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Multimodal Multi-objective Optimization: Comparative Study of the State-of-the-Art Supplementary Material

I. OVERVIEW

This is the supplementary material for Multimodal Multi-objective Optimization: Comparative Study of the State-of-the-Art. In this document, the detailed results (average values and variance of IGDX, IGD and RPSP) of the compared MMEAs on various MMOP test suites are given. In addition, some of the obtained PSs of all MMEAs are presented.

II. RESULTS

To comprehensively compared the performances of MMEAs, four groups of MMOP test problems are adopted. It's worth mentioning that, all experiments are independently executed 30 times and the average results are used to present and analyze.

III. PERFORMANCE COMPARISON ON CEC 2020 TEST PROBLEMS

Fig. 1 shows the Friedman ranking critical differences of all compared MMEAs on part of the CEC 2020 test suite. In particular, if the distance of ranks of two MMEAs is less than the critical distance, it means that there is no significant difference of these two algorithms in terms of the Friedman ranks. Fig. 2 and Fig. 3 present the solutions distribution on MMF1 and MMF3 respectively.

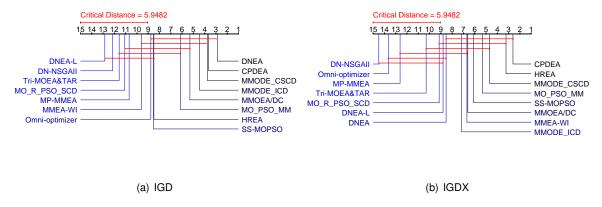


Fig. 1. The critical difference of all compared MMEAs on part of the CEC 2020 test suite, where the red lines indicate that there is no significant difference in the Friedman ranks of the two MMEAs.

IV. PERFORMANCE COMPARISON ON IDMP PROBLEMS

TABLE I
AVERAGE AND VARIANCE OF IGD RESULTS OF THE COMPARED ALGORITHMS ON PART OF THE CEC 2020 MULTIMODAL TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
MMF1	3.88E-03	4.65E-03	3.73E-03	2.68E-03	2.61E-03	4.61E-03	3.97E-03	2.60E-03	3.25E-03	2.53E-03	3.75E-03	3.48E-03	3.07E-03	3.85E-03	3.70E-03
	5.30E-04	8.90E-04	2.05E-04	9.78E-05	1.42E-04	6.12E-04	3.42E-04	1.03E-04	2.58E-04	1.02E-04	2.50E-04	1.38E-04	1.79E-04	2.23E-04	1.99E-04
MMF2	2.90E-02	2.94E-02	2.06E-02	1.54E-02	2.03E-02	3.39E-02	1.81E-02	1.23E-02	1.48E-02	7.39E-03	2.80E-02	9.73E-03	1.33E-02	1.59E-02	1.81E-02
	2.30E-02	2.28E-02	4.27E-03	2.74E-03	8.31E-03	5.88E-02	3.68E-03	2.52E-03	2.21E-03	1.02E-03	1.35E-02	1.67E-03	1.81E-03	1.37E-02	7.64E-03
MMF3	1.74E-02	2.23E-02	1.69E-02	1.35E-02	1.73E-02	2.25E-02	1.83E-02	1.22E-02	1.28E-02	6.02E-03	2.36E-02	9.67E-03	1.19E-02	1.12E-02	1.69E-02
MINIT 5	1.38E-02	1.32E-02	3.54E-03	2.34E-03	5.44E-03	1.24E-02	3.83E-03	1.70E-03	1.67E-03	6.66E-04	8.29E-03	2.34E-03	1.55E-03	1.79E-03	4.16E-03
MMF4	2.86E-03	3.14E-03	3.59E-03	2.66E-03	2.32E-03	3.31E-02	4.55E-03	2.56E-03	3.46E-03	2.41E-03	5.55E-03	2.97E-03	2.41E-03	3.75E-03	3.31E-03
	2.71E-04	1.90E-04	2.89E-04	1.62E-04	1.54E-04	6.82E-02	3.29E-04	1.72E-04	3.87E-04	1.60E-04	9.39E-04	5.95E-04	1.70E-04	2.81E-04	2.45E-04
MMF5	3.38E-03	3.92E-03	3.68E-03	2.73E-03	2.57E-03	4.68E-03	4.66E-03	2.62E-03	3.09E-03	2.54E-03	3.72E-03	3.61E-03	3.27E-03	3.62E-03	3.58E-03
	5.48E-04	7.25E-04	1.43E-04	8.60E-05	1.14E-04	1.49E-03	3.16E-04	7.46E-05	1.91E-04	8.11E-05	1.85E-04	1.60E-04	2.10E-04	2.00E-04	2.67E-04
MMF6	3.11E-03	3.80E-03	3.57E-03	2.58E-03	2.40E-03	3.79E-03	4.60E-03	2.57E-03	3.24E-03	2.44E-03	3.44E-03	3.51E-03	2.82E-03	3.75E-03	3.59E-03
	1.81E-04	5.49E-04	1.90E-04	7.84E-05	6.50E-05	6.46E-04	2.80E-04	8.82E-05	3.37E-04	6.27E-05	1.39E-04	1.08E-04	1.32E-04	2.81E-04	1.91E-04
MMF7	3.17E-03	3.89E-03	3.81E-03	2.62E-03	2.38E-03	4.30E-03	4.11E-03	2.55E-03	4.85E-03	2.43E-03	3.65E-03	3.57E-03	2.47E-03	3.96E-03	3.72E-03
	3.37E-04	2.95E-04	2.38E-04	7.17E-05	1.14E-04	1.29E-03	2.49E-04	6.68E-05	3.68E-03	5.81E-05	2.06E-04	4.95E-04	1.18E-04	2.01E-04	1.99E-04
MMF8	3.26E-03	4.06E-03	4.77E-03	3.66E-03	2.63E-03	3.45E-03	5.26E-03	3.13E-03	3.28E-03	3.75E-03	5.63E-03	2.82E-03	2.74E-03	3.82E-03	3.93E-03
	2.44E-04	5.50E-04	3.04E-04	2.37E-04	7.58E-05	7.55E-05	5.03E-04	1.31E-04	1.79E-04	2.96E-04	1.48E-03	3.56E-04	2.18E-04	2.92E-04	2.05E-04
MMF9	1.30E-02	1.41E-02	1.56E-02	1.25E-02	6.29E-03	6.84E-02	1.52E-02	6.72E-03	2.51E-02	1.03E-02	1.05E-02	7.02E-03	1.26E-02	1.05E-02	1.95E-02
	1.41E-03	1.46E-03	1.24E-03	7.79E-04	5.02E-04	4.85E-03	1.29E-03	3.50E-04	5.52E-03	6.99E-04	7.20E-04	4.27E-04	1.14E-03	1.06E-03	4.98E-03
MMF14	9.76E-02	1.11E-01	8.08E-02	7.86E-02	6.02E-02	8.66E-02	9.19E-02	5.75E-02	8.85E-02	7.29E-02	8.70E-02	6.64E-02	6.99E-02	6.94E-02	6.59E-02
	4.42E-03	9.91E-03	2.62E-03	2.15E-03	1.64E-03	1.11E-03	3.56E-03	9.41E-04	4.07E-03	1.59E-03	6.64E-03	1.26E-03	1.63E-03	1.13E-03	1.11E-03
MMF1 e	2.40E-02	2.45E-02	1.18E-02	8.99E-03	4.43E-03	1.92E-02	8.84E-03	1.06E-02	9.55E-03	1.35E-02	7.03E-03	5.82E-03	8.59E-03	2.26E-02	9.19E-03
	3.08E-02	1.62E-02	1.17E-03	1.05E-03	1.06E-03	3.53E-02	2.22E-03	1.31E-03	1.32E-03	2.02E-03	1.23E-03	9.21E-04	2.87E-03	9.12E-03	1.97E-03
MMF1 z	3.07E-03	3.46E-03	3.61E-03	2.61E-03	2.46E-03	4.39E-03	3.93E-03	2.61E-03	3.10E-03	2.46E-03	3.51E-03	3.30E-03	2.55E-03	3.76E-03	3.30E-03
	3.34E-04	3.03E-04	1.74E-04	8.43E-05	1.23E-04	7.10E-04	3.01E-04	9.03E-05	1.93E-04	7.44E-05	1.58E-04	3.46E-04	1.28E-04	2.73E-04	1.28E-04
MMF14 a	1.05E-01	1.21E-01	7.88E-02	7.45E-02	5.92E-02	7.92E-02	1.06E-01	5.92E-02	7.76E-02	7.23E-02	1.01E-01	6.74E-02	7.26E-02	7.43E-02	6.87E-02
	5.18E-03	5.44E-03	2.12E-03	1.74E-03	1.46E-03	1.58E-03	4.01E-03	9.18E-04	2.21E-03	1.53E-03	9.99E-03	2.06E-03	1.80E-03	1.62E-03	1.20E-03

TABLE II

AVERAGE AND VARIANCE OF IGDX RESULTS OF THE COMPARED ALGORITHMS ON PART OF THE CEC 2020 multimodal test suite, where the Best mean for each test instance is highlighted.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
MMF1	9.56E-02	9.68E-02	4.81E-02	4.01E-02	4.97E-02	7.27E-02	4.56E-02	3.72E-02	4.10E-02	4.24E-02	6.62E-02	4.48E-02	5.51E-02	4.45E-02	3.88E-02
	1.70E-02	1.48E-02	2.06E-03	1.34E-03	7.26E-03	1.03E-02	2.43E-03	1.05E-03	1.53E-03	1.58E-03	1.16E-02	1.37E-03	4.05E-03	2.09E-03	1.90E-03
MMF2	1.27E-01	1.33E-01	3.98E-02	2.86E-02	7.03E-02	7.21E-02	3.44E-02	2.82E-02	2.97E-02	2.00E-02	6.21E-02	1.70E-02	1.94E-02	3.90E-02	4.04E-02
	7.72E-02	7.03E-02	1.38E-02	6.95E-03	3.56E-02	4.53E-02	7.94E-03	4.61E-03	1.03E-02	1.02E-02	2.35E-02	4.40E-03	3.19E-03	1.61E-02	1.22E-02
MMF3	9.60E-02	1.04E-01	4.79E-02	4.23E-02	8.83E-02	8.17E-02	4.18E-02	4.51E-02	4.13E-02	4.02E-02	7.21E-02	3.68E-02	3.93E-02	5.07E-02	5.46E-02
	3.17E-02	3.64E-02	1.10E-02	6.04E-03	2.94E-02	3.29E-02	6.41E-03	4.05E-03	6.31E-03	7.25E-03	2.12E-02	7.40E-03	3.51E-03	9.45E-03	9.59E-03
MMF4	7.84E-02	8.58E-02	2.77E-02	2.35E-02	2.23E-02	9.74E-02	3.10E-02	1.95E-02	2.47E-02	2.21E-02	8.15E-02	2.65E-02	2.40E-02	2.52E-02	1.91E-02
	1.60E-02	1.87E-02	1.71E-03	1.25E-03	3.62E-03	1.45E-01	2.16E-03	5.12E-04	2.00E-03	8.59E-04	2.30E-02	3.07E-03	1.88E-03	1.76E-03	7.48E-04
MMF5	1.69E-01	1.77E-01	8.44E-02	7.34E-02	8.55E-02	1.17E-01	8.30E-02	6.48E-02	7.40E-02	7.29E-02	1.18E-01	7.84E-02	9.98E-02	7.47E-02	6.38E-02
	2.02E-02	2.55E-02	4.59E-03	3.60E-03	7.12E-03	1.50E-02	4.75E-03	1.83E-03	3.05E-03	3.04E-03	1.12E-02	3.08E-03	8.10E-03	3.86E-03	2.75E-03
MMF6	1.42E-01	1.43E-01	7.27E-02	6.34E-02	7.08E-02	9.24E-02	7.31E-02	5.74E-02	6.56E-02	6.40E-02	1.08E-01	6.75E-02	7.75E-02	6.78E-02	5.45E-02
	1.78E-02	1.44E-02	3.50E-03	2.79E-03	8.37E-03	9.09E-03	3.61E-03	1.53E-03	2.77E-03	3.02E-03	1.40E-02	2.19E-03	4.06E-03	3.65E-03	1.42E-03
MMF7	4.93E-02	5.14E-02	2.65E-02	2.12E-02	2.40E-02	4.71E-02	2.69E-02	1.95E-02	2.44E-02	2.29E-02	4.21E-02	2.80E-02	2.28E-02	2.49E-02	1.96E-02
	9.40E-03	1.07E-02	1.82E-03	8.65E-04	3.78E-03	2.06E-02	2.29E-03	9.21E-04	1.92E-03	2.15E-03	8.90E-03	2.36E-03	3.15E-03	2.27E-03	9.46E-04
MMF8	3.24E-01	2.92E-01	6.62E-02	5.39E-02	1.54E-01	3.56E-01	9.30E-02	5.23E-02	5.59E-02	5.43E-02	3.90E-01	6.52E-02	1.28E-01	8.09E-02	4.97E-02
	1.37E-01	9.83E-02	5.22E-03	3.63E-03	4.77E-02	9.75E-02	1.94E-02	4.54E-03	5.53E-03	6.52E-03	1.83E-01	1.16E-02	3.56E-02	1.62E-02	6.73E-03
MMF9	2.10E-02	2.31E-02	8.02E-03	5.93E-03	4.92E-03	3.02E-03	9.24E-03	4.73E-03	7.06E-03	5.87E-03	8.25E-03	4.93E-03	4.83E-03	4.55E-03	6.09E-03
	5.20E-03	9.68E-03	5.53E-04	2.99E-04	4.09E-04	8.66E-05	8.51E-04	1.90E-04	4.95E-04	3.59E-04	3.36E-03	1.88E-04	3.41E-04	1.38E-04	9.44E-04
MMF14	8.94E-02	9.68E-02	5.37E-02	5.37E-02	4.53E-02	3.65E-02	6.23E-02	3.96E-02	5.74E-02	5.10E-02	6.42E-02	5.14E-02	4.22E-02	4.17E-02	3.77E-02
	5.34E-03	7.16E-03	1.46E-03	1.27E-03	1.22E-03	4.77E-04	2.51E-03	5.61E-04	2.64E-03	1.47E-03	7.33E-03	1.10E-03	7.89E-04	6.92E-04	4.34E-04
MMF1 e	1.44E+00	1.37E+00	5.22E-01	4.65E-01	1.83E+00	1.55E+00	3.32E-01	3.28E-01	3.93E-01	5.57E-01	2.23E+00	5.08E-01	1.20E+00	7.15E-01	3.08E-01
	7.13E-01	6.59E-01	2.38E-01	1.39E-01	6.83E-01	5.24E-01	6.66E-02	3.47E-02	9.93E-02	4.37E-01	6.70E-01	1.98E-01	4.99E-01	2.01E-01	2.79E-02
MMF1_z	7.12E-02	9.13E-02	3.50E-02	2.87E-02	3.87E-02	7.38E-02	3.44E-02	2.73E-02	3.05E-02	2.94E-02	6.01E-02	3.12E-02	4.96E-02	3.26E-02	2.70E-02
	1.37E-02	4.11E-02	2.14E-03	9.80E-04	6.42E-03	1.21E-02	1.78E-03	1.03E-03	1.54E-03	1.18E-03	1.15E-02	1.67E-03	7.53E-03	2.86E-03	1.61E-03
MMF14 a	1.11E-01	1.20E-01	6.07E-02	6.02E-02	5.46E-02	5.71E-02	8.80E-02	5.09E-02	6.02E-02	6.07E-02	9.85E-02	7.74E-02	5.84E-02	5.68E-02	4.71E-02
	7.57E-03	8.81E-03	1.89E-03	1.35E-03	1.43E-03	2.02E-03	3.39E-03	5.10E-04	1.31E-03	1.42E-03	8.05E-03	3.42E-03	1.68E-03	1.23E-03	5.52E-04

TABLE III

AVERAGE AND VARIANCE OF RPSP RESULTS OF THE COMPARED ALGORITHMS ON PART OF THE CEC 2020 MULTIMODAL TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
MMF1	9.82E-02	9.86E-02	4.85E-02	4.04E-02	5.02E-02	7.42E-02	4.57E-02	3.73E-02	4.13E-02	4.27E-02	6.66E-02	4.49E-02	5.53E-02	4.46E-02	3.89E-02
	1.95E-02	1.52E-02	2.16E-03	1.39E-03	8.05E-03	1.12E-02	2.47E-03	1.06E-03	1.63E-03	1.61E-03	1.21E-02	1.42E-03	4.13E-03	2.13E-03	1.98E-03
MMF2	1.57E-01	1.63E-01	4.26E-02	3.00E-02	7.68E-02	8.32E-02	3.54E-02	2.82E-02	3.14E-02	2.00E-02	6.66E-02	1.71E-02	1.94E-02	4.10E-02	4.23E-02
	1.29E-01	1.11E-01	1.56E-02	7.55E-03	4.32E-02	6.89E-02	8.78E-03	4.62E-03	1.14E-02	1.02E-02	2.96E-02	4.39E-03	3.19E-03	2.22E-02	1.48E-02
MMF3	1.04E-01	1.15E-01	5.04E-02	4.39E-02	9.35E-02	9.11E-02	4.29E-02	4.52E-02	4.30E-02	4.02E-02	7.61E-02	3.71E-02	3.93E-02	5.15E-02	5.69E-02
	3.74E-02	4.40E-02	1.17E-02	6.71E-03	3.13E-02	4.48E-02	7.05E-03	4.07E-03	6.80E-03	7.25E-03	2.52E-02	7.64E-03	3.51E-03	9.53E-03	1.14E-02
MMF4	7.90E-02	8.63E-02	2.80E-02	2.37E-02	2.23E-02	1.26E-01	3.11E-02	1.96E-02	2.48E-02	2.22E-02	8.20E-02	2.66E-02	2.41E-02	2.52E-02	1.91E-02
	1.63E-02	1.87E-02	1.78E-03	1.27E-03	3.62E-03	2.11E-01	2.19E-03	5.14E-04	2.02E-03	8.70E-04	2.34E-02	3.08E-03	1.88E-03	1.77E-03	7.50E-04
MMF5	1.73E-01	1.81E-01	8.50E-02	7.37E-02	8.62E-02	1.20E-01	8.33E-02	6.49E-02	7.45E-02	7.34E-02	1.18E-01	7.87E-02	1.00E-01	7.49E-02	6.40E-02
	2.19E-02	2.61E-02	4.65E-03	3.68E-03	7.34E-03	1.71E-02	4.95E-03	1.82E-03	3.14E-03	3.15E-03	1.14E-02	3.17E-03	8.11E-03	3.88E-03	2.81E-03
MMF6	1.45E-01	1.46E-01	7.33E-02	6.38E-02	7.12E-02	9.40E-02	7.34E-02	5.75E-02	6.60E-02	6.44E-02	1.09E-01	6.78E-02	7.78E-02	6.80E-02	5.46E-02
	1.91E-02	1.52E-02	3.56E-03	2.83E-03	8.46E-03	9.26E-03	3.66E-03	1.54E-03	2.78E-03	3.09E-03	1.47E-02	2.21E-03	3.92E-03	3.66E-03	1.41E-03
MMF7	5.15E-02	5.32E-02	2.67E-02	2.13E-02	2.44E-02	6.35E-02	2.72E-02	1.95E-02	2.45E-02	2.31E-02	4.40E-02	2.81E-02	2.33E-02	2.52E-02	1.96E-02
	1.10E-02	1.38E-02	1.90E-03	8.90E-04	3.98E-03	4.88E-02	2.38E-03	9.15E-04	1.93E-03	2.21E-03	9.10E-03	2.36E-03	3.65E-03	2.31E-03	9.43E-04
MMF8	3.44E-01	3.11E-01	6.68E-02	5.45E-02	1.63E-01	4.03E-01	9.54E-02	5.26E-02	5.63E-02	5.53E-02	4.00E-01	6.62E-02	1.35E-01	8.11E-02	5.00E-02
	1.52E-01	1.19E-01	5.28E-03	3.94E-03	5.22E-02	1.21E-01	2.04E-02	4.60E-03	5.55E-03	6.88E-03	1.97E-01	1.21E-02	3.99E-02	1.62E-02	6.99E-03
MMF9	2.10E-02	2.31E-02	8.03E-03	5.93E-03	4.92E-03	3.02E-03	9.25E-03	4.73E-03	7.07E-03	5.88E-03	8.25E-03	4.93E-03	4.83E-03	4.55E-03	6.09E-03
	5.20E-03	9.68E-03	5.55E-04	2.99E-04	4.09E-04	8.68E-05	8.47E-04	1.90E-04	4.98E-04	3.59E-04	3.36E-03	1.88E-04	3.42E-04	1.38E-04	9.43E-04
MMF14	8.94E-02	9.68E-02	5.37E-02	5.37E-02	4.54E-02	3.65E-02	6.24E-02	3.96E-02	5.74E-02	5.10E-02	6.42E-02	5.14E-02	4.22E-02	4.17E-02	3.77E-02
	5.34E-03	7.16E-03	1.46E-03	1.27E-03	1.23E-03	4.77E-04	2.60E-03	5.61E-04	2.64E-03	1.47E-03	7.33E-03	1.09E-03	7.89E-04	6.92E-04	4.34E-04
MMF1 e	2.50E+00	2.46E+00	6.18E-01	5.36E-01	3.93E+00	2.64E+00	3.58E-01	3.35E-01	4.41E-01	7.10E-01	5.85E+00	6.02E-01	1.78E+00	9.93E-01	3.26E-01
	1.69E+00	2.19E+00	3.60E-01	2.08E-01	2.72E+00	1.33E+00	8.34E-02	3.76E-02	1.46E-01	7.04E-01	3.01E+00	3.02E-01	1.07E+00	3.96E-01	3.93E-02
MMF1 z	7.26E-02	9.41E-02	3.52E-02	2.89E-02	3.89E-02	7.51E-02	3.45E-02	2.73E-02	3.07E-02	2.96E-02	6.01E-02	3.13E-02	4.98E-02	3.27E-02	2.70E-02
	1.45E-02	4.41E-02	2.21E-03	1.04E-03	6.61E-03	1.24E-02	1.79E-03	1.03E-03	1.59E-03	1.21E-03	1.15E-02	1.69E-03	7.69E-03	2.92E-03	1.63E-03
MMF14 a	1.11E-01	1.20E-01	6.08E-02	6.03E-02	5.46E-02	5.71E-02	8.80E-02	5.09E-02	6.03E-02	6.07E-02	9.85E-02	7.74E-02	5.84E-02	5.68E-02	4.71E-02
711711 17_a	7.56E-03	8.81E-03	1.89E-03	1.34E-03	1.43E-03	2.02E-03	3.39E-03	5.10E-04	1.32E-03	1.42E-03	8.05E-03	3.40E-03	1.68E-03	1.23E-03	5.52E-04

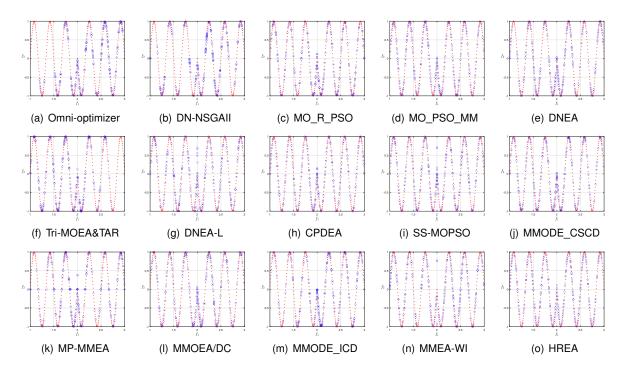


Fig. 2. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the decision spaces on MMF1, where the red points and blue circles are true PS and obtained solutions respectively.

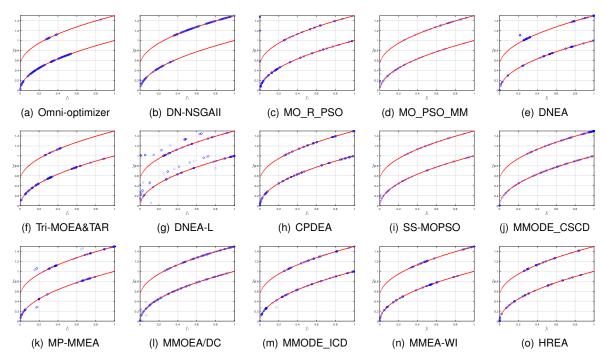


Fig. 3. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the decision spaces on MMF3, where the red points and blue circles are true PS and obtained solutions respectively.

TABLE IV

AVERAGE AND VARIANCE OF IGD RESULTS OF THE COMPARED ALGORITHMS ON IDMP TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
IDMPM2T1	6.73E-04	6.20E-04	3.07E-03	2.75E-03	3.91E-04	6.38E-04	7.85E-04	7.47E-04	2.39E-03	5.47E-04	8.09E-04	9.27E-04	4.68E-04	7.61E-04	5.83E-04
10.011.01211	1.37E-04	6.67E-05	2.36E-04	5.04E-04	2.21E-05	1.55E-05	1.61E-04	1.62E-04	1.98E-04	1.85E-05	1.23E-04	1.73E-04	2.79E-05	6.02E-05	1.12E-04
IDMPM2T2	5.63E-04	5.86E-04	1.52E-03	1.60E-03	4.02E-04	6.39E-04	6.23E-04	5.49E-04	1.26E-03	4.86E-04	5.80E-04	5.93E-04	4.63E-04	6.83E-04	5.36E-04
10.011.01212	5.22E-05	6.60E-05	1.45E-04	3.37E-04	1.66E-05	3.31E-05	1.55E-04	7.02E-05	1.40E-04	2.16E-05	4.15E-05	7.59E-05	1.45E-05	3.36E-05	2.45E-05
IDMPM2T3	5.70E-04	5.87E-04	1.66E-03	2.01E-03	4.25E-04	6.94E-03	6.16E-04	6.82E-04	1.20E-03	4.75E-04	6.01E-04	8.06E-04	4.60E-04	8.05E-04	5.42E-04
10.011.01213	4.15E-05	3.87E-05	1.83E-04	4.42E-04	2.15E-05	1.97E-02	8.77E-05	6.93E-05	9.87E-05	1.62E-05	6.09E-05	1.05E-04	1.72E-05	7.75E-05	2.59E-05
IDMPM2T4	1.04E-03	1.99E-03	3.42E-03	2.15E-03	3.84E-04	6.43E-04	5.30E-04	6.19E-04	3.24E-03	4.99E-04	6.26E-04	7.43E-04	4.74E-04	7.33E-04	5.07E-04
10.011.01214	8.70E-04	3.18E-03	7.52E-04	4.55E-04	2.91E-05	1.34E-05	1.90E-04	1.47E-04	6.59E-04	1.93E-05	8.76E-05	1.73E-04	3.57E-05	7.59E-05	9.27E-05
IDMPM3T1	6.64E-03	7.43E-03	1.33E-02	1.24E-02	3.92E-03	9.61E-03	5.70E-03	4.72E-03	1.07E-02	5.21E-03	5.91E-03	6.71E-03	4.50E-03	5.10E-03	4.99E-03
10.011	5.06E-04	1.47E-03	8.88E-04	1.06E-03	1.67E-04	5.04E-04	4.16E-04	2.48E-04	3.59E-04	3.00E-04	3.83E-04	5.23E-04	1.20E-04	1.63E-04	2.08E-04
IDMPM3T2	6.93E-03	8.00E-03	1.11E-02	1.08E-02	3.80E-03	9.60E-03	5.11E-03	4.34E-03	1.08E-02	4.69E-03	5.43E-03	5.62E-03	4.50E-03	4.97E-03	4.57E-03
10.011.012	1.10E-03	2.57E-03	1.18E-03	1.50E-03	8.66E-05	6.04E-04	4.08E-04	1.30E-04	9.32E-04	1.11E-04	2.46E-04	2.47E-04	1.35E-04	1.66E-04	1.17E-04
IDMPM3T3	5.99E-03	6.41E-03	1.05E-02	1.06E-02	3.93E-03	1.00E-02	5.34E-03	4.55E-03	9.46E-03	4.80E-03	5.40E-03	6.41E-03	4.61E-03	5.15E-03	4.62E-03
IDMI MOIO	6.00E-04	1.35E-03	9.43E-04	1.17E-03	1.28E-04	4.84E-03	3.37E-04	1.41E-04	8.28E-04	1.28E-04	2.84E-04	5.54E-04	1.97E-04	1.19E-04	1.51E-04
IDMPM3T4	1.60E-02	1.86E-02	2.10E-02	1.71E-02	3.71E-03	9.69E-03	4.73E-03	4.46E-03	2.56E-02	4.69E-03	5.47E-03	6.23E-03	4.52E-03	5.04E-03	4.52E-03
10.011.01314	1.53E-02	1.26E-02	4.55E-03	2.21E-03	8.39E-05	6.24E-04	6.00E-04	3.85E-04	8.22E-03	1.08E-04	3.99E-04	7.91E-04	2.75E-04	2.93E-04	2.09E-04
IDMPM4T1	1.73E-02	1.82E-02	3.46E-02	4.41E-02	4.96E-03	2.08E-02	5.58E-03	6.25E-03	3.88E-02	7.85E-03	8.78E-03	1.83E-02	6.09E-03	8.39E-03	9.13E-03
10.011.01411	6.89E-03	5.55E-03	3.10E-03	5.83E-03	2.30E-04	1.33E-03	4.30E-04	5.64E-04	4.39E-03	3.59E-04	7.89E-04	1.98E-03	4.47E-04	8.08E-04	1.66E-03
IDMPM4T2	1.84E-02	3.13E-02	3.20E-02	4.93E-02	4.70E-03	2.16E-02	5.41E-03	5.52E-03	4.57E-02	6.51E-03	7.27E-03	1.58E-02	7.10E-03	7.04E-03	6.57E-03
IDMI M412	6.57E-03	2.66E-02	6.18E-03	1.20E-02	1.88E-04	2.47E-03	5.30E-04	4.68E-04	1.38E-02	1.41E-04	3.01E-04	1.82E-03	1.57E-03	7.57E-04	1.31E-03
IDMPM4T3	1.14E-02	1.43E-02	3.17E-02	4.80E-02	5.03E-03	2.05E-02	5.79E-03	5.88E-03	3.80E-02	6.75E-03	7.64E-03	1.61E-02	7.39E-03	6.98E-03	6.29E-03
22/11/11/13	3.38E-03	5.11E-03	5.62E-03	8.26E-03	3.08E-04	1.33E-02	6.03E-04	3.79E-04	9.34E-03	4.51E-04	6.49E-04	1.50E-03	2.58E-03	4.08E-04	8.44E-04
IDMPM4T4	7.13E-02	1.16E-01	6.72E-02	1.02E-01	4.72E-03	2.06E-02	5.54E-03	5.61E-03	1.31E-01	6.53E-03	7.68E-03	1.87E-02	1.04E-02	6.88E-03	7.59E-03
10.011 101414	6.28E-02	1.10E-01	1.73E-02	4.23E-02	2.00E-04	2.20E-03	5.96E-04	8.81E-04	8.06E-02	1.88E-04	6.44E-04	2.88E-03	5.25E-03	1.03E-03	2.12E-03

 $TABLE\ V$ Average and variance of IGDX results of the compared algorithms on IDMP test suite, where the best mean for each test instance is highlighted.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
IDMPM2T1	3.88E-01	2.84E-01	5.90E-02	5.19E-03	6.07E-01	6.30E-01	1.62E-03	1.03E-03	4.13E-03	2.25E-01	2.37E-01	8.76E-04	5.38E-02	9.32E-04	2.42E-03
IDMI MZ11	3.31E-01	3.24E-01	1.67E-01	1.79E-03	2.03E-01	1.63E-01	2.30E-03	5.41E-04	2.71E-03	3.22E-01	1.62E-01	1.15E-04	1.69E-01	7.13E-05	6.29E-03
IDMPM2T2	2.99E-01	2.99E-01	5.58E-03	3.88E-03	4.95E-01	5.39E-01	1.97E-03	9.55E-04	2.88E-03	2.70E-01	1.67E-01	1.03E-03	3.35E-03	1.12E-03	9.45E-04
IDMI MIZIZ	3.33E-01	3.34E-01	2.91E-03	1.95E-03	3.01E-01	2.72E-01	1.35E-03	1.33E-04	4.56E-04	3.35E-01	1.73E-01	1.14E-04	5.67E-03	8.61E-05	5.88E-04
IDMPM2T3	1.19E-01	1.19E-01	3.35E-03	5.87E-03	1.42E-01	1.98E-01	2.90E-03	3.70E-03	2.81E-03	2.67E-03	1.30E-01	1.85E-03	2.64E-03	1.99E-03	2.96E-03
IDMI MZ13	2.57E-01	2.55E-01	4.22E-04	4.03E-03	2.71E-01	2.92E-01	1.58E-03	1.47E-03	4.14E-04	5.63E-03	1.65E-01	1.92E-04	1.47E-03	2.49E-04	1.36E-03
IDMPM2T4	5.44E-01	6.10E-01	8.67E-02	3.89E-03	6.28E-01	5.63E-01	1.32E-02	2.32E-02	1.26E-02	5.61E-01	2.89E-01	9.06E-02	7.65E-02	4.58E-02	1.04E-02
IDMIT MIZ 14	2.63E-01	1.94E-01	2.00E-01	1.61E-03	1.71E-01	2.50E-01	2.15E-02	1.23E-01	9.38E-03	2.55E-01	1.47E-01	2.32E-01	2.03E-01	1.71E-01	1.41E-02
IDMPM3T1	3.50E-01	3.49E-01	1.19E-01	3.88E-02	5.74E-01	7.50E-01	3.48E-02	1.53E-02	1.63E-02	2.60E-01	3.31E-01	8.41E-03	3.02E-01	7.48E-03	6.51E-03
IDMIT MIST I	2.30E-01	2.42E-01	1.47E-01	6.41E-02	3.05E-01	2.63E-01	7.39E-02	4.42E-02	1.68E-03	2.06E-01	1.10E-01	3.97E-04	1.88E-01	1.78E-04	2.16E-04
IDMPM3T2	6.00E-01	6.14E-01	1.45E-01	6.66E-02	4.55E-01	5.61E-01	3.69E-02	7.23E-03	3.06E-02	4.12E-01	2.58E-01	8.17E-03	2.63E-01	7.69E-03	6.65E-03
IDMIT MIST 2	2.29E-01	2.90E-01	1.25E-01	1.29E-01	2.20E-01	2.44E-01	7.35E-02	2.56E-04	4.38E-02	2.11E-01	1.64E-01	2.71E-04	1.41E-01	2.01E-04	6.23E-04
IDMPM3T3	3.71E-01	4.75E-01	2.65E-02	2.05E-02	2.87E-01	3.42E-01	3.87E-02	2.65E-02	1.71E-02	8.02E-02	3.60E-01	1.01E-02	2.37E-01	2.55E-02	9.14E-03
IDMI M313	2.03E-01	2.32E-01	4.34E-02	3.52E-03	2.10E-01	2.57E-01	7.37E-02	6.09E-02	2.06E-03	1.46E-01	1.38E-01	6.01E-04	1.92E-01	6.29E-02	1.56E-03
IDMPM3T4	8.24E-01	8.13E-01	2.64E-01	1.21E-01	7.03E-01	6.86E-01	8.36E-02	5.71E-02	3.60E-01	7.40E-01	4.02E-01	1.84E-02	2.50E-01	1.54E-01	1.07E-02
IDMI MS14	2.16E-01	2.27E-01	1.82E-01	1.47E-01	2.37E-01	2.58E-01	1.08E-01	9.87E-02	2.29E-01	2.54E-01	1.70E-01	3.13E-02	1.66E-01	1.52E-01	5.48E-03
IDMPM4T1	7.94E-01	6.36E-01	9.36E-01	5.15E-01	1.17E+00	1.18E+00	1.09E-01	7.03E-01	2.32E-01	8.58E-01	5.81E-01	4.44E-02	7.54E-01	2.68E-02	6.00E-02
IDMIT MI411	3.07E-01	3.33E-01	2.75E-01	2.93E-01	8.28E-02	8.14E-02	1.50E-01	2.89E-01	2.18E-01	3.23E-01	1.72E-01	7.50E-02	2.04E-01	6.77E-02	8.70E-02
IDMPM4T2	9.72E-01	9.24E-01	5.59E-01	5.25E-01	9.95E-01	1.11E+00	2.99E-01	5.47E-01	6.35E-01	8.83E-01	5.73E-01	2.62E-02	5.00E-01	3.62E-01	4.48E-01
IDMIT WI412	2.28E-01	2.37E-01	2.64E-01	3.07E-01	2.34E-01	1.80E-01	2.46E-01	2.36E-01	2.80E-01	2.35E-01	1.27E-01	5.25E-02	1.97E-01	2.81E-01	3.20E-01
IDMPM4T3	7.44E-01	7.25E-01	8.04E-02	1.35E-01	7.61E-01	7.70E-01	1.41E-01	4.07E-01	1.68E-01	2.31E-01	4.64E-01	1.66E-02	5.46E-01	4.16E-01	5.16E-01
IDMIT WI413	3.18E-01	3.05E-01	8.42E-02	1.54E-01	2.85E-01	2.94E-01	1.60E-01	2.56E-01	1.62E-01	2.53E-01	1.80E-01	1.33E-03	2.66E-01	2.92E-01	3.36E-01
IDMPM4T4	1.08E+00	1.11E+00	6.86E-01	6.77E-01	1.09E+00	1.06E+00	1.79E-01	7.94E-01	8.83E-01	9.92E-01	4.56E-01	3.87E-02	5.57E-01	7.28E-01	6.12E-01
11/11/1/1414	1.68E-01	1.53E-01	3.44E-01	3.31E-01	1.78E-01	1.87E-01	2.36E-01	3.19E-01	3.27E-01	2.97E-01	1.45E-01	6.08E-02	2.81E-01	3.28E-01	2.77E-01

 $TABLE\ VI \\ AVERAGE\ AND\ VARIANCE\ OF\ RPSP\ RESULTS\ OF\ THE\ COMPARED\ ALGORITHMS\ ON\ IDMP\ TEST\ SUITE,\ WHERE\ THE\ BEST\ MEAN\ FOR\ EACH\ TEST\ INSTANCE\ IS\ HIGHLIGHTED.$

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
IDMPM2T1	3.35E+01	3.03E+01	1.80E+00	5.23E-03	1.19E+02	Inf	1.62E-03	1.03E-03	4.15E-03	2.09E+01	4.41E-01	8.76E-04	1.75E+01	9.33E-04	2.50E-03
IDMI MZ11	3.08E+01	4.13E+01	6.82E+00	1.81E-03	8.63E+01	NaN	2.31E-03	5.42E-04	2.74E-03	3.03E+01	3.31E-01	1.15E-04	7.07E+01	7.15E-05	6.58E-03
IDMPM2T2	1.48E+01	1.45E+01	5.65E-03	3.90E-03	3.11E+01	5.22E+01	1.97E-03	9.56E-04	2.89E-03	1.34E+01	9.23E-01	1.03E-03	3.46E-03	1.12E-03	9.47E-04
IDMI MZ12	1.74E+01	1.70E+01	3.04E-03	1.96E-03	1.94E+01	4.51E+01	1.35E-03	1.33E-04	4.58E-04	1.67E+01	3.55E+00	1.14E-04	6.04E-03	8.64E-05	5.93E-04
IDMPM2T3	3.07E+00	4.27E+00	3.36E-03	5.98E-03	8.61E+00	1.73E+01	2.90E-03	3.74E-03	2.82E-03	2.77E-03	7.96E-01	1.85E-03	2.66E-03	2.00E-03	2.99E-03
10011 01213	9.37E+00	1.17E+01	4.24E-04	4.27E-03	1.75E+01	3.42E+01	1.58E-03	1.51E-03	4.22E-04	6.02E-03	3.26E+00	1.92E-04	1.50E-03	2.50E-04	1.38E-03
IDMPM2T4	4.56E+01	6.07E+01	4.46E+00	3.92E-03	1.01E+02	1.42E+02	1.34E-02	2.23E+00	1.29E-02	5.97E+01	2.91E+00	7.66E+00	5.03E+01	5.28E+00	1.06E-02
10.011.01214	2.45E+01	3.49E+01	1.37E+01	1.63E-03	4.45E+01	1.17E+02	2.17E-02	1.22E+01	9.77E-03	2.75E+01	9.19E+00	1.99E+01	1.57E+02	2.01E+01	1.44E-02
IDMPM3T1	1.18E+00	1.11E+00	1.66E-01	4.07E-02	8.15E+00	1.79E+01	3.73E-02	1.53E-02	1.63E-02	4.75E-01	4.99E-01	8.41E-03	5.63E-01	7.49E-03	6.51E-03
10011 01511	3.52E+00	3.06E+00	3.35E-01	7.12E-02	1.33E+01	2.08E+01	8.17E-02	4.46E-02	1.70E-03	6.10E-01	2.43E-01	3.96E-04	6.36E-01	1.78E-04	2.17E-04
IDMPM3T2	4.69E+00	6.62E+00	1.66E-01	1.10E-01	1.79E+00	4.20E+00	3.95E-02	7.24E-03	3.08E-02	9.63E-01	5.93E-01	8.17E-03	4.40E-01	7.70E-03	6.66E-03
101111111111111111111111111111111111111	7.59E+00	9.10E+00	1.47E-01	3.30E-01	4.34E+00	8.82E+00	8.17E-02	2.57E-04	4.40E-02	7.73E-01	1.56E+00	2.71E-04	4.44E-01	2.00E-04	6.24E-04
IDMPM3T3	9.11E-01	1.64E+00	2.66E-02	2.07E-02	5.64E-01	1.11E+00	4.13E-02	2.67E-02	1.71E-02	1.20E-01	5.55E-01	1.01E-02	4.18E-01	2.69E-02	9.18E-03
10.111.110.10	2.09E+00	2.71E+00	4.35E-02	3.60E-03	6.68E-01	2.31E+00	8.16E-02	6.13E-02	2.08E-03	3.16E-01	3.03E-01	6.00E-04	5.67E-01	6.85E-02	1.58E-03
IDMPM3T4	2.05E+01	1.83E+01	4.09E-01	1.70E-01	1.68E+01	1.85E+01	9.13E-02	5.85E-02	1.40E+00	1.58E+01	9.60E-01	1.89E-02	4.53E-01	1.60E-01	1.07E-02
	1.72E+01	1.54E+01	5.39E-01	3.47E-01	2.26E+01	2.54E+01	1.22E-01	1.02E-01	4.55E+00	1.79E+01	1.80E+00	3.30E-02	4.95E-01	1.65E-01	5.49E-03
IDMPM4T1	1.13E+01	6.83E+00	1.15E+01	2.13E+00	6.83E+01	8.98E+01	1.48E-01	1.49E+01	3.87E-01	2.19E+01	2.90E+00	4.97E-02	1.09E+01	3.09E-02	6.05E-02
	1.29E+01	1.11E+01	9.96E+00	4.47E+00	1.45E+01	2.60E+01	3.32E-01	2.60E+01	5.90E-01	2.37E+01	5.75E+00	8.70E-02	2.31E+01	8.34E-02	8.80E-02
IDMPM4T2	2.31E+01	1.77E+01	3.06E+00	3.48E+00	3.29E+01	5.70E+01	5.39E-01	2.59E+00	4.89E+00	1.71E+01	4.08E+00	2.92E-02	2.52E+00	3.48E+00	5.23E+00
10	1.38E+01	1.55E+01	7.53E+00	7.94E+00	2.42E+01	2.36E+01	6.54E-01	7.79E+00	9.85E+00	2.01E+01	5.16E+00	6.47E-02	7.43E+00	1.13E+01	1.38E+01
IDMPM4T3	9.17E+00	7.23E+00	8.34E-02	1.89E-01	1.36E+01	1.87E+01	1.88E-01	8.90E-01	2.18E-01	8.62E-01	1.53E+00	1.66E-02	4.67E+00	2.86E+00	8.77E+00
1211.11413	1.05E+01	1.06E+01	9.13E-02	3.86E-01	1.88E+01	2.68E+01	3.28E-01	8.50E-01	3.61E-01	2.85E+00	1.95E+00	1.33E-03	8.16E+00	9.75E+00	1.71E+01
IDMPM4T4	Inf	Inf	1.21E+01	1.83E+01	6.68E+01	7.29E+01	2.46E+00	Inf	Inf	4.34E+01	1.92E+00	3.87E-02	1.09E+01	2.48E+01	1.14E+01
1211.11414	NaN	NaN	1.94E+01	3.96E+01	2.93E+01	3.53E+01	1.24E+01	NaN	NaN	3.02E+01	4.25E+00	6.08E-02	2.30E+01	3.60E+01	2.35E+01

The final distribution of solutions in the decision space are presented in Fig. 5 and Fig. 6.

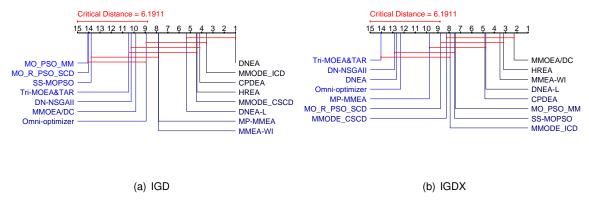


Fig. 4. The critical difference of all compared MMEAs on IDMP test suite, where the red lines indicate that there is no significant difference in the Friedman ranks of the two MMEAs.

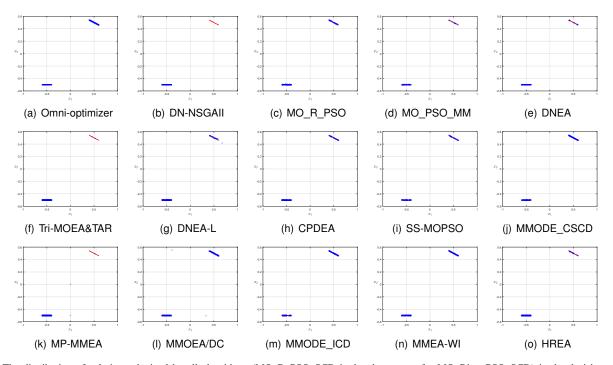


Fig. 5. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the decision spaces on IDMPM2T3, where the red points and blue circles are true PS and obtained solutions respectively.

V. PERFORMANCE COMPARISON ON PROBLEMS WITH LOCAL PFS

In this part, the performance of MMEAs on MMOPLs is discussed. Since there is no performance indicator designed for MMOPLs, we regard both global and local PSs as the true PS for calculating IGD, IGDX and RPSP.

VI. PERFORMANCE COMPARISON ON MULTI-POLYGON PROBLEMS

To study the performance of MMEAs on problems with many objectives and many decision variables, Multi-polygon problems are chosen as the benchmark, where M is set to 3, 4, 6, 8 and D is set to 2, 4, 8, 10 ,20 respectively.

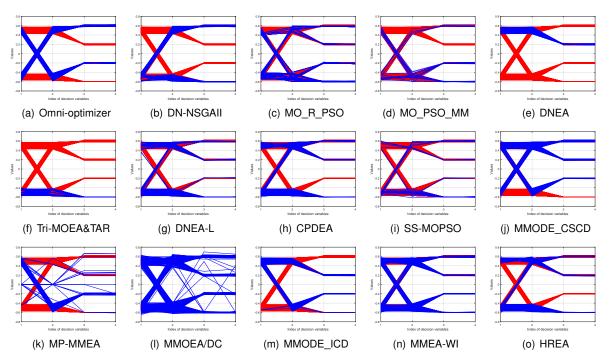


Fig. 6. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the decision spaces on IDMPM4T3.

TABLE VII

AVERAGE AND VARIANCE OF IGD RESULTS OF THE COMPARED ALGORITHMS ON MMOPL TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

	Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
2.76E-05 3.85E-05 1.66E-04 2.96E-04 3.75E-05 1.78E-05	IDMPM2T1e	7.20E-03	7.21E-03	7.18E-03	7.57E-03	7.20E-03	7.38E-03	3.42E-03	7.18E-03	7.12E-03	7.12E-03	7.00E-03	1.36E-03	7.31E-03	7.16E-03	1.02E-03
Table Tabl	IDMI M211e	2.76E-05	3.85E-05	1.66E-04	2.96E-04	3.75E-05	1.78E-05	1.72E-03	5.60E-05	1.13E-04	2.15E-05	2.40E-04	1.69E-04	1.31E-05	6.13E-05	1.38E-04
T.SELOS 2.06E+05 1.17E-04 2.98E+04 1.46E-05 9.15E+06 1.66E+03 3.84E+05 9.37E+05 2.20E+05 7.50E+05 1.49E+04 1.99E+05 6.04E-05 4.36E+05 1.75E+03 1.75E+03 1.75E+03 8.51E+04 6.54E+04 8.68E+04 2.81E+02 1.86E+04 2.45E+05 3.13E+04 1.72E+03 2.18E+03 2.95E+05 3.13E+03 1.66E+03 4.87E+05 7.46E+05	IDMPM2T2e	7.27E-03	7.27E-03	7.24E-03	7.52E-03	7.22E-03	7.40E-03	2.88E-03	7.22E-03	7.24E-03	7.19E-03	7.18E-03	9.65E-04	7.32E-03	7.26E-03	9.13E-04
Type	10.011 .012120	7.52E-05	2.06E-05	1.17E-04	2.98E-04	1.46E-05	9.15E-06	1.66E-03	3.84E-05	9.37E-05	2.20E-05	7.50E-05	1.49E-04	1.99E-05	6.04E-05	4.36E-05
Total Tota	IDMPM2T3e	5.80E-03	5.35E-03	8.67E-03	6.11E-03	5.09E-03	3.18E-02	1.64E-03	4.98E-03	6.08E-03	8.45E-03	4.09E-03	1.11E-03	6.99E-03	5.11E-03	1.16E-03
	10.011.012130	1.75E-03	1.17E-03	8.51E-04	6.54E-04	8.68E-04	2.81E-02	1.86E-04	2.45E-05	3.13E-04	1.72E-03	2.18E-03	9.26E-05	1.36E-03	4.87E-05	7.46E-05
ASPECCO ASPE	IDMPM2T/le	1.28E-02	1.42E-02	1.39E-02	1.42E-02	1.47E-02	1.49E-02	4.92E-03	1.60E-02	1.41E-02	1.60E-02	5.81E-03	1.61E-03	1.08E-02	1.58E-02	1.50E-03
Image 1.5 1.	IDMI M214c	4.59E-03	3.13E-03	1.25E-03	1.17E-03	3.42E-03	3.37E-03	3.49E-04	3.10E-04	1.01E-03	3.99E-05	7.01E-04	8.97E-04	2.96E-03	8.12E-04	7.18E-05
3.5FE-04 6.14E-04 7.53E-04 8.26E-04 1.23E-04 4.42E-04 8.30E-04 1.75E-04 5.43E-04 1.63E-04 6.34E-03 3.07E-04 1.24E-04 1.75E-04 2.51E-04 1.09E-03 1.29E-03 1.32E-03 1.01E-03 1.70E-04 3.72E-04 1.44E-03 2.20E-04 1.16E-03 2.75E-04 5.58E-03 2.08E-04 1.07E-04 2.59E-04 2.04E-109E-03 1.29E-03 1.32E-03 1.01E-03 1.70E-04 3.72E-04 1.44E-03 2.20E-04 1.16E-03 2.75E-04 5.58E-03 2.08E-04 1.07E-04 2.59E-04 2.04E-109E-03 1.09E-03 3.72E-02 3.68E-02 3.68E-02 3.68E-02 4.00E-02 1.65E-03 3.70E-02 3.70E-02 3.70E-02 3.59E-02 9.09E-03 3.77E-02 3.66E-02 3.67E-02 3.00E-02 3.70E-02 3.70E-02 3.59E-02 9.09E-03 3.77E-02 3.66E-02 3.67E-02 3.00E-02 3.00E-02 3.00E-02 3.00E-02 3.00E-03 3.00E-03 3.70E-03 3.00E-03	IDMPM3T1e	2.53E-02	2.55E-02	2.51E-02	2.51E-02	2.47E-02	2.79E-02	7.71E-03	2.46E-02	2.43E-02	2.46E-02	1.68E-02	7.61E-03	2.56E-02	2.47E-02	6.89E-03
1.09E-03 1.29E-03 1.32E-03 1.32E-03 1.01E-03 1.70E-04 3.72E-04 1.44E-03 2.20E-04 1.16E-03 2.75E-04 5.58E-03 2.08E-04 1.07E-04 2.59E-04 2.04E-10MPM3Ta* 1.09E-02 3.78E-02 3.78E-02 3.68E-02 3.68E-02 4.00E-02 1.65E-02 3.67E-02 3.70E-02 3.70E-02 3.59E-02 9.09E-03 3.77E-02 3.66E-02 8.32E-10MPM3Ta* 1.09E-02 4.40E-02 4.20E-02 4.12E-02 3.69E-02 3.98E-02 1.72E-02 3.67E-02 3.70E-02 3.70E-02 3.70E-02 3.98E-02 9.09E-03 3.77E-02 3.66E-02 8.55E-10 1.09E-02 7.77E-03 2.24E-03 3.74E-03 3.74E-	IDMI MSTIE	3.57E-04	6.14E-04	7.53E-04	8.26E-04	1.23E-04	4.42E-04	8.30E-04	1.75E-04	5.43E-04	1.63E-04	6.34E-03	3.07E-04	1.24E-04	1.75E-04	2.51E-04
1.09E-03 1.29E-03 1.32E-03 1.01E-03 1.70E-04 3.72E-04 1.44E-03 2.20E-04 1.16E-03 2.75E-04 5.58E-03 2.08E-04 1.07E-04 2.59E-04 2.04E-104 2.04E-	IDMPM3T2a	3.89E-02	3.87E-02	3.85E-02	3.75E-02	3.69E-02	4.02E-02	1.59E-02	3.66E-02	3.79E-02	3.70E-02	3.45E-02	8.12E-03	3.78E-02	3.67E-02	7.81E-03
DIMPM314	IDMIT WIST 26	1.09E-03	1.29E-03	1.32E-03	1.01E-03	1.70E-04	3.72E-04	1.44E-03	2.20E-04	1.16E-03	2.75E-04	5.58E-03	2.08E-04	1.07E-04	2.59E-04	2.04E-04
HIMPM3T46	IDMPM3T3a	3.80E-02	3.87E-02	3.72E-02	3.68E-02	3.68E-02	4.00E-02	1.65E-02	3.67E-02	3.70E-02	3.70E-02	3.59E-02	9.09E-03	3.77E-02	3.66E-02	8.32E-03
MMF10 1.09E-02 7.17E-03 2.24E-03 3.74E-03 2.01E-04 4.97E-04 1.48E-03 2.10E-04 2.41E-03 2.54E-04 8.59E-03 4.86E-04 1.22E-04 3.59E-04 2.73E-04 1.83E-01 1.93E-01 2.03E-01 1.62E-01 1.93E-01 2.26E-01 3.25E-02 1.92E-01 1.92E-01 1.62E-01 1.15E-01 1.67E-02 1.91E-01 1.91E-01 2.42E-03 2.00E-04 2.91E-02 2.91E-03 2	IDMI MS13e	6.44E-04	1.10E-03	8.40E-04	8.17E-04	1.80E-04	8.33E-04	1.45E-03	2.13E-04	7.26E-04	1.89E-04	3.69E-03	1.38E-03	2.73E-04	1.91E-04	4.97E-04
MMF10 1.09E-02 7.17E-03 2.24E-03 3.74E-03 2.01E-04 4.97E-04 1.48E-03 2.10E-04 2.41E-03 2.54E-04 8.59E-03 4.86E-04 1.22E-04 3.59E-04 2.73E-04 3.60E-02 4.93E-02 1.81E-02 1.53E-02 5.86E-04 3.81E-03 5.8EE-03 1.38E-03 1.59E-02 1.19E-02 8.21E-02 2.59E-02 1.91E-01 1.91E-01 2.42E-04 1.07E-03 1.69E-03 5.61E-03 5.74E-03 3.14E-04 7.42E-03 5.72E-03 2.02E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.18E-03 4.10E-04 4.74E-03 5.72E-03 2.02E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.18E-03 4.10E-04 4.74E-03 4	IDMPM3T/le	4.40E-02	4.34E-02	4.20E-02	4.12E-02	3.69E-02	3.98E-02	1.72E-02	3.67E-02	4.06E-02	3.70E-02	2.98E-02	9.31E-03	3.78E-02	3.67E-02	8.55E-03
MMF10 3.60E-02 4.93E-02 1.81E-02 1.53E-02 5.86E-04 3.81E-03 5.88E-03 1.38E-03 1.59E-02 1.19E-02 8.21E-02 2.59E-02 1.39E-02 1.40E-02 6.05E-03 1.60E-03 1.60E-03 5.61E-03 5.74E-03 3.14E-04 7.42E-03 5.72E-03 2.02E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.18E-03 4.10E-03 4.47E-03 2.35E-04 1.37E-02 1.07E-03 1.40E-02 2.74E-03 2.02E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.18E-03 4.10E-03 4.47E-03 2.35E-04 1.37E-02 1.07E-03 1.04E-01 1	IDMI MS14c	1.09E-02	7.17E-03	2.24E-03	3.74E-03	2.01E-04	4.97E-04	1.48E-03	2.10E-04	2.41E-03	2.54E-04	8.59E-03	4.86E-04	1.22E-04	3.59E-04	2.73E-04
MMF11 MMF12 MMF13 MMF15 MMF15 MMF16 MMF1	MMF10	1.83E-01	1.93E-01	2.03E-01	1.62E-01	1.93E-01	2.26E-01	3.25E-02	1.92E-01	1.92E-01	1.62E-01	1.15E-01	1.67E-02	1.91E-01	1.91E-01	2.42E-02
MMF12 1.07E-03 1.69E-03 5.61E-03 5.74E-03 3.14E-04 7.42E-03 5.72E-03 2.02E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.18E-03 4.10E-03 1.18E-03 4.10E-03 1.18E-03 4.10E-03 1.18E-03 4.10E-03 1.18E-03 4.10E-03 4	MINIFIO	3.60E-02	4.93E-02	1.81E-02	1.53E-02	5.86E-04	3.81E-03	5.88E-03	1.38E-03	1.59E-02	1.19E-02	8.21E-02	2.59E-02	1.39E-02	1.40E-02	6.05E-03
MMF12 8.37E-02 8.32E-02 6.80E-02 7.77E-02 8.25E-02 4.59E-03 5.72E-03 2.20E-04 6.75E-03 6.95E-03 1.68E-03 4.25E-04 1.76E-03 1.88E-03 4.10E-04 4.47E-03 2.35E-04 1.37E-02 1.07E-02 1.29E-04 5.22E-04 1.32E-02 2.58E-04 1.33E-02 1.73E-02 1.94E-04 1.94E-01 1.94E-01 1.24E-01 1	MMF11	9.61E-02	9.81E-02	8.46E-02	8.93E-02	9.17E-02	1.61E-01	3.85E-02	9.13E-02	8.87E-02	8.56E-02	9.35E-02	1.42E-02	9.71E-02	9.50E-02	2.74E-02
MMF16 13 13 13 14 15 15 15 15 15 15 15		1.07E-03	1.69E-03	5.61E-03	5.74E-03	3.14E-04	7.42E-03	5.72E-03	2.02E-04	6.75E-03	6.95E-03	1.68E-03	4.25E-04	1.76E-03	1.18E-03	4.10E-03
MMF16 13 2.35E-04 1.37E-02 1.07E-02 1.29E-04 5.22E-04 1.32E-02 2.58E-04 1.33E-02 1.73E-02 1.94E-04 7.92E-05 9.89E-04 3.04E-04 3.43E-04 1.47E-01 1.50E-01 1.06E-01 1.04E-01 1.45E-01 2.44E-01 1.49E-01 1.38E-01 9.25E-02 8.13E-02 1.27E-01 2.56E-02 1.51E-01 1.51E-0	MMF12	8.37E-02	8.32E-02	6.80E-02	7.77E-02	8.25E-02	8.52E-02	4.59E-02	8.28E-02	6.35E-02	6.96E-02	8.27E-02	2.56E-03	8.46E-02	8.31E-02	6.16E-03
MMF15 1.21E-03 4.20E-03 2.25E-02 3.01E-02 7.94E-04 5.05E-03 1.58E-02 2.19E-02 1.81E-02 2.57E-02 1.60E-02 6.33E-03 6.57E-03 6.18E-03 5.04E-04 5.04E-04 5.05E-03 1.58E-01 5.04E-04 5.04E-04 5.05E-03 5.04E-04 5.04E-04 5.05E-03 5.04E-04 5.04E-04 5.05E-03 5.04E-04 5.04E-04 5.05E-03 5.04E-04 5.05E-03 5.04E-04 5	MINIF 12	4.47E-03	2.35E-04	1.37E-02	1.07E-02	1.29E-04	5.22E-04	1.32E-02	2.58E-04	1.33E-02	1.73E-02	1.94E-04	7.92E-05	9.89E-04	3.04E-04	3.43E-04
MMF15 2.01E-01 2.21E-02 3.01E-02 7.94E-04 5.05E-03 1.58E-02 2.19E-02 1.81E-02 2.57E-02 1.60E-02 6.33E-03 6.57E-03 6.18E-03 5.04E-03 5	MMF13	1.47E-01	1.50E-01	1.04E-01	1.04E-01	1.45E-01	2.44E-01	1.49E-01	1.38E-01	9.25E-02	8.13E-02	1.27E-01	2.56E-02	1.51E-01	1.51E-01	2.45E-02
MMF16_13 Column MMF16_13 MMF16_12	MINIT 13	1.21E-03	4.20E-03	2.25E-02	3.01E-02	7.94E-04	5.05E-03	1.58E-02	2.19E-02	1.81E-02	2.57E-02	1.60E-02	6.33E-03	6.57E-03	6.18E-03	5.04E-03
MMF16_13 2.4E-01 2.24E-01 1.50E-03 3.16E-03 3.16E-03 4.03E-03 8.87E-04 6.72E-03 2.99E-03 2.99E-03 3.87E-03 4.93E-03 1.82E-03 1.26E-03 1.65E-03 2.18E-03 1.26E-03	MMF15	2.01E-01	2.11E-01	1.72E-01	1.70E-01	1.80E-01	2.07E-01	1.43E-01	1.71E-01	1.75E-01	1.66E-01	1.99E-01	1.00E-01	1.93E-01	1.85E-01	9.65E-02
MMF16_11 1.77E-01 1.90E-01 1.48E-01 1.44E-01 1.47E-01 1.72E-01 1.41E-01 1.47E-01 1.41E-01 1.42E-01 1.49E-01 1.43E-01	MINIT 13	6.74E-03	7.19E-03	2.23E-03	3.16E-03	4.03E-03	8.87E-04	6.72E-03	2.99E-03	2.99E-03	3.87E-03	4.93E-03	1.82E-03	1.26E-03	1.65E-03	2.18E-03
MMF16_12	MMF15 a	2.05E-01	2.21E-01	1.76E-01	1.71E-01	1.73E-01	1.97E-01	1.58E-01	1.69E-01	1.76E-01	1.66E-01	1.93E-01	1.35E-01	1.87E-01	1.78E-01	1.10E-01
MMF16_12	MINIF 15_a	6.57E-03	7.55E-03	3.91E-03	2.91E-03	2.78E-03	2.21E-03	4.12E-03	2.58E-03	3.83E-03	3.57E-03	7.70E-03	1.35E-02	2.82E-03	3.41E-03	3.70E-03
7.09E-03 8.84E-03 2.19E-03 1.92E-03 2.29E-03 8.49E-04 4.98E-03 3.45E-03 2.69E-03 2.64E-03 4.22E-03 2.49E-03 1.13E-03 2.72E-03 1.73E- MMF16_12 2.46E-01 2.54E-01 2.13E-01 2.10E-01 2.35E-01 2.01E-01 1.67E-01 2.24E-01 2.17E-01 2.09E-01 2.48E-01 1.34E-01 2.50E-01 2.39E-01 1.30E- MMF16_13 2.14E-01 2.24E-01 1.82E-01 1.82E-01 1.77E-01 1.92E-01 2.17E-01 1.68E-01 1.84E-01 1.83E-01 1.76E-01 1.83E-01 1.76E-01 2.07E-01 1.28E-01 1.28E-01 1.99E-01 1.24E- MMF16_13 2.14E-01 2.24E-01 1.82E-01 1.77E-01 1.92E-01 2.17E-01 1.68E-01 1.84E-01 1.83E-01 1.76E-01 2.07E-01 1.28E-01 2.06E-01 1.99E-01 1.24E- MMF16_13 2.14E-01 2.24E-01 1.82E-01 1.77E-01 1.99E-01 1.92E-01 1.68E-01 1.84E-01 1.83E-01 1.76E-01 2.07E-01 1.28E-01 2.06E-01 1.99E-01 1.24E- MMF16_13 2.14E-01 2.24E-01 1.82E-01 1.77E-01 1.99E-01 1.24E-01 1.84E-01 1.83E-01 1.76E-01 2.07E-01 1.28E-01 2.06E-01 1.99E-01 1.24E-01 1.84E-01	MMF16 11	1.77E-01	1.90E-01	1.48E-01	1.44E-01	1.47E-01	1.72E-01	1.41E-01	1.42E-01	1.49E-01	1.43E-01	1.68E-01	9.87E-02	1.60E-01	1.54E-01	9.46E-02
MMF16_12 8.21E-03 7.50E-03 4.23E-03 3.52E-03 5.02E-03 6.42E-04 5.57E-03 4.30E-03 5.87E-03 5.70E-03 6.97E-03 3.65E-03 9.49E-04 2.62E-03 4.94E-04 4.94E-04-04-04-04-04-04-04-04-04-04-04-04-04-	WIWIF TO_II	7.09E-03	8.84E-03	2.19E-03	1.92E-03	2.29E-03	8.49E-04	4.98E-03	3.45E-03	2.69E-03	2.64E-03	4.22E-03	2.49E-03	1.13E-03	2.72E-03	1.73E-03
8.21E-03 7.50E-03 4.23E-03 3.52E-03 5.02E-03 6.42E-04 5.57E-03 4.30E-03 5.87E-03 5.70E-03 6.97E-03 3.65E-03 9.49E-04 2.62E-03 4.94E-04	MMF16 12	2.46E-01	2.54E-01	2.13E-01	2.10E-01	2.35E-01	2.61E-01	1.67E-01	2.24E-01	2.17E-01	2.09E-01	2.48E-01	1.34E-01	2.50E-01	2.39E-01	1.30E-01
MMF16 13	112111110_12	8.21E-03	7.50E-03	4.23E-03	3.52E-03	5.02E-03	6.42E-04	5.57E-03	4.30E-03	5.87E-03	5.70E-03	6.97E-03	3.65E-03	9.49E-04	2.62E-03	4.94E-03
MINITIO_IS	MMF16 13	2.14E-01	2.24E-01	1.82E-01	1.77E-01	1.92E-01	2.17E-01	1.68E-01	1.84E-01	1.83E-01	1.76E-01	2.07E-01	1.28E-01	2.06E-01	1.99E-01	1.24E-01
6.98E-03 6.65E-03 3.99E-03 2.20E-03 3.56E-03 7.16E-04 5.08E-03 2.50E-03 3.39E-03 3.24E-03 6.01E-03 6.89E-03 1.17E-03 2.75E-03 3.66E-	1411VIF 1U_13	6.98E-03	6.65E-03	3.99E-03	2.20E-03	3.56E-03	7.16E-04	5.08E-03	2.50E-03	3.39E-03	3.24E-03	6.01E-03	6.89E-03	1.17E-03	2.75E-03	3.66E-03

TABLE VIII AVERAGE AND VARIANCE OF IGDX RESULTS OF THE COMPARED ALGORITHMS ON MMOPL TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
IDMPM2T1e	6.73E-01	6.73E-01	6.74E-01	6.53E-01	6.73E-01	6.73E-01	2.05E-03	6.73E-01	6.74E-01	6.73E-01	3.30E-01	8.92E-04	6.73E-01	6.73E-01	6.28E-04
10.011.012110	2.31E-04	2.31E-04	8.52E-04	1.16E-01	8.16E-05	6.28E-05	1.18E-03	1.92E-04	1.00E-03	4.97E-05	6.44E-02	1.11E-04	1.91E-04	1.83E-04	5.44E-05
IDMPM2T2e	6.74E-01	6.74E-01	6.74E-01	6.52E-01	6.73E-01	6.73E-01	3.10E-03	6.73E-01	6.74E-01	6.73E-01	3.37E-01	1.02E-03	6.73E-01	6.73E-01	9.22E-04
15.111 1112120	5.17E-04	5.77E-04	7.36E-04	1.18E-01	1.81E-04	1.04E-04	4.91E-03	3.20E-04	8.59E-04	2.08E-04	3.95E-02	1.05E-04	1.54E-04	3.84E-04	8.29E-05
IDMPM2T3e	6.12E-01	5.87E-01	1.18E-01	2.95E-01	4.71E-01	4.02E-01	3.16E-03	3.01E-01	2.99E-01	4.94E-01	1.92E-01	1.38E-03	1.22E-01	3.01E-01	1.40E-03
	1.60E-01	1.77E-01	1.49E-01	4.88E-02	1.75E-01	1.94E-01	4.01E-03	4.29E-04	5.02E-02	2.46E-01	1.56E-01	6.44E-05	1.38E-01	5.04E-04	7.42E-05
IDMPM2T4e	9.45E-01	9.21E-01	7.02E-01	7.11E-01	9.77E-01	9.94E-01	2.67E-01	1.01E+00	7.88E-01	1.01E+00	3.89E-01	1.28E-01	4.17E-01	1.00E+00	3.65E-03
	1.76E-01	1.67E-01	2.51E-01	2.79E-01	1.10E-01	8.42E-02	9.08E-02	2.00E-04	2.74E-01	6.63E-05	8.64E-02	9.28E-02	1.45E-01	3.64E-02	2.45E-03
IDMPM3T1e	7.47E-01	7.49E-01	6.42E-01	6.36E-01	7.69E-01	7.78E-01	3.51E-02	6.26E-01	6.31E-01	6.25E-01	2.97E-01	8.08E-03	6.28E-01	6.25E-01	6.97E-03
	1.62E-01	1.72E-01	1.09E-02	6.43E-03	1.83E-01	1.85E-01	7.43E-02	1.53E-03	3.72E-03	8.44E-04	8.85E-02	2.09E-04	3.10E-03	1.15E-03	1.32E-04
IDMPM3T2e	8.47E-01	7.35E-01	5.38E-01	4.95E-01	8.23E-01	8.64E-01	1.79E-01	4.96E-01	5.02E-01	8.48E-01	4.20E-01	7.84E-03	8.12E-01	4.96E-01	7.46E-03
	1.27E-01	1.91E-01	1.54E-01	1.00E-01	1.47E-01	9.51E-02	1.11E-01	9.46E-04	9.21E-02	1.19E-01	9.77E-02	1.38E-04	1.55E-01	9.61E-04	3.37E-04
IDMPM3T3e	7.17E-01	8.09E-01	5.05E-01	5.05E-01	6.99E-01	7.83E-01	2.44E-01	5.01E-01	5.03E-01	5.42E-01	4.72E-01	1.20E-02	5.46E-01	5.00E-01	9.25E-03
	2.46E-01	2.25E-01	6.09E-03	5.25E-03	2.38E-01	2.47E-01	5.54E-02	3.44E-03	3.89E-03	1.34E-01	1.10E-01	1.55E-02	1.28E-01	2.95E-03	1.75E-03
IDMPM3T4e	1.02E+00	1.02E+00	7.12E-01	7.29E-01	9.38E-01	9.60E-01	4.84E-01	8.50E-01	7.44E-01	9.43E-01	5.27E-01	1.32E-02	8.51E-01	9.49E-01	1.07E-02
	1.61E-01	1.55E-01	1.25E-01	1.64E-01	1.30E-01	1.23E-01	1.27E-01	1.61E-03	1.31E-01	1.40E-01	1.17E-01	6.90E-03	2.63E-03	1.65E-01	4.52E-04
MMF10	1.76E-01	1.48E-01	1.69E-01	1.64E-01	2.00E-01	2.01E-01	1.37E-02	2.01E-01	1.63E-01	1.64E-01	1.07E-01	1.28E-02	1.89E-01	1.98E-01	7.22E-03
	3.11E-02	2.97E-02	8.40E-03	1.03E-02	1.18E-03	5.18E-05	2.71E-03	5.26E-05	1.80E-02	1.37E-02	9.58E-02	3.21E-02	2.32E-02	1.02E-02	7.64E-04
MMF11	2.50E-01	2.50E-01	2.10E-01	2.40E-01	2.49E-01	2.52E-01	1.94E-02	2.49E-01	2.05E-01	2.11E-01	2.47E-01	5.62E-03	2.52E-01	2.49E-01	7.16E-03
	3.63E-04	4.16E-04	2.49E-02	2.08E-02	2.15E-04	7.16E-05	1.00E-02	1.45E-04	2.26E-02	2.99E-02	3.40E-03	1.82E-04	1.07E-04	1.81E-04	1.01E-03
MMF12	2.45E-01	2.47E-01	1.90E-01	2.26E-01	2.46E-01	2.48E-01	1.88E-01	2.45E-01	1.76E-01	2.08E-01	2.45E-01	2.50E-03	2.47E-01	2.45E-01	2.74E-03
	9.24E-03	5.35E-04	4.29E-02	3.31E-02	2.15E-04	6.14E-04	7.19E-02	1.95E-04	4.20E-02	4.96E-02	3.76E-04	1.18E-04	1.57E-04	2.57E-04	1.35E-04
MMF13	2.86E-01	2.86E-01	2.35E-01	2.47E-01	2.58E-01	2.72E-01	2.55E-01	2.50E-01	2.32E-01	2.31E-01	2.69E-01	8.97E-02	2.54E-01	2.52E-01	4.13E-02
	9.28E-03	9.59E-03	1.57E-02	1.35E-02	2.96E-03	8.09E-03	1.36E-02	8.60E-03	1.74E-02	1.60E-02	1.38E-02	2.68E-02	6.28E-04	5.98E-04	6.00E-04
MMF15	2.44E-01	2.26E-01	1.51E-01	1.50E-01	2.60E-01	2.71E-01	6.65E-02	2.30E-01	1.53E-01	1.37E-01	2.66E-01	5.41E-02	2.66E-01	2.58E-01	4.34E-02
	2.05E-02	2.38E-02	1.04E-02	1.47E-02	1.47E-03	3.23E-04	4.10E-03	1.82E-02	1.50E-02	1.33E-02	2.66E-03	1.61E-03	9.96E-04	1.04E-03	9.11E-04
MMF15_a	2.15E-01	2.10E-01	1.67E-01	1.60E-01	2.08E-01	2.20E-01	9.54E-02	2.05E-01	1.60E-01	1.55E-01	2.20E-01	9.17E-02	2.14E-01	2.08E-01	5.33E-02
	1.30E-02	1.69E-02	1.21E-02	1.60E-02	1.97E-03	1.52E-03	4.87E-03	4.26E-03	1.21E-02	9.35E-03	3.63E-03	1.45E-02	1.21E-03	3.76E-03	2.09E-03
MMF16_l1	1.85E-01	1.84E-01	1.16E-01	1.16E-01	1.53E-01	1.50E-01	8.12E-02	1.44E-01	1.16E-01	1.10E-01	1.70E-01	6.85E-02	1.54E-01	1.52E-01	4.77E-02
	9.03E-03	9.43E-03	8.55E-03	6.74E-03	1.19E-03	3.72E-04	4.31E-03	5.34E-03	7.24E-03	6.74E-03	5.78E-03	2.57E-03	5.12E-04	6.21E-04	1.01E-03
MMF16_12	2.99E-01	2.87E-01	1.94E-01	1.99E-01	3.33E-01	3.47E-01	8.35E-02	2.96E-01	2.00E-01	1.81E-01	3.37E-01	1.07E-01	3.42E-01	3.31E-01	6.14E-02
	3.55E-02	2.85E-02	1.86E-02	2.12E-02	3.08E-03	2.54E-04	5.00E-03	1.96E-02	1.65E-02	1.52E-02	4.17E-03	1.82E-02	1.02E-03	1.66E-03	1.03E-02
MMF16_13	2.32E-01	2.25E-01	1.55E-01	1.48E-01	2.09E-01	2.07E-01	1.24E-01	1.94E-01	1.55E-01	1.44E-01	2.22E-01	1.07E-01	2.10E-01	2.07E-01	5.89E-02
	1.23E-02	1.36E-02	1.30E-02	7.06E-03	8.87E-04	3.02E-04	4.78E-03	7.64E-03	7.86E-03	1.12E-02	1.09E-02	9.86E-03	6.09E-04	8.23E-04	2.73E-03

TABLE IX Average and variance of RPSP results of the compared algorithms on MMOPL test suite, where the best mean for each test instance is highlighted.

Problems	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
IDMPM2T1e	5.42E+01	5.82E+01	2.39E+01	2.23E+01	1.09E+02	Inf	2.05E-03	7.50E+01	2.55E+01	6.35E+01	6.16E-01	8.92E-04	2.63E+02	4.91E+01	6.29E-04
IDMPM211e	8.91E+00	1.14E+01	2.80E+00	5.66E+00	3.94E+01	NaN	1.19E-03	4.35E+01	3.28E+00	6.60E+00	1.89E-01	1.11E-04	5.67E+01	6.98E+00	5.44E-05
IDMPM2T2e	3.66E+01	3.50E+01	2.28E+01	2.30E+01	4.31E+01	8.45E+01	3.10E-03	3.46E+01	2.34E+01	3.43E+01	6.50E-01	1.02E-03	7.53E+01	3.21E+01	9.22E-04
IDMFWI212e	9.17E+00	2.44E+00	1.57E+00	5.00E+00	6.05E+00	7.60E+01	4.91E-03	4.79E+00	1.54E+00	2.32E+00	1.35E-01	1.05E-04	2.51E+01	4.90E+00	8.29E-05
IDMPM2T3e	3.69E+01	4.05E+01	4.69E-01	7.37E-01	3.02E+01	1.64E+01	3.17E-03	7.52E-01	7.46E-01	7.44E+00	3.79E-01	1.38E-03	4.50E-01	7.52E-01	1.40E-03
IDMIT WIZ I SE	2.74E+01	3.03E+01	7.49E-01	1.32E-01	3.26E+01	2.91E+01	4.01E-03	1.67E-03	1.35E-01	1.30E+01	5.20E-01	6.45E-05	1.02E+00	1.63E-03	7.43E-05
IDMPM2T4e	1.43E+02	8.68E+01	1.98E+01	2.72E+01	1.39E+02	Inf	3.20E-01	1.17E+02	3.70E+01	1.06E+02	6.50E-01	1.37E-01	1.58E+01	1.03E+02	3.65E-03
10/11/1/2146	1.97E+02	9.73E+01	2.84E+01	3.26E+01	7.65E+01	NaN	1.28E-01	2.23E+01	3.03E+01	4.90E+00	2.56E-01	1.16E-01	8.31E+01	2.38E+01	2.45E-03
IDMPM3T1e	7.08E+00	6.61E+00	1.82E+00	1.81E+00	1.30E+01	1.42E+01	3.75E-02	1.78E+00	1.79E+00	1.78E+00	3.93E-01	8.08E-03	1.80E+00	1.78E+00	6.97E-03
IDMI MSTIE	7.62E+00	7.48E+00	6.39E-02	4.33E-02	1.51E+01	1.70E+01	8.19E-02	1.41E-02	3.85E-02	5.80E-03	1.98E-01	2.09E-04	1.69E-02	1.31E-02	1.33E-04
IDMPM3T2e	1.55E+01	1.01E+01	2.48E+00	1.03E+00	1.84E+01	2.27E+01	2.02E-01	5.68E-01	1.03E+00	1.71E+01	7.38E-01	7.84E-03	2.07E+01	5.67E-01	7.46E-03
10311 313120	7.34E+00	8.17E+00	4.97E+00	2.60E+00	8.20E+00	6.47E+00	1.28E-01	1.37E-03	2.57E+00	5.69E+00	4.53E-01	1.38E-04	1.04E+01	1.10E-03	3.37E-04
IDMPM3T3e	8.08E+00	1.06E+01	5.82E-01	5.83E-01	9.17E+00	1.59E+01	2.80E-01	5.77E-01	5.79E-01	1.91E+00	9.77E-01	1.23E-02	2.55E+00	5.74E-01	9.26E-03
IDMI MSTSC	9.20E+00	8.41E+00	8.88E-03	8.67E-03	1.18E+01	1.52E+01	6.51E-02	5.74E-03	6.36E-03	4.61E+00	1.18E+00	1.73E-02	7.42E+00	4.22E-03	1.75E-03
IDMPM3T4e	2.33E+01	2.37E+01	2.10E+00	2.42E+00	2.00E+01	2.60E+01	8.73E-01	3.72E+00	2.38E+00	1.71E+01	1.58E+00	1.32E-02	3.74E+00	1.75E+01	1.07E-02
12.111.110.110	1.76E+01	1.72E+01	1.23E+00	1.37E+00	2.28E+01	2.70E+01	3.17E-01	2.61E-02	1.28E+00	1.86E+01	3.18E+00	6.90E-03	3.69E-02	2.35E+01	4.52E-04
MMF10	2.54E+00	6.31E-01	1.76E-01	4.43E-01	9.28E+00	Inf	1.38E-02	7.48E+00	1.66E-01	3.97E-01	2.67E+00	2.29E-02	1.73E+01	5.84E+00	7.22E-03
	3.29E+00	1.70E+00	1.15E-02	1.09E+00	2.71E+00	NaN	2.71E-03	1.09E+00	1.90E-02	1.05E+00	2.79E+00	8.72E-02	1.20E+01	2.19E+00	7.64E-04
MMF11	1.81E+00	1.74E+00	4.10E-01	1.26E+00	2.08E+00	Inf	1.97E-02	1.84E+00	3.76E-01	7.89E-01	1.43E+00	5.62E-03	Inf	1.68E+00	7.16E-03
	1.31E-01	1.97E-01	3.74E-01	4.89E-01	1.51E-01	NaN	1.01E-02	9.53E-02	3.88E-01	8.12E-01	3.30E-01	1.82E-04	NaN	1.40E-01	1.01E-03
MMF12	2.15E+00	2.23E+00	5.12E-01	1.06E+00	2.68E+00	Inf	5.56E-01	2.19E+00	4.28E-01	1.41E+00	2.10E+00	2.50E-03	Inf	1.98E+00	2.74E-03
	3.98E-01	2.34E-01	4.59E-01	5.37E-01	2.97E-01	NaN	3.42E-01	1.30E-01	4.70E-01	1.00E+00	2.08E-01	1.18E-04	NaN	1.78E-01	1.35E-04
MMF13	6.06E-01	6.16E-01	3.32E-01	4.79E-01	5.49E-01	6.51E-01	5.18E-01	5.12E-01	3.19E-01	3.72E-01	5.50E-01	9.75E-02	5.39E-01	5.28E-01	4.42E-02
	2.32E-02	6.83E-02	6.12E-02	8.98E-02	1.77E-02	8.26E-02	6.29E-02	5.53E-02	8.79E-02	9.74E-02	4.56E-02	3.25E-02	2.50E-03	4.07E-03	6.38E-04
MMF15	3.20E-01	2.40E-01	1.51E-01	1.50E-01	5.62E-01	Inf	6.66E-02	3.05E-01	1.53E-01	1.37E-01	5.94E-01	5.41E-02	9.47E-01	5.50E-01	4.34E-02
	1.29E-01	6.52E-02	1.04E-02	1.47E-02	7.27E-02	NaN	4.12E-03	1.52E-01	1.50E-02	1.33E-02	5.52E-02	1.61E-03	3.55E-01	6.37E-02	9.11E-04
MMF15_a	2.38E-01	2.24E-01	1.70E-01	1.61E-01	2.56E-01	2.74E-01	9.54E-02	2.36E-01	1.62E-01	1.56E-01	2.71E-01	9.17E-02	2.68E-01	2.55E-01	5.33E-02
	2.98E-02	3.22E-02	1.56E-02	1.65E-02	4.80E-03	3.35E-03	4.87E-03	2.54E-02	1.28E-02	9.31E-03	5.23E-03	1.45E-02	2.26E-03	5.26E-03	2.09E-03
MMF16_l1	2.10E-01	1.92E-01	1.16E-01	1.16E-01	1.99E-01	2.04E-01	8.12E-02	1.64E-01	1.16E-01	1.10E-01	2.24E-01	6.85E-02	2.08E-01	1.98E-01	4.77E-02
	3.44E-02	2.67E-02	8.55E-03	6.74E-03	7.71E-03	5.06E-04	4.31E-03	2.82E-02	7.24E-03	6.74E-03	8.32E-03	2.57E-03	8.87E-04	5.15E-03	1.01E-03
MMF16_12	4.30E-01	3.46E-01	1.94E-01	1.99E-01	7.30E-01	Inf	8.36E-02	3.97E-01	2.00E-01	1.81E-01	7.74E-01	1.20E-01	1.20E+00	7.37E-01	6.14E-02
	1.77E-01	1.03E-01	1.86E-02	2.12E-02	1.06E-01	NaN	5.21E-03	1.76E-01	1.65E-02	1.52E-02	8.84E-02	2.54E-02	2.23E-01	6.32E-02	1.03E-02
MMF16_13	2.82E-01	2.55E-01	1.55E-01	1.48E-01	2.92E-01	2.99E-01	1.27E-01	2.17E-01	1.56E-01	1.44E-01	3.08E-01	1.13E-01	3.01E-01	2.86E-01	5.89E-02
	4.92E-02	3.75E-02	1.32E-02	7.05E-03	6.65E-03	4.36E-04	8.96E-03	3.30E-02	7.86E-03	1.12E-02	2.20E-02	1.49E-02	1.54E-03	8.50E-03	2.73E-03

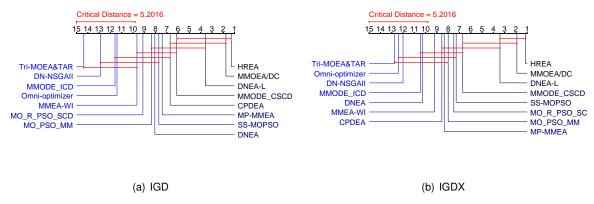


Fig. 7. The critical difference of all compared MMEAs on MMOPL test suite, where the red lines indicate that there is no significant difference in the Friedman ranks of the two MMEAs.

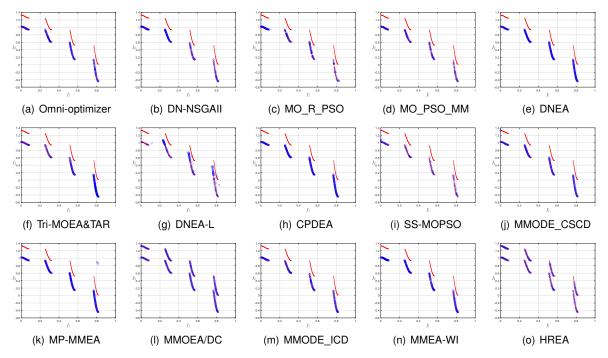


Fig. 8. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the objective space on MMF12.

TABLE X Average IGD results of the compared algorithms on Multi-Polygon test suite, where the best mean for each test instance is highlighted.

M	D	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
	2	2.96E+00	3.17E+00	2.17E-01	1.48E-01	7.80E-02	3.53E-01	1.24E-01	7.37E-02	2.26E-01	6.52E-02	1.67E-01	9.15E-02	6.72E-02	9.36E-02	5.11E-02
	4	1.90E+01	1.69E+01	2.38E+00	2.77E+00	1.76E+00	4.81E+00	2.93E-01	6.30E+00	7.69E+00	1.69E-01	4.23E+00	5.86E-01	7.11E-01	8.44E-01	1.87E+00
3	8	5.37E+01	4.77E+01	8.67E+00	1.56E+01	7.60E+00	7.51E+00	5.88E+00	7.24E+01	4.24E+01	2.23E+00	7.96E+00	1.60E+00	4.68E+00	2.37E+00	6.87E+00
	10	6.45E+01	5.73E+01	1.22E+01	2.66E+01	8.54E+00	8.70E+00	8.01E+00	4.85E+01	6.40E+01	4.06E+00	9.05E+00	8.85E+00	5.90E+00	8.05E+00	8.03E+00
	20	1.36E+02	1.24E+02	4.62E+01	8.90E+01	1.24E+01	1.25E+01	1.24E+01	9.19E+01	1.40E+02	1.88E+01	1.33E+01	1.27E+01	9.92E+00	1.16E+01	1.24E+01
	2	3.80E+00	3.25E+00	1.77E-01	1.23E-01	7.50E-02	7.73E-01	1.06E-01	8.14E-02	2.04E-01	9.73E-02	1.66E-01	8.80E-02	9.10E-02	8.69E-02	7.14E-02
	4	2.20E+01	1.70E+01	1.69E+00	2.07E+00	1.56E+00	3.84E+00	3.07E-01	3.06E+00	7.84E+00	2.20E-01	3.69E+00	5.09E-01	3.47E-01	6.27E-01	2.33E+00
4	8	5.13E+01	4.68E+01	7.42E+00	1.48E+01	6.87E+00	7.26E+00	5.20E+00	6.50E+01	4.22E+01	3.84E+00	7.59E+00	1.34E+00	4.24E+00	9.59E-01	6.66E+00
	10	7.43E+01	5.45E+01	1.05E+01	2.52E+01	8.18E+00	8.37E+00	7.27E+00	8.22E+00	6.59E+01	5.29E+00	8.68E+00	5.33E+00	5.98E+00	7.74E+00	7.72E+00
	20	1.27E+02	1.21E+02	4.10E+01	8.55E+01	1.20E+01	1.21E+01	1.22E+01	9.00E+01	1.43E+02	2.19E+01	1.30E+01	8.17E+00	1.09E+01	1.11E+01	1.19E+01
	2	3.25E+00	2.84E+00	2.25E-01	1.48E-01	7.12E-02	5.34E-01	8.98E-02	7.85E-02	2.37E-01	9.08E-02	1.23E-01	8.31E-02	8.88E-02	8.19E-02	6.83E-02
	4	1.95E+01	1.71E+01	1.87E+00	2.20E+00	4.10E-01	2.07E+00	3.43E-01	1.12E+01	6.12E+00	2.17E-01	3.67E+00	3.91E-01	6.71E-01	2.42E-01	2.35E+00
6	8	5.57E+01	4.94E+01	8.55E+00	1.54E+01	6.78E+00	7.36E+00	5.50E+00	6.62E+01	3.80E+01	1.37E+00	7.73E+00	1.67E+00	3.28E+00	1.19E+00	6.67E+00
	10	5.65E+01	4.84E+01	1.19E+01	2.62E+01	8.01E+00	8.54E+00	7.83E+00	8.72E+01	6.11E+01	3.95E+00	8.89E+00	2.76E+00	5.97E+00	4.74E+00	7.52E+00
	20	1.20E+02	1.30E+02	4.72E+01	8.78E+01	1.21E+01	1.28E+01	1.29E+01	1.72E+02	1.43E+02	1.69E+01	1.31E+01	5.06E+00	9.90E+00	4.86E+00	1.17E+01
	2	2.75E+00	2.35E+00	2.28E-01	1.48E-01	7.40E-02	7.16E-01	9.16E-02	8.06E-02	2.37E-01	9.40E-02	1.37E-01	8.58E-02	9.25E-02	8.44E-02	7.07E-02
	4	1.99E+01	1.72E+01	2.09E+00	2.19E+00	1.42E+00	4.70E+00	3.22E-01	2.89E+00	7.19E+00	2.20E-01	3.63E+00	3.72E-01	6.68E-01	5.74E-01	2.31E+00
8	8	4.81E+01	4.40E+01	8.27E+00	1.55E+01	7.04E+00	7.41E+00	5.47E+00	6.17E+01	4.33E+01	1.61E+00	7.67E+00	1.76E+00	4.09E+00	2.16E+00	6.55E+00
	10	7.10E+01	6.18E+01	1.22E+01	2.56E+01	8.22E+00	8.39E+00	6.91E+00	8.19E+00	6.26E+01	5.20E+00	8.81E+00	5.60E+00	5.68E+00	7.72E+00	7.54E+00
	20	1.28E+02	1.15E+02	4.67E+01	8.31E+01	1.13E+01	1.22E+01	1.25E+01	1.16E+01	1.41E+02	1.62E+01	1.30E+01	1.16E+01	9.62E+00	1.11E+01	1.18E+01

TABLE XI

AVERAGE IGDX RESULTS OF THE COMPARED ALGORITHMS ON MULTI-POLYGON TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

M	D	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCE	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
	2	2.96E+00	3.17E+00	2.17E-01	1.48E-01	7.80E-02	3.53E-01	1.24E-01	7.37E-02	2.26E-01	6.52E-02	1.67E-01	9.15E-02	6.72E-02	9.36E-02	5.11E-02
	4	1.90E+01	1.69E+01	2.38E+00	2.77E+00	1.76E+00	4.81E+00	2.93E-01	6.30E+00	7.69E+00	1.69E-01	4.23E+00	5.86E-01	7.11E-01	8.44E-01	1.87E+00
3	8	5.37E+01	4.77E+01	8.67E+00	1.56E+01	7.60E+00	7.51E+00	5.88E+00	7.24E+01	4.24E+01	2.23E+00	7.96E+00	1.60E+00	4.68E+00	2.37E+00	6.87E+00
	10	6.45E+01	5.73E+01	1.22E+01	2.66E+01	8.54E+00	8.70E+00	8.01E+00	4.85E+01	6.40E+01	4.06E+00	9.05E+00	8.85E+00	5.90E+00	8.05E+00	8.03E+00
	20	1.36E+02	1.24E+02	4.62E+01	8.90E+01	1.24E+01	1.25E+01	1.24E+01	9.19E+01	1.40E+02	1.88E+01	1.33E+01	1.27E+01	9.92E+00	1.16E+01	1.24E+01
	2	3.80E+00	3.25E+00	1.77E-01	1.23E-01	7.50E-02	7.73E-01	1.06E-01	8.14E-02	2.04E-01	9.73E-02	1.66E-01	8.80E-02	9.10E-02	8.69E-02	7.14E-02
	4	2.20E+01	1.70E+01	1.69E+00	2.07E+00	1.56E+00	3.84E+00	3.07E-01	3.06E+00	7.84E+00	2.20E-01	3.69E+00	5.09E-01	3.47E-01	6.27E-01	2.33E+00
4	8	5.13E+01	4.68E+01	7.42E+00	1.48E+01	6.87E+00	7.26E+00	5.20E+00	6.50E+01	4.22E+01	3.84E+00	7.59E+00	1.34E+00	4.24E+00	9.59E-01	6.66E+00
	10	7.43E+01	5.45E+01	1.05E+01	2.52E+01	8.18E+00	8.37E+00	7.27E+00	8.22E+00	6.59E+01	5.29E+00	8.68E+00	5.33E+00	5.98E+00	7.74E+00	7.72E+00
	20	1.27E+02	1.21E+02	4.10E+01	8.55E+01	1.20E+01	1.21E+01	1.22E+01	9.00E+01	1.43E+02	2.19E+01	1.30E+01	8.17E+00	1.09E+01	1.11E+01	1.19E+01
	2	3.25E+00	2.84E+00	2.25E-01	1.48E-01	7.12E-02	5.34E-01	8.98E-02	7.85E-02	2.37E-01	9.08E-02	1.23E-01	8.31E-02	8.88E-02	8.19E-02	6.83E-02
	4	1.95E+01	1.71E+01	1.87E+00	2.20E+00	4.10E-01	2.07E+00	3.43E-01	1.12E+01	6.12E+00	2.17E-01	3.67E+00	3.91E-01	6.71E-01	2.42E-01	2.35E+00
6	8	5.57E+01	4.94E+01	8.55E+00	1.54E+01	6.78E+00	7.36E+00	5.50E+00	6.62E+01	3.80E+01	1.37E+00	7.73E+00	1.67E+00	3.28E+00	1.19E+00	6.67E+00
	10	5.65E+01	4.84E+01	1.19E+01	2.62E+01	8.01E+00	8.54E+00	7.83E+00	8.72E+01	6.11E+01	3.95E+00	8.89E+00	2.76E+00	5.97E+00	4.74E+00	7.52E+00
	20	1.20E+02	1.30E+02	4.72E+01	8.78E+01	1.21E+01	1.28E+01	1.29E+01	1.72E+02	1.43E+02	1.69E+01	1.31E+01	5.06E+00	9.90E+00	4.86E+00	1.17E+01
	2	2.75E+00	2.35E+00	2.28E-01	1.48E-01	7.40E-02	7.16E-01	9.16E-02	8.06E-02	2.37E-01	9.40E-02	1.37E-01	8.58E-02	9.25E-02	8.44E-02	7.07E-02
	4	1.99E+01	1.72E+01	2.09E+00	2.19E+00	1.42E+00	4.70E+00	3.22E-01	2.89E+00	7.19E+00	2.20E-01	3.63E+00	3.72E-01	6.68E-01	5.74E-01	2.31E+00
8	8	4.81E+01	4.40E+01	8.27E+00	1.55E+01	7.04E+00	7.41E+00	5.47E+00	6.17E+01	4.33E+01	1.61E+00	7.67E+00	1.76E+00	4.09E+00	2.16E+00	6.55E+00
	10	7.10E+01	6.18E+01	1.22E+01	2.56E+01	8.22E+00	8.39E+00	6.91E+00	8.19E+00	6.26E+01	5.20E+00	8.81E+00	5.60E+00	5.68E+00	7.72E+00	7.54E+00
	20	1.28E+02	1.15E+02	4.67E+01	8.31E+01	1.13E+01	1.22E+01	1.25E+01	1.16E+01	1.41E+02	1.62E+01	1.30E+01	1.16E+01	9.62E+00	1.11E+01	1.18E+01

TABLE XII

AVERAGE RPSP RESULTS OF THE COMPARED ALGORITHMS ON MULTI-POLYGON TEST SUITE, WHERE THE BEST MEAN FOR EACH TEST INSTANCE IS HIGHLIGHTED.

M	D	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCE	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
	2	Inf	Inf	2.19E-01	1.49E-01	7.80E-02	3.61E-01	1.24E-01	7.37E-02	2.27E-01	6.52E-02	1.67E-01	9.15E-02	6.73E-02	9.36E-02	5.11E-02
	4	Inf	Inf	3.22E+00	4.51E+00	3.32E+00	Inf	2.93E-01	Inf	Inf	1.69E-01	7.08E+00	7.54E-01	8.93E-01	1.46E+00	3.89E+00
3	8	Inf	Inf	Inf	Inf	3.43E+01	Inf	1.39E+01	Inf	Inf	6.25E+00	3.49E+01	1.60E+00	1.09E+01	3.65E+00	2.95E+01
	10	Inf	Inf	Inf	Inf	4.03E+01	Inf	2.21E+01	Inf	Inf	1.01E+01	Inf	3.33E+01	1.88E+01	3.55E+01	4.00E+01
	20	Inf	Inf	Inf	Inf	6.55E+01	Inf	4.29E+01	Inf	Inf	Inf	Inf	4.70E+01	2.05E+01	5.21E+01	Inf
	2	Inf	Inf	1.78E-01	1.24E-01	7.50E-02	Inf	1.06E-01	8.14E-02	2.04E-01	9.74E-02	1.66E-01	8.80E-02	9.10E-02	8.69E-02	7.14E-02
	4	Inf	Inf	1.96E+00	2.30E+00	3.10E+00	1.08E+01	3.08E-01	7.23E+00	Inf	2.20E-01	8.30E+00	6.37E-01	3.58E-01	8.77E-01	4.76E+00
4	8	Inf	Inf	Inf	Inf	2.47E+01	2.93E+01	7.19E+00	Inf	Inf	9.70E+00	Inf	1.34E+00	8.73E+00	9.65E-01	2.50E+01
	10	Inf	Inf	Inf	Inf	3.19E+01	Inf	1.38E+01	3.13E+01	Inf	1.36E+01	Inf	1.37E+01	1.57E+01	2.86E+01	3.05E+01
	20	Inf	Inf	Inf	Inf	5.41E+01	Inf	2.35E+01	Inf	Inf	Inf	Inf	2.19E+01	3.66E+01	4.15E+01	5.98E+01
	2	Inf	1.06E+01	2.25E-01	1.48E-01	7.12E-02	Inf	8.98E-02	7.85E-02	2.38E-01	9.08E-02	1.23E-01	8.31E-02	8.88E-02	8.19E-02	6.83E-02
	4	Inf	Inf	2.01E+00	2.44E+00	5.51E-01	3.89E+00	3.43E-01	Inf	Inf	2.17E-01	8.99E+00	3.91E-01	8.29E-01	2.42E-01	5.51E+00
6	8	Inf	Inf	Inf	Inf	2.36E+01	Inf	7.68E+00	Inf	Inf	2.71E+00	2.81E+01	1.67E+00	5.15E+00	1.20E+00	2.49E+01
	10	Inf	Inf	Inf	Inf	3.02E+01	Inf	1.24E+01	Inf	Inf	9.14E+00	Inf	2.76E+00	1.59E+01	1.06E+01	2.81E+01
	20	Inf	Inf	Inf	Inf	5.03E+01	Inf	1.29E+01	Inf	Inf	Inf	Inf	5.06E+00	2.17E+01	6.47E+00	5.29E+01
	2	8.37E+00	7.81E+00	2.28E-01	1.48E-01	7.40E-02	7.71E-01	9.16E-02	8.06E-02	2.38E-01	9.40E-02	1.37E-01	8.58E-02	9.25E-02	8.44E-02	7.07E-02
	4	Inf	Inf	2.44E+00	2.54E+00	2.05E+00	1.66E+01	3.23E-01	6.34E+00	Inf	2.20E-01	9.17E+00	3.73E-01	6.87E-01	8.16E-01	4.83E+00
8	8	Inf	Inf	Inf	Inf	2.48E+01	Inf	7.61E+00	Inf	Inf	2.63E+00	Inf	1.76E+00	7.89E+00	3.20E+00	2.31E+01
	10	Inf	Inf	Inf	Inf	3.07E+01	4.29E+01	1.05E+01	2.98E+01	Inf	1.36E+01	Inf	1.36E+01	1.41E+01	2.76E+01	2.71E+01
	20	Inf	Inf	Inf	Inf	4.31E+01	Inf	2.06E+01	4.21E+01	Inf	Inf	Inf	3.41E+01	1.83E+01	4.07E+01	Inf

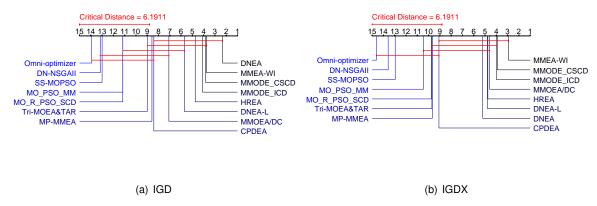


Fig. 9. The critical difference of all compared MMEAs on multi Polygon test suite, where the red lines indicate that there is no significant difference in the Friedman ranks of the two MMEAs.

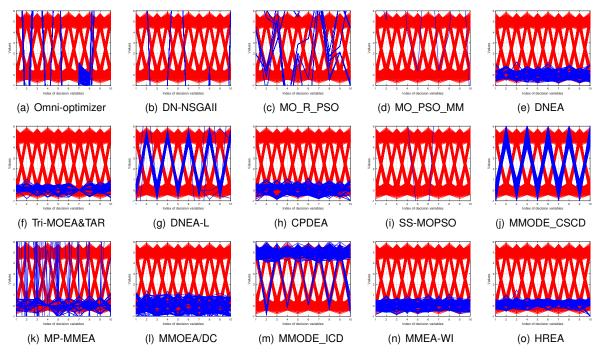


Fig. 10. The distribution of solutions obtained by all algorithms (MO_R_PSO_SCD is the short name for MO_Ring_PSO_SCD) in the decision space on Multi-polygon problem with 3 objectives and 10 decision variables.

TABLE XIII AVERAGE RANKS R OF IGD, IGDX and RPSP for 15 compared MMEAs on four different MMOP test suites, where the best rank is highlighted with gray background.

Problems	Indicators	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
MMF	IGD	8.71	11.53	10.88	6.10	3.10	11.29	12.36	3.83	8.61	4.10	10.49	5.69	5.08	9.40	8.83
	IGDX	13.73	14.05	8.59	5.45	8.21	10.23	8.84	2.86	6.29	5.23	12.53	6.59	7.53	6.49	3.35
	RPSP	13.71	14.02	8.63	5.51	8.24	10.32	8.84	2.80	6.37	5.23	12.51	6.54	7.48	6.45	3.35
IDMP	IGD	9.40	10.04	13.84	13.95	1.11	10.36	5.42	4.57	13.60	4.58	7.51	9.71	3.68	7.49	4.75
	IGDX	11.53	11.68	8.72	7.66	11.90	13.04	5.24	5.19	7.47	8.32	9.72	2.96	8.39	4.29	3.88
	RPSP	11.03	11.18	8.48	7.44	12.41	13.34	5.22	5.30	7.28	8.39	9.97	2.94	8.70	4.37	3.95
MMOPL	IGD	11.22	12.27	8.70	8.26	8.12	13.97	3.67	7.25	8.10	6.62	7.87	1.67	11.49	9.40	1.39
	IGDX	11.89	11.68	7.54	7.91	10.56	12.42	3.49	8.50	7.45	7.33	8.46	1.90	10.50	9.14	1.23
	RPSP	10.80	10.44	6.53	6.92	11.97	13.74	3.43	9.24	6.52	7.61	8.46	1.91	11.94	9.27	1.23
	IGD	13.49	13.31	10.86	11.25	2.33	8.52	6.07	8.67	13.01	4.11	8.19	7.27	4.35	3.55	5.05
Polygon	IGDX	14.02	13.65	9.78	10.48	5.25	9.13	5.31	9.35	12.83	4.25	9.37	4.43	4.25	3.05	4.88
	RPSP	13.17	12.97	9.89	10.93	5.90	10.15	4.18	8.92	12.45	4.68	9.07	3.54	4.29	3.75	6.11
	IGD	11.07	12.02	10.85	9.87	3.84	10.95	6.61	6.47	10.85	4.89	8.45	5.88	6.33	7.14	4.78
Overall	IGDX	12.89	12.82	8.71	8.17	8.61	11.02	5.54	6.95	8.95	6.09	9.85	3.90	7.45	5.68	3.36
	RPSP	12.22	12.15	8.43	8.02	9.32	11.79	5.15	7.02	8.55	6.32	9.80	3.61	7.91	5.95	3.78

VII. OVERALL PERFORMANCE AND TIME COMPLEXITY

This section listed the average ranks of all algorithms on all test problems. In addition, the detailed running time on problems with different numbers of objectives and decision variables are given.

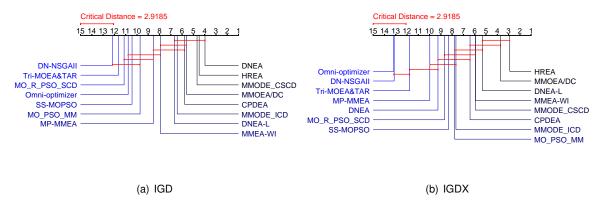


Fig. 11. The critical difference of all compared MMEAs on multi Polygon test suite, where the red lines indicate that there is no significant difference in the Friedman ranks of the two MMEAs.

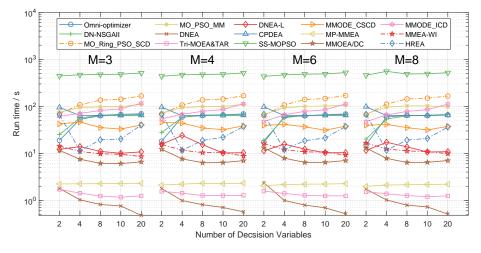


Fig. 12. The average running time of all algorithms on Multi-polygon problems with different numbers of objectives and decision variables.

TABLE XIV

Average running time (in second) of the compared algorithms on Multi-polygon test suite, where population size and function evaluations are set to 200 and 20000 respectively.

M	D	Omni- optimizer	DN- NSGAII	MO_Ring _PSO_SCD	MO_PSO _MM	DNEA	Tri-MO EA&TAR	DNEA-L	CPDEA	SS- MOPSO	MMODE_ CSCD	MP- MMEA	MMOEA /DC	MMODE_ ICD	MMEA- WI	HREA
3	2	1.89E+01	2.52E+01	7.05E+01	7.48E+01	1.79E+00	1.71E+00	1.22E+01	9.46E+01	4.41E+02	4.22E+01	2.24E+00	1.15E+01	6.13E+01	1.43E+01	6.61E+01
	4	5.29E+01	5.65E+01	1.08E+02	9.45E+01	1.03E+00	1.42E+00	1.39E+01	6.37E+01	4.69E+02	4.64E+01	2.25E+00	7.50E+00	7.08E+01	1.10E+01	1.14E+01
	8	6.31E+01	6.48E+01	1.36E+02	9.75E+01	8.18E-01	1.24E+00	1.10E+01	6.43E+01	4.76E+02	3.53E+01	2.27E+00	6.13E+00	8.14E+01	9.78E+00	1.94E+01
	10	6.74E+01	6.78E+01	1.42E+02	9.87E+01	7.61E-01	1.17E+00	1.00E+01	6.41E+01	4.82E+02	3.29E+01	2.28E+00	6.06E+00	8.86E+01	9.59E+00	2.02E+01
	20	6.94E+01	6.67E+01	1.67E+02	1.10E+02	4.79E-01	1.24E+00	1.08E+01	6.46E+01	5.12E+02	4.01E+01	2.30E+00	6.59E+00	1.17E+02	8.56E+00	4.01E+01
4	2	1.82E+01	2.77E+01	6.91E+01	7.25E+01	1.79E+00	1.55E+00	1.56E+01	9.57E+01	4.37E+02	4.60E+01	2.12E+00	1.22E+01	5.40E+01	1.53E+01	6.73E+01
	4	5.91E+01	5.86E+01	1.07E+02	9.40E+01	9.92E-01	1.42E+00	2.40E+01	6.34E+01	4.68E+02	4.39E+01	2.22E+00	7.64E+00	6.78E+01	1.17E+01	1.16E+01
	8	6.38E+01	6.52E+01	1.37E+02	9.88E+01	8.09E-01	1.27E+00	1.53E+01	6.42E+01	4.76E+02	3.47E+01	2.31E+00	6.32E+00	7.83E+01	1.04E+01	1.88E+01
	10	6.62E+01	6.64E+01	1.43E+02	9.94E+01	7.08E-01	1.26E+00	1.02E+01	6.42E+01	4.83E+02	3.19E+01	2.27E+00	6.38E+00	8.59E+01	1.06E+01	2.19E+01
	20	6.89E+01	6.74E+01	1.68E+02	1.11E+02	5.70E-01	1.28E+00	1.03E+01	6.46E+01	5.14E+02	3.84E+01	2.32E+00	6.98E+00	1.13E+02	8.75E+00	3.72E+01
	2	1.72E+01	1.87E+01	6.39E+01	6.76E+01	2.37E+00	1.57E+00	1.13E+01	9.74E+01	4.34E+02	3.94E+01	2.05E+00	1.31E+01	4.73E+01	1.61E+01	6.78E+01
	4	6.04E+01	5.72E+01	1.07E+02	9.35E+01	9.98E-01	1.40E+00	1.57E+01	6.35E+01	4.68E+02	4.15E+01	2.18E+00	7.89E+00	6.63E+01	1.20E+01	1.20E+01
6	8	6.27E+01	6.41E+01	1.40E+02	9.99E+01	7.94E-01	1.28E+00	1.24E+01	6.40E+01	4.84E+02	3.67E+01	2.21E+00	6.42E+00	7.84E+01	1.07E+01	1.86E+01
	10	6.65E+01	6.51E+01	1.47E+02	1.02E+02	6.96E-01	1.25E+00	1.03E+01	6.41E+01	4.90E+02	3.10E+01	2.23E+00	6.46E+00	8.44E+01	1.06E+01	2.13E+01
	20	6.86E+01	6.70E+01	1.70E+02	1.05E+02	5.18E-01	1.25E+00	1.03E+01	6.46E+01	5.21E+02	3.80E+01	2.27E+00	7.02E+00	1.13E+02	9.18E+00	3.71E+01
8	2	1.52E+01	2.01E+01	6.62E+01	6.88E+01	1.73E+00	1.52E+00	1.16E+01	9.83E+01	4.59E+02	3.95E+01	1.99E+00	1.30E+01	4.68E+01	1.66E+01	6.75E+01
	4	5.94E+01	5.35E+01	1.11E+02	9.57E+01	1.02E+00	1.38E+00	1.72E+01	6.37E+01	5.55E+02	4.14E+01	2.12E+00	7.83E+00	6.58E+01	1.24E+01	1.16E+01
	8	6.43E+01	6.32E+01	1.44E+02	1.02E+02	7.93E-01	1.26E+00	1.38E+01	6.41E+01	4.87E+02	3.52E+01	2.16E+00	6.40E+00	7.80E+01	1.13E+01	1.91E+01
	10	6.32E+01	6.46E+01	1.49E+02	1.02E+02	7.25E-01	1.20E+00	1.07E+01	6.43E+01	4.94E+02	3.15E+01	2.18E+00	6.45E+00	8.52E+01	1.09E+01	2.08E+01
	20	6.59E+01	6.75E+01	1.65E+02	9.74E+01	5.10E-01	1.24E+00	1.08E+01	6.50E+01	5.18E+02	3.76E+01	2.21E+00	7.03E+00	1.12E+02	9.83E+00	3.63E+01