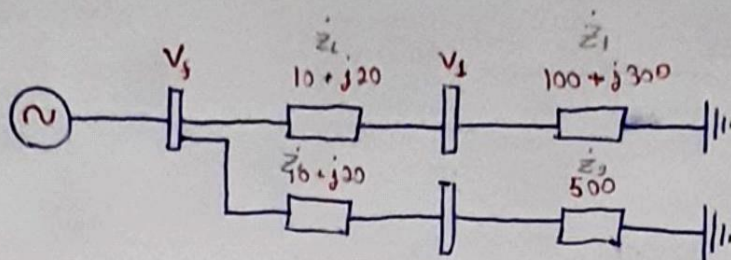


Lista de exercícios - 2

5.2



$V_s = 220 \text{ V}; \text{ABC}; V_m \angle 0^\circ$

- a)  $V_s$   $V = \text{Linha}$
- b)  $V_2$   $V' = \text{Fase}$
- c)  $I_T$
- d) FP
- e) S

a)  $V_s = 220 \angle 30^\circ \Rightarrow V_s' = \frac{220}{\sqrt{3}} \angle 0^\circ$

$I_1 = \frac{V_s'}{Z_1} \Rightarrow V_s' = \hat{I}_1 \cdot Z_1 \Rightarrow V_s' = \hat{I}_1 \left[ 1 + \frac{Z_1}{Z_1} \right] \sqrt{3} \angle 30^\circ = 235.41 \angle 29.46^\circ \text{ [V]}$

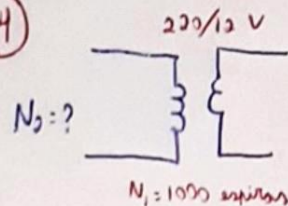
b)  $I_2 = \frac{V_s'}{Z_2 + Z_1} \Rightarrow V_2 = \hat{I}_2 \cdot Z_2 \Rightarrow V_2 = \left[ \frac{V_s'}{Z_2 + Z_1} \right] \left[ Z_2 \right] \left[ \sqrt{3} \angle 30^\circ \right] = 230.62 \angle 27.22^\circ \text{ [V]}$

c)  $I_T = I_1 + I_2 = \frac{V_s'}{Z_1} + \frac{V_s'}{Z_2 + Z_1} = 0.56 \angle -45.07^\circ \text{ [A]}$

d)  $\text{FP} = \cos((\angle 0.54^\circ) - (-45.07^\circ)) = 0.713$

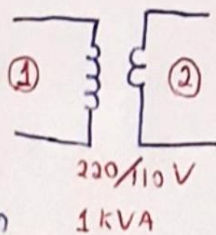
e)  $S_{3\phi} = 235.41 \times 0.56 \times \sqrt{3} = 226.8 \text{ [VA]}$

5.4



$\frac{V_1}{V_2} = \frac{N_1}{N_2} \Rightarrow N_2 = 1000 \times \frac{12}{220} = \frac{600}{11} \approx 55 \text{ espiras}$

5.8



$R_1' = 0.5 \Omega$   
 $X_1' = 1.5 \Omega$

$S_{b1} = 1 \text{ kVA}$

$V_{b1} = 220 \text{ V}$

$I_{b1} = \frac{50}{\sqrt{3}} \text{ A}$

$Z_{b1} = \frac{242}{5} \Omega$

$S_{b2} = 1 \text{ kVA}$

$V_{b2} = 110 \text{ V}$

$I_{b2} = \frac{100}{\sqrt{3}} \text{ A}$

$Z_{b2} = \frac{121}{10} \Omega$

$Z_1 = 0.5 + 1.5j = \frac{\sqrt{10}}{2} \angle 71.51^\circ \Omega$

$z_1 = \frac{Z_1}{Z_{b1}} = 0.03 \angle 71.57^\circ \text{ pu}$

$z_1 = 0.01 + 0.03j \text{ pu}$

$r = 1\% \text{ pu}$

$x = 3\% \text{ pu}$

Impedância Refletida

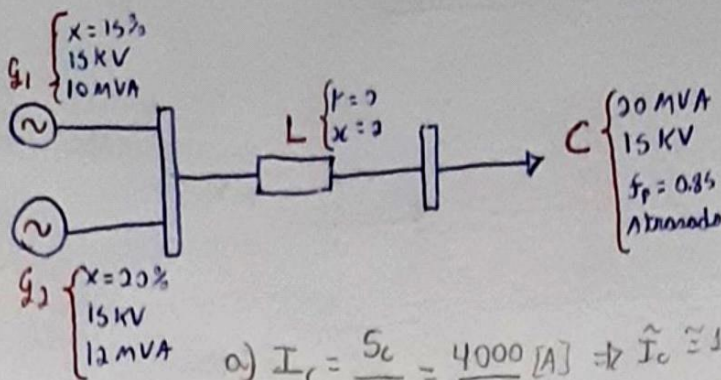
$Z_2 = \left( \frac{110}{220} \right)^2 \cdot Z_1 = \frac{\sqrt{10}}{8} \angle 71.57^\circ = 0.13 + 0.38j$

$z_2 = \frac{Z_2}{Z_{b2}} = 0.03 \angle 71.57^\circ = 0.01 + 0.03j \text{ pu}$

Logo, conclui-se que os valores são iguais no lado de alta tensão.



5.10



$V_{Am}^c = 15 \angle 0^\circ \text{ kV}$   
 $S_c = 20 \text{ MVA}$   
 $\cos \phi = 0.85 \Rightarrow 31.79^\circ$

a)  $I_c = \frac{S_c}{V_{Am}^c} = \frac{4000}{3} \text{ [A]} \Rightarrow \hat{I}_c \approx 1.33 \angle -31.79^\circ \text{ [kA]}$

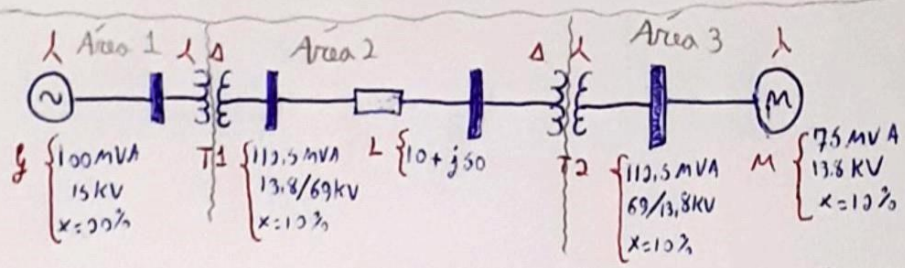
$\hat{V}_g' = \hat{I}_c * (\hat{Z}_L + \hat{Z}_C) = \hat{I}_c \hat{Z}_L + V_{Am}^c = 16.56 \angle 7.87^\circ \text{ [kV]}$

- a)  $V_g'$
- b)  $r \begin{cases} 20 \text{ MVA} \\ 15 \text{ kV} \end{cases}$
- c)  $S_{3\phi}$

b)  $\begin{cases} S_b = 20 \text{ MVA} \\ V_b = 15 \text{ kV} \\ I_b = 1.33 \text{ kA} \\ Z_b = 11.25 \Omega \end{cases}$  Mudando de base  
 $X_1 = (0.15) \left( \frac{20 \text{ MVA}}{10 \text{ MVA}} \right) \left( \frac{15 \text{ kV}}{15 \text{ kV}} \right) = 0.3 \text{ pu}$   
 $X_2 = (0.2) \left( \frac{20 \text{ MVA}}{12 \text{ MVA}} \right) \left( \frac{15 \text{ kV}}{15 \text{ kV}} \right) = \frac{1}{3} \text{ pu}$   
 $X_g = \frac{\left( \frac{X}{10} \right) \left( \frac{1}{X} \right)}{\left( \frac{3}{10} \right) + \left( \frac{1}{3} \right)} = \frac{3}{19}$   
 $X_g = 0.1579 \Rightarrow 15.79\%$

c)  $S_{3\phi} = \hat{V}_g' * \hat{I}_c^* = 22.08 \angle 39.66^\circ \text{ MVA}$

5.14



- a) Diagrama (150MVA, 69kV)
- b)  $V_m = 1 \text{ pu}$ ,  $f_p = 1$   
 $V_g' = ?$   $S_g = ?$

a) relação de transformação dos trafo:  $T1 = \frac{\sqrt{3}}{5} \angle 30^\circ$  e  $T2 = \frac{5}{\sqrt{3}} \angle -30^\circ$

$S_{b2} = 150 \text{ MVA}$   $\begin{cases} V_{b1} = 13.8 \text{ kV} \\ V_{b2} = 69 \text{ kV} \angle 0^\circ \end{cases}$   $S_{b3} = 150 \text{ MVA}$   $\begin{cases} V_{b3} = 13.8 \text{ kV} \end{cases}$

$X_g = (0.2) \left( \frac{150}{100} \right) \left( \frac{15 \text{ kV}}{13.8 \text{ kV}} \right)^2 = 0.3544 \text{ pu}$   
 $X_1 = (0.1) \left( \frac{150}{112.5} \right) \left( \frac{13.8 \text{ kV}}{13.8 \text{ kV}} \right)^2 = 0.1333 \text{ pu}$   
 $Z_{b2} = \frac{V_{b2}^2}{S_{b2}} \Rightarrow Z_L = \frac{Z_b}{Z_{b2}} = \frac{Z_b S_{b2}}{V_{b2}^2} = 0.3151 + j15.75 \text{ pu}$   
 $X_2 = (0.1) \left( \frac{150}{112.5} \right) \left( \frac{13.8 \text{ kV}}{13.8 \text{ kV}} \right)^2 = 0.1333 \text{ pu}$   
 $X_m = (0.1) \left( \frac{150}{75} \right) \left( \frac{13.8 \text{ kV}}{13.8 \text{ kV}} \right)^2 = 0.24 \text{ pu}$

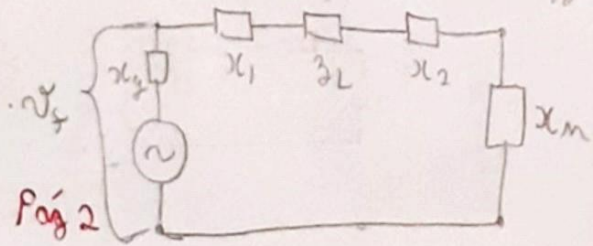
b)  $V_m = 1 \text{ pu}$   $\Rightarrow V_m = 1 \angle 0^\circ \text{ pu}$   
 $S_m = \frac{S}{S_b} = \frac{75 \text{ MVA}}{150 \text{ MVA}} = 0.5 \text{ pu} \Rightarrow I_m = 0.5 \angle 0^\circ \text{ pu}$   
 $i = \frac{0.5}{1} = 0.5 \text{ pu} \Rightarrow i = 0.5 \angle 0^\circ \text{ pu}$

$V_g' = V_m + i(X_1 + X_2 + Z_L) = 2.04 \angle 38.5^\circ \text{ [kV]}$

$V_g' = V_g + V_{b1} = 2.04 \angle 38.5^\circ \text{ [kV]}$

$I_g = V_g' \cdot i = 1.48 \angle 38.5^\circ \cdot 0.5 \angle 0^\circ = 0.74 \angle 38.5^\circ \text{ pu}$

$S_g = S_{b2} \cdot I_g = (150 \text{ MVA}) \cdot (0.74 \angle 38.5^\circ) = 110.9 \angle 38.5^\circ \text{ [MVA]}$



Pág 2

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