

Solution 21.5

Analytical solution:

$$\int_{-3}^5 (4x-3)^3 dx = \left[\frac{1}{16}(4x-3)^4 \right]_{-3}^5 = 2056$$

Simpson's rule ($n = 4$):

$$I = (5 - (-3)) \frac{-3375 + 4(-343 + 729) + 2(1) + 4913}{12} = 2056 \quad \varepsilon_t = 0\%$$

Simpson's rules ($n = 5$):

$$I = (0.2 - (-3)) \frac{-3375 + 4(-636.056) - 10.648}{6} \\ + (5 - 0.2) \frac{-10.648 + 3(74.088 + 1191.016) + 4913}{8} = -3162.6 + 5218.598 = 2056 \quad \varepsilon_t = 0\%$$

Because Simpson's rules are perfect for cubics, both versions yield the exact result for this cubic polynomial.