

# Neutron deep-penetration calculations & shielding design of proton therapy accelerators

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7<sup>th</sup> Int. Workshop on Radiation Safety at Synchrotron  
Radiation Sources (RADSYNCH2013)

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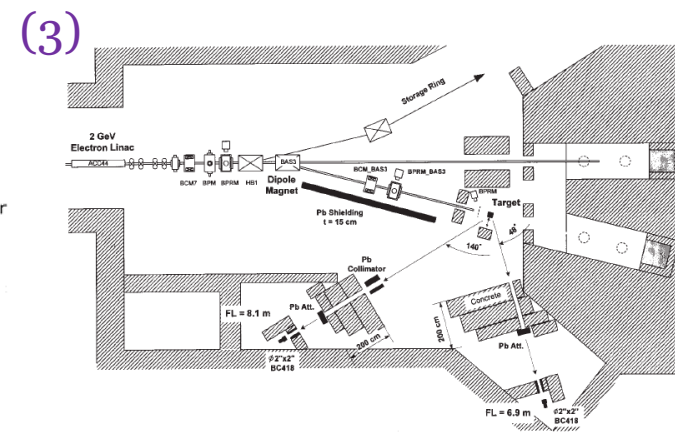
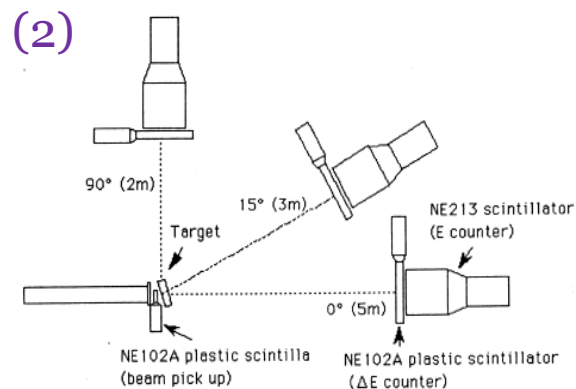
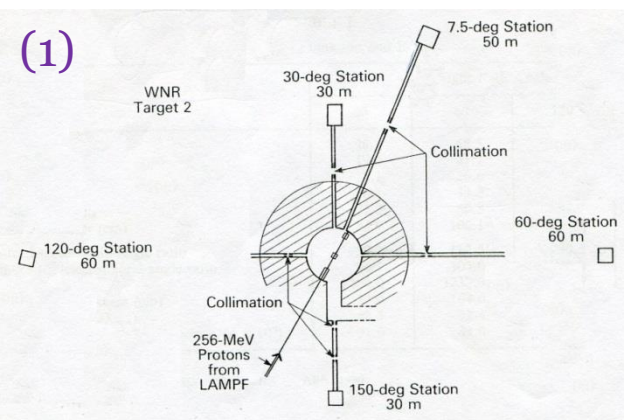
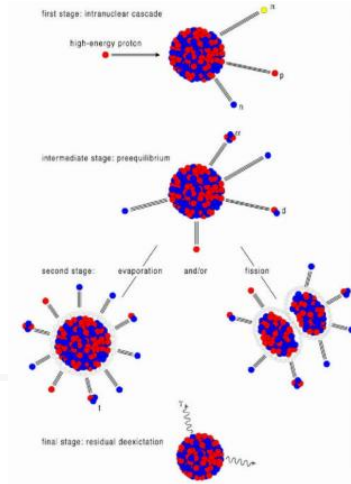
# New accelerators in Taiwan

- Taiwan Photon Source
  - NSRRC, Hsinchu
  - 3 GeV electron synchrotron
  - Installation 2013, commissioning 2014
- Proton therapy center
  - Chang Gung Memorial Hospital, Linkou
  - 235 MeV proton cyclotron
  - Commissioning 2013, clinical trial 2014
- Heavy ion therapy center
  - Veterans General Hospital, Taipei
  - 400 MeV/A carbon cyclotron
  - In planning



# Accelerator shielding

- Key issues in shielding design
  - Neutrons produced from hadronic cascade or EM cascade with photonuclear interaction are dominant dose component
  - Neutron production and deep-penetration calculations
- Selected experiments on thick-target neutron yield
  - 256 MeV proton on iron (Meier et al., 1990)<sup>1</sup>
  - 400 MeV/A carbon on copper (Nakamura et al., 2006)<sup>2</sup>
  - 2.04 GeV electron on copper (Lee et al., 2005)<sup>3</sup>

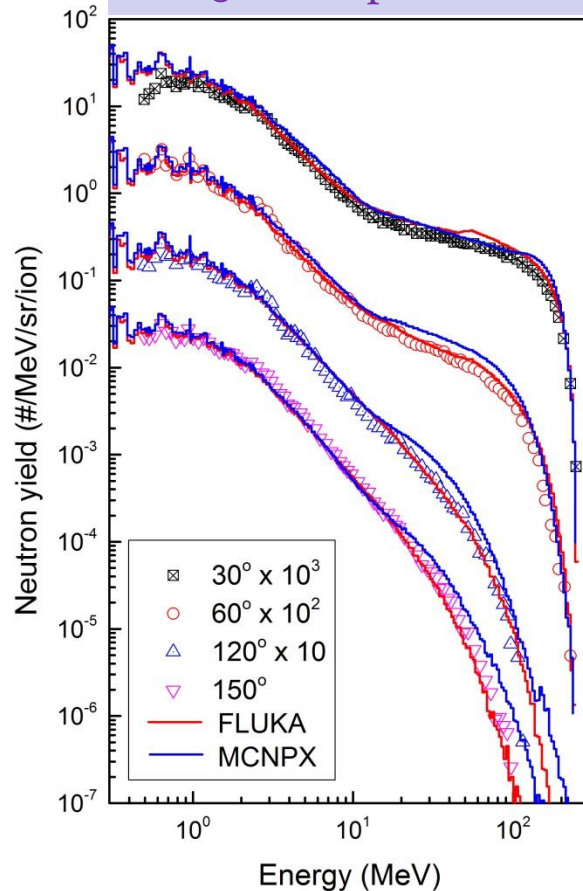


# Benchmark calculations for double differential neutron yield

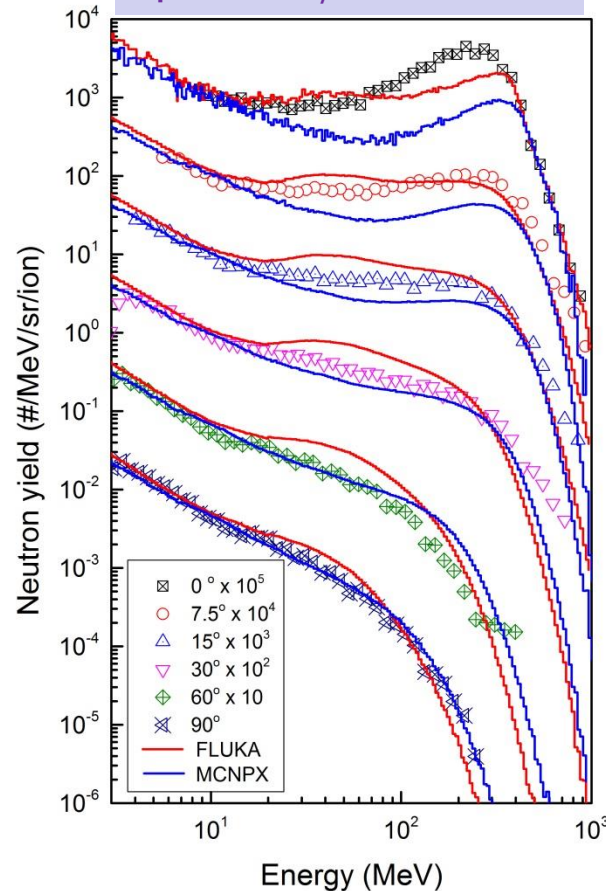
FLUKA v2011.2 & MCNPX v2.7.0

- Comparisons of experimental results with calculations

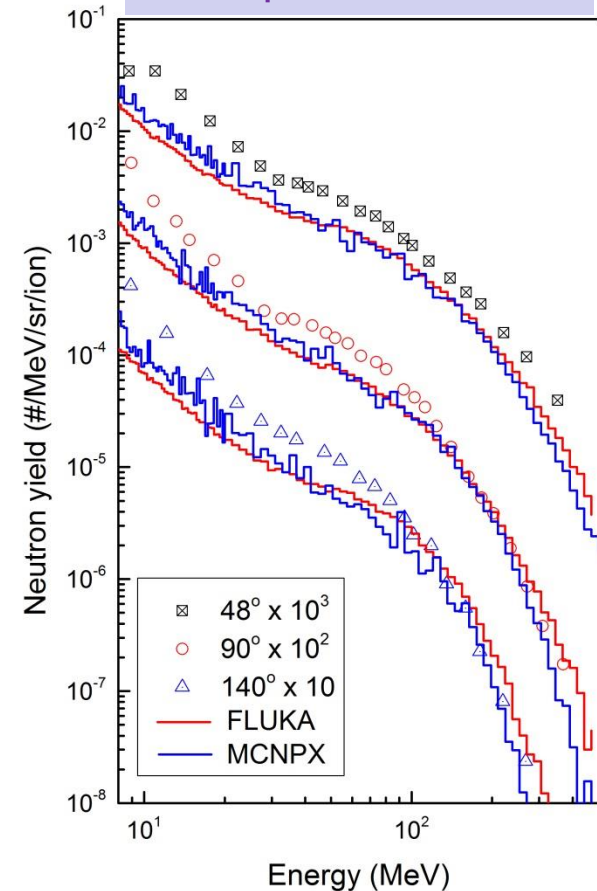
256 MeV p on Fe



400 MeV/A  $^{12}\text{C}$  on Cu



2.04 GeV  $e^-$  on Cu





# Ranges of neutron source intensities

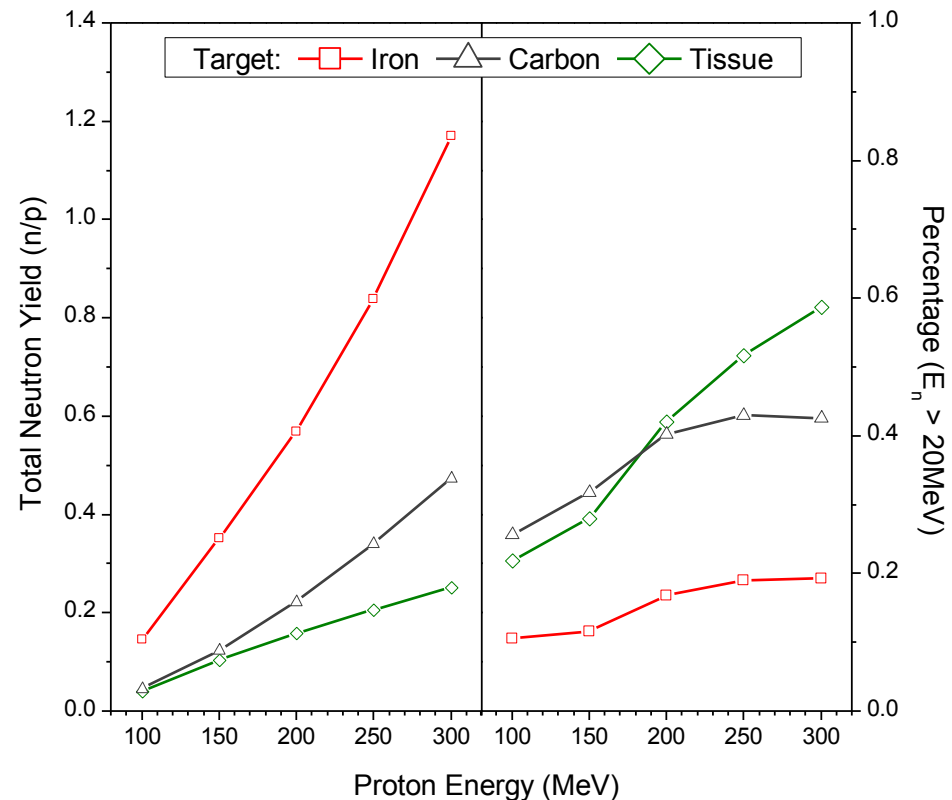
- For three accelerators of main concern
  - ✓ 235 MeV proton cyclotron
  - ✓ 400 MeV/A carbon cyclotron
  - ✓ 3.0 GeV electron synchrotron
  - Total number of neutrons produced per incident primary particle (n/p) calculated by FLUKA and MCNPX:

Beam	Target	FLUKA	MCNPX
235 MeV proton	Iron	$0.70 \pm 0.13\%$	$0.79 \pm 0.24\%$
400 MeV/A carbon	Copper	$9.02 \pm 0.14\%$	$5.92 \pm 0.24\%$
3.0 GeV electron	Copper	$0.63 \pm 0.36\%$	$0.51 \pm 0.21\%$

# Neutron production from proton bombardment

- For various proton energies and target materials
  - LHS: total neutron yield
  - RHS: percentage of high-energy neutrons ( $E_n > 20 \text{ MeV}$ )

- Neutron yield increases significantly as increasing proton energies, especially for high-Z targets.
- Low-Z targets cause harder neutron spectra, i.e. more forward-peaked neutrons and anisotropy of dose distribution.





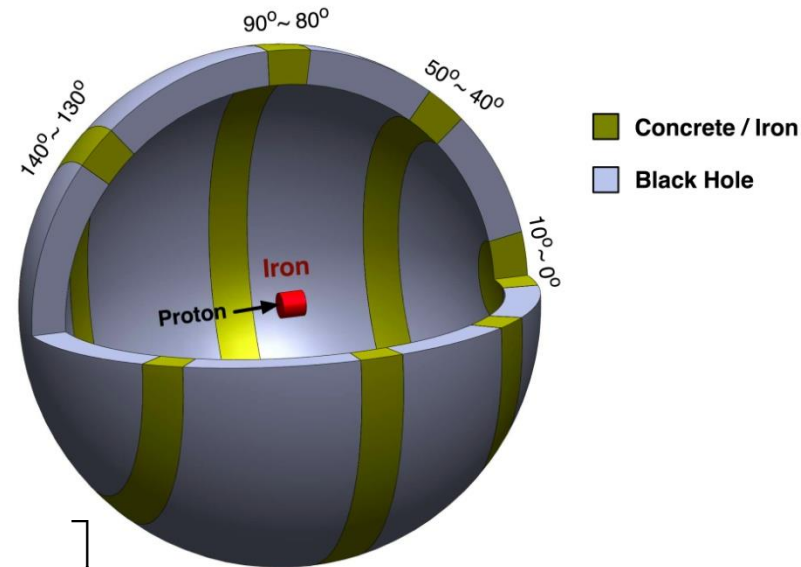
# Parameters for shielding design

Point- source line-of-sight model

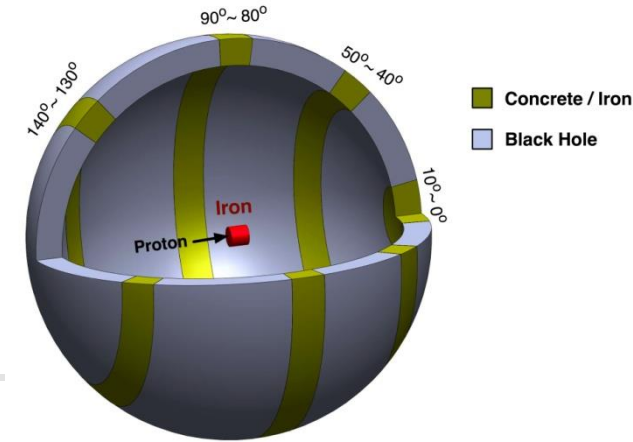
- A simplified method ~

$$H(E_p, \theta, d / \lambda_\theta) = \frac{H_0(E_p, \theta)}{r^2} \exp \left[ - \frac{d}{\lambda_\theta \cdot g(\alpha)} \right] + \dots$$

- Source term  $H_0$  and attenuation length  $\lambda_\theta = ?$ 
  - Literature data (a wide range of variability)
  - Radiation transport calculations (neutron deep penetration)
- Calculation model (Agosteo et al., 2007)
  - Primary beam: 200 MeV protons
  - Shielding material: concrete & iron
  - Use **FLUKA** & **MCNPX** to simulate the production and transport of all secondary radiation produced from proton bombardment
  - Depth dose distributions in shield
    - Curve fitting → Source terms & attenuation lengths

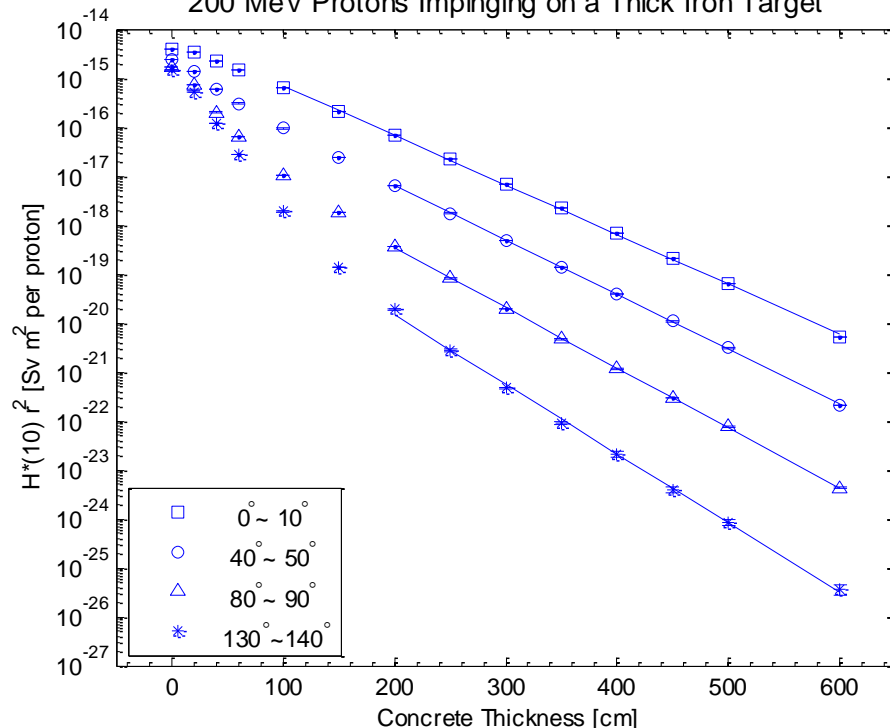


# Neutron deep-penetration calc.

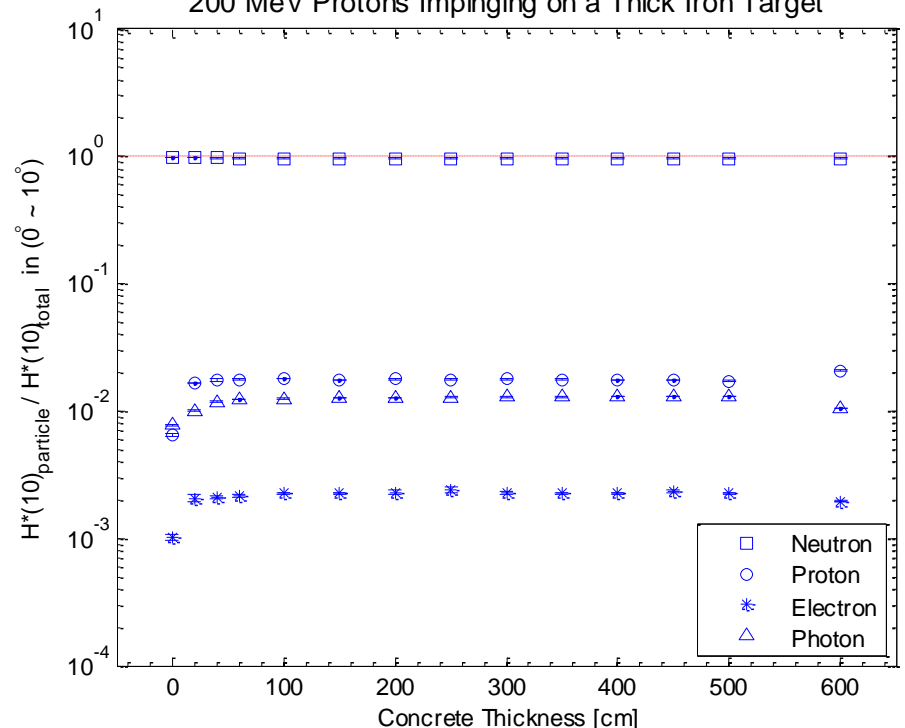


- Concrete shielding
- Consistent with reference: *NIM-B265, p.581, 2007*

Attenuation of Total Dose Equivalent in Ordinary Concrete for 200 MeV Protons Impinging on a Thick Iron Target

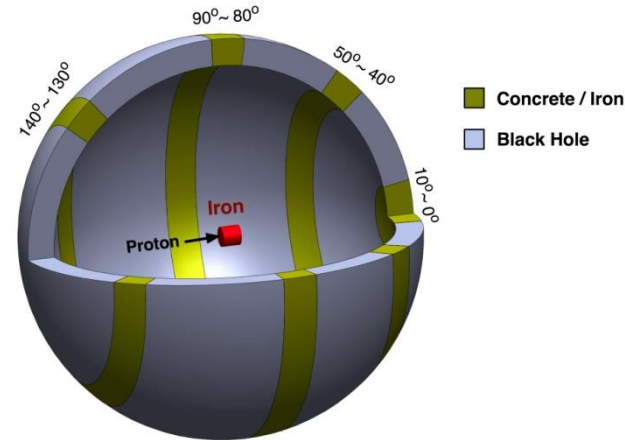


Relative Contribution of Various Particles to Total Dose in Concrete 200 MeV Protons Impinging on a Thick Iron Target





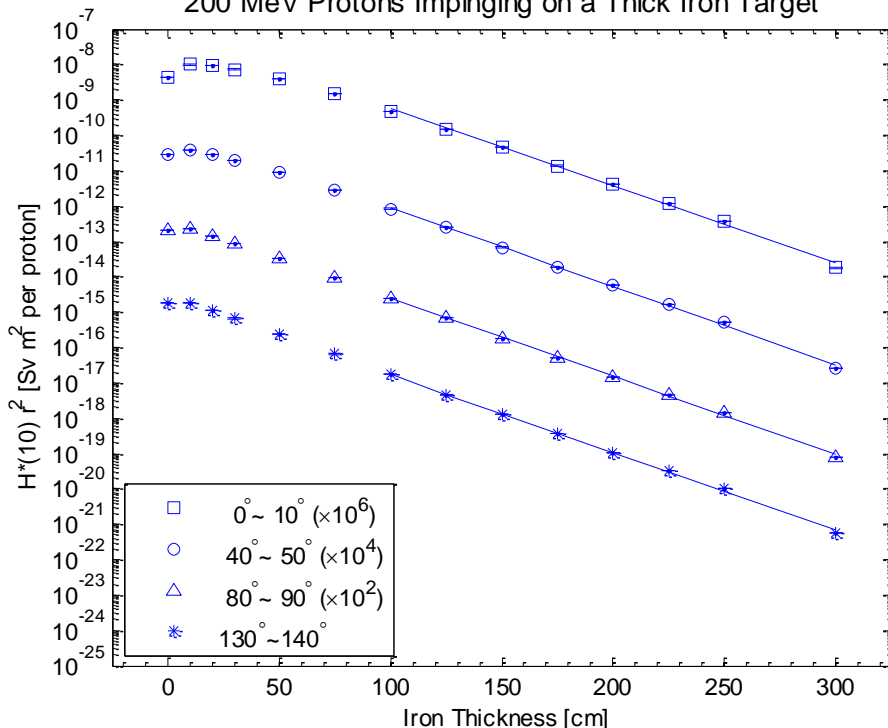
# Neutron deep-penetration calc.



## ■ Iron shielding

■ Inconsistent with reference: *NIM-B266, p.3406, 2008*

Attenuation of Total Dose Equivalent in Iron for 200 MeV Protons Impinging on a Thick Iron Target



### First exponential

$H_1$  [Sv m² per proton]  $\lambda_1$  [g cm⁻²]

0°~10° : 1.9573869e-014 231.26087

40°~50° : 7.0531340e-015 184.78711

80°~90° : 3.8826802e-015 158.39371

130°~140° : 3.0590892e-015 153.40506

### Second exponential

$H_2$  [Sv m² per proton]  $\lambda_2$  [g cm⁻²]

0°~10° : 8.6791123e-014 156.39452

40°~50° : 1.4822132e-014 153.90741

80°~90° : 4.0535242e-015 154.48923

130°~140° : 2.6849795e-015 155.24486

cf. *S. Agosteo et al. NIMB-266 (2008) 3406-3416, Table 3&2*

### First exponential

$H_1$  [Sv m² per proton]  $\lambda_1$  [g cm⁻²]

0°~10° :  $(9.7 \pm 0.07) \times 10^{-15}$  222.0  $\pm$  1.0

40°~50° :  $(4.0 \pm 0.02) \times 10^{-15}$  170.1  $\pm$  0.4

80°~90° :  $(2.3 \pm 0.01) \times 10^{-15}$  138.6  $\pm$  0.2

130°~140° :  $(1.6 \pm 0.01) \times 10^{-15}$  133.4  $\pm$  0.2

### Second exponential

$H_2$  [Sv m² per proton]  $\lambda_2$  [g cm⁻²]

0°~10° :  $(5.5 \pm 0.04) \times 10^{-14}$  140.8  $\pm$  0.2

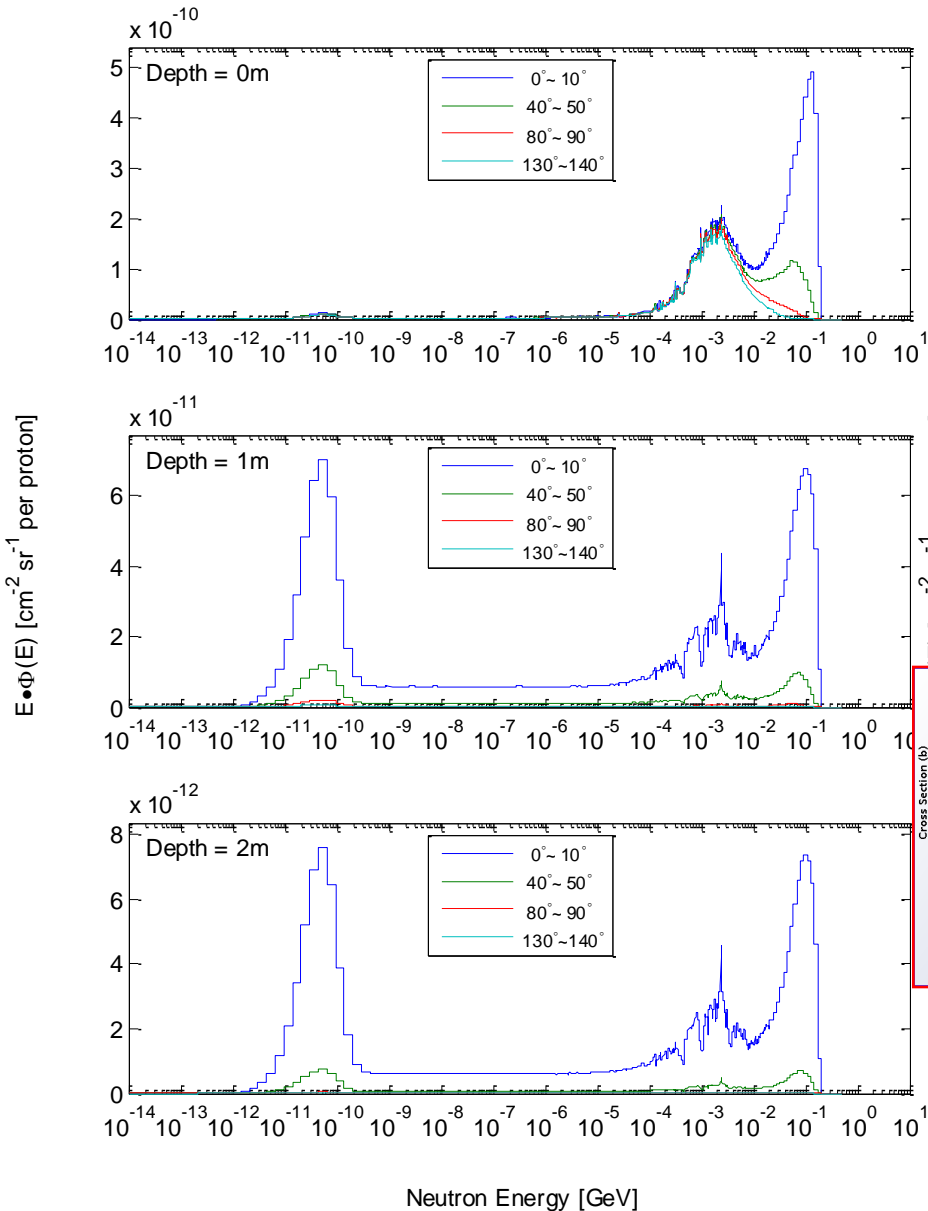
40°~50° :  $(1.7 \pm 0.01) \times 10^{-14}$  124.5  $\pm$  0.1

80°~90° :  $(1.0 \pm 0.01) \times 10^{-14}$  108.4  $\pm$  0.06

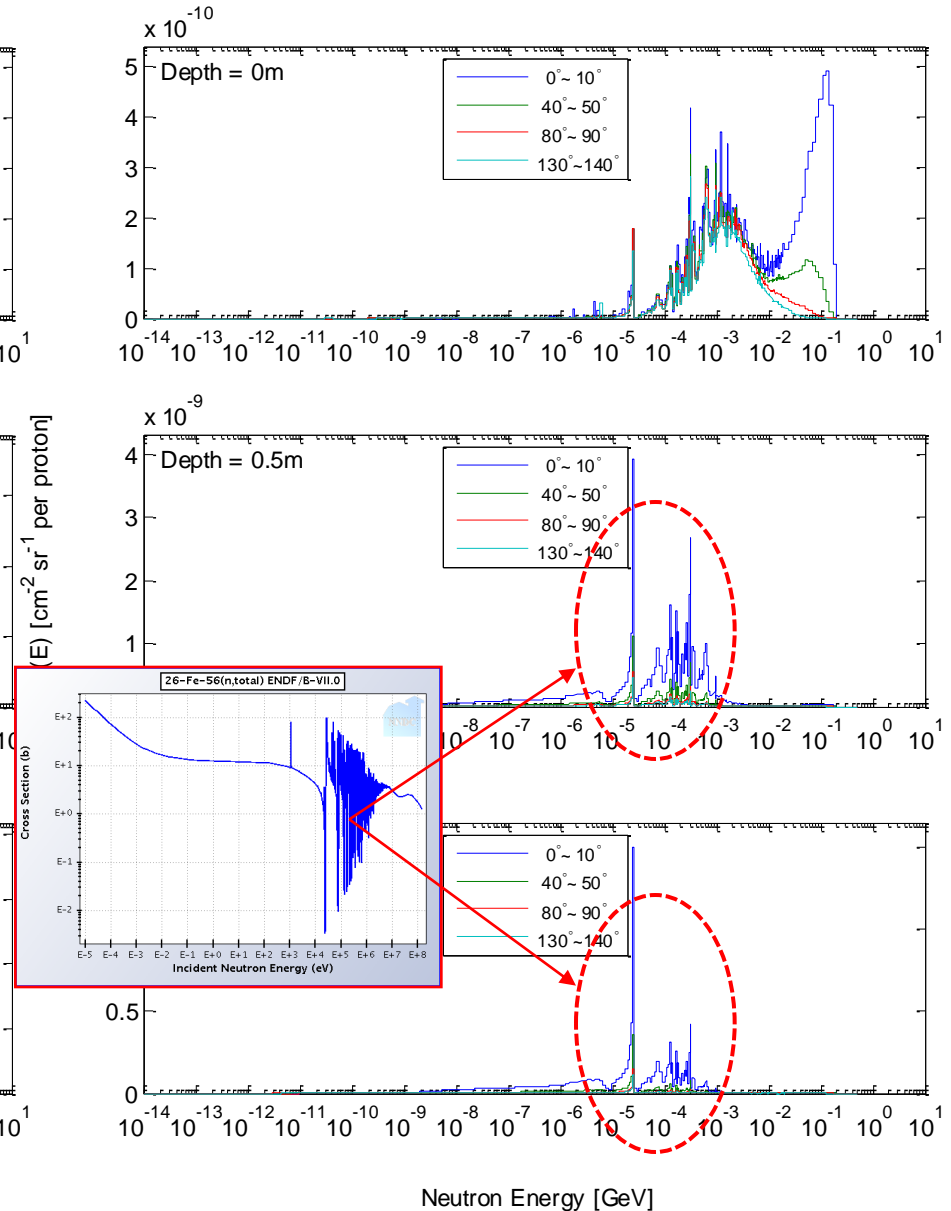
130°~140° :  $(7.5 \pm 0.03) \times 10^{-15}$  104.4  $\pm$  0.03

# Neutron spectra at various depths in concrete and iron shield

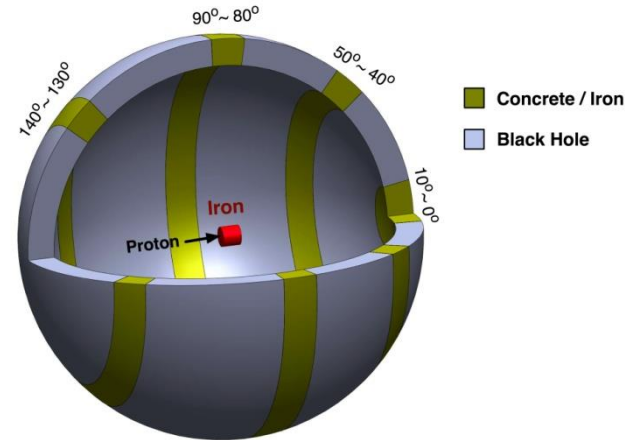
## Double Differential Distributions of Neutrons in Concrete



## Double Differential Distributions of Neutrons in Iron

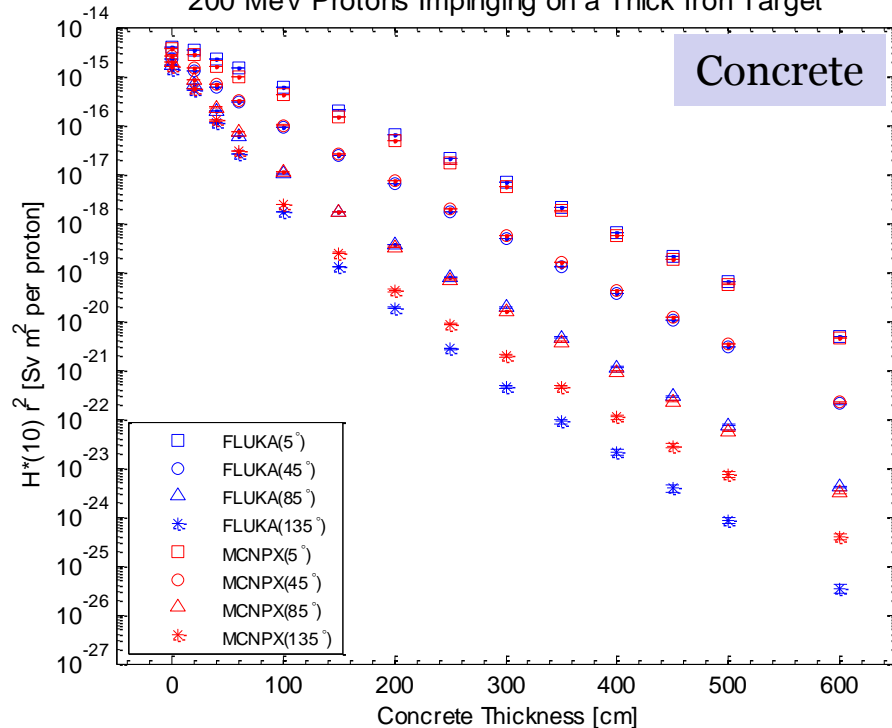


# Neutron deep-penetration calc.

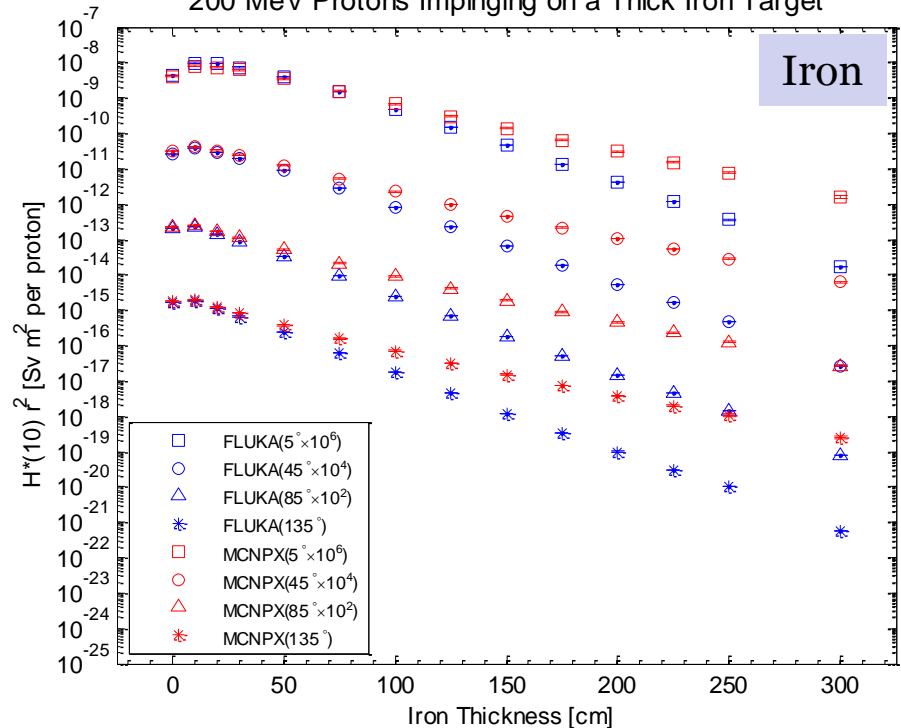


- Comparison: **FLUKA** & **MCNPX**
  - $E_n < 20\text{MeV}$ , multigroup vs. **continuous** cross sections

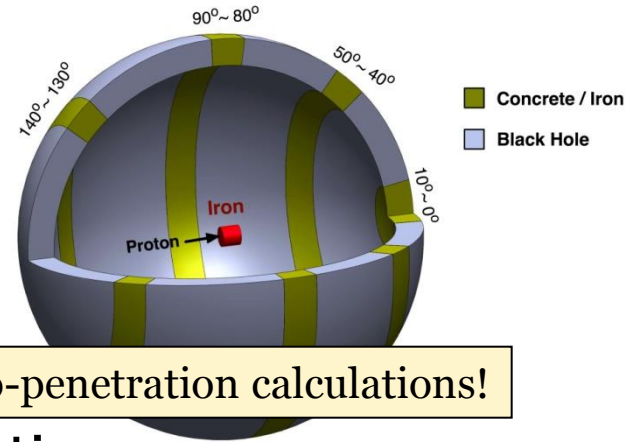
Attenuation of Neutron Dose Equivalent in Ordinary Concrete for 200 MeV Protons Impinging on a Thick Iron Target



Attenuation of Neutron Dose Equivalent in Iron for 200 MeV Protons Impinging on a Thick Iron Target



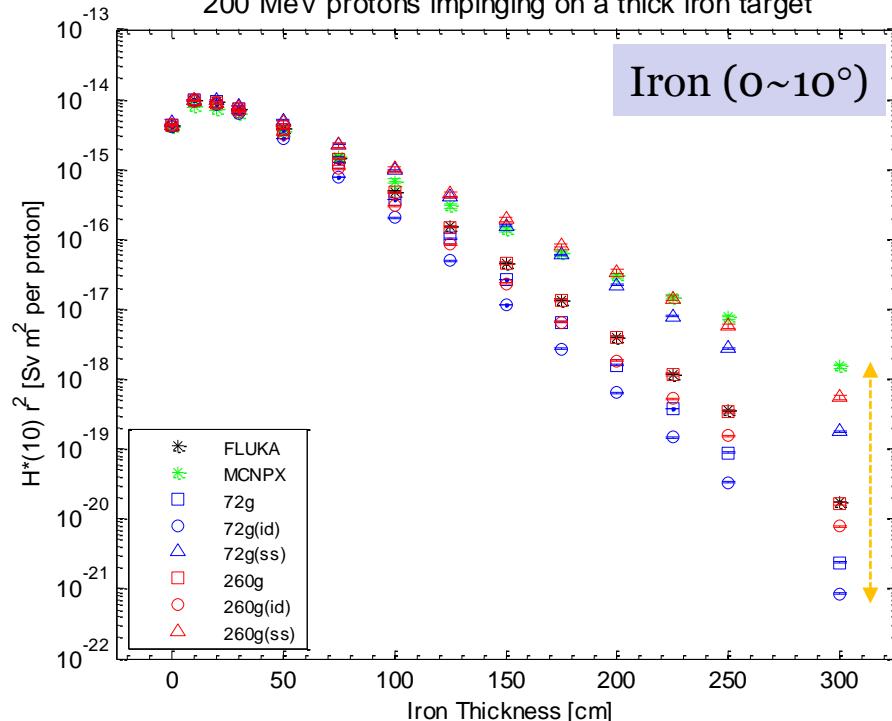
# Neutron deep-penetration calc.



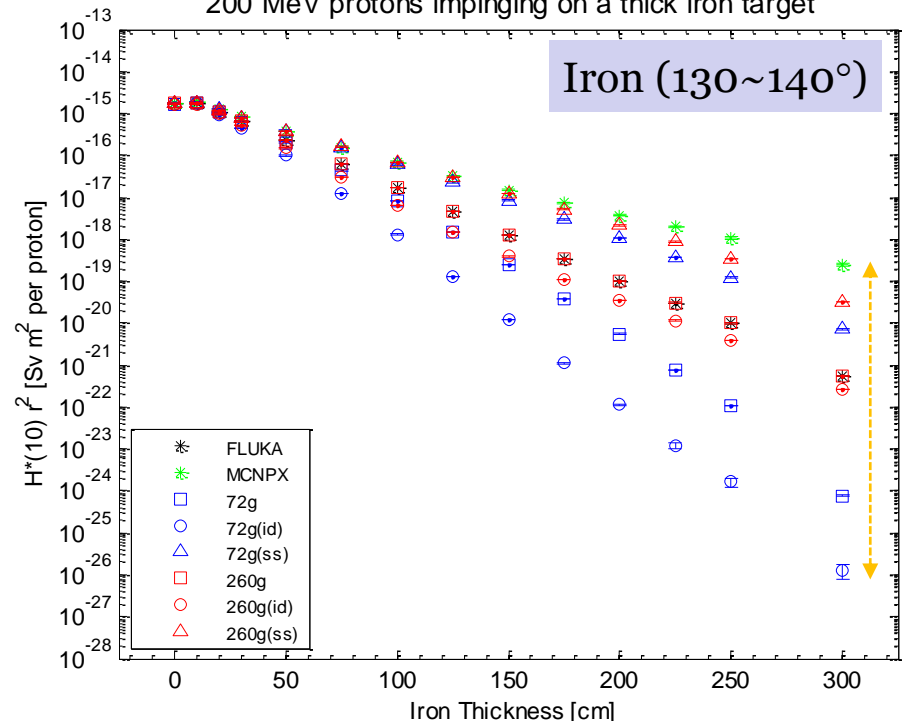
Orders of magnitude differences are possible for deep-penetration calculations!

- Effect of iron multigroup cross sections
  - Group structure: 72 or 260 groups
  - Self-shielding: infinitely dilute, partially and fully self-shielded

Attenuation of Neutron Dose Equivalent in  $0^\circ \sim 10^\circ$  in Iron Shield  
200 MeV protons impinging on a thick iron target



Attenuation of Neutron Dose Equivalent in  $130^\circ \sim 140^\circ$  in Iron Shield  
200 MeV protons impinging on a thick iron target





# A shielding database for proton therapy accelerators

- Point-source line-of-sight model

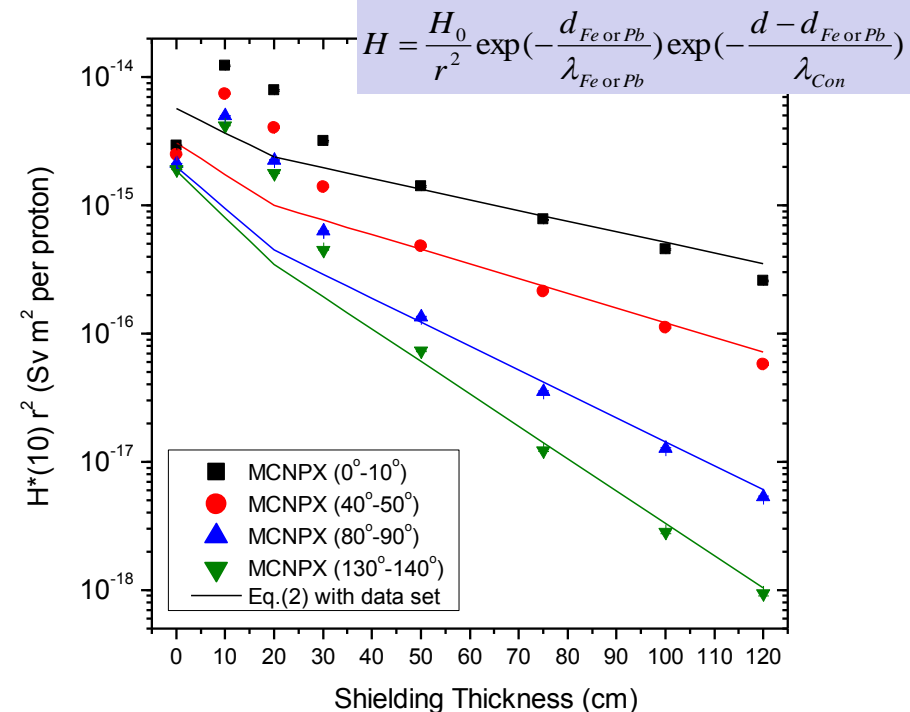
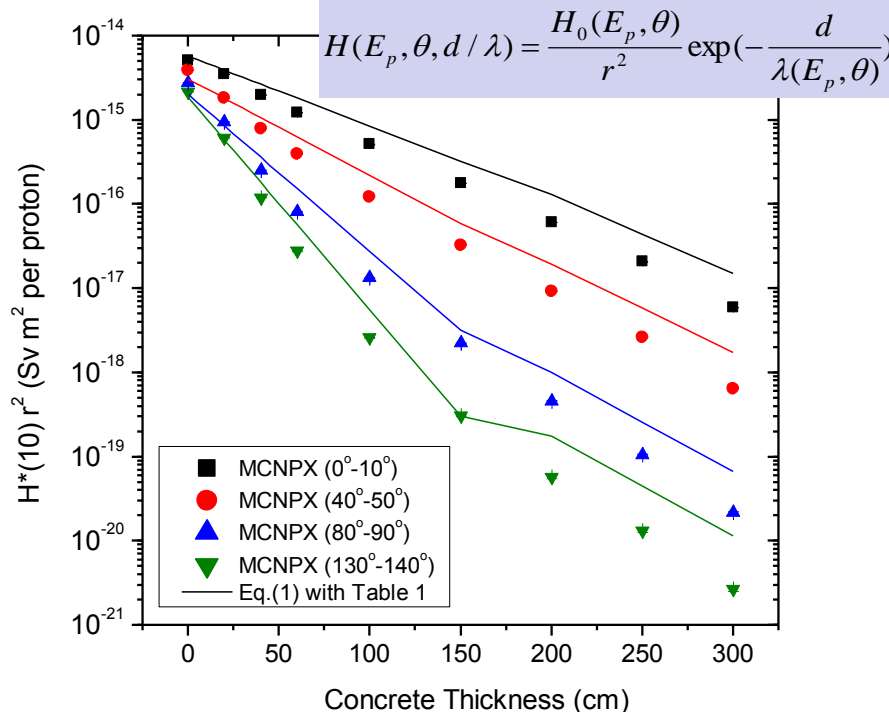
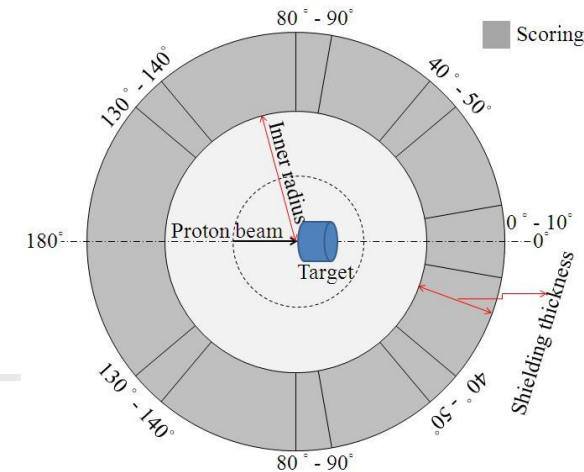
$$H(E_p, \theta, d / \lambda) = \frac{H_1(E_p, \theta)}{r^2} \exp\left(-\frac{d}{\lambda_1(E_p, \theta)}\right) + \frac{H_2(E_p, \theta)}{r^2} \exp\left(-\frac{d}{\lambda_2(E_p, \theta)}\right)$$

- Source term & attenuation length:  $(H_1, \lambda_1)$  &  $(H_2, \lambda_2)$   
Reasonable coverage of common beam/target/shielding/angle
  - Proton energies: 100, 150, 200, 250, 300 MeV
  - Target materials: iron, graphite, tissue
  - Shielding materials: concrete, iron, lead
  - Angles of neutron emission: 0°-10°, 40°-50°, 80°-90°, 130°-140°
- Monte Carlo simulations
  - MCNPX with continuous-energy cross sections
  - Generation of shielding parameters → Database
  - Case study and verification

# Demo by two simple cases

250 MeV proton on Fe

- Single-layer shielding: 3m concrete
  - Overestimation is acceptable and usually preferable
- Double-layer shielding: 20cm iron + 1m concrete
  - Reasonably good agreement with the Monte Carlo results

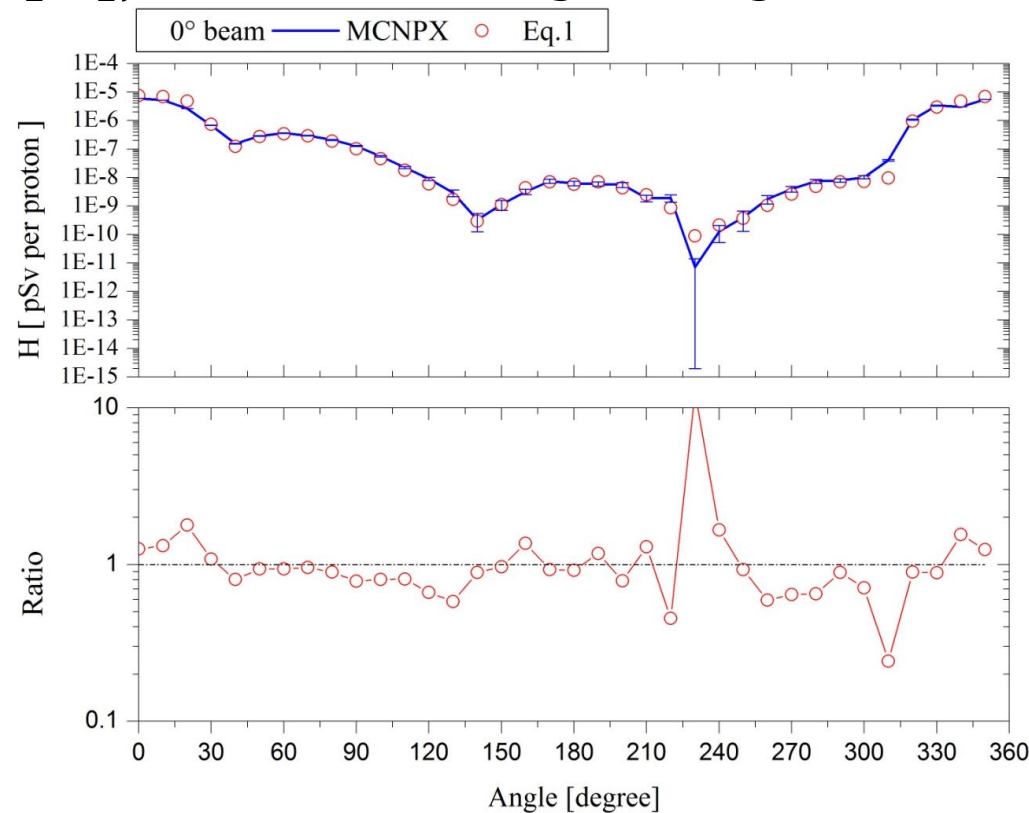
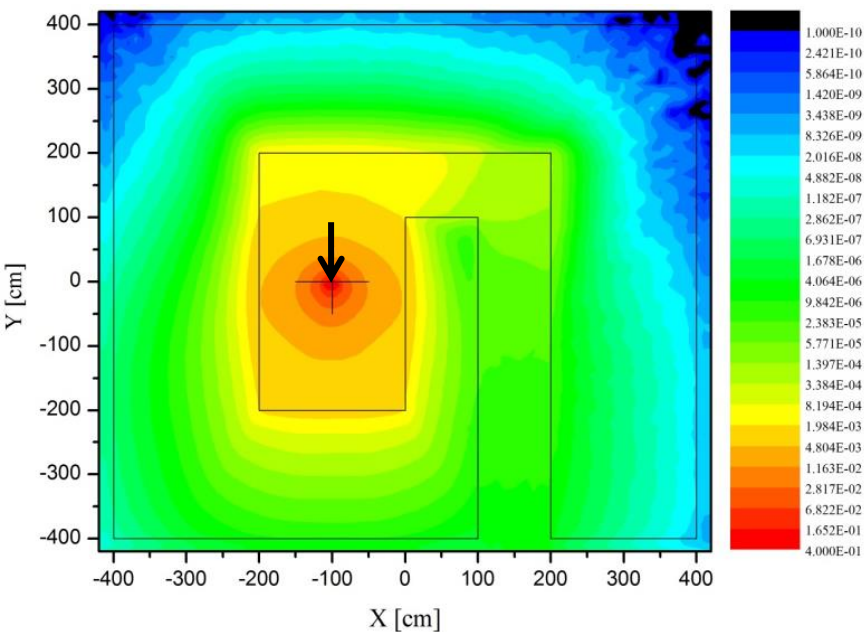
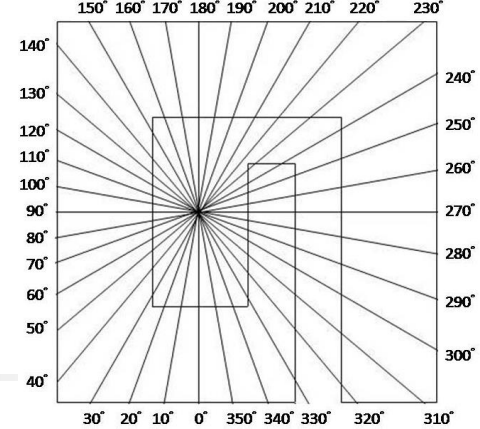




# Shielding design & dose analysis

250 MeV proton on Fe, concrete shielding

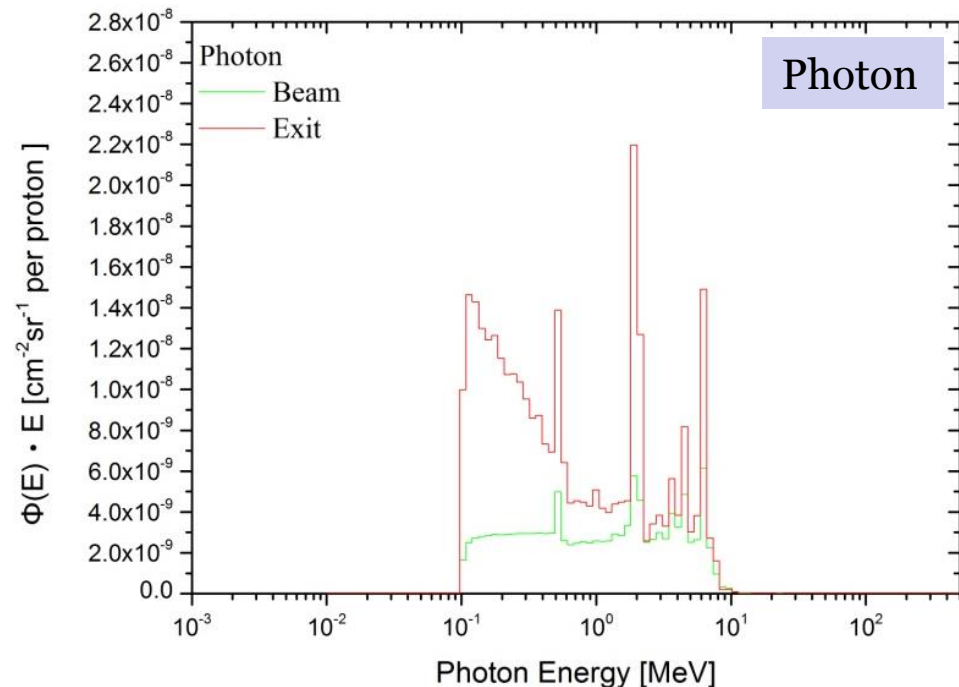
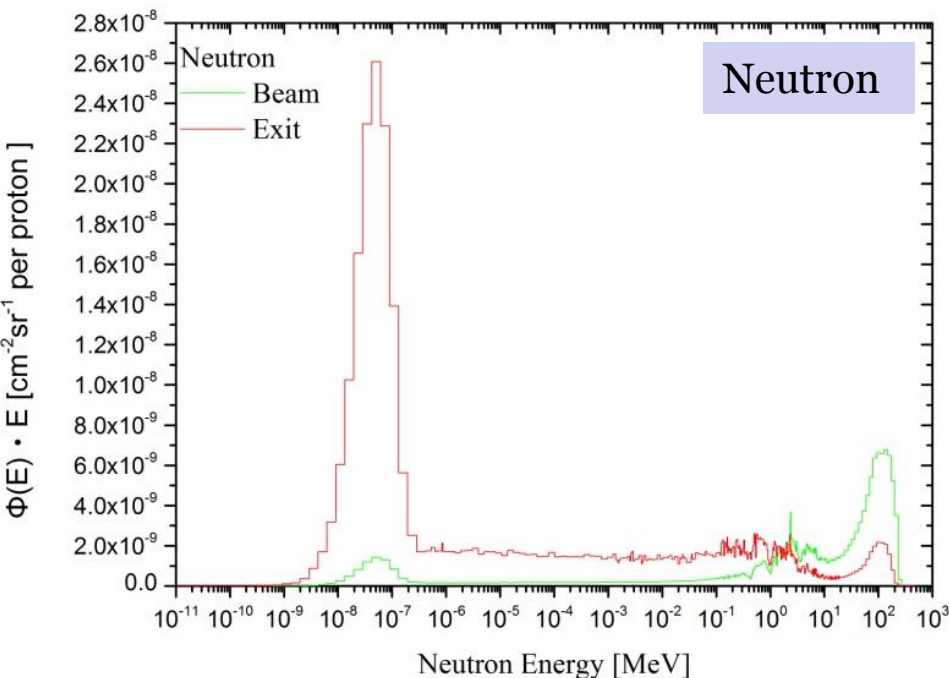
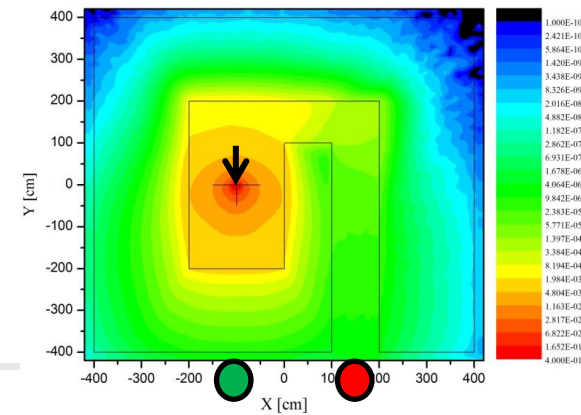
- Proton therapy treatment room
  - Direct Monte Carlo simulation
  - Database  $(H_1, \lambda_1), (H_2, \lambda_2)$  + Point-source light-of-sight model



# Shielding design & dose analysis

250 MeV proton on Fe, concrete shielding

- Proton therapy treatment room
  - Direct Monte Carlo simulation
  - Energy spectra of neutrons and gamma rays on the surface of the  $0^\circ$  shielding wall and near the maze entrance, respectively



# Radiation streaming

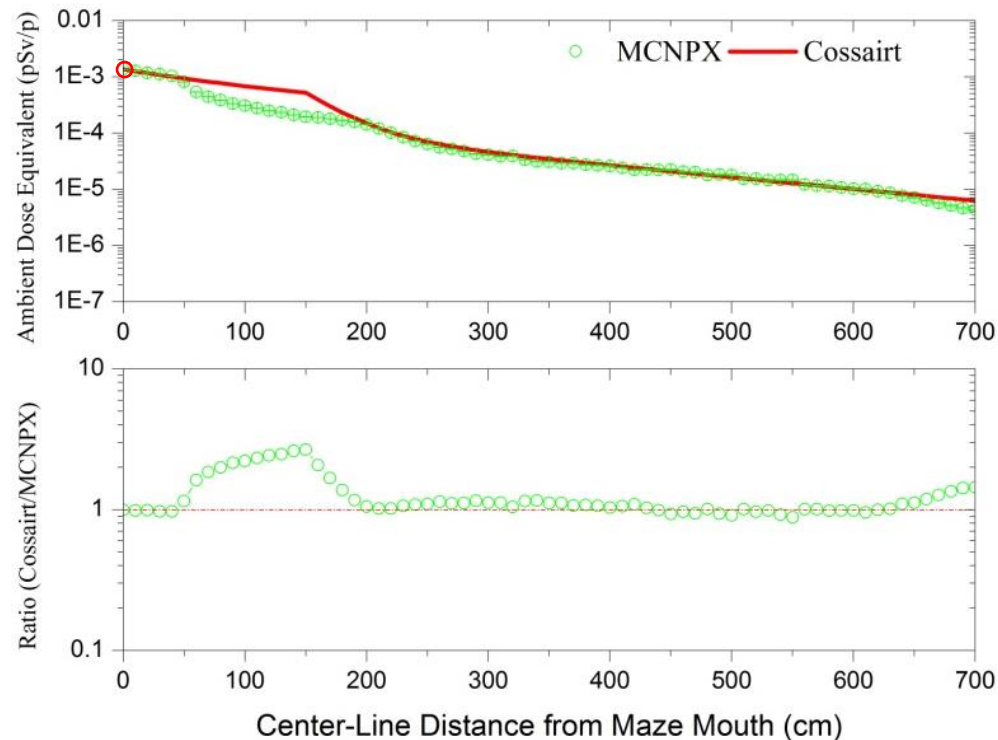
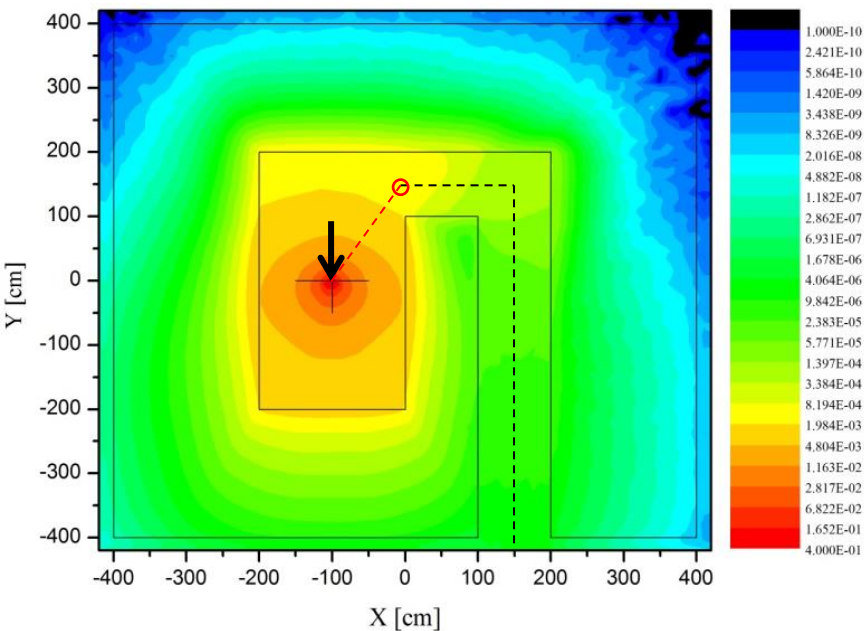
250 MeV proton on Fe, concrete shielding

- Proton therapy treatment room
  - Direct Monte Carlo simulation
  - Database ( $H_0/r^2$ ) + Cossairt's formula (FermiLab TM-1834, 2005)

$$H_1(\delta_1) = \left[ \frac{r_0}{\delta_1 + r_0} \right]^2 H_0(R) \quad \text{for 1}^{st} \text{ leg}$$

$$H_i(\delta_i) = \left\{ \frac{e^{-\delta_i/a} + Ae^{-\delta_i/b} + Be^{-\delta_i/c}}{1 + A + B} \right\} H_{i-1}(\delta_{i-1}) \quad \text{for } i^{th} \text{ leg } (i > 1)$$

where  $\delta_i = d_i/\sqrt{A}$  and the fitting parameters are :  
 $r_0 = 1.4$ ,  $a = 0.17$ ,  $b = 1.17$ ,  $c = 5.25$ ,  $A = 0.21$ ,  $B = 0.00147$





# Conclusions

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- Neutrons are dominant dose component at proton and heavy ion accelerators, also for high-energy electron accelerators with thick shielding.
- Benchmark calculations were performed for neutron production by proton, heavy ion, and electron with energies of our interest and their agreement with experiments are generally satisfactory.
- Selection of proper multigroup cross sections is important to neutron deep-penetration calculations.
- This work provides a set of reliable shielding data with reasonable coverage of common target and shielding materials for 100-300 MeV proton accelerators.
- General characteristics and possible applications of this data set in cases of single- and double-layer shielding are presented.