

Solution 23.21**(a)**

$$v = \frac{dx}{dt} = x'(t_i) = \frac{x(t_{i+1}) - x(t_{i-1}))}{2h} = \frac{7.3 - 5.1}{4} = 0.55 \frac{\text{m}}{\text{s}}$$

$$a = \frac{d^2x}{dt^2} = x''(t_i) = \frac{x(t_{i+1}) - 2x(t_i) + x(t_{i-1}))}{h^2} = \frac{7.3 - 2(6.3) + 5.1}{2^2} = -0.05 \frac{\text{m}}{\text{s}^2}$$

(b)

$$v = \frac{-x(t_{i+2}) + 4x(t_{i+1}) - 3x(t_i))}{2h} = \frac{-8 + 4(7.3) - 3(6.3)}{4} = 0.575 \frac{\text{m}}{\text{s}}$$

$$a = \frac{-x(t_{i+3}) + 4x(t_{i+2}) - 5x(t_{i+1}) + 2x(t_i))}{h^2} = \frac{-8.4 + 4(8) - 5(7.3) + 2(6.3)}{2^2} = -0.075 \frac{\text{m}}{\text{s}^2}$$

(c)

$$v = \frac{3x(t_i) - 4x(t_{i-1}) + x(t_{i-2}))}{2h} = \frac{3(6.3) - 4(5.1) + 3.4}{4} = 0.475 \frac{\text{m}}{\text{s}}$$

$$a = \frac{2x(t_i) - 5x(t_{i-1}) + 4x(t_{i-2}) - x(t_{i-3}))}{h^2} = \frac{2(6.3) - 5(5.1) + 4(3.4) - 1.8}{2^2} = -0.275 \frac{\text{m}}{\text{s}^2}$$