

# Learning with Naïve Bayes

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## Abstract

This paper describes our group’s findings when using a Naïve Bayesian approach for learning on various sets of data. We provide our findings on these data sets with and without noise in the data. More specifically, we show how the model performs on each data set using a percent accuracy statistic and two different loss functions. Prior to the project, we were expecting to find that generally the model would perform best on data with more feature variables, and also that the model would perform best on less noisy data. Though our hypotheses were not fully confirmed to the degree of statistical significance we had initially expected, we did find that these trends were present throughout the project, with exceptions for specific cases.

**Keywords:** Naïve Bayes

## 1. Problem Statement

Utilizing five datasets- each from unique and differing settings, we implemented a Naïve Bayesian learning model in an attempt to provide insights into the correlation of features within each set of data. More rigorously, each data set came with explicit classifications, and we sought to train our model in order to then guess the classification of a given set of feature data in the absence of a provided classification. Each of the five datasets we use in the project have a variable number of classes and either discrete or real valued attribute values. We then provided an analysis of each dataset with permutations on its feature values. We hypothesized that in general, more attributes would mean a better performance of our model, since more attribute data could be interpreted as gaining greater specificity in pinpointing revealing characteristics of a class. We presumed that this enhanced performance would be statistically significant, in that at least 90 percent of trials would show greater reliability of learning on datasets with more attribute data when compared to datasets with

fewer attributes. In this context, the reliability of learning then was measurable by the percent with which the model correctly guessed a class given only feature data, and also via two loss functions of our choosing. Additionally, we hypothesized that any given dataset would perform more reliably 90 percent of the time when compared to its corresponding permuted data, under the same measurements for reliability as for the first hypothesis.

## 2. Methods

In order to test our hypotheses, we ran our model on the five original given datasets and introduced noise into each dataset, comparing the results that our learning model was able to attain when comparing the original data to data with permutations. Initially, the datasets we used to test our model included breast cancer screening data, data referring to different properties of various kinds of glass, data on the properties of three different iris plant species, data referring to the properties of different kinds of soybeans, and the 1984 voting data of each congressman in the U.S. house of representatives on the sixteen key votes identified in the Congressional Quarterly Almanac. All of these data were real valued, with the exception of the data corresponding to the House of representatives, which was in the form of strings indicating a vote “y” for yes and “n” for no. We converted these strings into real valued entries by assigning all yes votes to the value 1, and all no votes to the value 0. We also needed to handle missing attribute values in our data, which were existent in two of our datasets. In the congressional voting dataset, missing values corresponded with a “present” vote, or a refusal to take sides. For this, we assigned all missing values 0, which corresponds to a “no”, since voting present most likely would indicate that the voter is against the proposal. The breast cancer dataset also had missing values which actually corresponded to data which was unavailable. Because the dataset was already real valued on a range from 1 to 10, we decided to give all missing entries a value of 5 which corresponds to the midpoint of the range. We rationalized that in a medical setting, this should indicate that a queried cancerous bump shouldn’t be negligently overlooked, but missing data also need not indicate severe cancer, so we decided that a middle value in this context was appropriate.

For each of these data sets, noise was introduced by permuting approximately 10% of the feature data in any given set. More precisely, for each and every feature value, there was a randomized 10% chance that permutation would occur. Permutation was conducted by computing the midpoint of values for every feature, and then “flipping” every selected data point over this midpoint by subtracting from the midpoint the distance between the midpoint and the data point if the data point were initially larger than the midpoint, and otherwise adding to the midpoint the distance between the midpoint and the data point if the point were initially smaller than the midpoint.

Mathematically, letting  $F_i$  be a feature in a dataset and  $f_j \in F_i$  be an individual data point of  $F_i$ , a midpoint  $m$  was computed by  $m = (\max(f \in F_i) + \min(f \in F_i))/2$ , and our permutations  $f_j^*$  were then conducted by computing on the randomly selected  $f_j$  composing approximately 10% of  $F_i$ :

$$\begin{cases} f_j^* = m - (f_j - m) & \text{if } f_j > m \\ f_j^* = m + (m - f_j) & \text{if } f_j < m \end{cases}$$

Having accomplished the permutations, another step of preprocessing this data was discretizing real-valued data into categorical data. To do this, we used “binning”, which is the processing of dividing values into a number of bins in order to convert it into a finite number of categories. Initially, we set the number of bins to 2 for every dataset before we would go back and fine tune hyperparameters once the algorithm was fully implemented.

After fully preprocessing our data, we were able to begin implementation of the Naïve Bayesian algorithm. After doing so, we needed a metric to determine how well our algorithm performs on each dataset. For this task, we introduced two loss functions to measure performance, a 0/1 loss function, and a log based loss function. These loss functions provide an effective method of determining model performance when certain features of the model are changed. Explicitly, letting  $c_i$  be the level of certainty with which a guess was made in our model for the  $i$ th line of test data, logarithmic loss for each data point was computed as follows:

$$\begin{cases} \ln(c_i) & \text{if correct} \\ \ln(1 - c_i) & \text{if incorrect} \end{cases}$$

Letting the value  $y_i$  be the value produced by the above equation for the  $i$ th line of test data, the logarithmic loss for the entire test set  $T$  is computed as:

$$\frac{-1}{|T|} \sum_{t \in T} y_i \quad (1)$$

The second loss function we introduced was the 0/1 loss function, which is the ratio of incorrect guesses to total guesses made on the testing data. Again denoting the test set  $T$ , and letting the number of correct guesses made on the test set by the model be denoted  $g_c$ , the 0/1 loss is computed with the simple ratio:

$$1 - \frac{g_c}{|T|} \quad (2)$$

We chose both of the above loss functions with the motivation that both are relatively simple to compute, as all of the terms are directly attainable from the output of our algorithm, and because they are metrics with importantly opposed qualities in the evaluation of a Bayesian model. Perhaps the most famous and immediately logical evaluation of loss is 0/1 loss, which is a measurement of the ratio of incorrect guesses made in a test set. Importantly, this is indicative of the accuracy of our model, but is not particularly informative of overfitting. Logarithmic loss however is helpful when evaluating the performance of a model while also keeping in mind the potential of overfitting. By incorporating punishments for having a high degree of certainty in an incorrect decision, logarithmic loss is useful in capturing the performance of a model with greater depth than simply counting the number of correct solutions- which in turn provides a weariness for overfitting. Both metrics are important to have an effective model, so both loss functions were chosen in the evaluation of our model on various data.

Once our algorithm and loss functions had been fully implemented, we began tuning hyperparameters to optimize model performance. Ten fold cross validation proved to be a useful method of training and testing our data. This involved dividing the dataset into ten groups, with nine being used for training and one being used for testing, and rotating so that

every group is eventually used for testing. The hyperparameter we were most interested in was the number of bins we used to discretize the real valued datasets. Using cross-validation, we determined that 4 bins offered the best performance for our model, and thus divided the real values into 4 bins to discretize it for features with more than four independent values assigned to any given entry. This was due in part to our findings that the performance of our model didn't seem to be altered once the bin size was increased above 4, and also due to some limitations in our implementation. Creating more bins seems to bog down our model, and introduces a host of potential problem areas in our implementation that don't seem to be worth minimal performance improvements in the best case, and in practice no real noticeable difference. However, improving our ability to fine tune binning is a clear area for future work for subsequent implementations. Yet, for this project, altering the number of bins seemed by observation to be around optimal with 4 bins for every feature in each dataset excluding the congressional voting data, which for practical purposes was also convenient in that it limited the number of areas where potential vulnerabilities could arise within our implementation.

### 3. Results

When running our learning algorithm on each of the datasets, we were able to quickly make observations as to which data our model was able to learn most effectively, and which sets of data our model had a more difficult time with. Using our chosen loss functions described above, we could notice that the datasets that our model was able to learn best were noticeably the house voting dataset and the breast cancer dataset, and their corresponding permutations. The Iris data and glass data retained relatively low log loss values, but were more dispersed with respect to 0/1 loss. The soybean data was the worst performing dataset for our model under our chosen metrics with relatively scattered log loss and 0/1 loss values. To present the performance of our model on each dataset under our chosen loss functions, we provide our results in the form of scatterplots whose y-axis is occupied by log loss values, and whose x-axis is occupied by 0/1 loss values. In doing so, we've provided the visualization that high performing datasets under our metrics will appear clustered in the bottom left corner of each scatterplot.

Our experiment was conducted with 30 trials for each dataset using 10-fold cross validation for each trial, to provide the data presented in 1 and 2. The mean log loss and 0/1 loss values for each dataset after 30 trials can be found in the following table (where data with permutations is denoted by \*):

Loss Function	Vote	Vote*	Cancer	Cancer*	Glass	Glass*	Iris	Iris*	Soy	Soy*
0/1 Loss	0.1041	0.1126	0.0348	0.0458	0.2206	0.4297	0.2654	0.2092	0.4300	0.4350
Log Loss	0.5809	0.4401	0.1890	0.2116	0.5194	0.7116	0.3633	0.3840	1.6919	1.706

### References

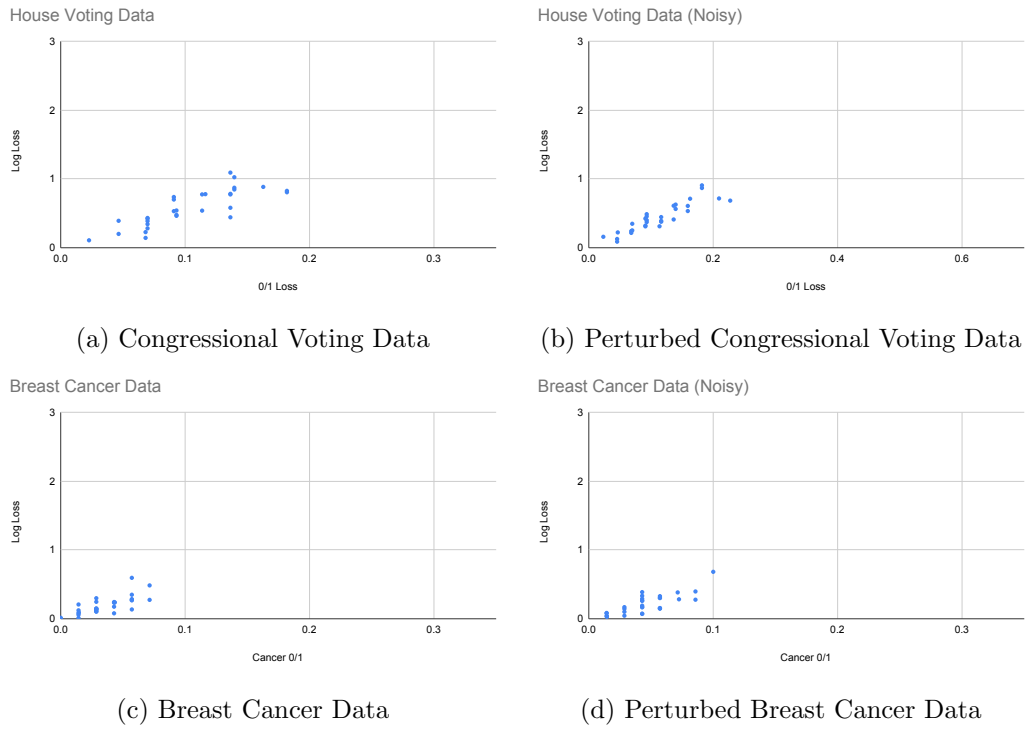


Figure 1: Log Loss vs 0/1 Loss for 1984 House of Representatives Voting Data and Breast Cancer Data, which were our best performing datasets with low 0/1 and Log Loss. (Data is clustered in the bottom left of scatterplot)

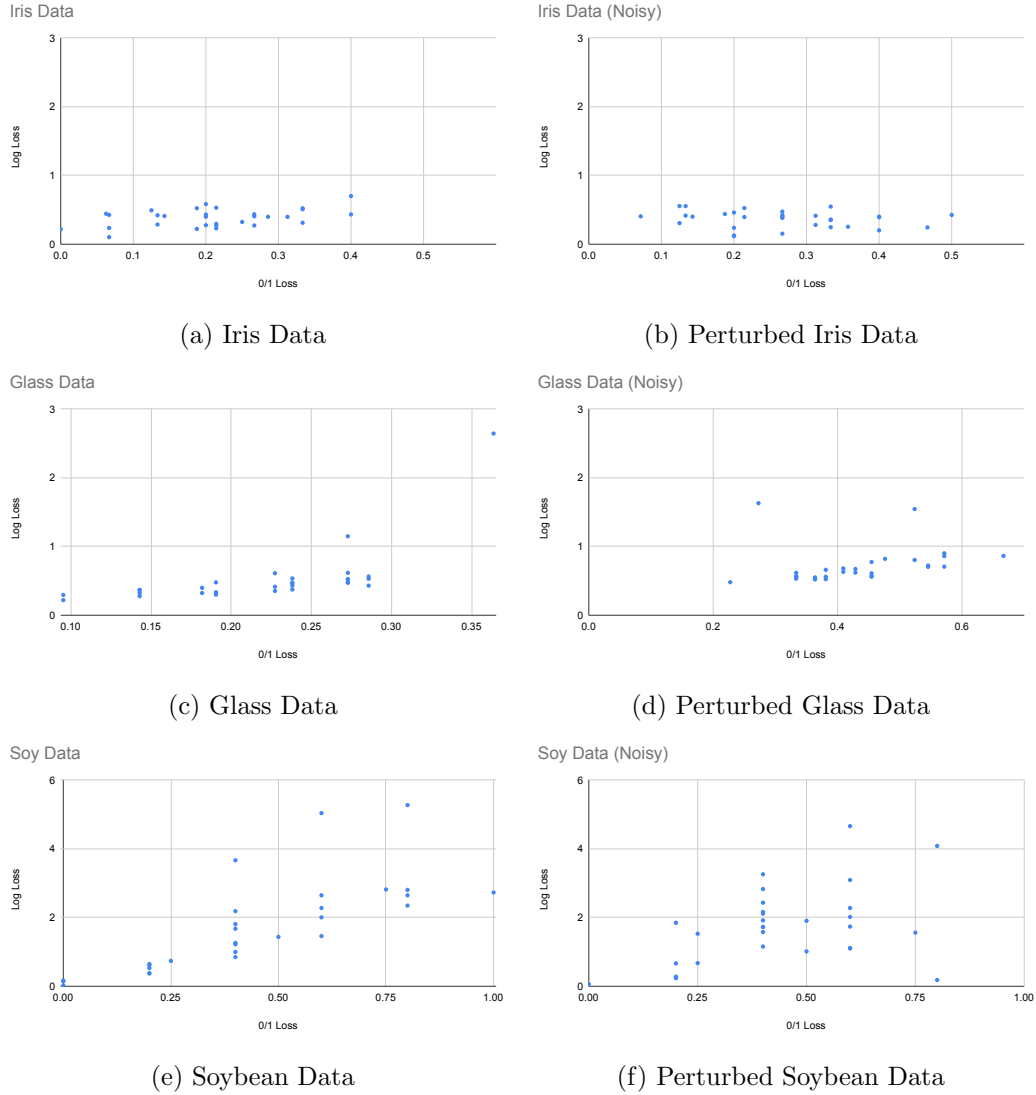


Figure 2: Log Loss vs 0/1 Loss for Iris, Glass, and Soybean data. These datasets did not perform quite as well as the four datasets in 1. (Data is more dispersed throughout the scatterplot)