

School of Science

# COSC2536/2537 Security in Computing and Information Technology

Assignment 1



Assessment Type: Individual assignment; no group work. Submit online via Canvas→Assignments→Assignment

Marks awarded for meeting requirements as closely as possible. Clarifications/updates may be made via announcements/relevant discussion forums.



Due date: Week 4, Friday the 14th Aug 2020 11:59pm

Deadlines will not be advanced, but they may be extended. Please check Canvas→Syllabus or via Canvas→Assignments→Assignment 1 for the most up to date information.

As this is a major assignment in which you demonstrate your understanding, a university standard late penalty of 10% per each working day applies for up to 5 working days late, unless special consideration has been granted.



Weighting: 15 marks (Contributes 15% of the total Grade)

#### 1. Overview

The objective of Assignment 1 is evaluating your knowledge on the topics covered in Lecture 1-4. Topics include Basic Cryptographic Techniques (symmetric-key cryptography, hash, and cryptanalysis), and Public-Key Cryptography (RSA, ElGamal and Paillier cryptosystems). Assignment 1 will focus on developing your abilities in application of knowledge, critical analysis and decision making. Assignment 1 contains several problems related to the topics mentioned above. You are required to prepare the solutions and upload them as a single PDF or Word document in CANVAS.

In this assignment, there are 4 (four) questions in total. The first question Q1 is on designing a **cryptographic algorithm for a secure vault** with a sophisticated digital keypad. In this question, a scenario is given that describes how a secret key for the digital keypad is generated and the digital keypad works. You need to design an algorithm that satisfies the requirements of the security of the digital keypad.

The second question Q2 is about designing an algorithm to perform *cryptanalysis* on a captured encrypted text. The term Cryptanalysis is used to breach cryptographic security systems and gain access to the contents of encrypted messages, even if the cryptographic key is unknown. Therefore, you are expected to apply cryptanalysis in to obtain plaintext from the given ciphertext in Q2.

The third question Q3 is about the designing a *Secure Online Property Auction System* using the *hash algorithm*. In Q3, you are expected to design an *Online Bidding System* where an attacker cannot determine the bid values of participants and the *hash algorithm* based bidding would work.

The fourth question Q4 is related to breaking the *RSA Encryption algorithm*. Only for this question, you can submit the solution individually or in a group. In the case of a group submission, the maximum group members can be 3 (three), and you must mention the names of group members in the solution of this question. In this question, you are expected to design an algorithm that would perform prime factorization using the computational power of 10 computers and determine the private-key *d* from the public-key *(n, e)*. You should demonstrate the detail steps with explanations how the RSA encryption algorithm can be broken. Marks will be deducted if you fail to show the detail computations correctly, skip the computational steps, or do not provide explanations.

Develop this assignment in an iterative fashion (as opposed to completing it in one sitting). You should be able to start preparing your answers immediately after the Lecture-1 (in Week-1). At the end of each week starting from Week-1 to Week-4, you should be able to solve at least one question.

If there are questions, you must ask via the relevant Canvas discussion forums in a general manner.

Submission instructions are detailed in Section 2.



#### 2. Submission Instructions

Overall, you must follow the following special instructions:

- You must use the values provided in the questions.
- Hand-written answers are not allowed and will not be assessed. Compose your answers using any word processing software (e.g. MS Word or Latex).
- You are required to show all of the steps and intermediate results for each question.
- Upload your solution as a single PDF or Word document in CANVAS.

### 3. Assessment Criteria

This assessment will determine your ability to:

- Follow requirements provided in this document and in the lessons.
- Independently solve a problem by using cryptography and cryptanalysis concepts taught over the first four weeks of the course.
- Meeting deadlines.

## 4. Learning Outcomes

This assessment is relevant to the following Learning Outcomes:

- 1. CLO 1: explain the functioning of security services in computing environments and the security issues in networked applications.
- 2. CLO 2: discuss various types of data integrity and confidentiality mechanisms including public key cryptography.
- 3. CLO 3: describe basic system security mechanisms and protocols, such as those used in operating systems, file systems and computer networks.

### 5. Assessment details

Please ensure that you have read **Section 1** to **3** of this document before going further. Assessment details (i.e. question Q1 to Q4) are provided in the <u>next page</u>.



# Q1. Designing Cryptographic Algorithm for Secure Vault (3 Marks)

One day, three friends (Alice, Bob, and Laura) miraculously found huge number of ancient gold coins of equal size while bushwalking. They decided to equally divide those coins and bring them home. However, given that homes may not be safe to store the coins, they decided to put them in a strong vault in a bank (see **Figure-1.1**).

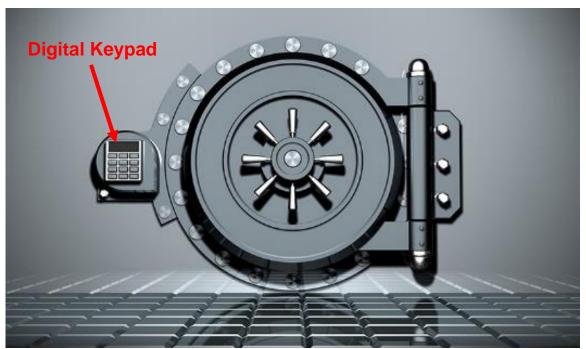


Figure-1.1: A vault with digital keypad

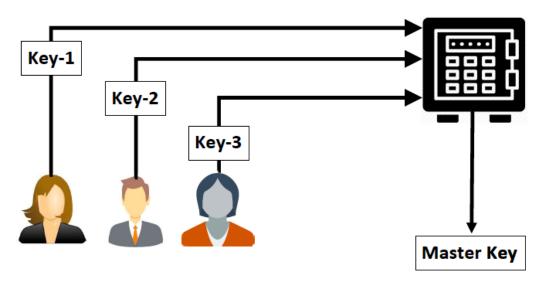


Figure-1.2: Master Key generation at vault from three keys

The vault has a digital keypad (see **Figure-1.1**) which is used to enter secret password for opening it. However, this keypad is very sophisticated and specially designed for the three friends. It can accept three secret keys one after another. Each secret key is an integer number of 5 digits.

When the keypad is initialized each friend enters individual secret key without anyone knowing that number. Once all three friends enter their secret numbers, the sophisticated logic in the keypad performs a mathematical operation and generates a master key by using the three numbers (see **Figure-1.2**). It then stores the master key in the memory and deletes the individual secret keys.



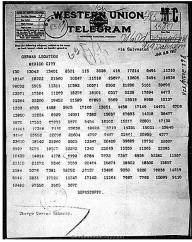
Once the digital keypad is initialized, they can come anytime but they must come all at the same time and enter the secret keys one after another. Similar to the initialization phase, keypad performs a mathematical operation and generates a new master key by using the three numbers. The new master key is then compared with old master key saved in the keypad. If they are same, the vault opens.

Explain the algorithm with an example to design the sophisticated keypad for the excellent vault which has gold coins!

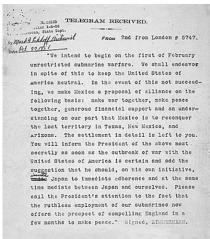
[Note: If you are interested to implement a broader version of this system as a Capstone project, please contact the Lecturer]

# Q2. Designing Algorithm for Cryptanalysis with Missing Encrypted Text (3 Marks)

On January 16, 1917, British code breakers intercepted an encrypted message from Zimmermann intended for Heinrich von Eckardt, the German ambassador to Mexico. The challenge was, the encrypted message had many missing ciphertext. The ciphertext and decoded message of Zimmermann is shown in **Figure-2**. In spite of missing encrypted text, the British cryptographic office known as "Room 40" decoded the Zimmermann Telegram and handed it over to the United States in late-February 1917.



(a) Encoded Message



(b) Decoded Message

Figure-2: Zimmermann Telegram

In this task, you have to decrypt an encrypted message. However, here we have encrypted a long English message a bit differently. Every single alphabet in the message has been substituted by another unique alphabet. While the encrypted message was captured, some of the alphabets were missing. A missing encrypted alphabet is marked as '\_'. The encrypted message is shown below:

EFA OBE\_HA FBK OA\_D IBNGDN BHH JBM G\_ EFA JGKEBDRA BDJ \_ BP SDBOHA EC BKRAIEBGD LFAEFAI BDMEFGDN FBK OAAD NBGDAJ CI DCE. \_ FCL G HCDN QCI EFGK LBI EC ADJ. FCL G HC\_N QCI TABRA. FCL LG\_H G FBGH EFA JBM LFAD G IAESID EC EFA OCKCP CQ PM QBPGHM. P\_ JABI G FCTA EC KAA MCS.

You need to perform the followings:

- a) Decipher and find out the actual message. Show step-by-step processes.
- b) Provide the decryption algorithm (in pseudocode or actual code in any programming language).



# Q3. Designing Secure Online Property Auction System using Hash Algorithm (4 Marks)

Covid-19 has changed the way we conduct business these days. This is true for property auctions as well. The Prime minister of Australia recently announced a ban on in-person auctions and open-for-inspections. Large number of sellers and property agents are opting for online auctions. Based on an article published (URL: <a href="https://www.domain.com.au/news/saturday-auctions-how-will-they-work-now-they-are-all-online-944545/">https://www.domain.com.au/news/saturday-auctions-how-will-they-work-now-they-are-all-online-944545/</a>), we would like to highlight few facts about the current practice in online auctions:

- "Online auctions run like a mix between a live stream and a traditional auction, with buyers registering and placing bids while watching the video as if they were there."
- "Another method involves buyers sending off bids, similar to eBay, and the time allotted for the auction is extended by five minutes every time a bid is entered."

Obviously, there are many issues with online auction, but one of the critical issues is trust – the way online bidding process is conducted. We want to make sure the online bidding process is trustworthy, and nobody can cheat to win.

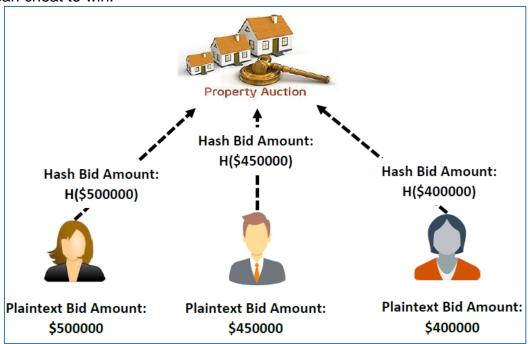


Figure-3: Cryptographic Hash Function based Online Bidding Application

Design a cheating-proof online property auction system using cryptographic hash function with the following requirements:

- A bidder can only bid with the hash value of the bid amount.
- The bidder can bid only once.
- Guessing the plaintext bid amount should be difficult.

Show step-by-step process with concrete examples.

[Note: If you are interested to implement a broader version of this system as a Capstone project, please contact the Lecturer]



# Q4. Breaking RSA Key Faster with Multiple Servers (5 Marks)

[Note: Only for this question, you can submit the solution individually or in a group. In the case of a group submission, the maximum group members can be 3 (three), and you must mention the names of group members in the solution of this question.]

It has been found that a quantum computer with 4099 perfectly stable qubits could break the RSA-2048 encryption in 10 seconds, while a classic computer of present days requires 300 trillion years. It means, the powerful computers make the RSA cryptosystem vulnerable.

RSA cryptosystem is mainly built on the concept of prime numbers. The public-key component (n) of RSA cryptosystem is an integer that is the product of two prime numbers. Hence, prime factorization is a technique that can be used for breaking RSA private-key (d).

Prime factorization or integer factorization of a number is breaking a number down into the set of prime numbers which multiply together to result in the original number. This is also known as prime decomposition. Assume a number '77' has two prime factors. That is, '77' is a product of two prime numbers: 7 and 11 (i.e.,  $77 = 7 \times 11$ ).

```
The First 10,000 Primes
                       (the 10,000th is 104,729)
        For more information on primes see http://primes.utm.edu/
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                   5
                         7
                                11
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                                                           23
                                                                  29
    31
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103087 103091 103093 103099 103123 103141 103171 103177 103183 103217
103231 103237 103289 103291 103307 103319 103333 103349 103357 103387
103391 103393 103399 103409 103421 103423 103451 103457 103471 103483
103511 103529 103549 103553 103561 103567 103573 103577 103583 103591
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104309 104311 104323 104327 104347 104369 104381 104383 104393 104399
104417 104459 104471 104473 104479 104491 104513 104527 104537 104543
104549 104551 104561 104579 104593 104597 104623 104639 104651 104659
104677 104681 104683 104693 104701 104707 104711 104717 104723 104729
end.
```

Figure-4: Partial list of first 10000 Prime Numbers



However, a simple method to find the prime factors is to take a list of prime numbers, and start dividing a number by each prime number starting from '2' in the prime number's list. For example, first 10 prime numbers are: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29. Now, to find out the prime factors of '77', you should divide '77' by each prime number in the above list as follows unless you get another prime number as a quotient:

77 / 2 = Quotient is NOT a prime number 77 / 3 = Quotient is NOT a prime number 77 / 5 = Quotient is NOT a prime number 77 / 7 = 11 (Quotient is a prime number)

Hence, 7 and 11 are two prime factors of 77.

As you know from Lecture-3 and Tutorial-3, the public-key component (n) of the RSA cryptosystems is an integer that has two prime numbers. Assume that you have found the RSA public-key as: n = 10772542097 and e = 95177. You want to find the **private-key (d)** for the above RSA public-key.

Say, you have the list of first 10000 prime numbers as partially shown in **Figure-4**. A complete list of first 10000 prime numbers can be found in the URL: <a href="https://primes.utm.edu/lists/small/10000.txt">https://primes.utm.edu/lists/small/10000.txt</a>. Assume that you have **10 computers**. How can you take advantage of the 10 computers and perform the integer factorization tasks mentioned above to break RSA faster? Explain your algorithm and show detail steps. Please note that we are not interested in any established approach found in textbooks to find prime factors. A simple brute-force method should do the work.

[https://www.quintessencelabs.com/blog/breaking-rsa-encryption-update-state-art/]

# 6. Academic integrity and plagiarism (standard warning)

Academic integrity is about honest presentation of your academic work. It means acknowledging the work of others while developing your own insights, knowledge, and ideas. You should take extreme care that you have:

- Acknowledged words, data, diagrams, models, frameworks and/or ideas of others you have quoted (i.e. directly copied), summarized, paraphrased, discussed, or mentioned in your assessment through the appropriate referencing methods,
- Provided a reference list of the publication details so your reader can locate the source if necessary. This includes material taken from Internet sites.

If you do not acknowledge the sources of your material, you may be accused of plagiarism because you have passed off the work and ideas of another person without appropriate referencing, as if they were your own.

RMIT University treats plagiarism as a very serious offence constituting misconduct. Plagiarism covers a variety of inappropriate behaviors, including:

- Failure to properly document a source
- Copyright material from the internet or databases
- Collusion between students

For further information on our policies and procedures, please refer to the **University website**.

# 7. Assessment declaration

When you submit work electronically, you agree to the assessment declaration.



# UNIVERSITY 8. Rubric/assessment criteria for marking

All of the computations must be correct and only provided values must be used. Instructions must be followed.

Criteria The characteristic or outcome that is being judged.								Total
Question 1  Designing Cryptographic Algorithm	The answer is correct and the explanation is up to the mark  3 Marks	ne explanation is up to the appla up to the mai		explanation is not explanation is not up to the r		The question is attempted with the correct approach but the answer is not correct.  0.5 Marks	Not answered.  0 Marks	3 Marks
Question 2 Designing Algorithm for Cryptanalysis	Plaintext is correct  Steps are shown in a systematic way and algorithm is presented well.  3 Marks		Plaintext is correct  Steps are shown in a systematic way, but algorithm is not presented well or somewhat incorrect.		Plaintext is partially correct  Or Plaintext is correct. Steps are not shown in a systematic way and algorithm is not presented.		Not answered  0 Marks	3 Marks
Question 3 Cryptographic Hash Algorithm	The answer is correct, and the explanation is up to the mark  4 Marks	The answer is correct, but the explanation is not up to the mark  3 Marks		The answer is partially correct, and the explanation is not up to the mark  2 Marks		The question is attempted but the answer is not correct.  1 Marks	Not answered  0 Marks	4 Marks
Question 4 Breaking RSA Encryption algorithm	Step-by-step processes of private-key computation are shown with a distributed algorithm.  All of the computations are shown correctly in detail	Step-by-step processes of private-key computation are shown with a distributed algorithm.  Not all of the computations are shown correctly in detail		Step-by-step processes of private-key computation are shown correctly and distributed algorithm is not convincing or somewhat incorrect.  However, private-key computation steps are not shown or incorrectly shown		Step-by-step processes of private-key computation are shown that are partially correct/ completely wrong.  Distributed algorithm is not discussed.	Not answered  0 Marks	5 Marks