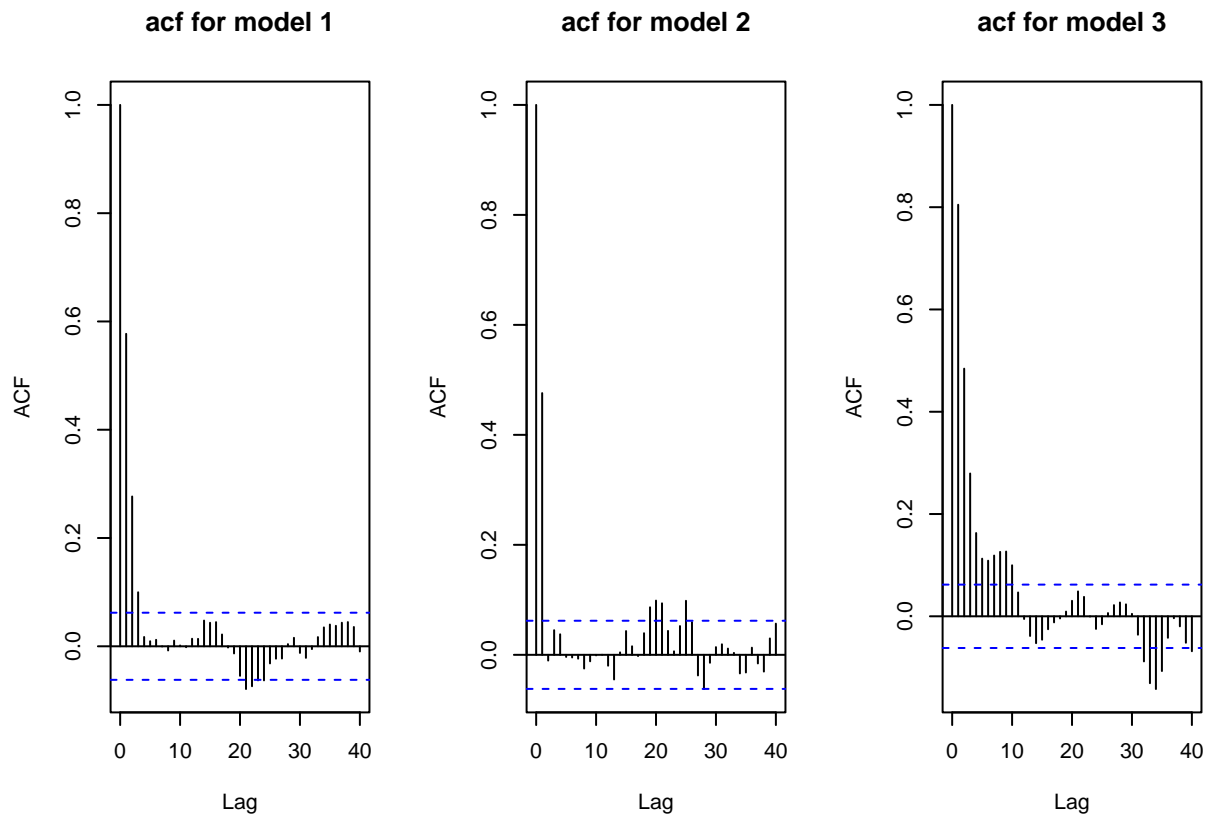
## [626] 0.768759611 -1.798996857 -0.811513928 -1.320653619 -2.524817963
## [631] -2.396448312 -2.695011556 -1.522399417 -1.484594047 -4.521524506
## [636] -5.639747974 -5.063762957 -4.841441797 -2.093123899 1.150717190
## [641] 1.092147173 -1.452865512 -4.573300993 -5.587827175 -4.493373942
## [646] -3.323900705 -3.645059243 -3.974686798 -3.598042243 -1.888957130
## [651] 0.182118010 0.377605522 0.832945002 0.005798867 -1.372145371
## [656] -0.184753329 0.893850615 -0.157664562 -0.156888779 1.588029241
## [661] 4.547269979 5.574452888 4.569171134 3.980094581 2.348355304
## [666] -0.183118719 -0.227449087 1.735053479 2.435540451 2.189991206
## [671] 3.304346885 2.487880686 0.360449698 0.662474186 -0.452950823
## [676] -0.203076811 1.730949552 0.994563356 0.337574068 -0.827718127
## [681] -1.829826122 0.566506472 2.614030395 1.777519818 1.110723208
## [686] 1.424797682 1.455305697 2.311055908 3.157145601 2.485691911
## [691] 2.638542247 3.849238828 2.410302774 2.602524135 3.701032499
## [696] 3.233384447 1.065552328 -0.327651300 1.255406123 0.667975758
## [701] -1.325335408 -3.556875832 -4.625911311 -3.861938799 -2.440118029
## [706] -1.617676118 -1.442891899 -1.341196953 -0.376372742 0.921959927
## [711] 1.120155431 2.060282377 2.005598232 1.769932588 3.144330070
## [716] 2.678277992 0.984780456 0.219200099 -0.610859529 -0.342345073
## [721] 0.429707386 0.472349740 1.233682628 0.538162690 1.259808337
## [726] 3.623779246 1.890411013 1.642954686 2.903321601 1.099934936
## [731] -1.256819282 -0.675745949 0.388219495 -0.859008249 1.509473705
## [736] 3.991014578 3.000010355 2.356100987 1.699060820 0.131907970
## [741] -1.239785914 -0.233286100 0.685957728 0.997034802 -0.395472018
## [746] -0.493702649 -0.629611009 -2.695626152 -2.499483443 -4.137653868
## [751] -4.626349131 -1.573962720 -0.912059588 -1.171617321 -1.592050355
## [756] -1.882140660 -0.926083617 -0.064601912 -3.016701447 -6.329806500
## [761] -5.981378551 -4.792670871 -2.974099747 -1.970392024 -1.436834758
## [766] -1.448714303 -1.316722297 -2.171949218 -2.438546688 -1.618851603
## [771] -1.592386043 -0.133628498 2.065444340 3.243054755 3.646871075
## [776] 3.138687533 1.261831423 0.111991034 0.423245461 1.005972232
## [781] 1.318539710 1.720898767 2.001598652 0.707385906 -0.974616273
## [786] -1.853904358 -0.009822156 2.428417821 3.724753496 2.547347679
## [791] 1.666691788 1.252839468 1.237960097 1.198752401 -1.633192447
## [796] -2.231838320 -1.169564276 -1.578223913 -1.212009198 1.591687185
## [801] 2.474871500 1.105321016 0.349897745 -1.202059695 -2.883545838
## [806] -4.038149269 -3.815793309 -2.239230891 0.293265927 3.375261182
## [811] 4.459205464 4.212081815 1.625530665 -1.270383693 -1.769221714
## [816] -1.160200183 -1.505991873 -0.751408261 2.088903231 2.758227047
## [821] 2.573271602 1.520006674 -0.280878099 -1.512577269 -0.386328120
## [826] 1.785456387 2.923546982 2.737893883 0.832797182 0.361127763
## [831] 1.423693582 2.249260114 0.638795478 0.833794078 -1.966297796
## [836] -5.701459165 -3.501920753 -0.990931879 -0.961071880 -1.172943180
## [841] 0.371286631 2.385838020 1.784448235 1.357479669 2.323052176
## [846] 1.514034106 2.574775499 2.615096834 2.102698596 2.160010170
## [851] 1.571233493 2.370576214 4.276196788 3.590804512 0.668075123
## [856] 0.938570344 0.138580667 -2.380996305 -1.514533287 -1.911954398
## [861] -2.253226781 0.381321220 1.827328287 -0.259496734 -1.478570436
## [866] -2.150805470 -5.047573710 -3.635688107 -0.732236745 -0.370161265
## [871] -0.219375839 -0.983502766 -1.199868070 0.047912165 0.157342555
## [876] -2.562883563 -3.250499972 0.835613446 2.733201576 0.859643741
## [881] -0.747832763 -2.096516730 -1.956340223 -1.035388184 -1.045702263
## [886] -1.453613033 -1.302134473 -1.601318819 -0.540362278 0.365410108
## [891] 0.252305016 0.865698809 -0.504908320 -1.057499706 1.741309218

```



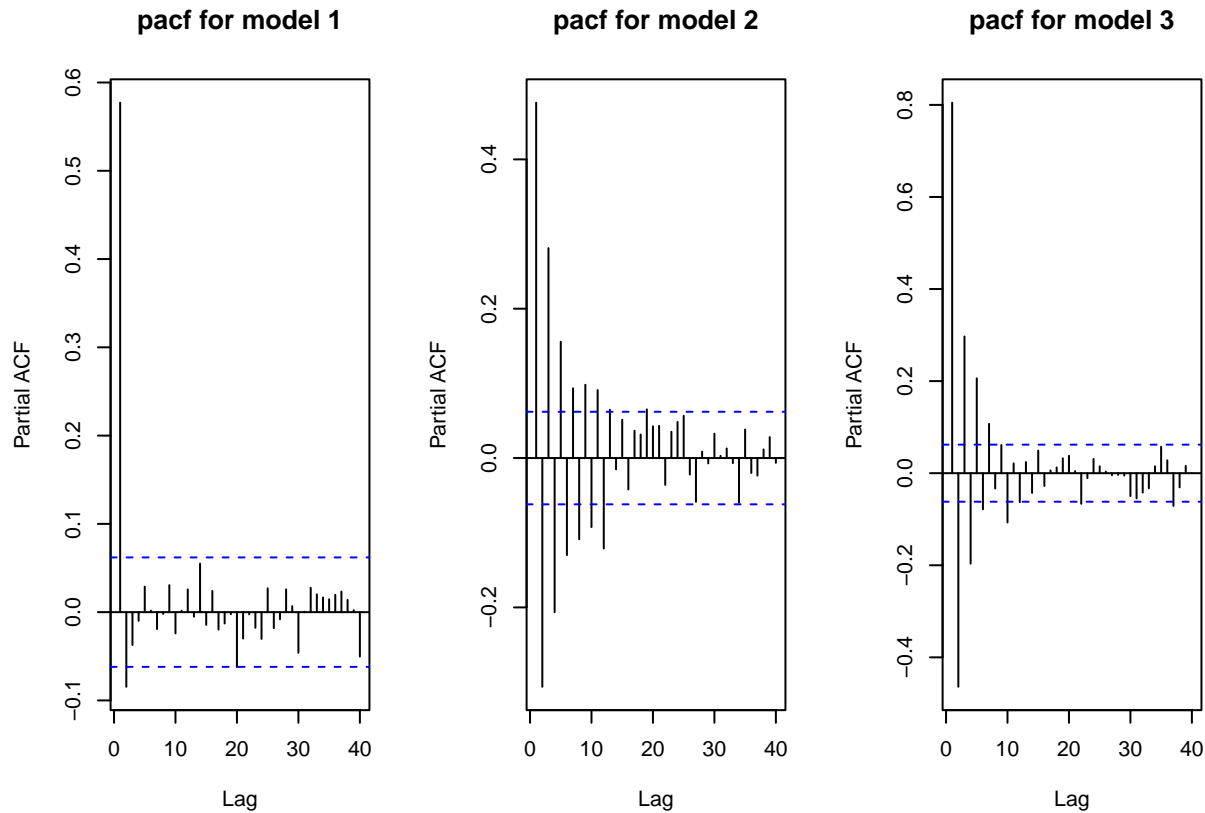
```
## [896]  2.622223466  0.049696815 -0.721895715 -0.284743512 -1.285654913
## [901] -0.537888898  0.528748326  1.416398144  3.842554020  4.566635810
## [906]  2.611882074 -1.936617870 -3.485124732 -2.227199675 -1.464806022
## [911]  1.298020085  1.434678627 -0.351531273 -0.216928524  0.203137140
## [916]  0.310898010  1.515893393  1.441778538  0.528438330  0.948093796
## [921]  0.661254387 -0.540154962 -0.688570665  0.195546203  0.391976542
## [926] -0.707704243 -1.991161127 -2.718286199 -1.906712457 -1.568140583
## [931] -1.678375008 -1.816537765 -0.837691298  0.208646021 -0.555396748
## [936] -0.064621317  0.619863891  0.546510002  0.853263182  2.833759584
## [941]  5.906107157  6.810469700  4.591874349  1.246220833  0.240681135
## [946] -1.644777636 -3.091616053 -0.559558089  1.027954885 -0.301758881
## [951] -0.822902970  0.259331501 -0.624789665 -1.730052599 -2.739507105
## [956] -1.827781143 -0.471621437 -1.389013803 -1.936898435 -1.377516386
## [961] -0.712946210  0.567776228  1.443776886  1.236239644 -0.947336849
## [966] -2.601298836 -3.486828117 -4.589142584 -4.903200683 -4.094573472
## [971] -1.077245726 -1.006743156 -2.291225849 -2.131057074 -3.276089482
## [976] -3.122268556 -1.893029990 -0.655116731  0.204527702 -2.978028862
## [981] -2.760948083 -0.569588189 -1.254735194 -2.115823126 -1.780604770
## [986]  0.244600078  0.972831041  0.966777047  1.922290026  2.289504058
## [991]  1.960533276  2.317255994  1.814053740  0.421120798 -0.841506667
## [996] -1.425442049 -0.310456470  0.406921941  0.758312203 -0.736090599
```

```
par(mfrow=c(1,3))
acf(ARMAmodel_1_new, lag.max = 40, main = "acf for model 1")
acf(ARMAmodel_2_new, lag.max = 40, main = "acf for model 2")
acf(ARMAmodel_3_new, lag.max = 40, main = "acf for model 3")
```



```
par(mfrow=c(1,3))
pacf(ARMAmodel_1_new, lag.max = 40, main = "pacf for model 1")
```

```
pacf(ARMAmodel_2_new, lag.max = 40, main = "pacf for model 2")
pacf(ARMAmodel_3_new, lag.max = 40, main = "pacf for model 3")
```



- (c) Look at the ACFs and PACFs. Imagine you had these plots for a data set and you were asked to identify the model, i.e., is it AR, MA or ARMA and the order of each component. Would you be identify them correctly? Explain your answer.

Answer: Model 1 is AR, model 2 is MA, model 3 is ARMA. Model 1 is AR model because ACF will decay exponentially with time, and we found that it is decaying with lags in the ACF of model 1. Model 2 is MA model because pacf has an obvious slow decay. Model 3 is ARMA model because in the PACF initial values dependent on the AR followed by the decay due to the MA part

- (d) Compare the ACF and PACF values R computed with the theoretical values you provided for the coefficients. Do they match? Explain your answer.

Answer: The AR model matches with the theoretical value. We set $\phi=0.6$, meaning that the coefficient of AR should be 0.6, we can find that the pacf of lag 1 is 0.6 for model 1. It didn't match with the theoretical value for MA model since we didn't find 0.9 at lag 1. For the ARMA model, ar coefficient at lag 1 in pacf didn't match with the theoretical value (0.6) and ma coefficient at lag 1 in acf didn't match with the theoretical value (0.9).

Q3

Consider the ARIMA model $y_t = 0.7 * y_{t-1} - 0.25 * y_{t-12} + a_t - 0.1 * a_{t-1}$

- (a) Identify the model using the notation $ARIMA(p, d, q)(P, D, Q)_s$, i.e., identify the integers p, d, q, P, D, Q, s (if possible) from the equation.

Answer: $ARIMA(1,0,1)(1,1,0)$

(b) Also from the equation what are the values of the parameters, i.e., model coefficients.

Answer: AR coefficient: 0.7 , MA coefficient: 0.1, SAR coefficient: -0.25

Q4

Plot the ACF and PACF of a seasonal ARIMA(0,1) \times (1,0)₁₂ model with $\phi = 0.8$ and $\theta = 0.5$ using R. The 12 after the bracket tells you that $s = 12$, i.e., the seasonal lag is 12, suggesting monthly data whose behavior is repeated every 12 months. You can generate as many observations as you like. Note the Integrated part was omitted. It means the series do not need differencing, therefore $d = D = 0$. Plot ACF and PACF for the simulated data. Comment if the plots are well representing the model you simulated, i.e., would you be able to identify the order of both non-seasonal and seasonal components from the plots? Explain.

```
#install.packages("sarima")
library(sarima)

## Loading required package: stats4

##
## Attaching package: 'sarima'

## The following object is masked from 'package:stats':
##
##      spectrum

SARIMAmoel_4<- sim_sarima(model=list(ma=0.5,sar=0.8, nseasons=12), n=1000)
SARIMAmoel_4

##      [1]  2.560442631  2.078847354  1.692164867  0.090356129 -1.094258751
##      [6]  1.306493887  2.782853869  0.747669798  0.917834544 -0.645432084
##     [11] -0.196664945  0.986995903  1.983159261  1.891323285  0.370558470
##     [16] -0.932533785 -2.064942319 -1.142595995  0.634808732 -0.294056759
##     [21]  1.377935163 -0.115571892 -0.094886456  0.589897303  0.869631028
##     [26]  0.392184577  0.303707408  0.183378075 -1.835487608 -1.919014735
##     [31]  0.161435845 -0.168044905  1.223222424 -0.192594342  0.029396777
##     [36]  0.480330261 -0.568181184  0.881315680 -0.594733202 -0.075356475
##     [41] -1.302358574 -2.694716094 -1.756321672 -0.756147864  1.733863393
##     [46]  0.205457188 -0.008312718  1.750967948  0.193293069  0.495514500
##     [51] -2.065861837 -1.534827659 -0.903869498 -3.832599926 -2.765883454
##     [56] -1.228825179  2.378418123  1.100089706  1.519610004  1.995902427
##     [61]  0.539176074  1.793377407 -0.940478058 -0.830245681 -0.723206175
##     [66] -2.751909608 -2.655749171 -3.250053711 -1.231300954 -0.132255403
##     [71]  1.820602276  3.639552715  1.077334718  1.314416732 -2.073216810
##     [76] -2.308760647 -1.075622362 -1.070050387 -0.573835845 -0.602740005
##     [81]  0.169370517  0.840206230  2.113538720  2.044505616  0.393426907
##     [86] -0.636142440 -2.356576895 -3.140513141 -2.687392905 -2.064740741
##     [91] -0.912035954  1.028157110  1.010181659  1.483625844  2.657967310
##     [96]  1.440737052 -0.268543858 -0.363407342 -0.531481457 -2.119196936
##    [101] -2.155589867 -1.303914438  0.551508742  1.950114706  1.517101522
##    [106]  0.578205662  0.373221555  1.238146607  0.244628100 -0.317597128
##    [111]  1.861752119  2.201107590 -1.469244694 -1.834632159 -0.727106954
##    [116]  1.053274673  0.934287871 -1.173233362 -0.850500777  2.006164832
##    [121]  1.692405097  0.679747672  1.025845189  2.017328226  0.312553002
##    [126] -1.495929762 -0.932440573  0.105688194 -1.556077737 -2.169829492
##    [131]  0.638539704  2.913128642  0.648238387  1.206640729  0.596623530
##    [136]  0.545727445 -0.851998531  0.037430421 -0.966686806 -0.860900421
##    [141] -1.078498447 -1.621585394  0.910134422  1.863744107 -0.403327649
```

```

## [146] 2.014964967 1.001854928 0.736134742 -0.150608269 2.533438753
## [151] 3.262356312 0.281462997 0.788638860 -1.560406375 -1.438748310
## [156] 0.555681367 -1.386594405 1.841687719 0.689319215 -0.711174720
## [161] 2.996079797 3.573477259 1.851461711 -0.992408608 1.530102491
## [166] -0.848564664 -1.783374913 -1.413926157 -1.362730597 1.760425288
## [171] -0.539465877 -0.787683508 2.329224434 4.869019773 3.132835232
## [176] 0.170212983 1.968632293 0.024365742 -2.064614414 -0.391615663
## [181] 1.305770172 1.147406889 -0.921162871 -0.162419457 1.497030740
## [186] 2.672367525 1.970873471 2.278499665 2.137575509 2.111743246
## [191] 0.279233508 -0.406363682 0.768016570 1.663469827 -1.441087080
## [196] 1.041312853 4.497686844 3.945379827 1.974341492 1.642418849
## [201] 1.461559780 1.514024213 -1.630770553 -1.885028169 0.042984773
## [206] 0.756162027 -0.563780355 0.358024014 2.766300359 4.794669148
## [211] 1.187373827 1.030951743 0.788601497 2.529682948 0.401965505
## [216] 0.978595038 1.067489366 2.191372427 0.276152226 -1.354211410
## [221] 2.046263105 4.528328757 0.998149684 -0.550390986 -1.582776295
## [226] 1.972145305 0.386548125 -0.271830646 -1.485278827 -0.547466992
## [231] -0.366161538 -2.254114169 0.899675307 3.901284194 0.374300249
## [236] 0.811710301 -1.276984986 -0.045637669 -0.532230521 -0.872085532
## [241] -0.872837116 -0.869391577 -1.014551802 0.250653954 2.055693569
## [246] 3.801123216 1.405795422 -0.506884084 -1.635237805 -0.712899497
## [251] -0.957352565 -0.289140438 -0.510247728 -0.083841682 0.210746065
## [256] 0.208123842 2.616578962 3.028138700 0.066320740 -1.314479740
## [261] -1.332682875 0.728103703 -0.527564740 2.428424652 -0.315893636
## [266] -0.728395431 0.578673765 -0.160627921 1.097199424 1.623503270
## [271] -0.743269269 0.178527964 0.269220824 1.194557066 0.906303200
## [276] 2.643840285 1.520380575 1.343968636 1.653178465 0.242216477
## [281] -0.597041768 1.386163139 -1.279493776 -0.075568545 1.937650480
## [286] 3.187876958 3.048830356 2.633989232 2.619721974 0.528350343
## [291] 1.108911465 0.129581668 -0.944750246 1.097305038 -0.896919162
## [296] -1.236142847 1.422950608 2.558181929 2.414480826 3.641474240
## [301] 2.146957009 0.958217869 0.865255604 -0.386281828 -1.099609645
## [306] -0.044674044 -2.307938417 -1.970794190 0.669520824 0.738866266
## [311] 2.885716328 3.589846953 3.130305826 3.061759603 2.956673254
## [316] -0.003188698 -1.914365087 -0.583349665 -1.875987710 -1.669581623
## [321] 2.435463568 4.022687064 2.185461073 3.435071994 2.037353081
## [326] 0.251716521 0.355686819 -1.184676685 -1.575593250 0.145276634
## [331] -1.340533819 -1.474064637 2.839395820 4.488175417 2.002688482
## [336] 2.429832359 1.321089101 -0.393186895 0.960375822 -0.083993945
## [341] -0.684895822 1.407947492 -0.693808580 -1.064820108 2.432383869
## [346] 5.090343043 2.598175140 2.746213561 2.191998425 -1.870598384
## [351] -0.579950353 0.902576233 -0.362970475 1.655480172 0.406415872
## [356] -0.037146274 0.621434461 3.555561802 0.416450452 1.913413453
## [361] 0.560151151 -1.716542653 0.090205339 2.371131543 1.520635126
## [366] 0.397304875 0.363401135 1.569056553 0.023008117 2.065898907
## [371] 0.535166371 0.472209484 -0.598943290 -2.559418096 0.046877281
## [376] 2.583605496 2.989095910 0.758442770 1.072836657 2.144325995
## [381] 1.918920364 3.350064931 -0.928525304 0.097817682 0.771523397
## [386] -0.928288808 0.733876023 2.011508304 1.790983401 1.261890577
## [391] 0.744872219 2.076429147 1.713010564 3.544023968 1.292546145
## [396] 1.086611381 2.721307072 0.386732821 -0.553385912 1.131053311
## [401] 1.171427460 1.506520899 3.117874344 2.723894512 2.837839024
## [406] 4.485707873 2.064836454 2.281248010 3.456472544 1.009307088
## [411] -1.003302999 0.056203981 0.629474143 1.560778111 3.080163724

```

```

## [416] 3.211621102 1.748157987 3.497666893 2.652426257 1.453648758
## [421] 0.892585781 -1.638283398 -1.489620810 1.277717490 1.227682521
## [426] -0.801619007 2.776680507 3.616227743 3.244190168 4.933537763
## [431] 3.973562311 0.941329100 0.318566390 -2.030781130 -1.040056117
## [436] 0.675589482 2.701239453 0.618277913 2.593341582 3.586732937
## [441] 2.861599634 4.385557580 3.340472301 2.155367945 2.095630306
## [446] -0.610400572 -1.882353905 1.833653320 2.661588808 2.275803262
## [451] 3.151755451 2.330738949 2.182517497 5.462927749 3.779937866
## [456] 1.490095545 0.871768527 -2.735970179 -1.641827099 3.597170546
## [461] 3.582670750 1.355864577 2.775335712 1.676697808 0.854802169
## [466] 3.822832667 2.401703740 1.633460769 0.868391749 -2.250601385
## [471] -1.347414039 4.232732891 4.094443468 0.934467634 1.870530748
## [476] 0.203709949 -1.427093468 1.688509843 1.412542488 2.005432478
## [481] 1.134392661 -1.340852943 -2.232895897 2.486065895 4.021392806
## [486] -0.436467235 1.107601464 0.909439532 -1.346436658 0.396713641
## [491] 0.058036890 0.846671775 0.098714706 -0.518502642 -0.583644227
## [496] 2.303736580 2.882824353 0.453990049 1.655724207 1.336683898
## [501] -1.722935464 -2.999899299 -0.309279709 2.300180499 0.092576832
## [506] -0.256322583 0.461754629 1.414391901 1.920221620 -0.377916445
## [511] -0.021106105 -0.244558751 -1.927800437 -2.309523838 -0.248741233
## [516] 0.867807162 0.122241333 -0.427820016 0.484681772 1.699315486
## [521] 1.574260564 -0.788633549 -0.493133627 -0.360513761 -3.193770510
## [526] -3.139789598 -1.497634065 0.481210663 -0.289409923 0.388446088
## [531] 0.265884597 0.163738534 0.797142345 -1.089314303 0.027078554
## [536] -2.086028619 -3.506034192 -3.364526048 -2.721716358 0.185725371
## [541] -1.987093112 -1.622237347 0.244753369 0.756639053 2.489885277
## [546] 0.988125627 0.630513095 -1.733363645 -3.025535113 -1.236481992
## [551] -1.519678053 -0.165758699 -3.402328461 -2.320839755 0.105086993
## [556] 0.458935897 -0.725048536 -0.993529084 -0.777015729 -1.361981338
## [561] -4.623258164 -1.897018188 -0.621280294 0.735317693 0.018415963
## [566] -0.756192297 1.988517893 3.407686517 0.143103961 -2.519586565
## [571] -1.422780431 -1.160066004 -3.435649595 -1.164935007 -1.962637470
## [576] -1.502805601 -1.514681978 -1.391211094 1.713448001 4.892240038
## [581] -1.135661813 -3.287936516 -0.455564532 -0.738518583 -2.596876608
## [586] -0.632937392 0.345287158 -1.169497238 -2.181936378 -1.455192882
## [591] -1.041435938 1.721378327 -2.914190263 -4.120938485 -0.041770952
## [596] -1.952802440 -2.671025005 -1.327671043 1.026526538 -0.086124760
## [601] -1.805895861 -0.992795845 0.008823899 1.867105917 -1.592353642
## [606] -2.423470788 -0.824955380 -0.692838622 -2.003595778 -1.754912106
## [611] -1.374676885 -0.471275552 0.564480153 -0.946217152 -3.563458636
## [616] 0.368342451 0.642202560 -2.462451315 -3.352639087 -2.529369040
## [621] -2.758293131 -1.660021982 -0.627326813 -1.254996133 0.212826654
## [626] -0.472145323 -3.328116795 0.258547368 0.833866148 -0.403110040
## [631] -1.267156902 -2.489502227 -5.820745931 -3.183663562 -2.725169601
## [636] -2.782613532 -2.076871805 -0.352937793 -2.755986241 0.020083400
## [641] -0.756923252 -2.546511386 -0.625708762 -1.389671151 -4.587999776
## [646] -1.910665846 -0.716360059 -1.526010789 -0.159207626 1.707617212
## [651] -1.715835868 0.872757665 -1.093297682 -1.774066097 -0.499912856
## [656] -0.056608837 -0.989908101 -2.730689737 -0.169638356 -0.936347730
## [661] -1.257647906 1.563124334 -1.638139750 2.303696268 -0.209075502
## [666] -2.354410619 -1.258429344 0.129935780 0.917778528 0.827075198
## [671] 1.083521514 -0.166953842 -1.100462191 1.382036223 -0.479352876
## [676] 1.748068023 1.096595812 -1.691194977 -1.603542916 -0.768685083
## [681] 0.269733931 1.273653940 -0.394288713 -1.745970193 0.669343524

```

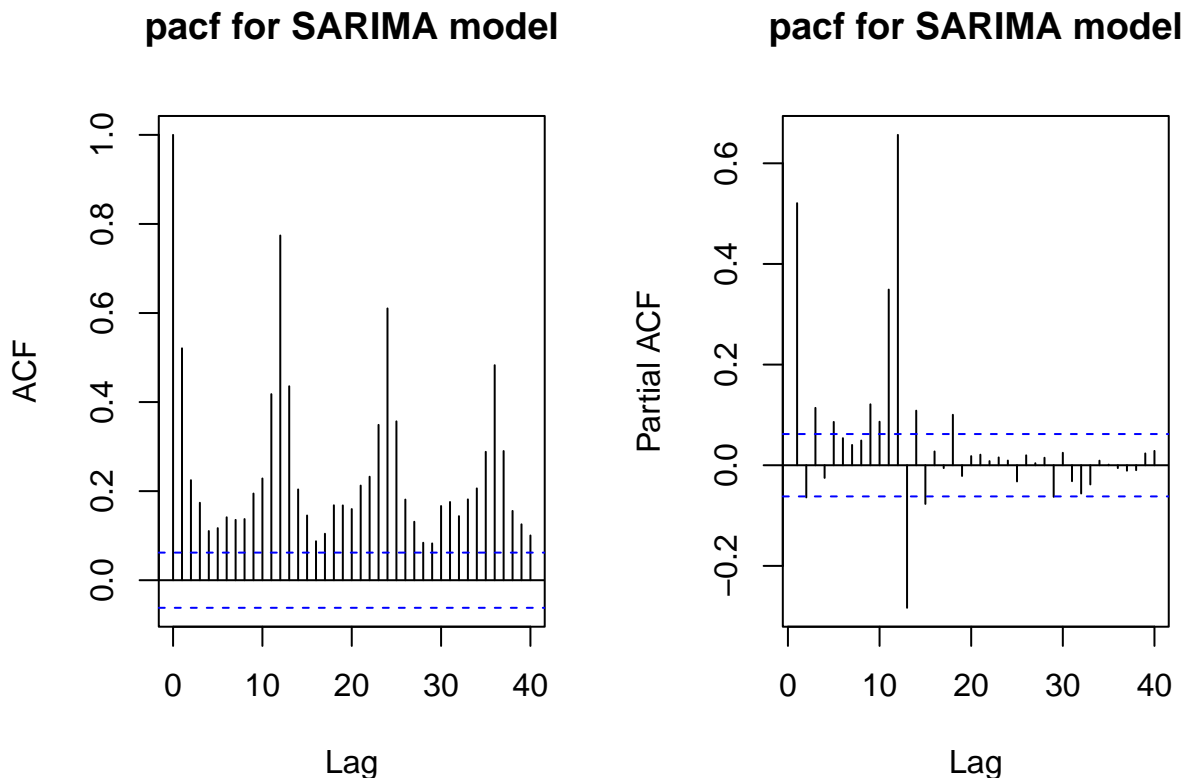
```

## [686] 1.831165340 0.118736584 2.123620442 1.915499210 -0.493936185
## [691] 0.087912889 -0.481450660 -0.030363722 0.443833778 -0.659373588
## [696] -2.191481526 0.922748701 0.193842838 -1.326921985 1.771508917
## [701] 0.387063598 -1.807876870 -1.495971546 -0.926619222 -0.320277179
## [706] 0.223753184 0.360781156 -2.438528937 1.213369955 0.704622447
## [711] 0.020233817 1.176316373 0.851169976 -0.301253241 -0.715259346
## [716] -0.477437004 -0.627623770 -0.133072643 1.748804717 -1.844980814
## [721] 0.273992822 -0.036732294 -1.172785474 0.229418293 -0.514177858
## [726] -1.699434345 -0.888460627 -1.617652963 -0.533389736 0.796459178
## [731] 1.323923864 -2.122620334 -0.857650003 -0.177698680 0.204486412
## [736] 1.015018173 0.364147342 -0.929278475 -0.328548076 -1.187995475
## [741] 0.009544491 0.550491038 2.329432369 -0.364968416 -1.668854846
## [746] -0.568998146 0.423925034 0.589123404 1.036124348 0.145243975
## [751] 1.905675576 -0.707125632 -0.504054118 1.174512853 2.363530914
## [756] -0.297972230 -0.009764418 -0.714714480 0.647794404 1.584837886
## [761] 0.998822006 0.834625061 1.597809561 -1.050058104 -0.757467099
## [766] 1.545455966 2.332503560 -1.001838746 1.455571587 -0.388807736
## [771] -0.377421397 0.218352222 -0.367724368 1.108961117 1.757120584
## [776] -2.613825692 -0.441754127 2.503971151 2.467950846 -0.623102700
## [781] 0.622391215 -0.800736858 0.248884626 -1.386233329 -1.243319988
## [786] -0.407416485 -1.123933266 -1.319815102 0.779338912 1.214556046
## [791] 1.770166870 2.650062395 1.549314092 -2.015872843 -0.102125054
## [796] -1.497383043 -0.834339686 -0.707856525 -0.941585052 -0.052638686
## [801] 0.566551602 -0.867965175 2.411217302 1.849687666 0.583582825
## [806] -0.410379631 -1.458436483 -2.612845826 -0.826924423 -0.640265813
## [811] -1.863567745 -1.974684403 1.170183547 -0.084736252 3.537533871
## [816] 1.592323957 1.251653097 -1.955991581 -0.548582393 0.343437686
## [821] -0.415903260 -1.544840175 -1.464918154 -1.405033792 1.502134404
## [826] 0.364158199 1.799314019 -0.675604752 0.571915870 -0.085064123
## [831] -0.392211115 0.178792236 -0.994812813 -1.367438178 -1.685686337
## [836] -2.177603007 2.300367974 2.611337475 2.255820672 -0.686139094
## [841] -0.107651814 -2.711739594 -1.126268264 1.174498291 -0.075615798
## [846] -1.820374532 -2.279682406 -2.716869706 -0.759796897 0.427773753
## [851] 1.685651460 -2.204849992 -2.996022712 -4.657714668 -2.386791422
## [856] 0.272360820 -1.595025063 -1.717498648 -3.058381356 -2.987399281
## [861] 0.131518718 -0.552753480 -1.101124251 -3.925729978 -0.166800048
## [866] -3.748247040 -1.478610335 1.442521874 -2.375574591 -3.636515242
## [871] -3.800737022 -2.742094931 -0.019896599 0.171980881 -0.813488996
## [876] -3.038627933 -0.855745836 -3.336222008 -0.528908021 0.346974538
## [881] -1.641087813 -2.059101671 -4.235456915 -4.465898598 -0.102657408
## [886] 1.478380617 -1.522771287 -4.392727249 -2.246140469 -4.950798918
## [891] -1.059360381 0.087428647 -1.004109722 -1.946856548 -2.295966905
## [896] -2.623740863 0.410623585 0.048588871 -1.657963543 -2.402519242
## [901] -1.900383584 -5.287843319 -1.249306881 0.332397026 -0.910639467
## [906] -3.182742891 -2.928325519 -0.681569403 0.714864340 0.785991970
## [911] -1.628962534 -2.445414691 -1.356100658 -2.719050412 -0.769815651
## [916] 0.368155395 0.352219167 -0.038939066 -2.849290262 -1.979064065
## [921] -1.235964667 0.393067025 -1.457672420 -3.261602132 -1.667685751
## [926] -3.302805315 -2.011633118 -0.052973354 1.316964435 1.306858497
## [931] -2.137088494 -2.565509275 -3.829166400 -0.748694975 -0.941884154
## [936] -3.631238119 -0.735726613 -3.055533306 -2.497477499 0.289429791
## [941] -0.429534727 2.069013415 -2.561168670 -2.462751625 -2.345232175
## [946] 0.140598770 0.201175210 -2.778801078 -0.053936729 -2.274324774
## [951] -3.058389947 0.548830964 1.194163368 1.795828527 -2.529669080

```

```
## [956] -1.950041500 -1.328250332 -0.570411636 -0.700923568 -0.696033052
## [961]  0.849242771 -2.525097911 -1.462290475  1.741829097  1.816892141
## [966]  3.454873644 -2.934653057 -2.031958792 -1.510724465 -0.113490390
## [971] -1.186667056 -2.060309641 -0.131409407 -1.428959316 -2.215650251
## [976] -1.524952527  0.503522697  2.433127805 -2.791140206 -1.267172852
## [981] -2.653776561 -0.613931954 -0.912994139  0.479776726  2.012353571
## [986] -1.102860765 -2.647870252 -1.636615509 -0.240103651  0.217914877
## [991] -2.976164451 -1.840268531 -2.161327106 -0.215674936  0.189969036
## [996]  0.511867041  0.708756600 -1.499782245 -2.597800679 -3.014224965
```

```
par(mfrow=c(1,2))
acf(SARIMAmode1_4, lag.max = 40, main = "pacf for SARIMA model")
pacf(SARIMAmode1_4, lag.max = 40, main = "pacf for SARIMA model")
```



Comment if the plots are well representing the model you simulated, i.e., would you be able to identify the order of both non-seasonal and seasonal components from the plots? Explain.

Answer: From the non-seasonal part of the acf plot, it cuts off which is a MA process, and $q=1$. From the non-seasonal part of the pacf plot, it also tails off which shows a MA process, and $p=2$. From the seasonal part of the acf plot, there are multiple positive spikes at seasonal lags (lag 12, 24, 36), showing that it is a SAR process and $P=1$. From the seasonal part of pacf plot, there is a single spike which also reflects a SAR process and $Q=0$.