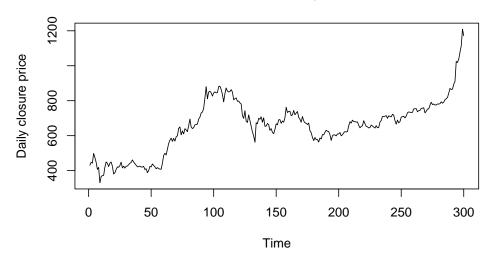
Stats 153 Project - Zoey

2. Exploratory Data Analysis

Here we explore the data. Naturally, the first plot you should make is the data itself. Point out any visible features, e.g. heteroscedasticity, seasonality, trend. To observe the recent pattern better, we only use the last 300 data points from the time series. Each data point represents daily closure price for TSLA stock. From observing the original data, it seems that the variability of the time series data set appears to be non-constant, which is heterscedasticity. Therefore we transform original data through $f(Y_t) = log(Y_t)$.

```
t = 1:300
data <- read.csv("data/TSLA.csv")
open <- data$Open
close <- data$Adj.Close
close_data = tail(close, 300)
plot.ts(close_data, main="TSLA stock closure price data", ylab="Daily closure price")</pre>
```

TSLA stock closure price data

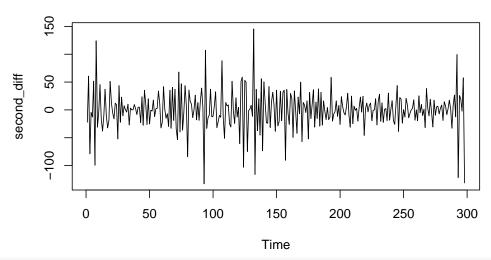


Models considered: Second Order Differencing + ARMA

Second order differencing, observe the data, the data seems stationary without obvioud trend or seasonality.

```
diff = diff(close_data, lag=1)
second_diff = diff(diff, lag = 1)
plot.ts(second_diff, main="second order differencing on TSLA data")
```

second order differencing on TSLA data



acf2(second_diff, main="Series: TSLA closure price data")

##

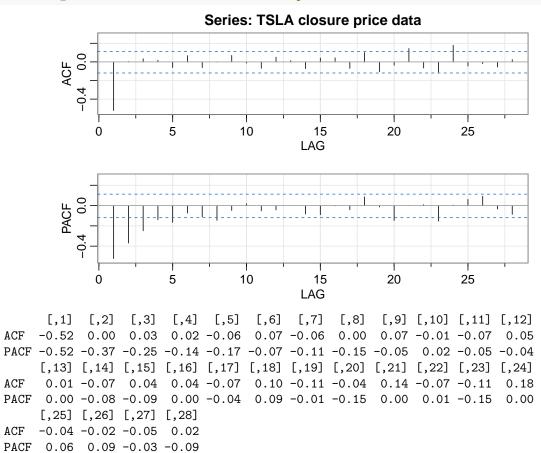
ACF

ACF

PACF

##

ACF ## PACF



Evaluation Evaluating AIC, BIC, AICc, and time-series cross validation. Evaluate model based on how well they predict future values. Choose model: (1, 2, 1)(0, 0, 0)[0]. This is because observing ACF plot on data after second order differencing, there is a cut off on approximately lag=1, and Recall that for MA(q) model, the sample ACF will contain zero values for lag |h| > q. Therefore we try MA(1) model. Observing partial ACF plot, there is an exponential decay, indicating we should use an ARMA(p, q) model. We use the function auto.arima to build intuition on what p, q value to choose.

```
auto.arima(second_diff)

## Series: second_diff

## ARIMA(1,0,1) with zero mean

##

## Coefficients:

## ar1 ma1

## -0.1087 -0.9488
```

sigma^2 estimated as 582.9: log likelihood=-1371.93 ## AIC=2749.87 AICc=2749.95 BIC=2760.96

0.0276

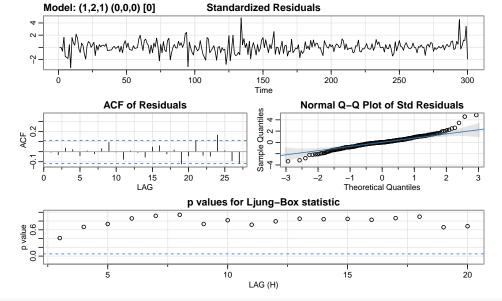
The model looks well on Ljung-Box statistic with all p values above 0.05. Also the ACF of residuals shows no ACF go beyond two blue band.

```
model1 <- sarima(close_data, p=1, d=2, q=1, P=0, D=0, Q=0, S=0)
```

```
## initial value 3.556748
## iter
        2 value 3.293231
## iter
        3 value 3.236037
## iter
        4 value 3.208883
## iter
        5 value 3.193975
## iter
         6 value 3.187240
## iter
         7 value 3.185019
## iter
         8 value 3.182390
## iter
         9 value 3.181715
## iter
       10 value 3.181599
       11 value 3.181571
## iter
## iter
       12 value 3.181571
## iter 12 value 3.181571
## iter 12 value 3.181571
## final value 3.181571
## converged
## initial value 3.184899
## iter
        2 value 3.184872
## iter
        3 value 3.184869
## iter
        4 value 3.184869
## iter
         4 value 3.184869
## iter
         4 value 3.184869
## final value 3.184869
## converged
```

s.e.

0.0635

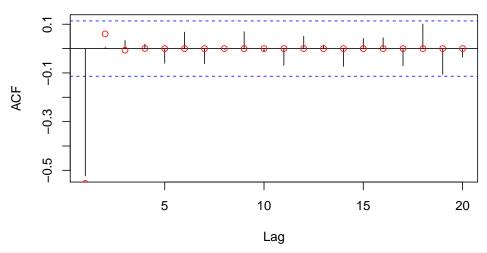


model1\$ttable

```
## Estimate SE t.value p.value
## ar1 -0.1087 0.0635 -1.7118  0.088
## ma1 -0.9488 0.0276 -34.3423  0.000

model1.acf=ARMAacf(ar=c(-0.1087), ma=c(-0.9488), lag.max = 20, pacf=FALSE)
acf(as.vector(second_diff), lag.max=20)
points(0:20, model1.acf, col='red')
```

Series as.vector(second_diff)



```
cat("AIC", model1$AIC)
```

AIC 9.227749

cat("BIC", model1\$BIC)

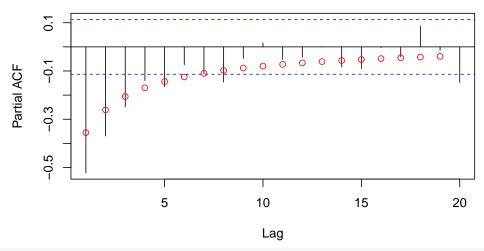
BIC 9.264968

cat("AICc", model1\$AICc)

AICc 9.227885

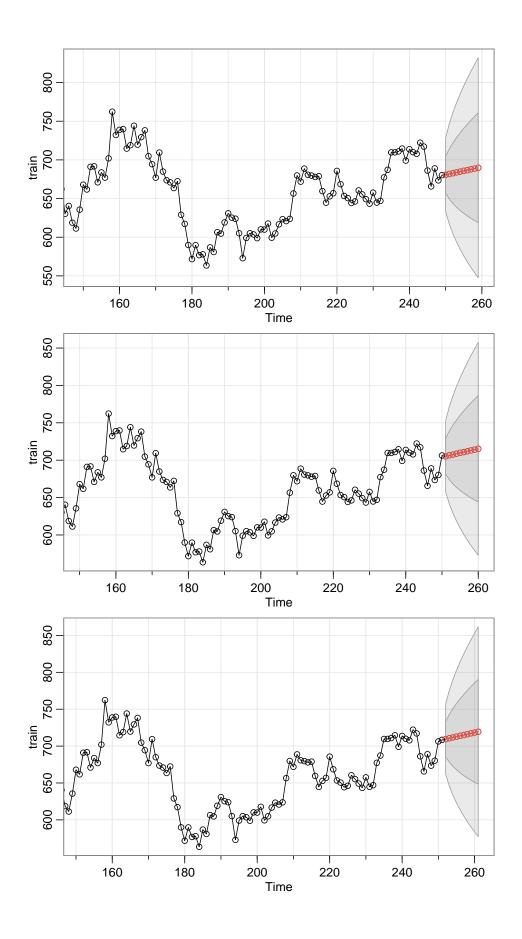
```
model1.pacf=ARMAacf(ar=c(-0.1087), ma=c(-0.9488), lag.max = 20, pacf=TRUE)
pacf(as.vector(second_diff), lag.max=20)
points(0:19, model1.pacf, col='red')
```

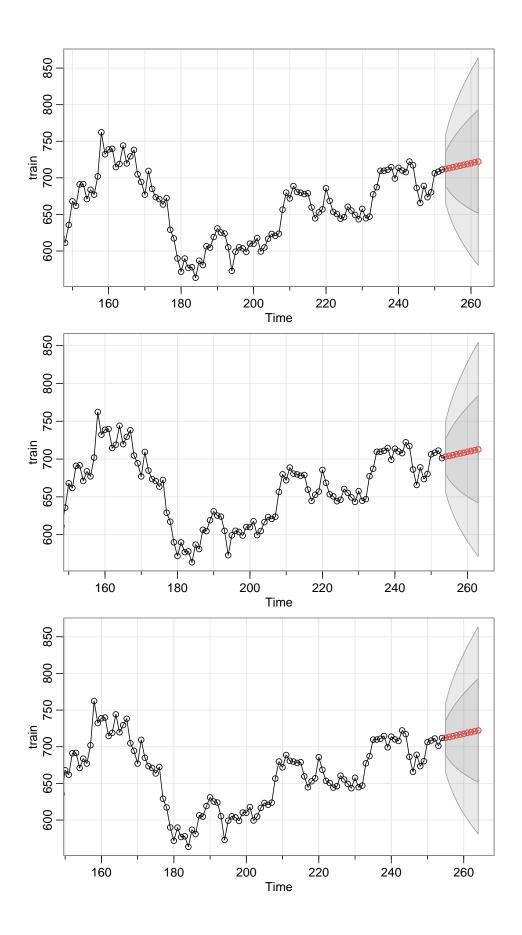
Series as.vector(second_diff)

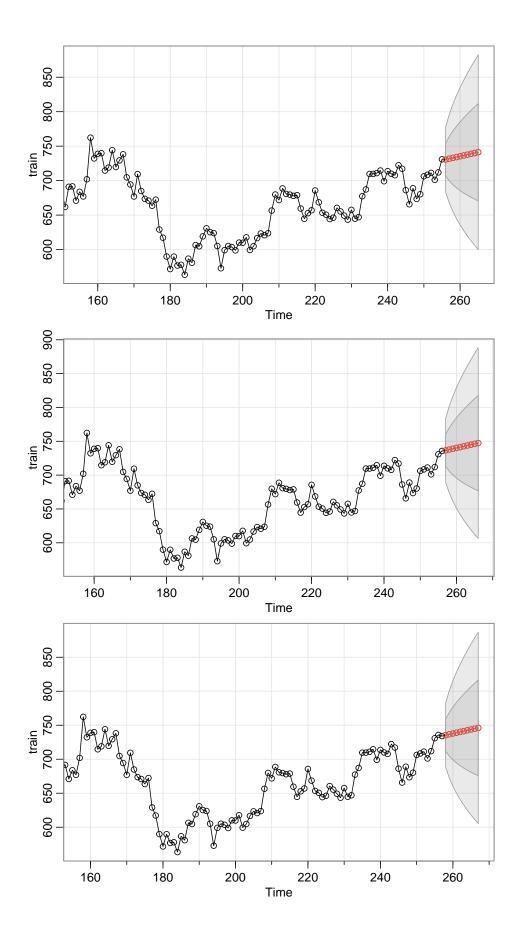


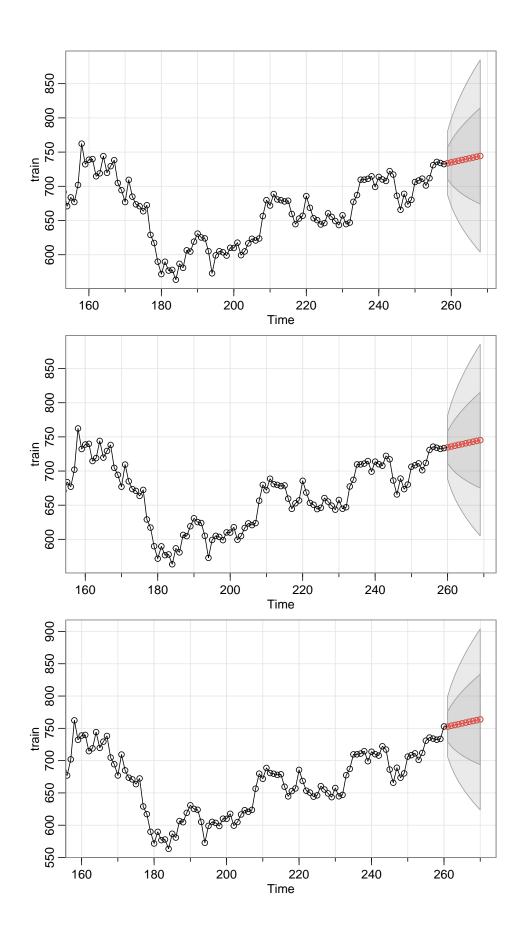
```
# cross validation
start_day <- 250
end_day <- 290
jump = 10
error = 0
forward_time = 10
# we are performing n-fold validation
n = (end_day - start_day) / jump

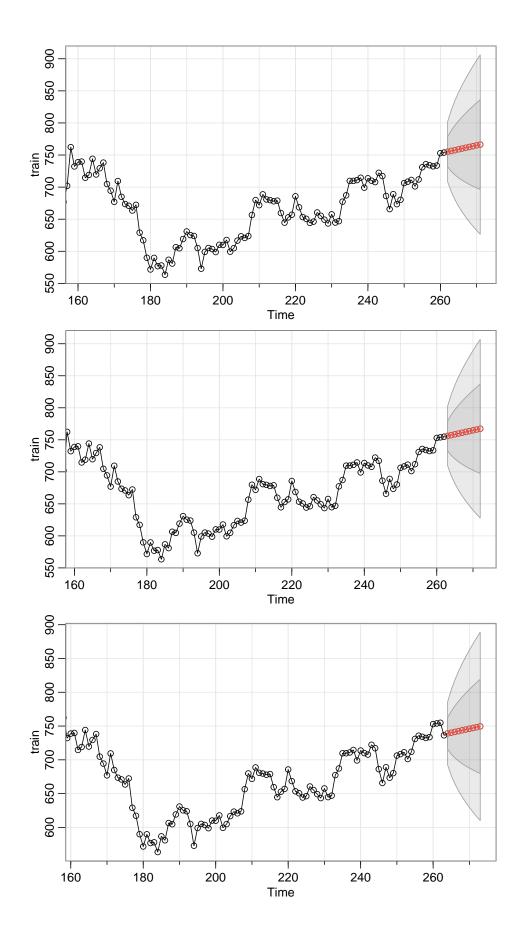
for (k in start_day:end_day) {
   train <- window(close_data, end=k-0.001)
   test <- window(close_data, start=k, end=k + forward_time - 0.01)
   forecast <- sarima.for(train, n.ahead = forward_time, p=1, d=2, q=1, P=0, D=0, Q=0, S=0)
   error = error + sum((forecast$pred - test)^2)
   k = k + 10
}</pre>
```

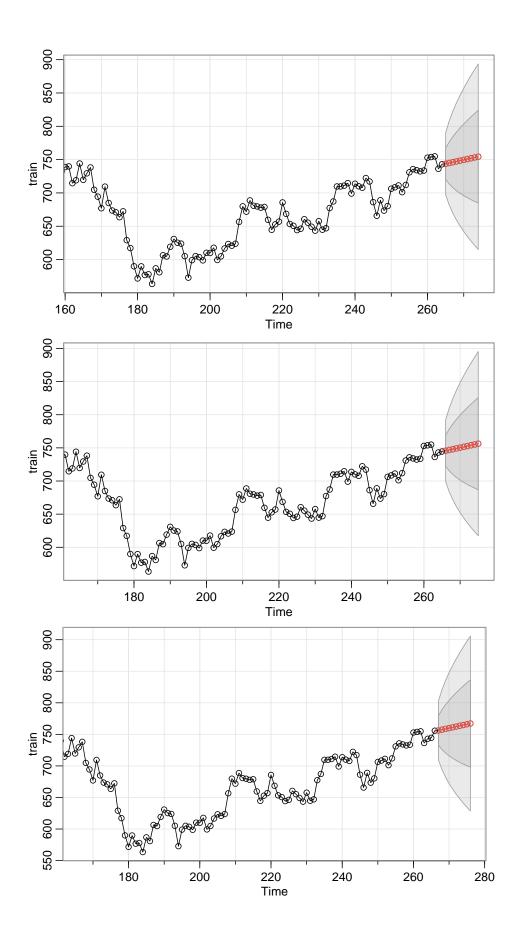


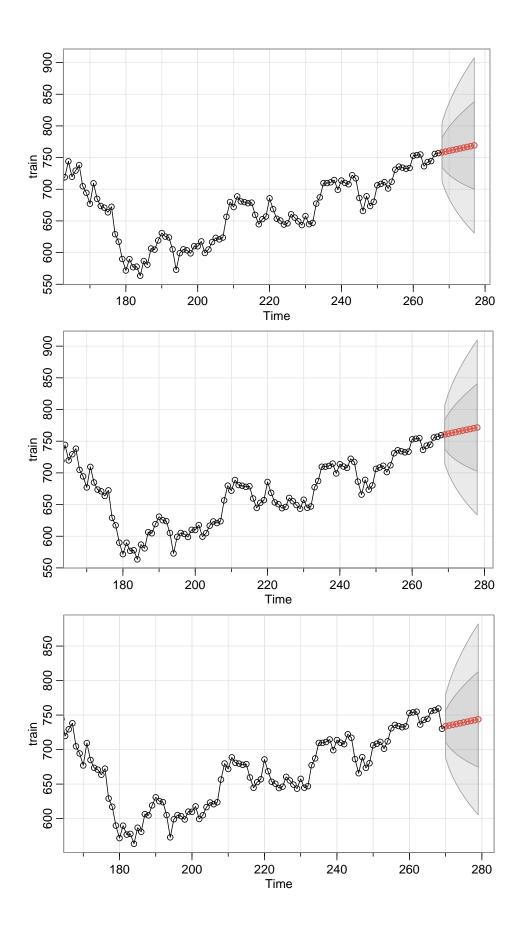


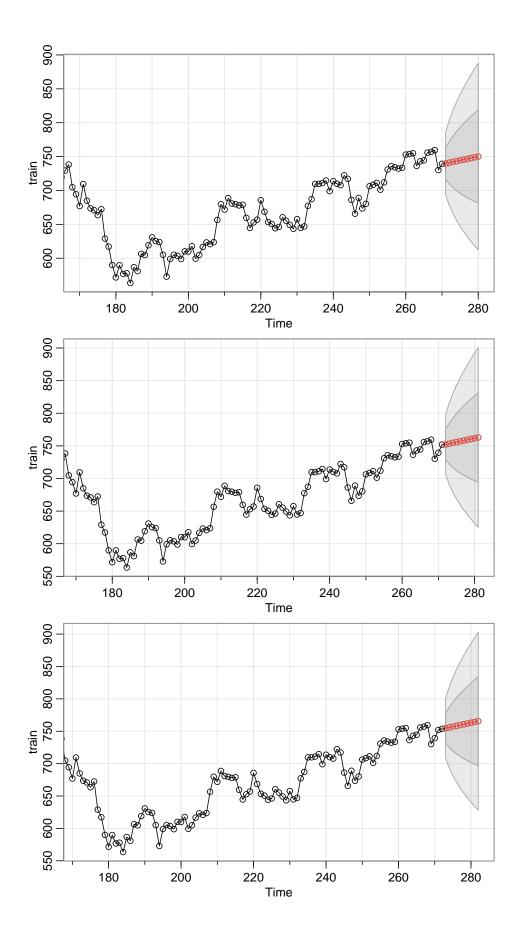


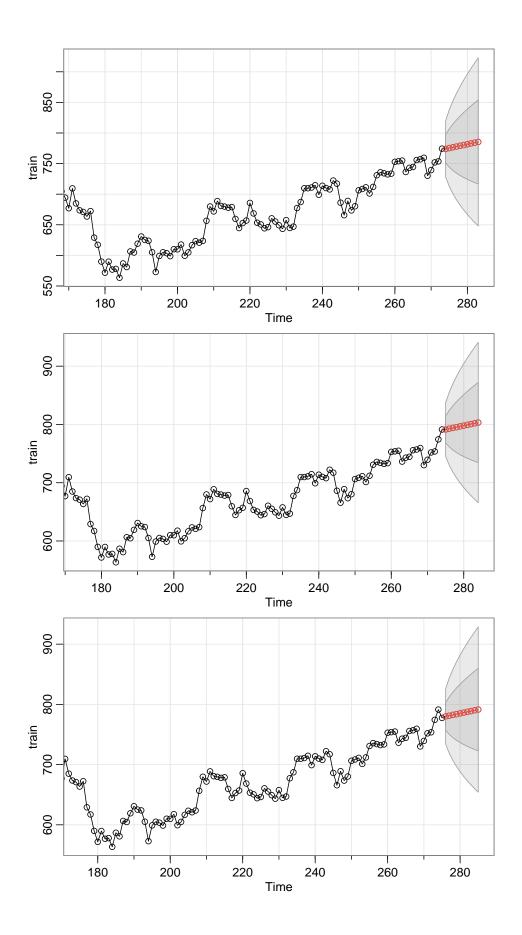


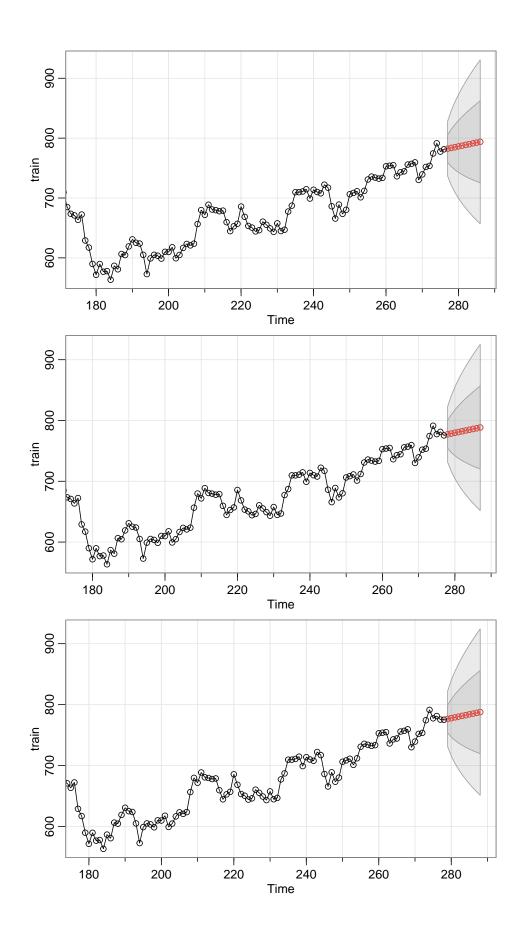


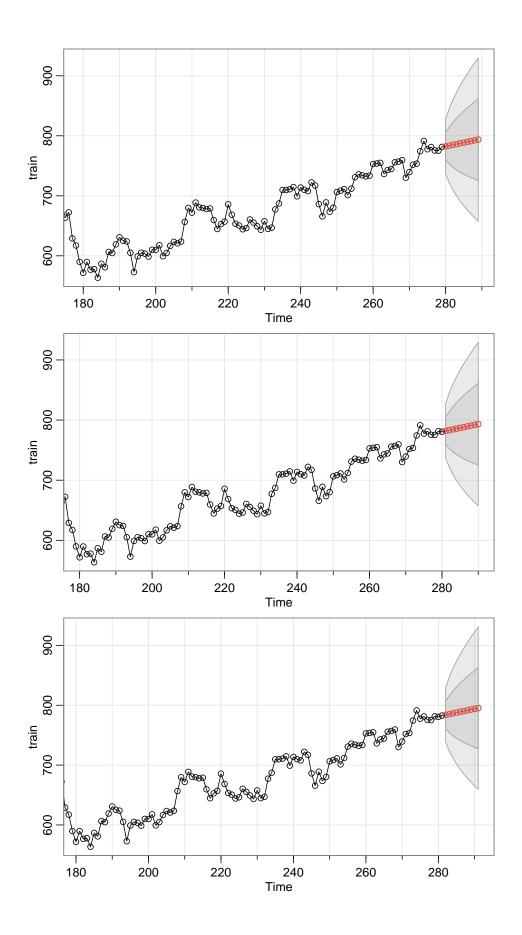


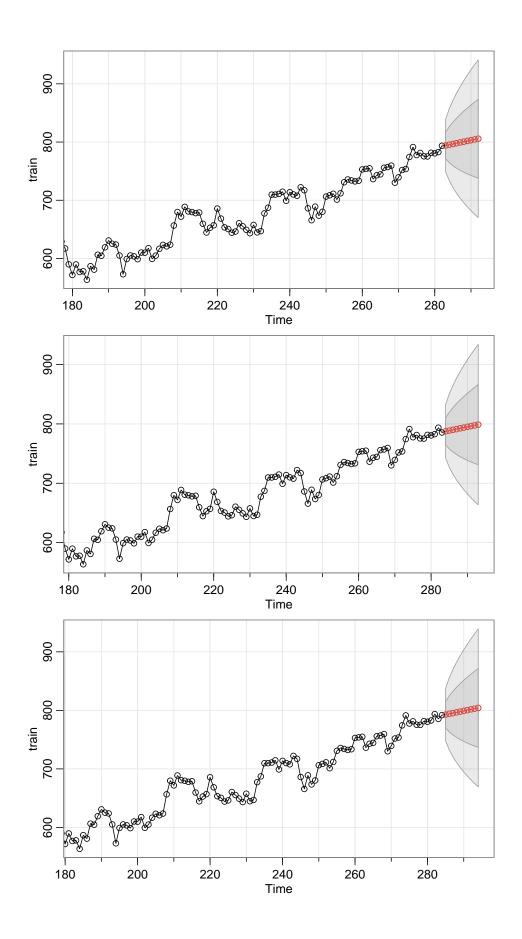


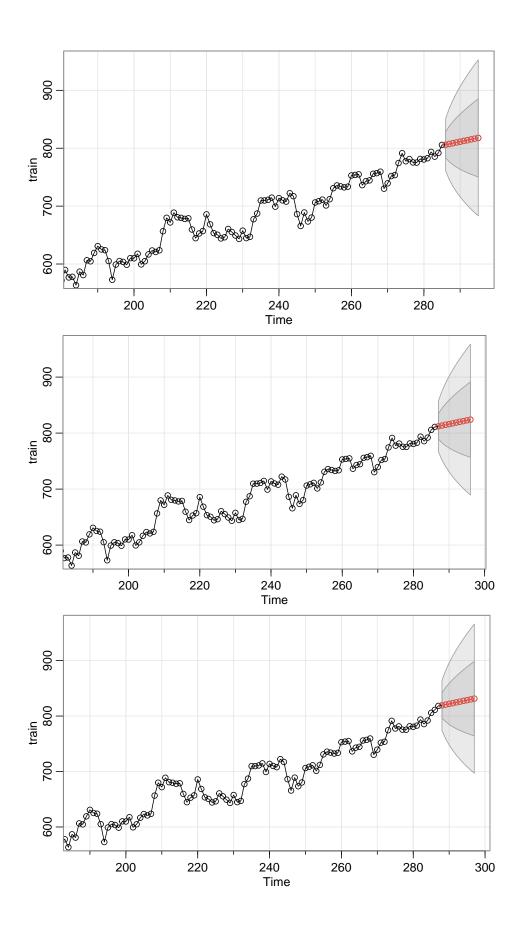


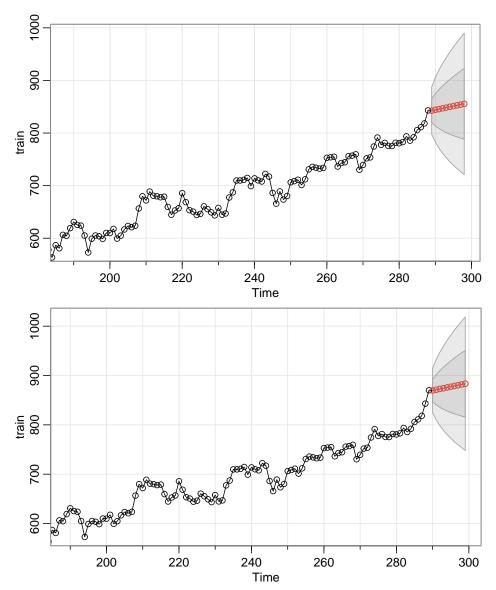












```
error = error / n
cat("cross validation error", error)
```

cross validation error 311970.1

5. Results

We choose model 3: 2nd-order differencing + ARMA 2A model. First, write out model mathematically. Let original time series stock data denoted by $\{X_t\}$ and second order differenced time series data denoted by $\{Z_t\}$. Then $(1 - \phi_1 B)\nabla^2 X_t = (1 - \theta_1 B)W_t$ or equivalently $(1 - \phi_1 B)Z_t = (1 - \theta_1 B)W_t$. Second, estimate the parameters of your chosen model, probably in a table.

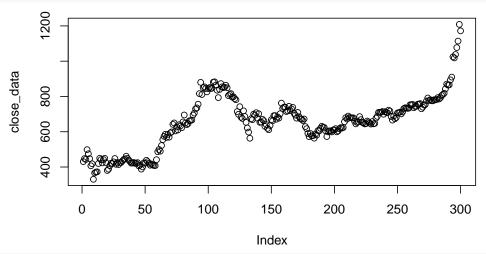
model1\$ttable

```
## Estimate SE t.value p.value
## ar1 -0.1087 0.0635 -1.7118 0.088
## ma1 -0.9488 0.0276 -34.3423 0.000
```

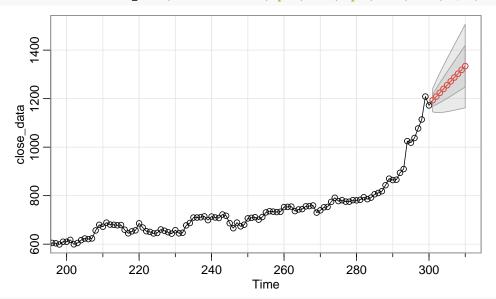
Third, forecast appropriately and include a plot of your forecasted values appended to the end of your time series. Here I choose to forecast TSLA closure price for next 10 days. TODO: address uncertainty about

prediction?

plot(close_data)



forecast <- sarima.for(close_data, n.ahead = 10, p=1, d=2, q=1, P=0, D=0, Q=0, S=0)



forecast\$pred

```
## Time Series:
## Start = 301
## End = 310
## Frequency = 1
## [1] 1193.389 1208.478 1224.251 1239.950 1255.657 1271.364 1287.070 1302.776
## [9] 1318.482 1334.189
```

5.1 Estimation of model parameters