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## TIME AND STATE IN DISTRIBUTED SYSTEMS

- 1. Time in Distributed Systems
- 2. Lamport's Logical Clocks
- 3. Vector Clocks
- 4. Causal Ordering of Messages
- 5. Global States and their Consistency
- 6. Cuts of a Distributed Computation
- 7. Recording of a Global State

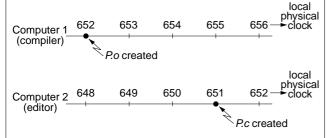


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#### Time in Distributed Systems (cont'd)

#### The make-program example

 When the programmer has finished changing some source files he starts make; make examines the times at which all object and source files were last modified and decides which source files have to be (re)compiled.



Although *P.c* is modified after *P.o* has been generated, because of the clock drift the time assigned to *P.c* is smaller.



P.c will not be recompiled for the new version!

# SYSTEMS

#### **Time in Distributed Systems**

- Because each machine in a distributed system has its own clock there is no notion of global physical time.
  - The n crystals on the n computers will run at slightly different rates, causing the clocks gradually to get out of synchronization and give different values.

#### Problems:

 Time triggered systems: these are systems in which certain activities are scheduled to occur at predefined moments in time. If such activities are to be coordinated over a distributed system we need a coherent notion of time.

Example: time-triggered real-time systems

 Maintaining the consistency of distributed data is often based on the time when a certain modification has been performed.

Example: a make program.



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#### Time in Distributed Systems (cont'd)

#### Solutions:

#### Synchronization of physical clocks

- Computer clocks are synchronized with one another to an achievable, known, degree of accuracy 

  within the bounds of this accuracy we can coordinate activities on different computers using each computer's local clock.
- Physical clock synchronization is needed for distributed real-time systems.

#### Logical clocks

- In many applications we are not interested in the physical time at which events occur; <u>what is</u> <u>important is the relative order of events!</u>
   The <u>make-program</u> is such an example (slide 3).
- In such situations we don't need synchronized physical clocks.
   Relative ordering is based on a virtual notion of time - logical time.
- Logical time is implemented using logical clocks.





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#### **Lamport's Logical Clocks**

- The order of events occurring at different processes is critical for many distributed applications. <u>Example</u>: P.o\_created and P.c\_created in slide 3.
- Ordering can be based on two simple situations:
  - If two events occurred in the same process then they occurred in the order observed following the respective process;
  - 2. Whenever a message is sent between processes, the event of sending the message occurred before the event of receiving it.
- Ordering by Lamport is based on the happened-before relation (denoted by →):
  - a → b, if a and b are events in the same process and a occurred before b;
  - a → b, if a is the event of sending a message m in a process, and b is the event of the same message m being received by another process;
  - If a → b and b → c, then a → c (the relation is transitive).



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#### Lamport's Logical Clocks (cont'd)

- Using physical clocks, the happened before relation can not be captured. It is possible that  $b \to c$  and at the same time  $T_b > T_c$  ( $T_b$  is the physical time of b).
- Logical clocks can be used in order to capture the happened-before relation.
  - A logical clock is a monotonically increasing software counter.
  - There is a logical clock C<sub>Pi</sub> at each process P<sub>i</sub> in the system.
  - The value of the logical clock is used to assign timestamps to events.
  - C<sub>Pi</sub>(a) is the timestamp of event a in process P<sub>i</sub>.
    There is no relationship between a logical clock and any physical clock.

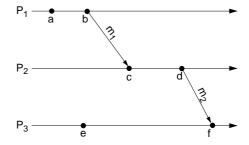
To capture the happened-before relation, logical clocks

have to be implemented so that if 
$$a \rightarrow b$$
, then  $C(a) < C(b)$ 



#### Lamport's Logical Clocks (cont'd)

- If a → b, we say that event a causally affects event b.
   The two events are causally related.
- There are events which are not related by the happened-before relation.
   If both a → e and e → a are false, then a and e are concurrent events; we write a || e.



P1, P2, P3: processes; a, b, c, d, e, f: events;

$$\begin{array}{l} a\rightarrow b,\, c\rightarrow d,\, e\rightarrow f,\, b\rightarrow c,\, d\rightarrow f\\ a\rightarrow c,\, a\rightarrow d,\, a\rightarrow f,\, b\rightarrow d,\, b\rightarrow f,\, ...\\ a\parallel e,\, c\parallel e,\, ... \end{array}$$

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#### Lamport's Logical Clocks (cont'd)

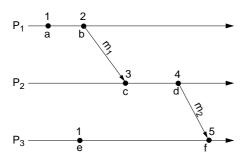
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- Implementation of logical clocks is performed using the following rules for updating the clocks and transmitting their values in messages:
- [R1]:  $C_{Pi}$  is incremented before each event is issued at process  $P_i$ :  $C_{Pi}$  :=  $C_{Pi}$  + 1.
- [R2]: a) When a is the event of sending a message m from process  $P_i$ , then the timestamp  $t_m = C_{Pi}(a)$  is included in m ( $C_{Pi}(a)$  is the logical clock value obtained after applying rule R1).
  - b) On receiving message m by process  $P_j$ , its logical clock  $C_{Pj}$  is updated as follows:  $C_{Pi} := \max(C_{Pj}, t_m)$ .
  - c) The new value of  $C_{Pj}$  is used to timestamp the event of receiving message m by  $P_j$  (applying rule R1).
  - If a and b are events in the same process and a occurred before b, then a → b, and (by R1) C(a) < C(b).</li>
  - If a is the event of sending a message m in a process, and b is the event of the same message m being received by another process, then a → b, and (by R2) C(a) < C(b).</li>
  - If a → b and b → c, then a → c, and (by induction)
     C(a) < C(c).</li>



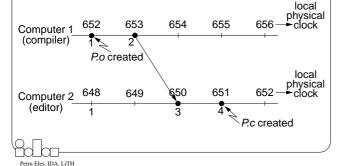
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#### Lamport's Logical Clocks (cont'd)



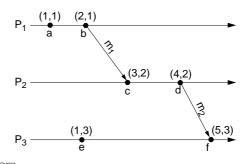
For the make-program example we suppose that a
process running a compilation notifies, through a
message, the process holding the source file about
the event Po created 

a logical clock can be used
to correctly timestamp the files.



#### **Problems with Lamport's Logical Clocks**

- Lamport's logical clocks impose only a <u>partial order</u> on the set of events; pairs of distinct events generated by <u>different</u> processes can have identical timestamp.
  - For certain applications a total ordering is needed; they consider that no two events can occur at the same time.
  - In order to enforce total ordering a global logical timestamp is introduced:
    - the global logical timestamp of an event a occurring at process P<sub>i</sub>, with logical timestamp C<sub>Pi</sub>(a), is a pair (C<sub>Pi</sub>(a), i), where i is an identifier of process P<sub>i</sub>.
    - we define  $(C_{Pi}(a),\ i) < (C_{Pj}(b),\ j) \text{ if and only if}$   $C_{Pi}(a) < C_{Pi}(b), \text{ or } C_{Pi}(a) = C_{Pi}(b) \text{ and } i < j.$

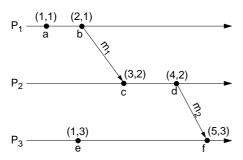


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#### Problems with Lamport's Logical Clocks (cont'd)

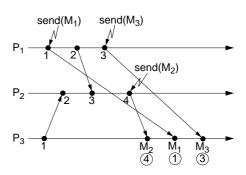
- Lamport's logical clocks are not powerful enough to perform a <u>causal ordering of events</u>.
- if a → b, then C(a) < C(b).
   However, the reverse is not always true (if the events occurred in different processes):
   if C(a) < C(b), then a → b is not necessarily true.
   (it is only guaranteed that b → a is not true).</li>



C(e) < C(b), however there is no causal relation from event e to event b.

 By just looking at the timestamps of the events, we cannot say whether two events are causally related or not. Distributed Systems Fö 5 - 12

#### Problems with Lamport's Logical Clocks (cont'd)



- We would like messages to be processed according to their causal order.
- Process  $P_3$  receives messages  $M_1$ ,  $M_2$ , and  $M_3$ .  $M_1 \rightarrow M_2$ ,  $M_1 \rightarrow M_3$ ,  $M_3 \parallel M_2$
- M<sub>1</sub> has to be processed before M<sub>2</sub> and M<sub>3</sub>.
   However P<sub>3</sub> has not to wait for M<sub>3</sub> in order to process it before M<sub>2</sub> (although M<sub>3</sub>'s logical clock timestamp is smaller than M<sub>2</sub>'s).





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#### **Vector Clocks**

- Vector clocks give the ability to decide whether two events are causally related or not by simply looking at their timestamp.
  - Each process P<sub>i</sub> has a clock C<sup>V</sup><sub>Pi</sub>, which is an integer vector of length n (n is the number of processes).
  - The value of C<sup>V</sup><sub>Pi</sub> is used to assign timestamps to events in process P<sub>i</sub>.
     C<sup>V</sup><sub>Pi</sub>(a) is the timestamp of event a in process P<sub>i</sub>.
  - C<sup>V</sup><sub>Pi</sub>[j], the ith entry of C<sup>V</sup><sub>Pi</sub>, corresponds to P<sub>i</sub>'s own logical time.
  - C<sup>V</sup><sub>Pi</sub>[J], j≠ i, is P<sub>i</sub>'s "best guess" of the logical time at P<sub>j</sub>.
     C<sup>V</sup><sub>Pi</sub>[J] indicates the (logical) time of occurrence of the last event at P<sub>j</sub> which is in a happened-before relation to the current event at P<sub>j</sub>.



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# Vector Clocks (cont'd) P<sub>1</sub> (1,0,0) (2,0,0) (3,0,0) R<sub>2</sub> (0,1,0) (2,2,0) (2,3,1) (2,4,1) P<sub>3</sub> (0,0,1) (2,4,2) R<sub>3</sub> (2,4,2)

For any two vector timestamps u and v, we have:

- u = v if and only if  $\forall i$ , u[i] = v[i]
- $u \le v$  if and only if  $\forall i, u[i] \le v[i]$
- u < v if and only if  $(u \le v \land u \ne v)$
- $u \mid\mid v \text{ if and only if } \neg(u < v) \land \neg(v < u)$
- Two events a and b are causally related if and only if  $C^{v}(a) < C^{v}(b)$  or  $C^{v}(b) < C^{v}(a)$ . Otherwise the events are concurrent.
- With vector clocks we get the property which we missed for Lamport's logical clocks:
  - a → b if and only if C<sup>v</sup>(a) < C<sup>v</sup>(b).
     Thus, by just looking at the timestamps of the events, we can say whether two events are causally related or not.



- Implementation of vector clocks is performed using the following rules for updating the clocks and transmitting their values in messages:
- [R1]:  $C_{j_i}^{k}$  is incremented before each event is issued at process  $P_{j_i}$ :  $C_{j_i}^{k}[i] := C_{j_i}^{k}[i] + 1$ .
- [R2]: a) When a is the event of sending a message m from process  $P_i$ , then the timestamp  $t_m = C_{P_i}^{\nu}(a)$  is included in  $m\left(C_{P_i}^{\nu}(a)\right)$  is the vector clock value obtained after applying rule R1).
  - b) On receiving message m by process  $P_j$ , its vector clock  $C_{P_j}^V$  is updated as follows:  $\forall k \in \{1,2,...,n\}, C_{P_j}^V[k] := \max(C_{P_j}^V[k], t_m[k]).$
  - c) The new value of  $C_{P_j}^V$  is used to timestamp the event of receiving message m by  $P_j$  (applying rule R1).



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#### Causal Ordering of Messages Using Vector Clocks

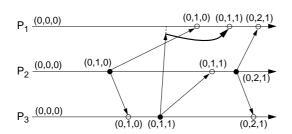
The problem has been formulated on slide 12:

- We would like messages to be processed according to their causal order.
  - If Send(M<sub>1</sub>) → Send(M<sub>2</sub>), then every recipient of both messages M<sub>1</sub> and M<sub>2</sub> must receive M<sub>1</sub> before M<sub>2</sub>.



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#### Causal Ordering of Messages Using Vector Clocks (cont'd)



- A message delivery protocol which preforms causal ordering based on vector clocks.
  - Basic Idea:
    - A message is delivered to a process only if the message immediately preceding it (considering the causal ordering) has been already delivered to the process. Otherwise, the message is buffered.
  - We assume that processes communicate using broadcast messages.
     (There exist similar protocols for non-broadcast communication too.)



#### Causal Ordering of Messages Using Vector Clocks (cont'd)

- The events which are of interest here are the sending of messages 

  vector clocks will be incremented only for message sending.
- Implementation of the protocol is based on the following rules:
- [R1]: a) Before broadcasting a message m, a process  $P_i$  increments the vector clock:  $C^V_{P_i}[i] := C^V_{P_i}[i] + 1$ .
  - b) The timestamp  $t_m = C_{Pi}^{V}$  is included in m.
- [R2]: The receiving side, at process  $P_i$ , delays the delivery of message m coming from  $P_i$  until both the following conditions are satisfied:
  - 1.  $C_{Pi}^{V}[i] = t_{m}[i] 1$
  - 2.  $\forall k \in \{1,2,..,n\} \{i\}, C_{P_i}^{V}[k] \ge t_m[k]$

Delayed messages are queued at each process in a queue that is sorted by their vector timestamp; concurrent messages are ordered by the time of their arrival.

- [R3]: When a message is delivered at process  $P_j$  its vector clock  $C_{ij}^{V}$  is updated according to rule R2b for vector clock implementation (see slide 14).
  - \* t<sub>m</sub>[i] 1 indicates how many messages originating from P<sub>i</sub> precede m.
    Step R2.1 ensures that process P<sub>j</sub> has received all the messages originating from P<sub>i</sub> that precede m.
    Step R2.2 ensures that P<sub>i</sub> has received all those

messages received by  $P_i$  before sending m.



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#### **Global States**

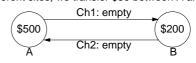
The problem is how to collect and record a consistent global state in a distributed system.

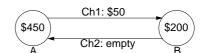
#### Why a problem?

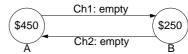
 Because there is no global clock (no coherent notion of time) and no shared memory! Distributed Systems Fö 5 - 20

#### Global States (cont'd)

Consider a bank system with two accounts A and B at two different sites; we transfer \$50 between A and B.







A	Ch1	В	C : consistent NC: not consistent
500	empty	200	С
500	50	200	NC
450	50	200	C
450	empty	200	NC
500	50	250	NC
450	50	250	NC
450	empty	250	C
500	empty	250	NC





#### Global States (cont'd)

- In general, a global state consists of a set of local states and a set of states of the communication channels.
- The state of the communication channel in a consistent global state should be the sequence of messages sent along the channel before the sender's state was recorded, excluding the sequence of messages received along the channel before the receiver's state was recorded.
- It is difficult to record channel states to ensure the above rule ⇒ global states are very often recorded without using channel states.
   This is the case in the definition below.



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#### Formal Definition (cont'd)

A global state GS = {LS<sub>1</sub>, LS<sub>2</sub>, ..., LS<sub>n</sub>} is consistent if and only if:

$$\forall i, \ \forall j: \ 1 \leq i, \ j \leq n :: inconsistent(LS_{i}, LS_{j}) = \emptyset$$

- In a consistent global state for every received message a corresponding send event is recorded in the global state.
- In an inconsistent global state, there is at least one message whose receive event is recorded but its send event is not recorded.
- A global state  $GS = \{LS_1, LS_2, ..., LS_n\}$  is transitless if and only if:

$$\forall i, \forall j$$
:  $1 \le i, j \le n$  ::  $transit(LS_i, LS_i) = \emptyset$ 

- All messages recorded to be sent are also recorded to be received.
- A global state is strongly consistent if it is consistent and transitless.
  - A strongly consistent state corresponds to a consistent state in which all messages recorded as sent are also recorded as received.

Note: the global state, as defined here, is seen as a collection of the local states, without explicitely capturing the state of the channel.



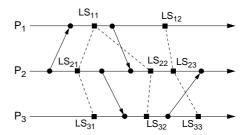
#### **Formal Definition**

- LS<sub>i</sub> is the local state of process P<sub>i</sub>.
   Beside other information, the local state also includes a record of all messages sent and received by the process.
- We consider the global state GS of a system, as the collection of the local states of its processes:
   GS = {LS<sub>1</sub>, LS<sub>2</sub>, ..., LS<sub>n</sub>}.
- A certain global state can be consistent or not!
- send(m<sup>k</sup><sub>ij</sub>) denotes the event of sending message m<sup>k</sup><sub>ij</sub> from P<sub>i</sub> to P<sub>j</sub>,
   rec(m<sup>k</sup><sub>ij</sub>) denotes the event of receiving message m<sup>k</sup><sub>ij</sub> by P<sub>j</sub>.
- send(m<sup>k</sup><sub>ij</sub>) ∈ LS<sub>i</sub> if and only if the sending event occurred before the local state was recorded;
   rec(m<sup>k</sup><sub>ij</sub>) ∈ LS<sub>j</sub> if and only if the receiving event occurred before the local state was recorded.
- transit( $LS_i, LS_j$ ) = { $m_{ij}^k$  | send( $m_{ij}^k$ )  $\in LS_i \land rec(m_{ij}^k) \notin LS_j$ } inconsistent( $LS_i, LS_j$ ) = { $m_{ij}^k$  | send( $m_{ij}^k$ )  $\notin LS_i \land rec(m_{ij}^k) \in LS_j$ }

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#### Formal Definition (cont'd)

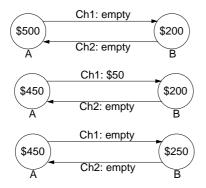


 $\{LS_{11}, LS_{22}, LS_{32}\}$  is inconsistent;  $\{LS_{12}, LS_{23}, LS_{23}\}$  is consistent;  $\{LS_{11}, LS_{21}, LS_{31}\}$  is strongly consistent.



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#### Formal Definition (cont'd)



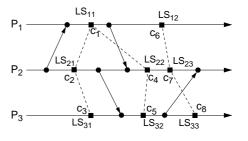
A	В	C : consistent NC: not consistent
500	200	{A,B}: strongly C
450 (mess <sub>1</sub> sent)	200	{A,B}: C
500	250 (mess <sub>1</sub> received)	{A,B}: NC
450 (mess <sub>1</sub> sent)	250 (mess <sub>1</sub> received)	{A,B}: strongly C

 After registering of the receive event(s) a consistent state becomes strongly consistent. It is considered to be a normal (transient) situation.



#### **Cuts of a Distributed Computation**

- A cut is a graphical representation of a global state. A consistent cut is a graphical representation of a consistent global state.
- A cut of a distributed computation is a set
   Ct = {c<sub>1</sub>, c<sub>2</sub>, ..., c<sub>n</sub>}, where c<sub>i</sub> is the cut event at
   process Pi.
- A cut event is the event of recording a local state of the respective process.

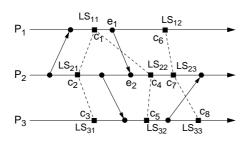


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#### Cuts of a Distributed Computation (cont'd)

 A cut is consistent if every message that was received before a cut event was sent before the cut event at the sender process.



 $\{c_1,c_4,c_5\}$  is not consistent:  $(e_1\rightarrow e_2) \land (e_2\rightarrow c_4) \land \neg (e_1\rightarrow c_1)$ 

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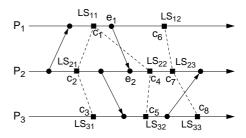
#### Cuts of a Distributed Computation (cont'd)

#### Theorem

A cut  $Ct = \{c_1, c_2, ..., c_n\}$  is a consistent cut if and only if no two cut events are causally related, that is:

 $\forall c_i, \ \forall c_j :: \neg(c_i \rightarrow c_j) \land \neg(c_j \rightarrow c_i)$ 

A set of concurrent cut events form a consistent cut.



 $\{c_1, c_2, c_3\}$ : strongly consistent (no communication line is

 $\{c_6, c_7, c_8\}$ : consistent (communication line is crossed but no causal relation).

 $\{c_1,c_4,c_5\}$ : not consistent;  $c_1 \rightarrow c_4$ 





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### Global State Recording (Chandy-Lamport Algorithm)

- The algorithm records a collection of local states which give a consistent global state of the system. In addition it records the state of the channels which is consistent with the collected global state.
- Such a recorded "view" of the system is called a snapshot.
- We assume that processes are connected through one directional channels and message delivery is FIFO.
- We assume that the graph of processes and channels is strongly connected (there exists a path between any two processes).
- The algorithm is based on the use of a special message, snapshot token, in order to control the state collection process.

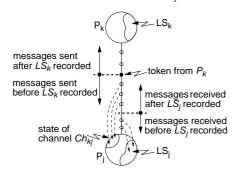


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#### Global State Recording (cont'd)

What about the channel states?

- P<sub>i</sub> sends a token to P<sub>j</sub> and this is the first time P<sub>j</sub> received a token ⇒ P<sub>j</sub> immediately records its state.
   All the messages sent by P<sub>j</sub> before sending the token have been received at P<sub>j</sub> ⇒ SCh<sub>jj</sub> := Ø.
- P<sub>j</sub> receives a token from P<sub>k</sub>, but P<sub>j</sub> already recorded its state. M is the set of messages that P<sub>j</sub> received from P<sub>k</sub> after P<sub>j</sub> recorded its state and before P<sub>j</sub> received the token from P<sub>k</sub> ⇒ SCh<sub>kj</sub> := M.



- The algorithm terminates when all processes have received tokens on all their input channels.
- The process that initiated the snapshot should be informed; it can collect the global snapshot.

#### Global State Recording (cont'd)

Some discussion on how to collect a global state:

- A process P<sub>i</sub> records its local state LS<sub>i</sub> and later sends a message m to P<sub>i</sub>, LS<sub>j</sub> at P<sub>j</sub> has to be recorded before P<sub>i</sub> has received m.
- The state SCh<sub>ij</sub> of the channel Ch<sub>ij</sub> consists of all messages that process P<sub>i</sub> sent before recording LS<sub>i</sub> and which have not been received by P<sub>j</sub> when recording LS<sub>i</sub>.
- A snapshot is started at the request of a particular process P<sub>i</sub>, for example, when it suspects a deadlock because of long delay in accessing a resource; P<sub>i</sub> then records its state LS<sub>i</sub> and, before sending any other message, it sends a token to every P<sub>i</sub> that P<sub>i</sub> communicates with.
- When P<sub>j</sub> receives a token from P<sub>i</sub>, and this is the
  first time it received a token, it must record its state
  before it receives the next message from P<sub>i</sub>. After
  recording its state P<sub>j</sub> sends a token to every
  process it communicates with, before sending them
  any other message.

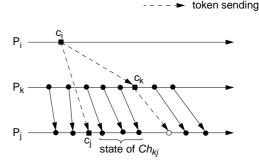


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#### Global State Recording (cont'd)

Maybe, you prefer this view:



 Don't forget when you look to the picture: we assumed that message passing on a channel connecting two processes is FIFO.





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#### Global State Recording (cont'd)

#### The algorithm

/\* performed by the initiating process and by any other process at the reception of the first token \*/

[SR1]: P<sub>i</sub> records its state.

[SR2]:  $P_i$  sends a token on each of its outgoing channels.

/\* executed whenever  $P_j$  receives a token from another process  $P_i$  on channel  $Ch_{ij}$ \*/

[RR1]: if  $P_j$  has not yet recorded its state then Record the state of the channel:  $SCh_{ij} := \emptyset$ . Follow the "Rule for sender".

#### else

Record the state of the channel:  $SCh_{ij} := M$ , where M is the set of messages that  $P_j$  received from  $P_i$  after  $P_j$  recorded its state and before  $P_j$  received the token on  $Ch_{jj}$ .

end if.



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#### Summary (cont'd)

- As there doesn't exist a global notion of physical time, it is very difficult to reason about a global state in a distributed system.
- We can consider a global state as a collection of local states and, possibly, a set of states of the communication channels.
- · A global state can be consistent or not.
- A cut is a graphical representation of a global state.
   Using cuts it is easy to elegantly reason about consistency of global states.
- It is possible to record local states and states of the channels, so that together they provide a consistent view of the system. Such a view is called a snapshot.



#### **Summary**

- In a distributed system there is no exact notion of global physical time. Physical clocks can be synchronized to a certain accuracy.
- In many applications not physical time is important but only the relative ordering of certain events.
   Such an ordering can be achieved using logical clocks.
- Lamport's logical clocks are implemented using a monotonic integer counter at each site. They can be used in order to capture the happened-before relation.
- The main problem with Lamport's clocks is that they are not powerful enough to perform a causal ordering of events.
- Vector clocks give the ability to decide whether two events are causally related or not, by simply looking at their timestamps.

