

1. Give a *\*detailed\** outline of the steps to show that a decision problem  $D$  is NP-complete.
2. [Exercise 8.10 from the textbook] Prove that each problem below is NP-complete. For part of your proof, show that the problem is a generalization of a known NP-complete problem.
  - (a) SubgraphIsomorphism: Given two graphs  $G$  and  $H$ , is  $G$  a subgraph of  $H$ ? (In other words, is it possible to map every vertex of  $G$  to some vertex of  $H$  so that  $H$  contains exactly the same edges as  $G$  on those vertices?)
  - (c) MaxSat: Given a CNF formula  $F$  and positive integer  $k$ , is there an assignment of truth values that satisfies at least  $k$  clauses of  $F$ ?
  - (e) SparseSubgraph: Given a graph  $G$  and positive integers  $a, b$ , is there a subset of  $a$  vertices of  $G$  with no more than  $b$  edges between them?
  - (f) SetCover: Given a set  $S$ , subsets  $S_1, \dots, S_m$  of  $S$ , and positive integer  $k$ , is there a collection of  $k$  subsets whose union is equal to  $S$ ?
3. Construct polytime reductions between any two of VertexCover, IndependentSet, and Clique.