Worksheet Week 21

Problems

- **Q1.** X and Y are two (binary) random variables. If X and Y are independent, then P(X,Y) = P(X)P(Y)
 - (a) Give an example of two random variables that are independent.
 - (b) Complete the probability table below in such way that the variables X and Y are independent.

	X = 0	X = 1
Y = 0		
Y = 1		

(c) Determine the missing entries (a, b) of the joint distribution in such a way that the variables X and Y are again independent.

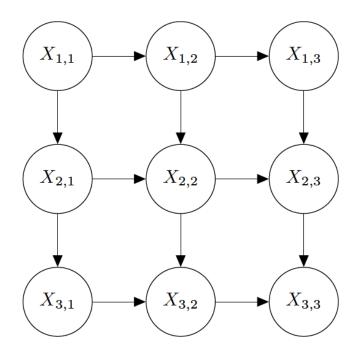
$$P(Y = 0, X = 0) = 0.1$$

$$P(Y = 0, X = 1) = 0.3$$

$$P(Y = 1, X = 0) = a$$

$$P(Y = 1, X = 1) = b$$

Q2. Consider the following Bayesian network:



- (a) Which random variables are independent of $X_{3,1}$?
- (b) Which random variables are independent of $X_{3,1}$ given $X_{1,1}$?
- Q3. Solve the questions on slides 42 and 44 of the lecture slides.
- **Q4.** A patient can have a symptom, S, that is caused by two different diseases, A and B. It is known that the presence of a gene G is important in the manifestation of disease A. The Bayes net and conditional probability tables are shown in Figure 2.

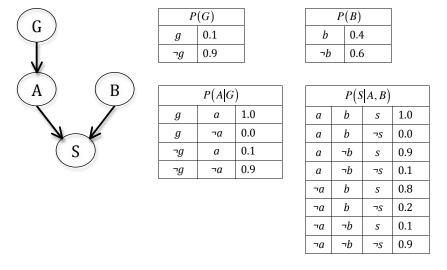


Figure 1: Bayes net and probability tables for Q5

(a) What is the probability that a patient has disease A

- (b) What is the probability that a patient has disease A if we know that the patient has disease B
- (c) What is the probability that a patient has disease A if we know that the patient has disease B AND symptom S