HW₁

Program 1

• 1.3

After setting bias, it made 430 mistakes in total.

The error rate on training set is 0. And it is 0.02(2%) on validation set.

• 1.4

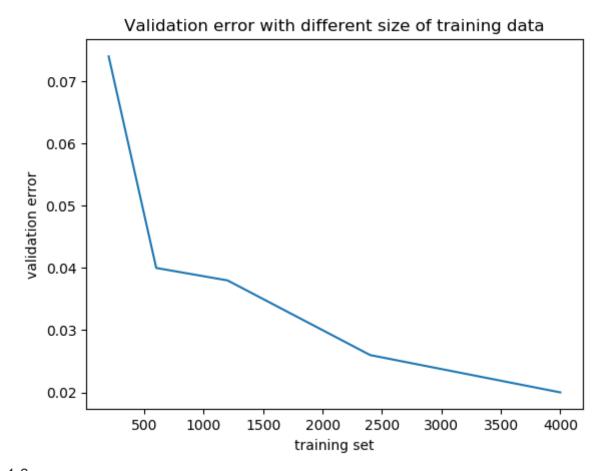
Postive(largest weights) words:

```
most positive weights are:
market
remov
guarante
our
click
sight
deathtospamdeathtospam
pleas
submit
minut
purchas
size
```

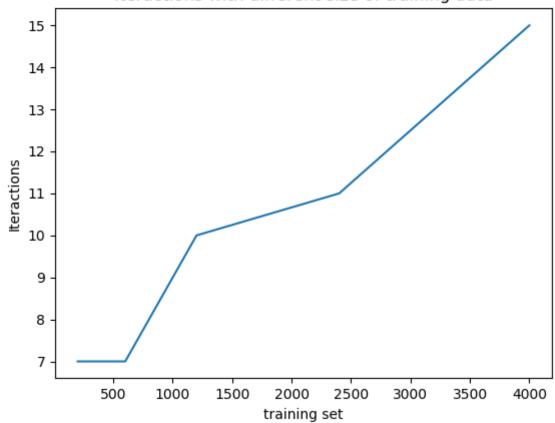
Negative words:

```
most negative weights are:
11
version
wrote
review
newslett
standard
i
david
upgrad
prefer
thei
which
```

• 1.5



Iteractions with different size of training data



- 1.7 Set a max iteration to 30.
- 1.8

0.024 - 0.022 - 0.020 - 0.018 - 0.016 - 0.014 - 0.012

From the grpah, we can tell the best config is X = 27. And the error rate on the whole test-set is 0.012(1.2%).

23

22

• 1.9

38 features(37 words plus a bias). Error rate is 0.169(16.9%).

24

It is not separable. With such a huge number, we can only get a vector that describes the most common words among all email types.

25

training set

26

27

28

Also, such a X also shows a huge validation error.

• 1.10

By using the validatoin set, we can tune the hyper-parameter in our model like the x in our case. Also, bescuase the model has no prior-knowledge about the test dataset. We can get a more accurate benchmark on the test dataset.

Problem 2

Let's take two arbitrary points from the hyperplane x_1 amd x_2 .

Substitute the two points to the hyperplane, we will get:

$$w \cdot x_1 + b = 0$$

$$w \cdot x_2 + b = 0$$

By doing subtrackion on above equations, we will get:

$$w\cdot(x_1-x_2)=0$$

which shows, vector w dot product any line in the plane equals zero and it means vector w is perpendicular to the hyperplane.

Problem 3

• Claim 2:

We have $w_t \Rightarrow w_{t-1} + x_{t-1}y_{t-1}$ $\Rightarrow w_t \cdot w^* = (w_{t-1} + x_{t-1}y_{t-1})w^* = w_{t-1}w^* + y_{t-1}x_{t-1}w^*.$ $\Rightarrow y_i w^* x_i \geq \gamma$, then we know $w_t w^* = w_{t-1}w^* + y_{t-1}x_{t-1}w^* \geq w_{t-1}w^* + \gamma.$ $\Rightarrow w_t w^* \geq \gamma + w_{t-1}w^*;$ $\Rightarrow w_{t-1}w^* \geq \gamma + w_{t-2}w^*$

$$w_t w^* \geq \gamma + w_{t-1} w^*$$

$$w_{t-1}w^* \geq \gamma + w_{t-2}w^*$$

:

$$w_1w^* \geq \gamma + w_0w^*$$

By substituting them iteratively, we will have $w_t \cdot w^* \geq M_t \gamma$ Claim 2 proof done.

Claim 3:
 Given Claim2 & Claim3, we have:

$$\left\|w_{t}
ight\|^{2} \leq M_{t}R^{2}$$

$$w_t \cdot w^* \geq M_t \gamma$$

For second claim:

$$w_t \cdot w^* \geq M_t \gamma \Rightarrow \|w_t\| \|w^*\| cos\theta \geq M_t \gamma$$

Since we know by defination, $\|W^*\|=1$,

$$w_t \cdot w^* \geq M_t \gamma \Rightarrow \|w_t\| cos heta \geq M_t \gamma \Rightarrow \|w_t\|^2 cos^2 heta \geq M_t^2 \gamma^2$$

We know that $M_t R^2 \geq \left\|w_t
ight\|^2 \geq \left\|w_t
ight\|^2 cos^2 heta \geq M_t^2 \gamma^2$,

$$M_t R^2 \geq {M_t}^2 \gamma^2 \Rightarrow M_t \leq rac{R^2}{\gamma^2}$$

Problem 4

By calculation, we know the R^2 for X=26 is 1114. Also, we know the $M_t=430$. Therefore, we get $\gamma^2 \leq \frac{R^2}{M_t} \Rightarrow 0 \leq \gamma \leq 1.61$