

# Escape Ratio Contributes More Than Fluorescence Yield to SIF–GPP Relationship Over Crops and Rainforest

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**Abstract**—Solar-induced chlorophyll fluorescence (SIF) is an effective indicator to track the gross primary productivity (GPP). However, there is still a lack of a clear understanding for the contribution of physiological and structural factors to the SIF–GPP relationship at the canopy scale. To quantify the influence of different SIF components, particularly the photon escape ratio ( $f_{\text{esc}}$ ) and fluorescence yield ( $\Phi_F$ ), on the SIF–GPP relationship, this study evaluated the performance of various vegetation indices (VIs), SIF components, light use efficiency (LUE), and GPP over two typical biomes (crops and rainforest), using a range of satellite remote sensing products. In August of each year from 2018 to 2020, both SIF and GPP over United States (U.S.) Corn Belt are higher than those over the Amazon rainforest, attributed to the consistent pattern of higher  $f_{\text{esc}}$  and LUE over crops than over rainforest, as well as  $\Phi_F$ . Furthermore, the structural signals represented by  $f_{\text{esc}}$  ( $R = 0.41\text{--}0.64$ ) can better capture the LUE variations than  $\Phi_F$  ( $R = 0.10\text{--}0.30$ ) for each biome. This study highlights that  $f_{\text{esc}}$ , determined by canopy structure, has great potential to capture LUE and GPP changes within and across biomes.

**Index Terms**—Canopy structure, escape ratio, gross primary productivity (GPP), light use efficiency (LUE), solar-induced chlorophyll fluorescence (SIF), vegetation indices (VIs).

## I. INTRODUCTION

ACCURATELY estimating gross primary productivity (GPP), which represents the overall quantity of carbohydrates synthesized by plants via photosynthesis, is essential for investigating terrestrial carbon cycles [1]. Advances in remote sensing of solar-induced chlorophyll fluorescence (SIF) have shown great potential of capturing GPP at large scales. SIF is an optical signal emitted within the spectral wavelength range of 650–850 nm from the chlorophyll *a* molecule present in vegetation [2]. The existing studies have indicated that SIF is closely related to GPP at the leaf, canopy, and ecosystem scales [3], [4].

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Mechanically, SIF at the top of the canopy can be separated into three components: absorbed photosynthetically active radiation (APAR), physiological SIF emission yield of the whole canopy ( $\Phi_F$ ), and the escape ratio of photons from the canopy ( $f_{\text{esc}}$ ). Previous studies suggested that the relationship between SIF and GPP is determined jointly by the shared term of APAR and  $\text{SIF}_{\text{yield}}$  ( $\text{SIF}_{\text{yield}} = \text{SIF}/\text{APAR}$ )–light use efficiency (LUE) relationship [5]. At the canopy scale, APAR can explain the linear relationship between GPP and SIF to some extent [6]. However, how the  $\text{SIF}_{\text{yield}}$ –LUE relationship varies and further influences the SIF–GPP correlation are still unclear.  $\text{SIF}_{\text{yield}}$  is jointly determined by  $\Phi_F$  and  $f_{\text{esc}}$ . Seasonally, a positive correlation between  $f_{\text{esc}}$  and LUE contributes to the SIF–GPP relationship, while  $\Phi_F$  shows a low correlation to LUE at a few crop sites [5]. Nonetheless, under drought conditions,  $\Phi_F$  can track variations in LUE, assisting SIF in estimating GPP [7]. These researches have demonstrated that both  $\Phi_F$  and  $f_{\text{esc}}$  are related to LUE, thereby affecting the estimation of GPP by SIF. However, the existing investigations are mostly at site scales and mainly focus on structurally uniform crops, with a lack of analysis at regional scales and complexly structured ecosystems, such as rainforest. The relative contributions of  $\Phi_F$  and  $f_{\text{esc}}$  to the SIF–GPP relationship at large scales remain underinvestigated, particularly given that the SIF–GPP relationship exhibits variations among various biomes [8].

Previous research revealed that the shadows generated by complex forest structure had larger impacts on SIF magnitude, resulting in the SIF of United States (U.S.) Corn Belt being larger than that of the Amazon rainforest in August, despite the latter having a larger leaf area index (LAI) [9]. Similarly, GPP also exhibited higher values in U.S. Corn Belt compared to the Amazon rainforest [10], showing a similar pattern to SIF. Nevertheless, the underlying drivers of the similar spatial patterns of SIF and GPP in these two biomes and the roles of  $\Phi_F$  and  $f_{\text{esc}}$  are still unclear.

The objectives of this study are twofold: first, to investigate the roles of  $\Phi_F$  and  $f_{\text{esc}}$  in the contrasting pattern across biomes with distinct canopy structures (i.e., U.S. Corn Belt and the Amazon rainforest); and second, to evaluate the contributions of  $\Phi_F$  and  $f_{\text{esc}}$  to the  $\text{SIF}_{\text{yield}}$ –LUE relationship within each biome. Specifically, we analyzed and compared SIF, SIF components, GPP, LUE, and various vegetation indices (VIs) within and across the two biomes using a series of remote sensing products.

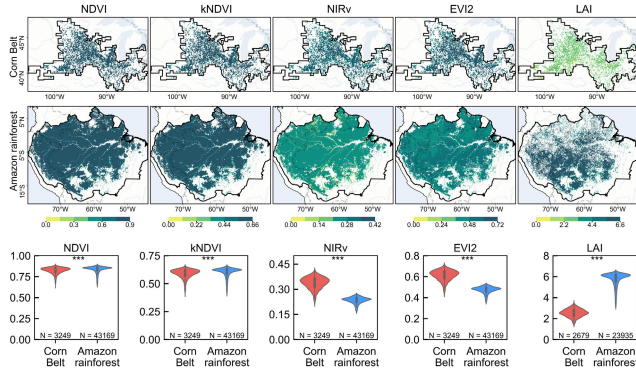


Fig. 1. Comparison of NDVI, kNDVI, NIRv, EVI2, and LAI across U.S. Corn Belt and the Amazon rainforest. The violin plots exhibit the quartiles and mean values of variables, showcasing their distribution patterns. Statistical significance level is denoted as: “\*\*\*\*” for  $p < 0.001$ , “\*\*\*” for  $p < 0.01$ , “\*\*” for  $p < 0.05$ , “ns” for  $p \geq 0.05$ , and “N” represents the number of samples.

TABLE I  
DETAILS OF THE VEGETATION INDICES IN THIS STUDY

Abbreviation	Name	Equation and derivation
NDVI	Normalized difference vegetation index	$NDVI = \frac{NIR - Red}{NIR + Red}$
kNDVI	Kernel NDVI	$kNDVI = \tanh(NDVI^2)$
NIRv	Near-infrared reflectance of vegetation	$NIRv = \frac{NIR - Red}{NIR + Red} \times NIR$
EVI2	Two-band enhanced vegetation index	$EVI2 = 2.5 \times \frac{NIR - Red}{NIR + 2.4 \times Red + 1}$

## II. MATERIALS AND METHODS

### A. Study Area

The Amazon rainforest spans the latitudes of 19.6°S–8.6°N and longitudes of 79.7°W–44°W (see Fig. 1). This biome is primarily characterized by its evergreen forest cover and stands as one of the most important land carbon sinks [1].

U.S. Corn Belt is situated between latitudes 37.4°N and 47.7°N and longitudes 105.1°W and 82.1°W (see Fig. 1). In this region, corn and soybeans were uniformly cultivated [19].

### B. Datasets and Data Processing

The MODIS MCD43A1.061 product provides the isotropic, volumetric, and geometric model parameters at red (620–670 nm) and NIR (841–876 nm) bands to calculate reflectance at a fixed view geometry of  $VZA = 0^\circ$  (view zenith angle) and solar geometry of  $SZA = 45^\circ$  (solar zenith angle) with the resolution of daily temporally and 500 m spatially [15], [33]. The normalized reflectance was used to ascertain the four VIs listed in Table I [31].

1) *FPAR and LAI Products*: The MODIS MCD15A2H.061 product leverages multiple spectral bands from Terra and Aqua satellite data to provide estimates of the fraction of

photosynthetically active radiation (FPAR) and LAI with a resolution of eight day and 500 m [11]. We used MODIS products with good quality assurance (QA)/quality control (QC) flags.

2) *ERA5-Land*: The ERA5 dataset is released by the European Center for Medium-Range Weather Forecasts. The photosynthetically active radiation (PAR) was estimated from this product in all sky conditions [12].

3) *TROPOMI SIF*: The Copernicus Sentinel-5P TROPOMI mission provides SIF observations with enhanced spatiotemporal resolution [13], [14]. To ensure data quality, observations with far-red (740 nm) daily SIF values not within  $-2$ – $4$   $mW/m^2/sr/nm$  and SIF signal uncertainty greater than  $0.55$   $mW/m^2/sr/nm$  were excluded. Besides, any SIF observations with cloud fraction over 50% were excluded [23].

4) *CEDAR GPP*: The effect of atmospheric  $CO_2$  on photosynthesis, known as the  $CO_2$  fertilization effects, increases the canopy-level GPP and LUE [32]. The CEDAR GPP product incorporates this effect using both theoretical and data-driven approaches to generate monthly GPP estimations with a spatial resolution of  $0.05^\circ$  [16].

5) *X-BASE GPP*: The X-BASE product is the global product of the upgraded FLUXCOM-X framework, providing high-resolution GPP data. In this study, the product at a monthly  $0.05^\circ$  resolution was used. The variability of X-BASE GPP has been demonstrated to be highly consistent with TROPOMI SIF variability [17].

6) *Land Cover Datasets*: This study used the International Geosphere-Biosphere Program classification layer in the MCD12Q1 product to filter uniform pixels of two different biomes [18]. In the Amazon rainforest, only evergreen broad-leaved forest with tree coverage  $>60\%$  was selected, and in U.S. Corn Belt, only cultivated land accounting for at least 60% of the land was selected. The USDA NASS Cropland data layer (CDL) was further employed to filter and select only the arable land, where corn was planted that year, which has been shown to classify corn in the Midwest with an accuracy of up to 95% [19].

All data were aggregated monthly temporally and  $0.1^\circ$  spatially, confined to August of each year from 2018 to 2020.

Additionally, to ensure data quality, the top and bottom 2% of all data were removed consistently to mitigate the impact of outliers on the results.

### C. Methods

1) *BRDF Correction*: The directional reflectance is highly sensitive to the sun-target-sensor geometry. The RossThick-LiTransit (RTLT) was employed to normalize this effect to nadir view ( $VZA = 0^\circ$  and  $SZA = 45^\circ$ ), preventing the potential misinterpretation of variations induced by geometry as physiological signals. The RTLT kernel-driven semi-empirical BRDF model has been evidenced to show good fitting capabilities, delivering more precise bidirectional reflectance [20], [21]

$$R(\theta_s, \theta_v, \varphi, \lambda) = f_{iso}(\lambda) + f_{vol}(\lambda) K_{vol}(\theta_s, \theta_v, \varphi) + f_{geo}(\lambda) K_{geo}(\theta_s, \theta_v, \varphi) \quad (1)$$

where  $R(\theta_s, \theta_v, \varphi, \lambda)$  represents the reflectance at a given wavelength  $\lambda$ , considering the SZA  $\theta_s$ , the VZA  $\theta_v$ , and the relative azimuth angle (RAA)  $\varphi$ . The reflectance was obtained by linearly combining three scattering components, expressed as the product of the weights and the corresponding kernels.

The isotropic kernels have a constant weight of 1. The weights  $f_{\text{vol}}(\lambda)$  and  $f_{\text{geo}}(\lambda)$  represent the empirical kernel parameters at wavelength  $\lambda$ . The kernels  $K_{\text{vol}}(\theta_s, \theta_v, \varphi)$  and  $K_{\text{geo}}(\theta_s, \theta_v, \varphi)$  represent the volume scattering kernel RossThick and the geometric-optical surface scattering kernel LiTransit, respectively.

2) *Disentangle the Structural and Physiological Signals of the Canopy-Level SIF*: The observed canopy-level SIF is primarily determined by three mechanistic factors: APAR,  $\Phi_F$ , and  $f_{\text{esc}}$ . SIF is thus defined as

$$\text{SIF} = \text{APAR} \times \Phi_F \times f_{\text{esc}}. \quad (2)$$

APAR denotes the total PAR absorbed by vegetation for photosynthesis and growth and can be estimated by combining the FPAR from the MCD15A2H.061 product and PAR from the ERA-5 reanalysis

$$\text{APAR} = \text{PAR} \times \text{FPAR}. \quad (3)$$

$f_{\text{esc}}$  is a new physical parameter introduced in radiative transfer theory. In this study, a previously well-validated method based on the spectral invariants theory was adopted, whereby  $f_{\text{esc}}$  in the far-red band was estimated through [22]

$$f_{\text{esc}} \approx \frac{\text{NIRv}}{\text{FPAR}}. \quad (4)$$

$\Phi_F$  was calculated using SIF divided by NIRvP, which is the substitute for nonphysiological signals [23]. Crucially, noting that NIRv should be adjusted to the same direction as observed SIF before multiplying by instantaneous PAR for the NIRvP estimation

$$\Phi_F \approx \frac{\text{SIF}}{\text{NIRv} \times \text{PAR}}. \quad (5)$$

3) *Estimating LUE*: GPP is expressed as a semi-empirical LUE framework comprising APAR and LUE [24]. Then, LUE was calculated as

$$\text{LUE} = \frac{\text{GPP}}{\text{APAR}}. \quad (6)$$

4) *Statistical Analysis*: Across biomes, the analysis of variance (ANOVA) was primarily employed to compare the mean values of data between biomes for statistically significant differences.

Within each biome, correlation evaluations were conducted utilizing the Pearson correlation coefficient ( $R$ ), with the assessment of statistical significance executed through a two-sided  $t$ -test, employing a 95% confidence interval. Linear regression analysis between variables was also conducted.

### III. RESULTS

#### A. $f_{\text{esc}}$ Distorts the Interpretation of VIs

Except for NDVI and kNDVI, which show minor differences between the two biomes, with the values of (mean  $\pm$  s.d.,  $0.82 \pm 0.04$ ,  $0.59 \pm 0.04$ ) in U.S. Corn Belt and

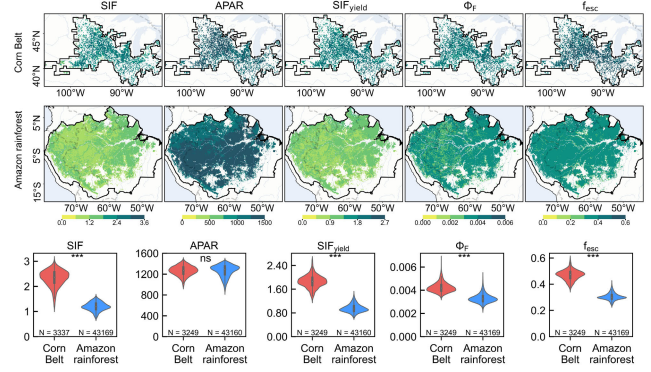


Fig. 2. Comparison of SIF ( $\text{mW}/\text{m}^2/\text{nm}/\text{sr}$ ), APAR ( $\mu\text{mol}/\text{m}^2/\text{s}$ ),  $\text{SIF}_{\text{yield}}$  ( $\text{mW}\cdot\text{s}/\mu\text{m}/\text{sr}/\mu\text{mol}$ ),  $\Phi_F$  ( $\text{mW}\cdot\text{s}/\text{nm}/\text{sr}/\mu\text{mol}$  photons), and  $f_{\text{esc}}$  (unitless) between U.S. Corn Belt and the Amazon rainforest.

( $0.83 \pm 0.04$ ,  $0.60 \pm 0.05$ ) in the Amazon rainforest, respectively, NIRv ( $0.34 \pm 0.04$ ) and EVI2 ( $0.61 \pm 0.05$ ) exhibit higher values in U.S. Corn Belt compared to the Amazon rainforest characterized by complex canopy structure, where NIRv ( $0.23 \pm 0.02$ ) and EVI2 ( $0.47 \pm 0.03$ ) were lower (see Fig. 1).

Previous studies have demonstrated the hypothesis that complex canopy structure can distort the interpretation of vegetation greenness [9]. Our research findings also demonstrate the important role of  $f_{\text{esc}}$ , indicating that high VIs and low LAI ( $2.53 \pm 0.38$ ) in uniform crops but with high  $f_{\text{esc}}$  ( $0.47 \pm 0.04$ ), while low VIs and high LAI ( $5.75 \pm 0.67$ ) in rainforest with low  $f_{\text{esc}}$  ( $0.30 \pm 0.03$ ) (see Fig. 2).

#### B. Contrasting Patterns of SIF and SIF Components

The APAR over U.S. Corn Belt ( $1264.44 \mu\text{mol}/\text{m}^2/\text{s}$ ) and the Amazon rainforest ( $1262.50 \mu\text{mol}/\text{m}^2/\text{s}$ ) exhibits minimal difference. SIF and  $\text{SIF}_{\text{yield}}$ , as well as  $\Phi_F$  and  $f_{\text{esc}}$ , consistently show that U.S. Corn Belt is higher than the Amazon rainforest, albeit to varying degrees (see Fig. 2).

The SIF of U.S. Corn Belt ( $2.32 \text{ mW}/\text{m}^2/\text{nm}/\text{sr}$ ) exceeds that of the Amazon rainforest ( $1.20 \text{ mW}/\text{m}^2/\text{nm}/\text{sr}$ ) by 94.5%. Similarly,  $\text{SIF}_{\text{yield}}$  in the former ( $1.86 \text{ mW}\cdot\text{s}/\mu\text{m}/\text{sr}/\mu\text{mol}$ ) also surpasses the latter ( $0.95 \text{ mW}\cdot\text{s}/\mu\text{m}/\text{sr}/\mu\text{mol}$ ) by 94.7%. Although the relative differences in  $\Phi_F$  (28.5%) and  $f_{\text{esc}}$  (53.9%) were not as pronounced as those in SIF and  $\text{SIF}_{\text{yield}}$ , it still manifests that  $\Phi_F$  and  $f_{\text{esc}}$  of the former ( $0.0042 \text{ mW}\cdot\text{s}/\text{nm}/\text{sr}/\mu\text{mol}$ ,  $0.47$ ) were higher than those of the latter ( $0.0033 \text{ mW}\cdot\text{s}/\text{nm}/\text{sr}/\mu\text{mol}$ ,  $0.30$ ) (see Fig. 2).

#### C. GPP and LUE Differences Between Biomes

Between the two biomes, GPP and LUE show significant differences (ANOVA:  $p < 0.001$ ) (see Fig. 3). The X-BASE GPP indicates that U.S. Corn Belt was approximately twice that of the Amazon rainforest, yielding a similar ratio of 2.00 for LUE. Similarly, both CEDAR GPP and CEDAR LUE show that the crops exceeded the rainforest, with GPP and LUE values exhibiting ratios of 1.46 and 1.44, respectively (see Fig. 3).

CEDAR GPP shows higher values in the rainforest than X-BASE GPP, with correspondingly higher LUE, which may



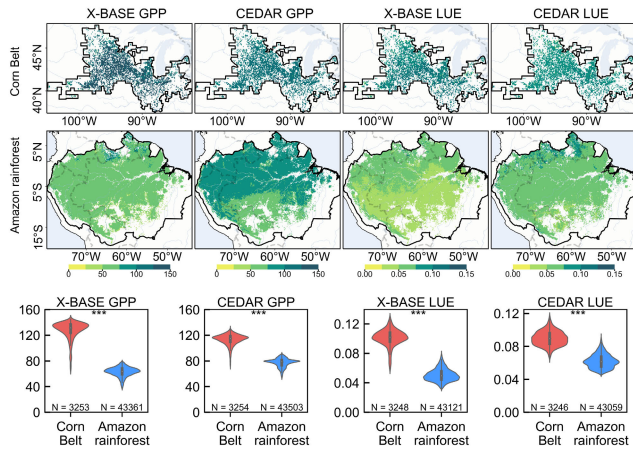


Fig. 3. Comparison of GPP ( $\mu\text{mol}/\text{m}^2/\text{s}$ ) and LUE ( $\text{mol CO}_2/\text{mol photons}$ ) between U.S. Corn Belt and the Amazon rainforest. The X-BASE LUE and CEDAR LUE were calculated from the corresponding GPP products.

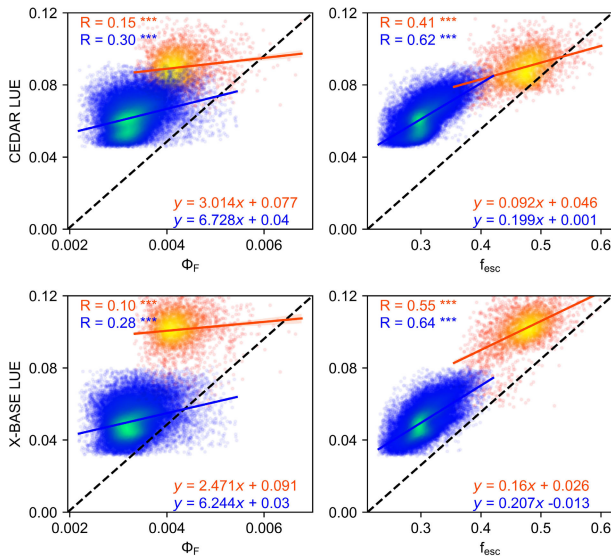


Fig. 4. Comparison of the correlation of  $\Phi_F$  ( $\text{mW}\cdot\text{s}/\text{nm}/\text{sr}/\mu\text{mol photons}$ ) and  $f_{\text{esc}}$  (unitless) with CEDAR LUE and X-BASE LUE for 2018–2020, in August, in U.S. Corn Belt (the red one) and the Amazon rainforest (the blue one). The error bars represent 95% confidence intervals. LUE is in the units of  $\text{mol CO}_2/\text{mol photons}$ .

be caused by considering the  $\text{CO}_2$  fertilization effect favoring GPP estimation for C3 vegetation [16].

#### D. Separating the Structural and Physiological Contributions

To directly assess the contributions of each component within each biome, the correlations between  $\Phi_F$ ,  $f_{\text{esc}}$ , and LUE were further quantified (see Fig. 4). Our analysis revealed that in both biomes, the correlations between  $f_{\text{esc}}$  and LUE (0.41–0.64) were greater than those between  $\Phi_F$  and LUE (0.10–0.30). These findings revealed that there was a moderate positive correlation between  $f_{\text{esc}}$  and LUE, while the correlation between  $\Phi_F$  and LUE was relatively weak in each biome.

### IV. DISCUSSION

#### A. Analyzing Experimental Results

In comparing the SIF patterns between the two biomes, this study shows that APAR differences are minimal, while  $\text{SIF}_{\text{yield}}$

is higher in U.S. Corn Belt and relatively lower in the Amazon rainforest. The  $\text{SIF}_{\text{yield}}$  pattern was more similar to SIF than to APAR, suggesting a greater contribution of  $\text{SIF}_{\text{yield}}$  to SIF, consistent with previous studies [25]. This performance was due to the combined contributions of  $f_{\text{esc}}$  and  $\Phi_F$ , both of which were higher in U.S. Corn Belt than in the Amazon rainforest [26]. The difference in  $f_{\text{esc}}$  (53.9%) between the two biomes was larger than that of  $\Phi_F$  (28.5%) and more closely matched the difference in SIF (94.5%), and thus,  $f_{\text{esc}}$  difference may contribute more to the  $\text{SIF}_{\text{yield}}$  and SIF patterns. For GPP, the similar APAR between biomes indicates that differences in GPP among biomes were mainly controlled by LUE. This analysis suggests that the contrasting SIF–GPP patterns were determined by a complicated relationship between  $\Phi_F$ ,  $f_{\text{esc}}$ , and LUE [29].

In each biome, there was a highly positive correlation between  $f_{\text{esc}}$  and LUE in both the structurally uniform crops and the complex rainforest. This correlation surpassed that between  $\Phi_F$  and LUE, consistent with earlier studies focused on the site scales and crops [5], while now corroborated across regional scales and complexly structured ecosystems. Moreover, building upon past findings that a positive  $f_{\text{esc}}$ –LUE relationship can strengthen the SIF–GPP relationship [30], this regional investigation reveals the importance of  $f_{\text{esc}}$  in explaining SIF–GPP variations across different ecosystems, further underscoring the relationship between  $f_{\text{esc}}$  and LUE, which may benefit the large-scale GPP estimations.

From the perspective of vegetation physiology, photosynthetic activity and even leaf shape at the leaf level will change under different conditions (e.g., light saturation, stress) [27], [28]. Together, the responses of the individual leaves across the canopy form the coupling mode of  $f_{\text{esc}}$ ,  $\Phi_F$ , and LUE. Besides, product uncertainties remain, especially under different environmental conditions, and these uncertainties and their further effects should be taken into account. For example, FPAR directly influences APAR, which further affect the quantification of the relationship between GPP and SIF [34]. During the study period, the regions were not subjected to any large-scale environmental stresses, and thus, further investigation is needed to explore the corresponding SIF–GPP patterns during stress conditions.

#### B. Limitations and Prospects

Temporally, due to the short operational span of TROPOMI, the analysis was restricted from 2018 to 2020. Moreover, this study focused on August, a period of peak ecosystem activity for U.S. Corn Belt (July and August) in the northern hemisphere, to enable the comparisons of different regions globally at the same time. Further extension of longer time series will allow us to explore interannual and long-term changes in vegetation canopy structure and physiological components, contributing to a more comprehensive understanding.

Spatially, this study mainly focuses on two typical biomes: evergreen broadleaf forest and corn belt. In future, we plan to incorporate additional biomes under varying climate zones to study potential differences in the ability of  $f_{\text{esc}}$  capturing LUE, which will help us better understand the SIF–GPP relationship and benefit the large-scale GPP mapping.

## V. CONCLUSION

Starting from the perspective that  $f_{\text{esc}}$  distorts the interpretation of VIs, we conducted a comparative analysis of SIF, SIF components, GPP, and LUE in two typical biomes characterizing different canopy complexities. This study reveals that SIF and GPP in summer crops were higher than those in tropical rainforest, with both  $f_{\text{esc}}$  and  $\Phi_F$  contributing positively to this pattern. Furthermore, both  $\Phi_F$  and  $f_{\text{esc}}$  within each biome show positive correlations with LUE, while the correlation between  $f_{\text{esc}}$  (0.41–0.64) and LUE surpassed that of  $\Phi_F$  (0.10–0.30) and LUE, indicating that  $f_{\text{esc}}$  better captured the variations in LUE. This letter emphasizes the important contribution of  $f_{\text{esc}}$  to the SIF–GPP relationship. We advocate for increased attention to  $f_{\text{esc}}$ , representing canopy structure importantly.

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