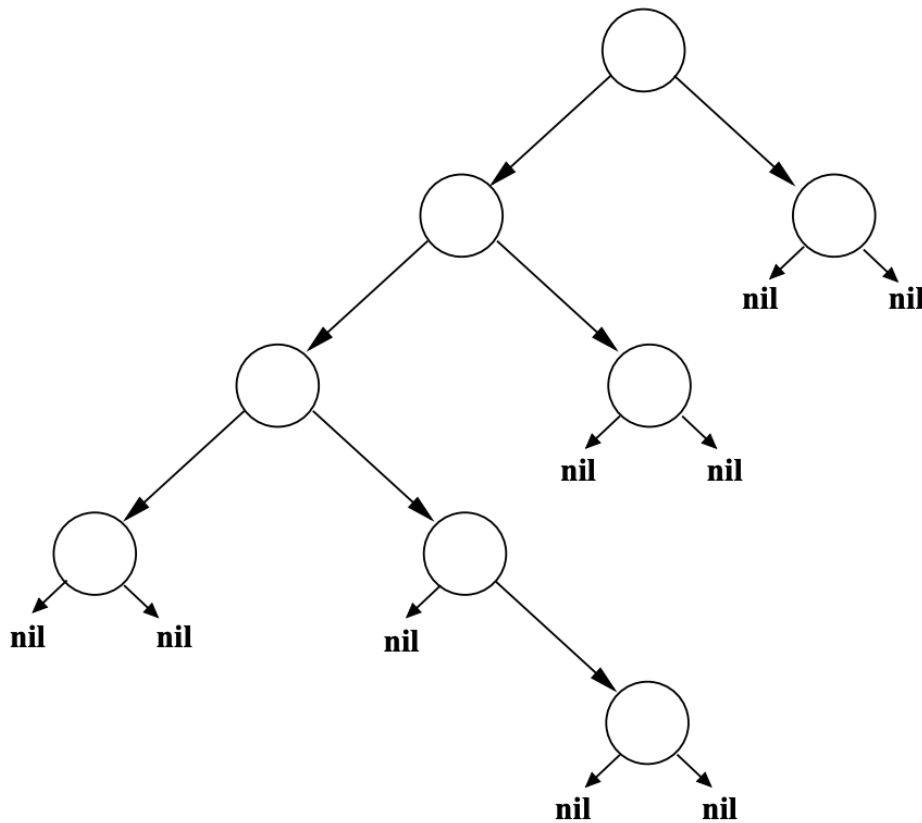


### 1. Red-Black Tree (10x3=30 pts.)

(A) Assign the keys 2, 3, 5, 7, 11, 13, 17, 19 to the nodes of the binary search tree below so that they satisfy the binary-search-tree property.



(B) State if this binary search tree can be colored to form a legal red-black tree? Explain your answer.

(C) The binary search tree can be transformed into a red-black tree by performing a single rotation. Draw the red-black tree that results, labeling each node with a “red” or “black”. Also include the keys from part (A).

## 2. Generalized Heap (40 pts.)

Let us consider a generalized binary heap structure where every node has children. It is an almost complete, d-ary tree, and a node must be less than or equal to all its children. Design an array representation of the heap. Also design a **Deletemin** procedure for this data structure.

## 3. Hashing (10x3=30 pts.)

Let us assume you are implementing a hash table where your choices are between using a **Probing strategy** vs. **Chaining strategy**. Chaining strategy assumes a linked list that can hold as many records as needed. For both these strategies, you use the same function and hash table sizes.

- (A) Which of the two strategies: Probing or Chaining will give you lower collisions. Justify your answer.
- (B) One drawback of chaining is linear traversal when collision happens. Consider a small but significant number of collisions happen, would linear probing be more effective than chaining? Justify your answer.
- (C) Reconsider part (B) under the assumption that you are using Quadratic probing instead of Linear probing as an alternative to Chaining. Justify your answer.