

HW1

Program 1

- 1.3

After setting bias, it made 430 mistakes in total.

The error rate on training set is 0. And it is 0.02(2%) on validation set.

- 1.4

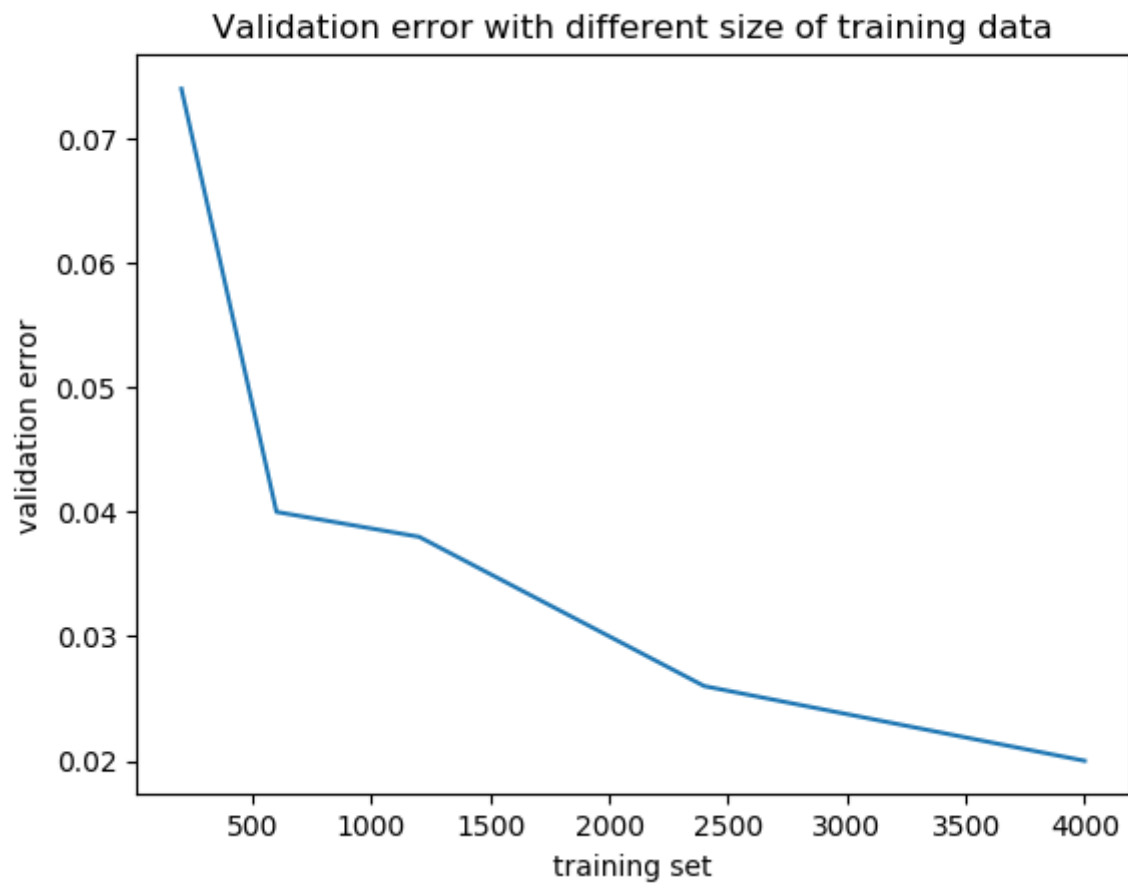
Postive words:

```
most positive weights are:
remov
best
from
take
lost
numbercnumb
captur
t
have
program
some
how
```

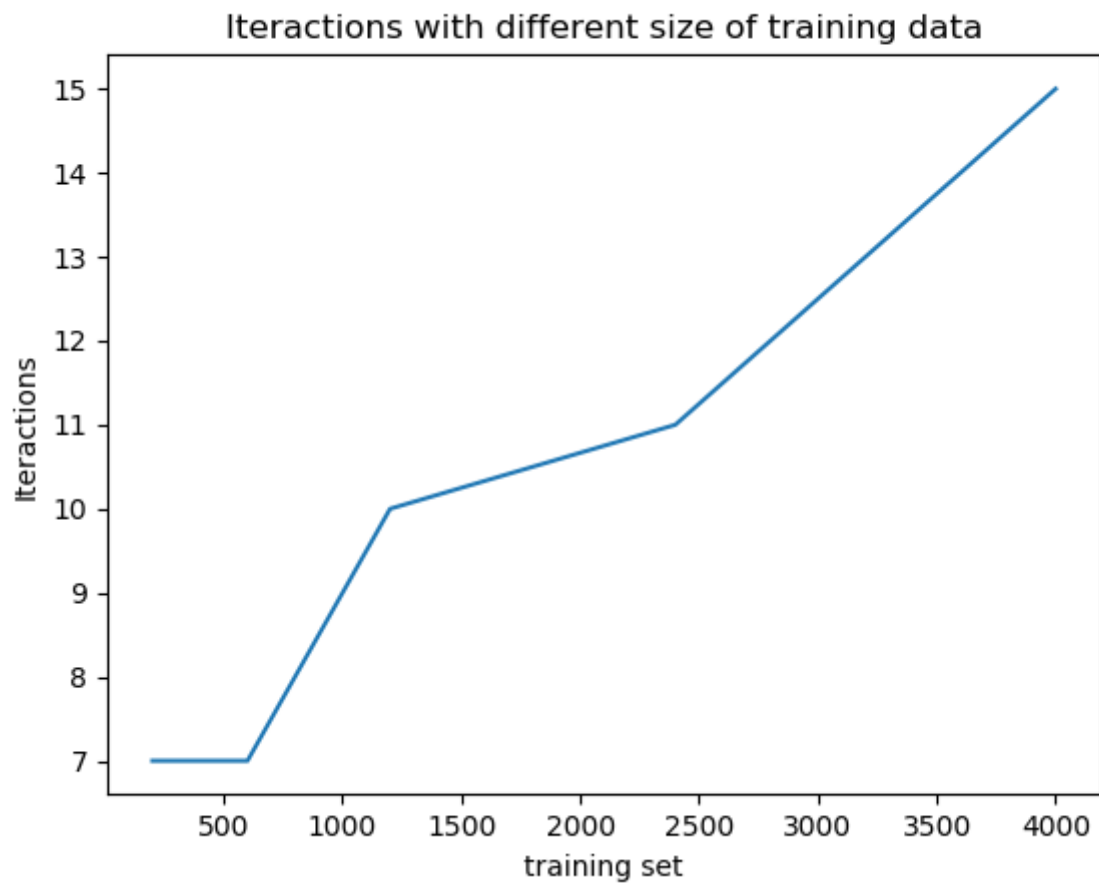
Negative words:

```
most negative weights are:
what
iso
matthia
few
log
discuss
found
transpar
se
file
sponsor
also
```

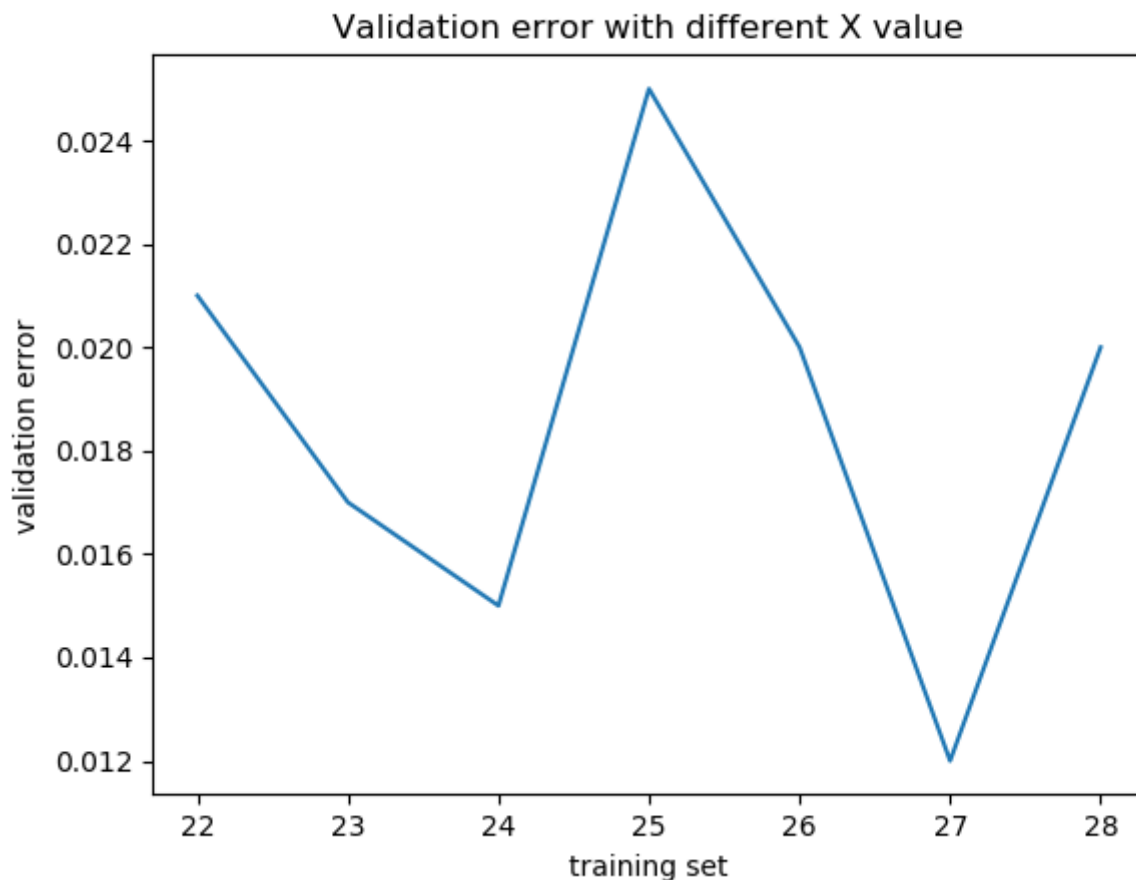
- 1.5



- 1.6



- 1.7
Set a max iteration to 30.
- 1.8



From the graph, we can tell the best config is $X = 27$.

And the error rate on the whole test-set is 0.012(1.2%).

- 1.9

38 features(37 words plus a bias). Error rate is 0.169(16.9%).

It is not separable. With such a huge number, we can only get a vector that describes the most common words among all email types.

Also, such a X also shows a huge validation error.

- 1.10

By using the validation set, we can tune the hyper-parameter in our model like the x in our case.

Also, because the model has no prior-knowledge about the test dataset. We can get a more accurate benchmark on the test dataset.

Problem 2

Let's take two arbitrary points from the hyperplane x_1 and x_2 .

Substitute the two points to the hyperplane, we will get:

$$w \cdot x_1 + b = 0$$

$$w \cdot x_2 + b = 0$$

By doing subtraction on above equations, we will get:

$$w \cdot (x_1 - x_2) = 0$$

which shows, vector w dot product any line in the plane equals zero and it means vector w is perpendicular to the hyperplane.

Problem 3

- Claim 2 :

We have $w_t \Rightarrow w_{t-1} + x_{t-1}y_{t-1}$

Therefor, $w_t \cdot w^* = (w_{t-1} + x_{t-1}y_{t-1})w^* = w_{t-1}w^* + y_{t-1}x_{t-1}w^*$.

We know that $y_i w^* x_i \geq \gamma$, then we know $w_t w^* = w_{t-1} w^* + y_{t-1} x_{t-1} w^* \geq w_{t-1} w^* + \gamma$.

Thus, we know $w_t w^* \geq \gamma + w_{t-1} w^*$;

Similarly, we know $w_{t-1} w^* \geq \gamma + w_{t-2} w^*$

By substituting them iteratively, we will have $w_t \cdot w^* \geq M_t \gamma$

Claim 2 proof done.

- Claim 3:

Given Claim2 & Claim3, we have:

$$\|w_t\|^2 \leq M_t R^2$$

$$w_t \cdot w^* \geq M_t \gamma$$

For second claim:

$$w_t \cdot w^* \geq M_t \gamma \Rightarrow \|w_t\| \|w^*\| \cos \theta \geq M_t \gamma$$

Since we know by defination, $\|W^*\| = 1$,

$$w_t \cdot w^* \geq M_t \gamma \Rightarrow \|w_t\| \cos \theta \geq M_t \gamma \Rightarrow \|w_t\|^2 \cos^2 \theta \geq M_t^2 \gamma^2$$

We know that $\|w_t\|^2 \geq \|w_t\|^2 \cos^2 \theta$,

$$M_t R^2 \geq M_t^2 \gamma^2 \Rightarrow M_t \leq \frac{R^2}{\gamma^2}$$

Problem 4

By calculation, we know the R^2 for $X = 26$ is 1114. Also, we know the $M_t = 430$.

Therefore, we get $\gamma^2 \leq \frac{R^2}{M_t} \Rightarrow 0 \leq \gamma \leq 1.61$