

Solution 23.12

(a) This problem amounts to solving the following integral:

$$x = \int_0^t v(t) dt$$

We can use Simpson's 1/3 and 3/8 rule to make this evaluation,

$$\begin{aligned} x &= (16-0) \frac{0 + 4(34.7 + 82.8) + 2(61.8) + 99.2}{3(4)} + (28-16) \frac{99.2 + 3(112 + 121.9) + 129.7}{8} \\ &= 923.7333 + 1395.9 = 2319.633 \text{ m} \end{aligned}$$

(b) Because the points around $t = 28$ are equispaced, a centered finite divided difference provides a good estimate

$$a = \frac{dv}{dt} = \frac{135.7 - 121.9}{32 - 24} = 1.725 \frac{\text{m}}{\text{s}^2}$$

(c) For this case, an $O(h^2)$ forward difference can be used,

$$a = \frac{dv}{dt} = \frac{-61.8 + 4(34.7) - 3(0)}{8 - 0} = 9.625 \frac{\text{m}}{\text{s}^2}$$