

$$\textcircled{2} \quad R = G = 0, \quad L = 1.33 \times 10^{-7}, \quad C = 8.86 \times 10^{-12} \text{ F/m}, \quad V(0) = \frac{220}{\sqrt{3}} \angle 0^\circ \text{ kV}$$

$$S(0) = 150 + j50 \text{ MVA}$$

$$a) \gamma \quad b) Z_c \quad c) V, I, S \text{ am } 300 \text{ km} \quad \omega = 2\pi f = 120\pi$$

$$\gamma = \sqrt{zy} = \sqrt{(R + j\omega L)(G + j\omega C)} = j\omega \sqrt{LC} = j4.0925 \times 10^{-7} \text{ m}^{-1} //$$

$$Z_c = \sqrt{z/y} = \sqrt{(R + j\omega L)/(G + j\omega C)} = \sqrt{L/C} = 120.5206 \Omega //$$

$$l = 300 \text{ km}$$

$$I(0) = \left(\frac{S(0)}{V(0)} \right)^* = \left(\frac{(150 + j50) \text{ M}}{\frac{220}{\sqrt{3}} \angle 0^\circ \text{ k}} \right)^* = 1244.9913 \angle -18.43^\circ \text{ A}$$

$$\left. \begin{aligned} \cosh(\gamma x) &\approx \cosh(j\beta x) \approx \cos(\beta x) \\ \sinh(\gamma x) &\approx \sinh j\beta x \approx j\sin(\beta x) \end{aligned} \right\} \begin{aligned} \gamma &= \alpha + j\beta \\ \gamma &= 0 + j4.0925 \times 10^{-7} \text{ m}^{-1} \\ \beta &= 4.0925 \times 10^{-7} \end{aligned}$$

~~$$V(x) = \frac{220}{\sqrt{3}} \cos(\gamma x) - Z_c I_0 \sinh(\gamma x)$$~~

$$V(x) = \frac{220}{\sqrt{3}} \cos(\gamma x) - Z_c I_0 \sinh(\gamma x) \Rightarrow$$

$$I(x) = I(0) \cos(\beta x) - \frac{V(0)}{Z_c} j \sinh(\beta x) \Rightarrow$$

$$V(x) = 127 \times 10^3 \cos(4.0925 \times 10^{-7} \times x) - 150.5371 \times 10^3 \angle -18.43^\circ \sinh(4.0925 \times 10^{-7} \times x)$$

$$I(x) = 1244.9913 \angle -18.43^\circ \cos(4.0925 \times 10^{-7} \times x) - 1036.5604 \sinh(4.0925 \times 10^{-7} \times x)$$

$$S(x) = V(x) \times I(x)^*$$

$$\text{Forwards } X = l = 300 \text{ km}$$

$$V(300) = 121.4400 \angle -8.39^\circ \text{ kV} //$$

$$I(300) = 1281.3949 \angle -23.82^\circ \text{ A} //$$

$$S(300) = 155.6128 \angle 15.43^\circ \text{ MVA} = 150 + j41.4024 \text{ MVA} //$$

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- ① $V = 500\text{KV}$, $l = 250\text{Km}$, Impedância série = $0.045 + j0.4 \Omega$ por fase por Km
admitância shunt = $4j \times 10^{-6} \text{ S}$ / por fase por Km

Determino equivalente π e defino a matriz da linha.

$$z = 0.045 + j0.4$$

$$y = j4 \times 10^{-6}$$

$$\text{Matriz} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 0.9504 + 0.0055j & 10.8778 + 98.3624j \\ -0.0000 + 0.0010j & 0.9504 + 0.0055j \end{bmatrix}$$

$$\gamma = \sqrt{zy} = \sqrt{(0.045 + j0.4)(j4 \times 10^{-6})} = 0.0001 + 0.0013j$$

$$Z_c = \sqrt{\frac{z}{y}} = \sqrt{(0.045 + j0.4) / (j4 \times 10^{-6})} = 316.73 - 17.760j$$

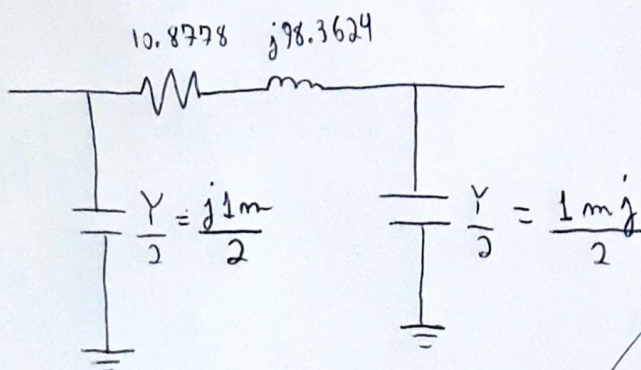
$$A = \cosh(\gamma l) = \cosh((0.0001 + 0.0013j)(250)) = 0.9504 + 0.0055j$$

$$B = Z_c \sinh(\gamma l) = (316.73 - 17.76j) \sinh(\gamma l) = 10.8778 + 98.3624j$$

$$C = \frac{1}{Z_c} \sinh(\gamma l) = \frac{1}{(316.73 - 17.76j)} \sinh(\gamma l) = -0.0000 + 0.0010j$$

$$D = \cosh(\gamma l) = \cosh(\gamma l) = 0.9504 + 0.0055j$$

Modelo π



$$Z = B$$

$$Y = \frac{2}{Z_c} \tanh\left(\frac{\gamma l}{2}\right) = 0.0000 + 0.0010j$$