

Solution 21.13**(a)** Analytical solution:

$$\int_0^{0.6} 2e^{-1.5x} dx = \left[-1.33333e^{-1.5x} \right]_0^{0.6} = -0.54209 - (-1.33333) = 0.79124$$

(b) Trapezoidal rule

$$\begin{aligned} I = & (0.05 - 0) \frac{2 + 1.8555}{2} + (0.15 - 0.05) \frac{1.8555 + 1.597}{2} + (0.25 - 0.15) \frac{1.597 + 1.3746}{2} \\ & + (0.35 - 0.25) \frac{1.3746 + 1.1831}{2} + (0.475 - 0.35) \frac{1.1831 + 0.9808}{2} \\ & + (0.6 - 0.475) \frac{0.9808 + 0.8131}{2} = 0.79284 \end{aligned}$$

$$\varepsilon_t = \left| \frac{0.79124 - 0.79284}{0.79124} \right| \times 100\% = 0.2022\%$$

(c) Trapezoidal/Simpson's rules

$$\begin{aligned} I = & (0.05 - 0) \frac{2 + 1.8555}{2} + (0.35 - 0.05) \frac{1.8555 + 3(1.597 + 1.3746) + 1.1831}{8} \\ & + (0.6 - 0.35) \frac{1.1831 + 4(0.9808) + 0.8131}{6} = 0.791282 \end{aligned}$$

$$\varepsilon_t = \left| \frac{0.79124 - 0.791282}{0.79124} \right| \times 100\% = 0.0052\%$$