

Consider again the problem of making change when the denominations are arbitrary.

Input: Positive integer amount  $A$ , positive integer denominations

$d[1] < d[2] < \dots < d[m]$  for  $m \geq 1$ .

Output: List of coins  $c = [c[1], \dots, c[n]]$ , where each  $c[i]$  is in  $d$ , repeated coins are allowed (possible for  $c[i] = c[j]$  with  $i \neq j$ ),  $c[1] + \dots + c[n] = A$ , and  $n$  is minimum. If no solution is possible, the empty list  $[]$  is returned.

For example, if we only have pennies, dimes and quarters to make change for 30c, then the input is  $d = [1, 10, 25]$  and an optimum output is  $c = [10, 10, 10]$ . If we only have nickels, dimes and quarters to make change for 52c, then an optimum output is  $c = []$  -- no solution exists.

Follow the dynamic programming paradigm given in class to solve this problem.

Then, analyze the worst-case runtime of your algorithm carefully. Does it run in polynomial time? Explain.