

Everything you wanted to know (and more) about

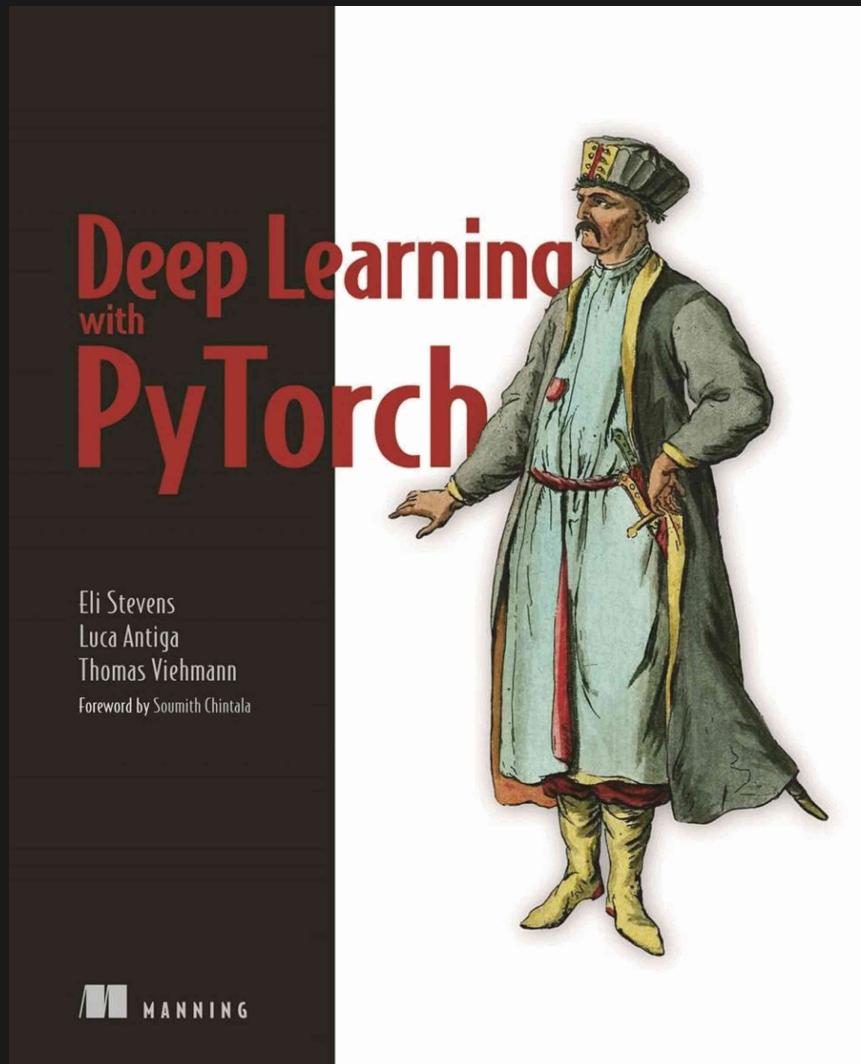
PyTorch tensors

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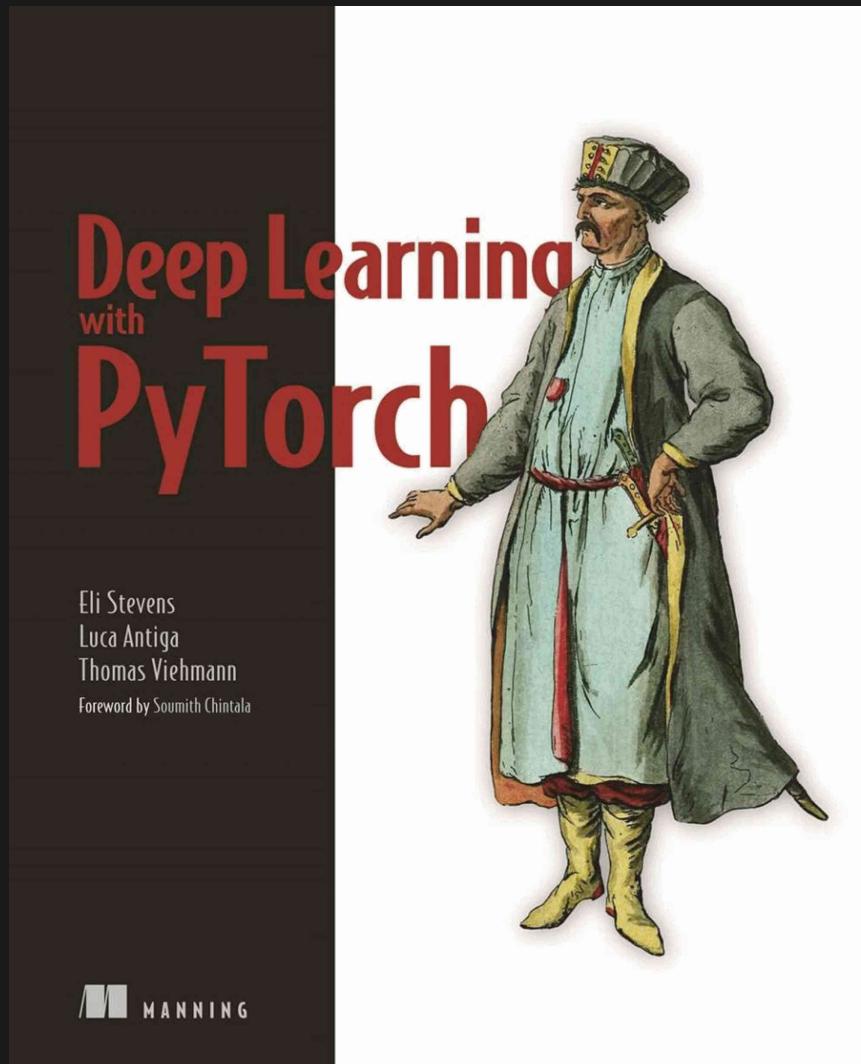
January 19, 2022



All drawings in this webinar come from the book:



The section on storage is also highly inspired by it



Using tensors locally

You need to have **Python** and **PyTorch** installed

Additionally, you might want to use an IDE such as **elpy** if you are an Emacs user, **JupyterLab**, etc.

Note that PyTorch does not yet support Python 3.10 except in some Linux distributions or on systems where a wheel has been built

For the time being, you might have to use it with Python 3.9

Using tensors on CC clusters

In the cluster terminal:

```
avail_wheels "torch*" # List available wheels & compatible Python versions
module avail python    # List available Python versions
module load python/3.9.6          # Load a sensible Python version
virtualenv --no-download env      # Create a virtual env
source env/bin/activate           # Activate the virtual env
pip install --no-index --upgrade pip # Update pip
pip install --no-index torch       # Install PyTorch
```

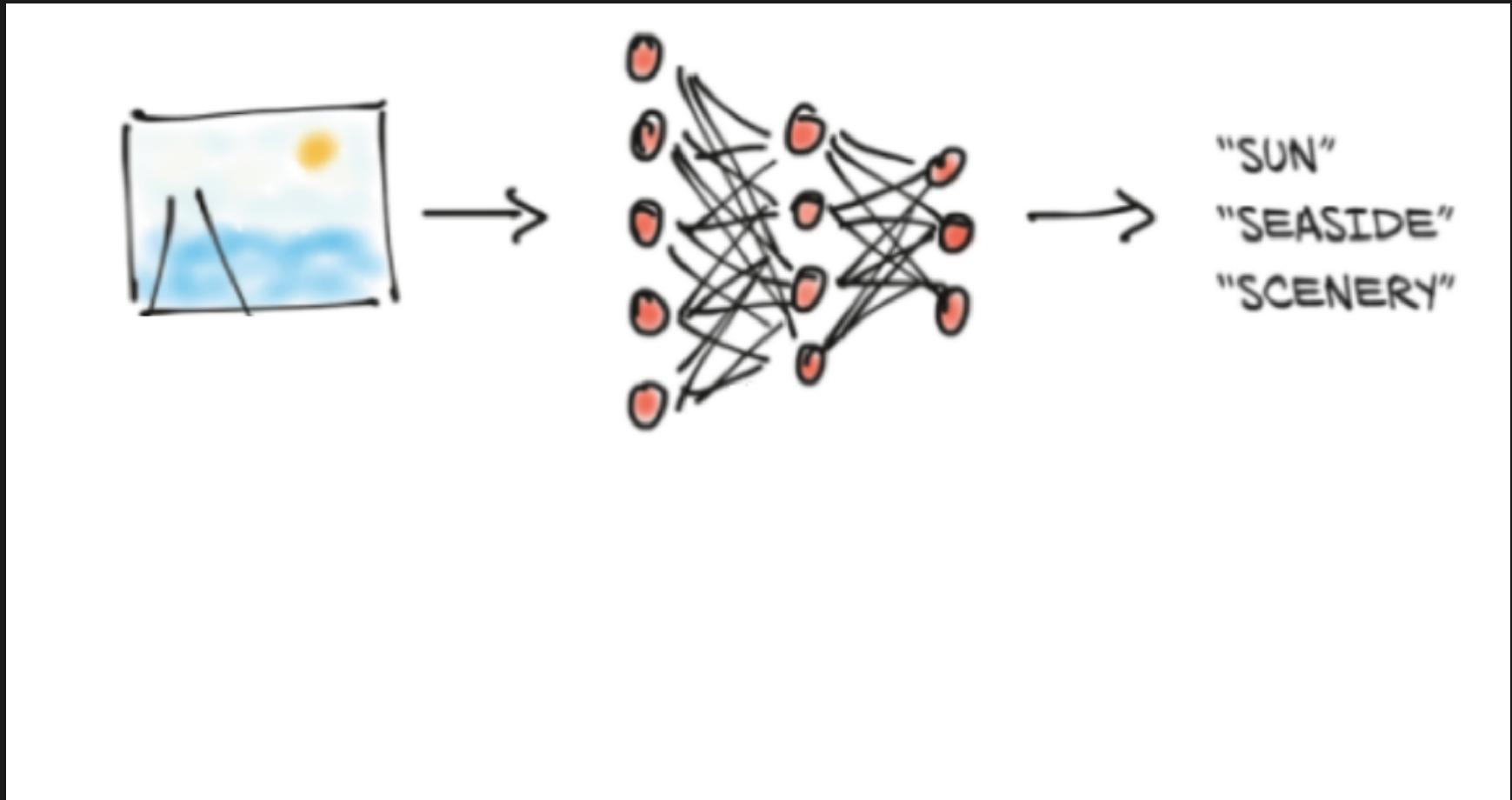
You can then run jobs with `sbatch` or `salloc`

You can leave the Python virtual env with `deactivate`

- What is a PyTorch tensor?
- Memory storage
- Data type (dtype)
- Basic operations
- Working with NumPy
- Linear algebra
- Harvesting the power of GPUs
- Distributed operations

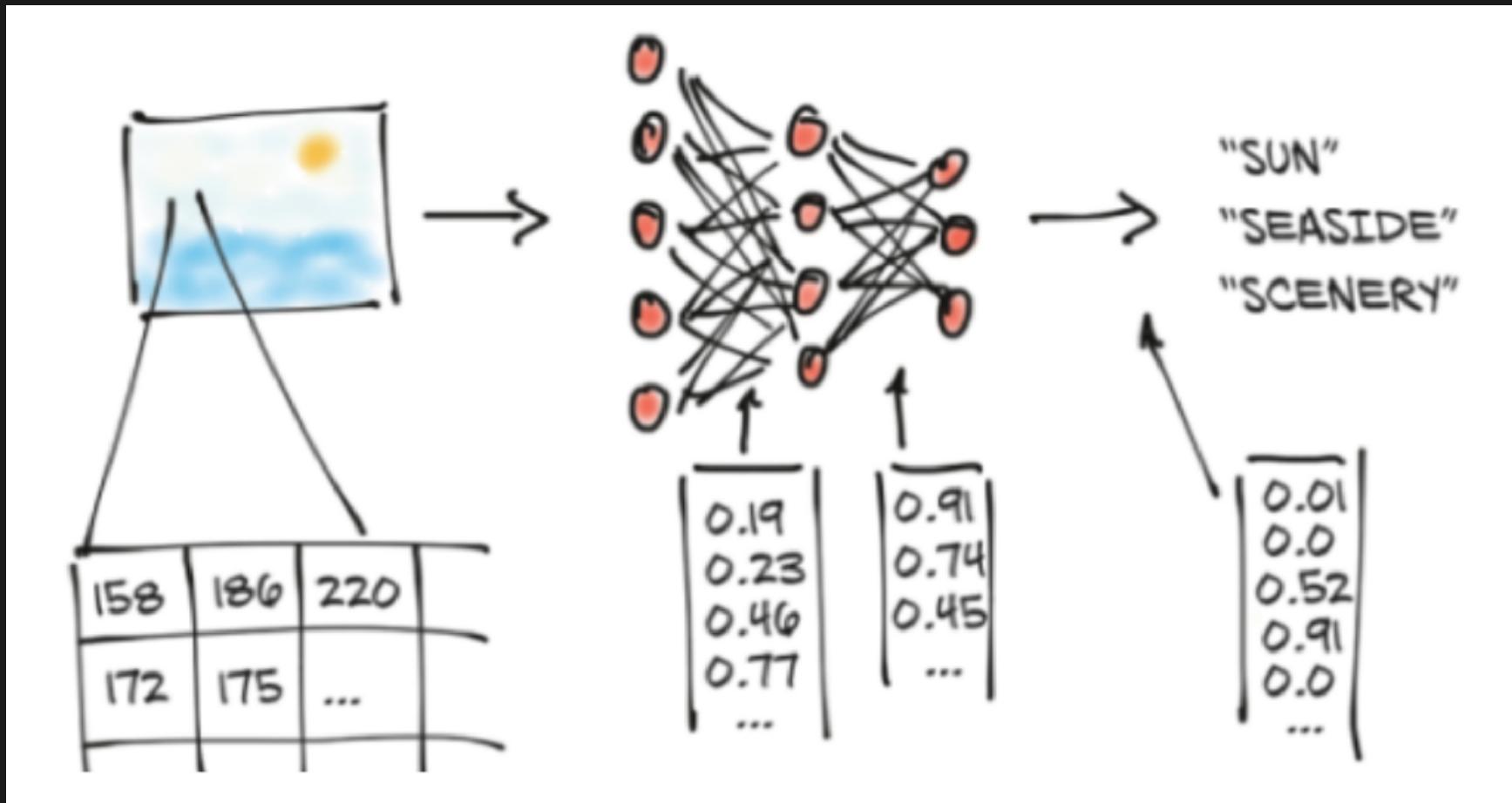
- What is a PyTorch tensor?
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ANN do not process information directly



Modified from Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

It needs to be converted to numbers

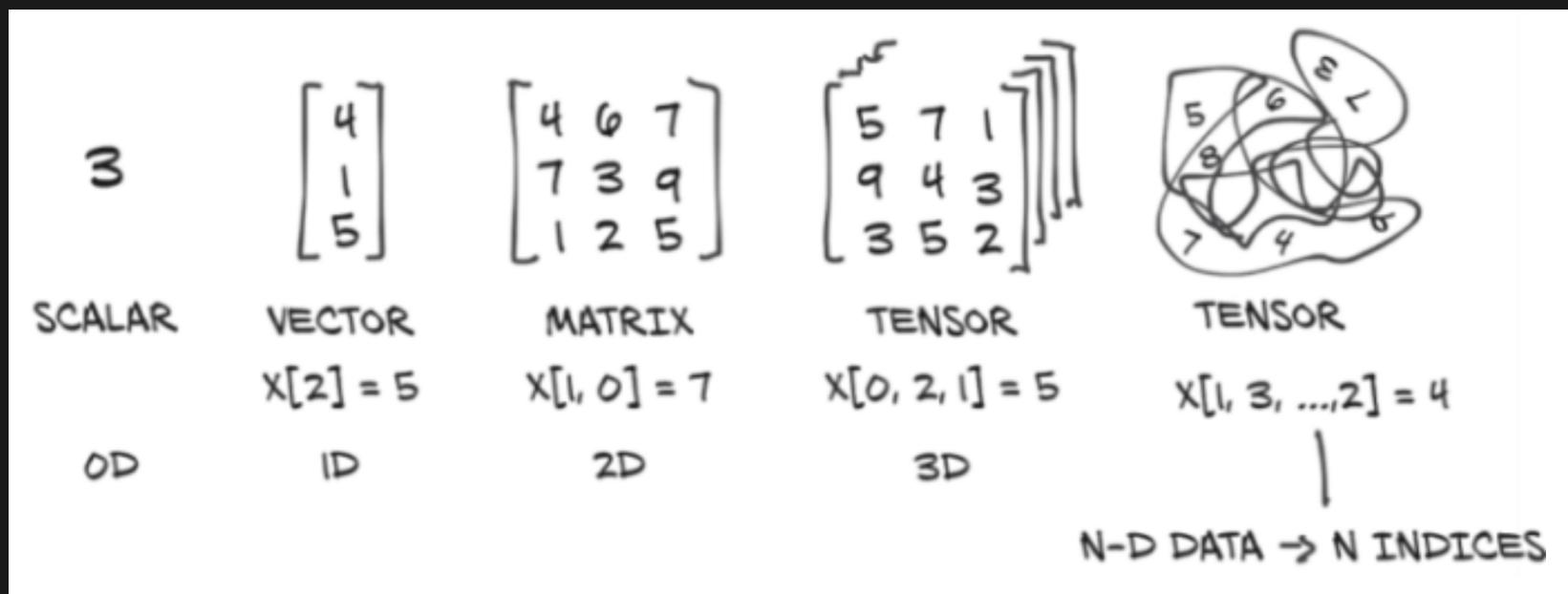


Modified from Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

**All these numbers need to be stored
in a data structure**

All these numbers need to be stored in a data structure

PyTorch tensors are Python objects holding multidimensional arrays



Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Why a new object when NumPy ndarray already exists?

- Can run on accelerators (GPUs, TPUs...)
- Keep track of computation graphs, allowing automatic differentiation
- Future plan for sharded tensors to run distributed computations

What is a PyTorch tensor?

PyTorch is foremost a **deep learning library**

In deep learning, the information contained in objects of interest (e.g. images, texts, sounds) is converted to **floating-point numbers** (e.g. pixel values, token values, frequencies)

As this information is complex, **multiple dimensions are required** (e.g. 2 dimensions for the width & height of an image, plus 1 dimension for the 3 RGB colour channels)

Additionally, as various objects are grouped into batches to be processed together, batch size adds yet another dimension

Multidimensional arrays are thus particularly well suited for deep learning

What is a PyTorch tensor?

Artificial neurons perform basic computations on these tensors

Their number however is huge & computing efficiency is paramount

GPUs are particularly well suited to perform many simple operations in parallel

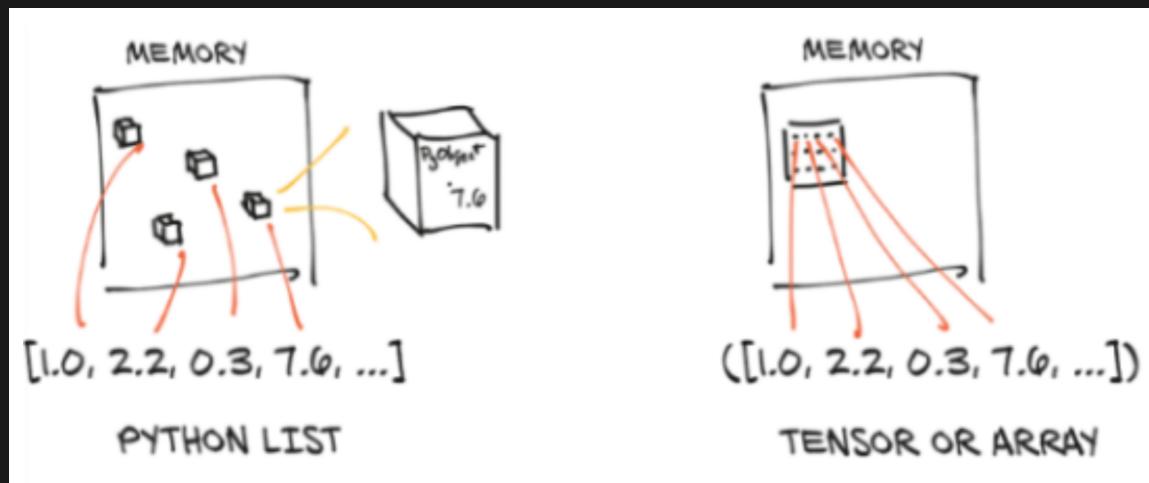
The very popular **NumPy library** has at its core a mature multidimensional array object well integrated into the scientific Python ecosystem

But the PyTorch tensor has additional efficiency characteristics ideal for machine learning & it can be converted to/from NumPy's ndarray if needed

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Efficient memory storage

In Python, collections (lists, tuples) are groupings of boxed Python objects
PyTorch tensors and NumPy ndarrays are made of unboxed C numeric types

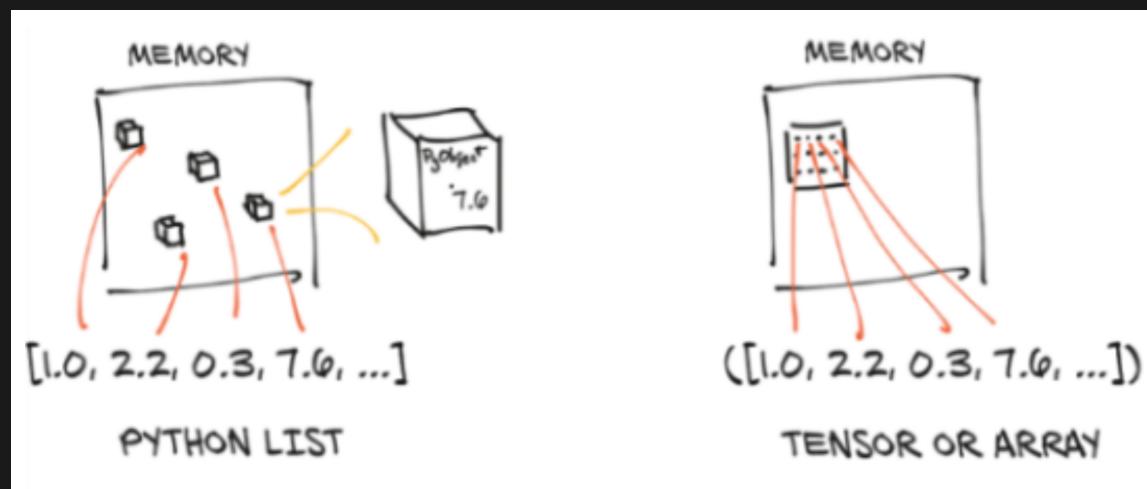


Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Efficient memory storage

They are usually contiguous memory blocks, but the main difference is that they are unboxed: floats will thus take 4 or 8 bytes each

Boxed values take up more memory (memory for the pointer + memory for the primitive)



Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Implementation

Under the hood, the values of a PyTorch tensor are stored as a `torch.Storage` instance which is a **one-dimensional array**

```
import torch
t = torch.arange(10.).view(2, 5); print(t) # Functions explained later
```

Output>>>

```
tensor([[ 0.,  1.,  2.,  3.,  4.],
        [ 5.,  6.,  7.,  8.,  9.]])
```

Implementation

```
storage = t.storage(); print(storage)
```

Output>>>

```
0.0
1.0
2.0
3.0
4.0
5.0
6.0
7.0
8.0
9.0
[torch.FloatTensor of size 10]
```

Implementation

Storage can be indexed

```
storage[3]
```

Output >>>

```
3.0
```

Implementation

```
storage[3] = 10.0; print(storage)
```

Output >>>

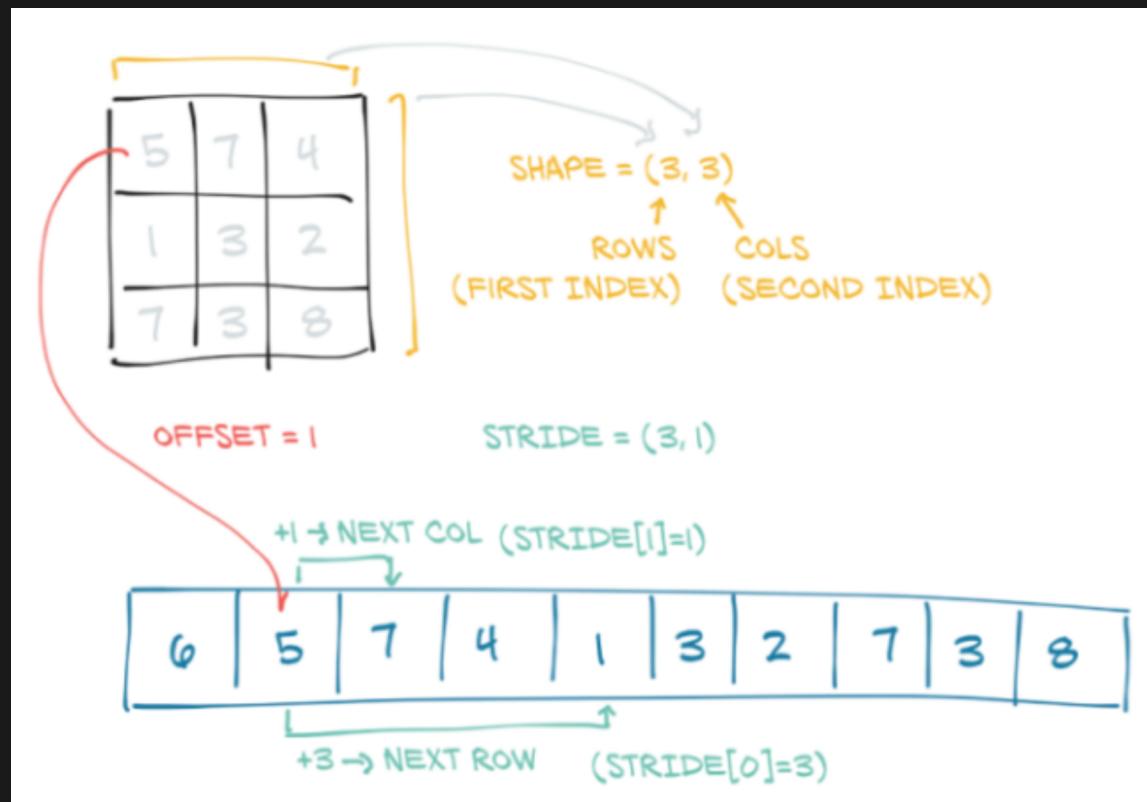
```
0.0
1.0
2.0
10.0
4.0
5.0
6.0
7.0
8.0
9.0
[torch.FloatTensor of size 10]
```

Implementation

To view a multidimensional array from storage, we need **metadata** :

- the **size** (*shape* in NumPy) sets the number of elements in each dimension
- the **offset** indicates where the first element of the tensor is in the storage
- the **stride** establishes the increment between each element

Storage metadata



Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Storage metadata

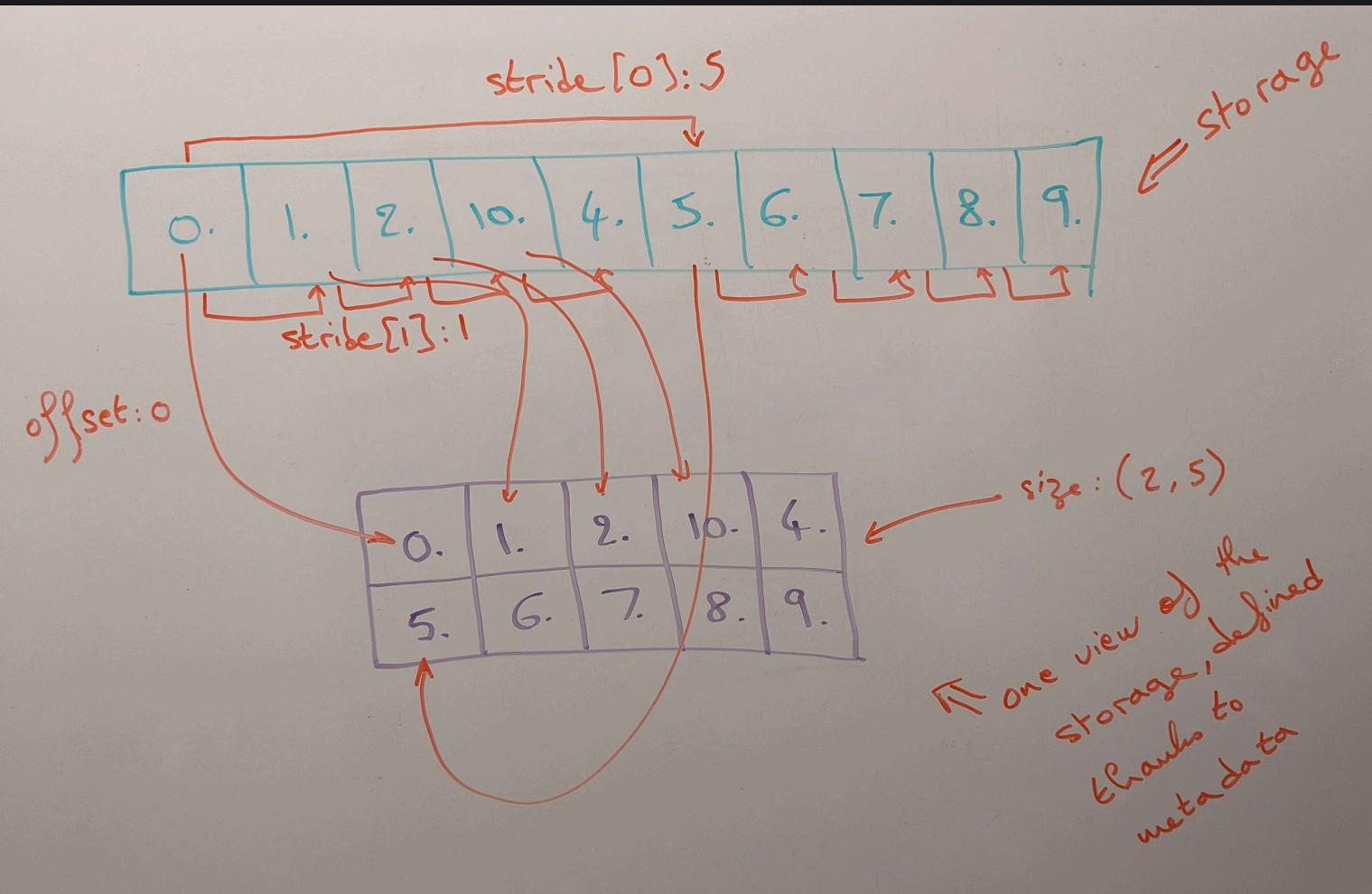
```
t.size()  
t.storage_offset()  
t.stride()
```

Output>>>

```
torch.Size([2, 5])  
0  
(5, 1)
```

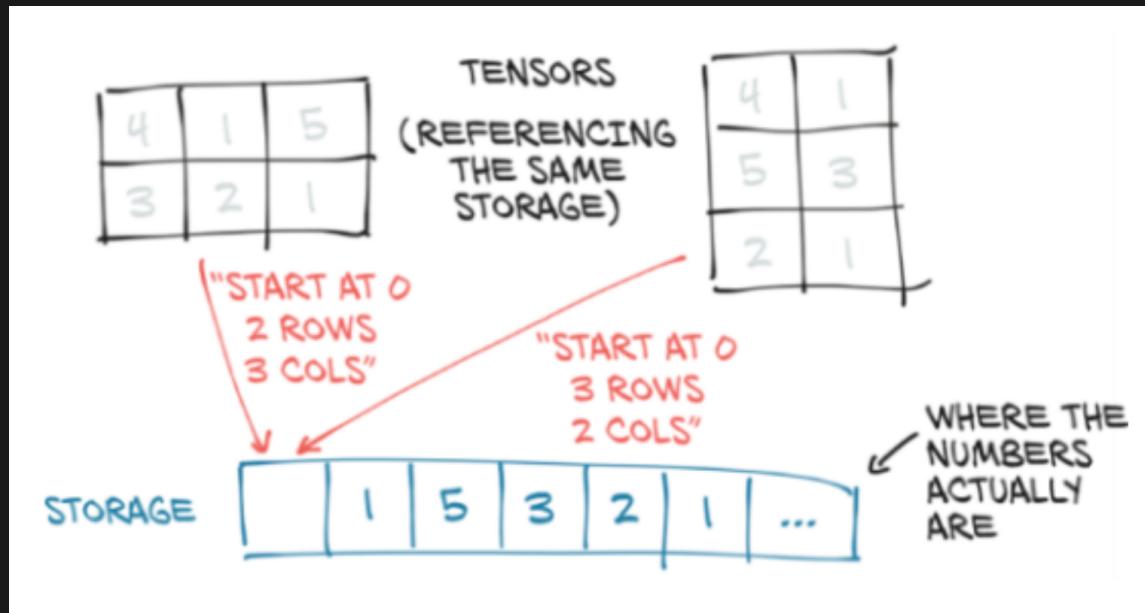
```
size: (2, 5)  
offset: 0  
stride: (5, 1)
```

Storage metadata



Sharing storage

Multiple tensors can use the same storage, saving a lot of memory since the metadata is a lot lighter than a whole new array



Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Transposing in 2 dimensions

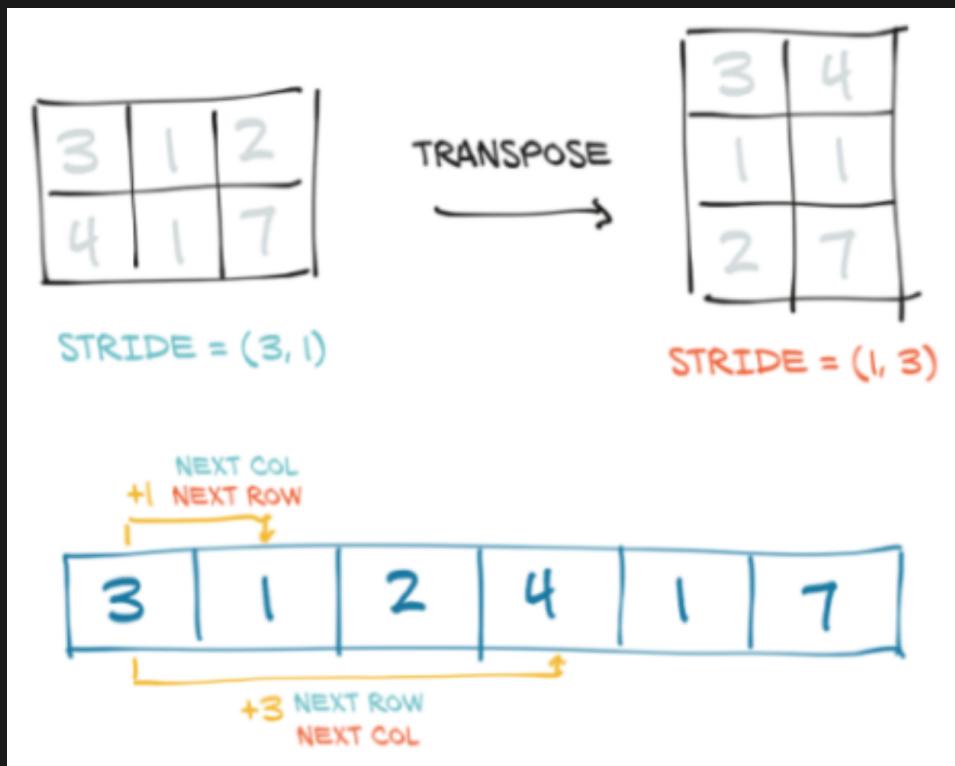
```
t = torch.tensor([[3, 1, 2], [4, 1, 7]]); print(t)
t.size()
t.t()
t.t().size()
```

Output >>>

```
tensor([[3, 1, 2],
        [4, 1, 7]])
torch.Size([2, 3])
tensor([[3, 4],
        [1, 1],
        [2, 7]])
torch.Size([3, 2])
```

Transposing in 2 dimensions

= flipping the stride elements around



Stevens, E., Antiga, L., & Viehmann, T. (2020). Deep learning with PyTorch. Manning Publications

Transposing in higher dimensions

`torch.t()` is a shorthand for `torch.transpose(0, 1)`:

```
torch.equal(t.t(), t.transpose(0, 1))
```

Output>>>

```
True
```

While `torch.t()` only works for 2D tensors, `torch.transpose()` can be used to transpose 2 dimensions in tensors of any number of dimensions

Transposing in higher dimensions

```
t = torch.zeros(1, 2, 3); print(t)  
t.size()
```

Output>>>

```
tensor([[[0., 0., 0.],  
        [0., 0., 0.]]])  
  
torch.Size([1, 2, 3])
```

Transposing in higher dimensions

```
t.transpose(0, 1)
```

```
t.transpose(0, 1).size()
```

Output>>>

```
tensor([[[0., 0., 0.]],  
       [[0., 0., 0.]]])
```

```
torch.Size([2, 1, 3])
```

Transposing in higher dimensions

```
t.transpose(0, 2)
```

```
t.transpose(0, 2).size()
```

Output>>>

```
tensor([[[0.],
          [0.]],
         [[0.],
          [0.]],
         [[0.],
          [0.]]])
```

```
torch.Size([3, 2, 1])
```

Transposing in higher dimensions

```
t.transpose(1, 2)
```

```
t.transpose(1, 2).size()
```

Output>>>

```
tensor([[[0., 0.],  
        [0., 0.],  
        [0., 0.]]])
```

```
torch.Size([1, 3, 2])
```

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Default dtype

Since PyTorch tensors were built with utmost efficiency in mind for neural networks, the default data type is **32-bit floating points**

This is sufficient for accuracy and much faster than 64-bit floating points

| Note that, by contrast, NumPy ndarrays use 64-bit as their default

List of PyTorch tensor dtypes

torch.float16 / torch.half	16-bit / half-precision floating-point
torch.float32 / torch.float	32-bit / single-precision floating-point
torch.float64 / torch.double	64-bit / double-precision floating-point
hrule	hrule
torch.uint8	unsigned 8-bit integers
torch.int8	signed 8-bit integers
torch.int16 / torch.short	signed 16-bit integers
torch.int32 / torch.int	signed 32-bit integers
torch.int64 / torch.long	signed 64-bit integers
hrule	hrule
torch.bool	boolean

Checking & changing dtype

```
t = torch.rand(2, 3); print(t)
t.dtype    # remember that the default dtype for PyTorch tensors is float32
t2 = t.type(torch.float64); print(t2) # if dtype ≠ default, it is printed
t2.dtype
```

Output>>>

```
tensor([[0.8130, 0.3757, 0.7682],
        [0.3482, 0.0516, 0.3772]])
torch.float32
tensor([[0.8130, 0.3757, 0.7682],
        [0.3482, 0.0516, 0.3772]], dtype=torch.float64)
torch.float64
```

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Creating tensors

- `torch.tensor`: Input individual values
- `torch.arange`: Similar to `range` but creates a 1D tensor
- `torch.linspace`: 1D linear scale tensor
- `torch.logspace`: 1D log scale tensor
- `torch.rand`: Random numbers from a uniform distribution on $[0, 1)$
- `torch.randn`: Numbers from the standard normal distribution
- `torch.randperm`: Random permutation of integers
- `torch.empty`: Uninitialized tensor
- `torch.zeros`: Tensor filled with `0`
- `torch.ones`: Tensor filled with `1`
- `torch.eye`: Identity matrix

Creating tensors

```
torch.manual_seed(0) # If you want to reproduce the result  
torch.rand(1)
```

```
torch.manual_seed(0) # Run before each operation to get the same result  
torch.rand(1).item() # Extract the value from a tensor
```

Output>>>

```
tensor([0.4963])
```

```
0.49625658988952637
```

Creating tensors

```
torch.rand(1)
torch.rand(1, 1)
torch.rand(1, 1, 1)
torch.rand(1, 1, 1, 1)
```

Output >>>

```
tensor([0.6984])
tensor([[0.5675]])
tensor([[[0.8352]]])
tensor([[[[0.2056]]]])
```

Creating tensors

```
torch.rand(2)  
torch.rand(2, 2, 2, 2)
```

Output>>>

```
tensor([0.5932, 0.1123])  
tensor([[[[0.1147, 0.3168],  
         [0.6965, 0.9143]],  
        [[0.9351, 0.9412],  
         [0.5995, 0.0652]]],  
       [[[0.5460, 0.1872],  
         [0.0340, 0.9442]],  
        [[0.8802, 0.0012],  
         [0.5936, 0.4158]]]])
```

Creating tensors

```
torch.rand(2)
torch.rand(3)
torch.rand(1, 1)
torch.rand(1, 1, 1)
torch.rand(2, 6)
```

Output >>>

```
tensor([0.7682, 0.0885])
tensor([0.1320, 0.3074, 0.6341])
tensor([[0.4901]])
tensor([[[0.8964]]])
tensor([[ [0.4556, 0.6323, 0.3489, 0.4017, 0.0223, 0.1689],
          [0.2939, 0.5185, 0.6977, 0.8000, 0.1610, 0.2823]]])
```

Creating tensors

```
torch.rand(2, 4, dtype=torch.float64) # You can set dtype  
torch.ones(2, 1, 4, 5)
```

Output>>>

```
tensor([[0.6650, 0.7849, 0.2104, 0.6767],  
       [0.1097, 0.5238, 0.2260, 0.5582]], dtype=torch.float64)  
tensor([[[[1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.]]],  
       [[[1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.],  
          [1., 1., 1., 1., 1.]]]])
```

Creating tensors

```
t = torch.rand(2, 3); print(t)
torch.zeros_like(t)                  # matches the size of t
torch.ones_like(t)
torch.randn_like(t)
```

Output>>>

```
tensor([[0.4051,  0.6394,  0.0871],
        [0.4509,  0.5255,  0.5057]])
tensor([[0.,  0.,  0.],
        [0.,  0.,  0.]])
tensor([[1.,  1.,  1.],
        [1.,  1.,  1.]])
tensor([[[-0.3088, -0.0104,  1.0461],
        [ 0.9233,  0.0236, -2.1217]]])
```

Creating tensors

```
torch.arange(2, 10, 4)      # from 2 to 10 in increments of 4  
torch.linspace(2, 10, 4)   # 4 elements from 2 to 10 on the linear scale  
torch.logspace(2, 10, 4)   # Same on the log scale  
torch.randperm(4)  
torch.eye(3)
```

Output>>>

```
tensor([2, 6])  
tensor([2.0000, 4.6667, 7.3333, 10.0000])  
tensor([1.0000e+02, 4.6416e+04, 2.1544e+07, 1.0000e+10])  
tensor([1, 3, 2, 0])  
tensor([[1., 0., 0.],  
       [0., 1., 0.],  
       [0., 0., 1.]])
```

Tensor indexing

```
x = torch.rand(3, 4)
x[:]                      # With a range, the comma is implicit: same as x[:, :]
x[:, 2]
x[1, :]
x[2, 3]
```

Output >>>

```
tensor([[0.6575,  0.4017,  0.7391,  0.6268],
       [0.2835,  0.0993,  0.7707,  0.1996],
       [0.4447,  0.5684,  0.2090,  0.7724]]))
tensor([0.7391,  0.7707,  0.2090])
tensor([0.2835,  0.0993,  0.7707,  0.1996])
tensor(0.7724)
```

Tensor indexing

```
x[-1:]      # Last element (implicit comma, so all columns)
x[-1]       # No range, no implicit comma: we are indexing
# from a list of tensors, so the result is a one dimensional tensor
# (Each dimension is a list of tensors of the previous dimension)
x[-1].size() # Same number of dimensions than x (2 dimensions)
x[-1:].size() # We dropped one dimension
```

Output>>>

```
tensor([[0.8168, 0.0879, 0.2642, 0.3777]])
tensor([0.8168, 0.0879, 0.2642, 0.3777])

torch.Size([4])
torch.Size([1, 4])
```

Tensor indexing

```
x[0:1]      # Python ranges are inclusive to the left, not the right  
x[:-1]      # From start to one before last (and implicit comma)  
x[0:3:2]    # From 0th (included) to 3rd (excluded) in increment of 2
```

Output>>>

```
tensor([[0.5873, 0.0225, 0.7234, 0.4538]])  
tensor([[0.5873, 0.0225, 0.7234, 0.4538],  
       [0.9525, 0.0111, 0.6421, 0.4647]])  
tensor([[0.5873, 0.0225, 0.7234, 0.4538],  
       [0.8168, 0.0879, 0.2642, 0.3777]])
```

Tensor indexing

```
x[None]           # Adds a dimension of size one as the 1st dimension  
x.size()  
x[None].size()
```

Output >>>

```
tensor([[[0.5873, 0.0225, 0.7234, 0.4538],  
        [0.9525, 0.0111, 0.6421, 0.4647],  
        [0.8168, 0.0879, 0.2642, 0.3777]]])  
torch.Size([3, 4])  
torch.Size([1, 3, 4])
```

Tensor information

```
t = torch.rand(2, 3); print(t)
t.size()
t.dim()
t.numel()
```

Output>>>

```
tensor([[0.5885, 0.7005, 0.1048],
        [0.1115, 0.7526, 0.0658]])
torch.Size([2, 3])
2
6
```

Vectorized operations

Since PyTorch tensors are homogeneous (i.e. made of a single data type), **as with NumPy's ndarrays**, operations are vectorized & thus staggeringly fast

Simple mathematical operations

```
t1 = torch.arange(1, 5).view(2, 2); print(t1)
t2 = torch.tensor([[1, 1], [0, 0]]); print(t2)
t1 + t2 # Operation performed between elements at corresponding locations
t1 + 1 # Operation applied to each element of the tensor
```

Output>>>

```
tensor([[1, 2],
        [3, 4]])
tensor([[1, 1],
        [0, 0]])
tensor([[2, 3],
        [3, 4]])
tensor([[2, 3],
        [4, 5]])
```

Reduction

```
t = torch.ones(2, 3, 4); print(t)
t.sum()    # Reduction over all entries
```

Output>>>

```
tensor([[[1., 1., 1., 1.],
         [1., 1., 1., 1.],
         [1., 1., 1., 1.]],
        [[1., 1., 1., 1.],
         [1., 1., 1., 1.],
         [1., 1., 1., 1.]]])
tensor(24.)
```

| Other reduction functions (e.g. mean) behave the same way

Reduction

```
# Reduction over a specific dimension  
t.sum(0)  
t.sum(1)  
t.sum(2)
```

Output>>>

```
tensor([[2., 2., 2., 2.],  
       [2., 2., 2., 2.],  
       [2., 2., 2., 2.]])  
tensor([[3., 3., 3., 3.],  
       [3., 3., 3., 3.]])  
tensor([[4., 4., 4.],  
       [4., 4., 4.]])
```

Reduction

```
# Reduction over multiple dimensions  
t.sum((0, 1))  
t.sum((0, 2))  
t.sum((1, 2))
```

Output>>>

```
tensor([6., 6., 6., 6.])  
tensor([8., 8., 8.])  
tensor([12., 12.])
```

In-place operations

With operators post-fixed with `_`:

```
t1 = torch.tensor([1, 2]); print(t1)
t2 = torch.tensor([1, 1]); print(t2)
t1.add_(t2); print(t1)
t1.zero_(); print(t1)
```

Output>>>

```
tensor([1, 2])
tensor([1, 1])
tensor([2, 3])
tensor([0, 0])
```

In-place operations vs reassignments

```
t1 = torch.ones(1); t1, hex(id(t1))
t1.add_(1); t1, hex(id(t1))      # In-place operation: same address
t1 = t1.add(1); t1, hex(id(t1))  # Reassignment: new address in memory
t1 = t1 + 1; t1, hex(id(t1))    # Reassignment: new address in memory
```

Output>>>

```
(tensor([1.]), '0x7fc61accc3b0')
(tensor([2.]), '0x7fc61accc3b0')
(tensor([3.]), '0x7fc61accc5e0')
(tensor([4.]), '0x7fc61accc6d0')
```

Tensor views

```
t = torch.tensor([[1, 2, 3], [4, 5, 6]]); print(t)
t.size()
t.view(6)
t.view(3, 2)
t.view(3, -1) # Same: with -1, the size is inferred from other dimensions
```

Output>>>

```
tensor([[1, 2, 3],
        [4, 5, 6]])
torch.Size([2, 3])
tensor([1, 2, 3, 4, 5, 6])
tensor([[1, 2],
        [3, 4],
        [5, 6]])
```

Note the difference

```
t1 = torch.tensor([[1, 2, 3], [4, 5, 6]]); print(t1)
t2 = t1.t(); print(t2)
t3 = t1.view(3, 2); print(t3)
```

Output>>>

```
tensor([[1, 2, 3],
        [4, 5, 6]])
tensor([[1, 4],
        [2, 5],
        [3, 6]])
tensor([[1, 2],
        [3, 4],
        [5, 6]])
```

Logical operations

```
t1 = torch.randperm(5); print(t1)
t2 = torch.randperm(5); print(t2)
t1 > 3                         # Test each element
t1 < t2                         # Test corresponding pairs of elements
```

Output>>>

```
tensor([4, 1, 0, 2, 3])
tensor([0, 4, 2, 1, 3])
tensor([ True, False, False, False, False])
tensor([False,  True,  True, False, False])
```

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Conversion without copy

PyTorch tensors can be converted to NumPy ndarrays & vice-versa in a very efficient manner as both objects share the same memory

```
t = torch.rand(2, 3); print(t)
t_np = t.numpy(); print(t_np)      # From PyTorch tensor to NumPy ndarray
```

Output >>>

```
tensor([[0.8434,  0.0876,  0.7507],
        [0.1457,  0.3638,  0.0563]])  # PyTorch Tensor

[[0.84344184 0.08764815 0.7506627 ]
 [0.14567494 0.36384273 0.05629885]] # NumPy ndarray
```

Mind the different defaults

```
t_np.dtype
```

Output >>>

```
dtype('float32')
```

Remember that PyTorch tensors use 32-bit floating points by default
(because this is what you want in neural networks)

But NumPy defaults to 64-bit
Depending on your workflow, you might have to change dtype

From NumPy to PyTorch

```
import numpy as np
a = np.random.rand(2, 3); print(a)
a_pt = torch.from_numpy(a); print(a_pt)      # From ndarray to tensor
```

Output>>>

```
[[0.55892276 0.06026952 0.72496545]
 [0.65659463 0.27697739 0.29141587]]

tensor([[0.5589, 0.0603, 0.7250],
        [0.6566, 0.2770, 0.2914]], dtype=torch.float64)
```

| Here again, you might have to change dtype

Notes about conversion without copy

`t` and `t_np` are objects of different Python types, so, as far as Python is concerned, they have different addresses

```
id(t) == id(t_np)
```

Output >>>

```
False
```

Notes about conversion without copy

However—and that's quite confusing—they share an underlying C array in memory & modifying one in-place also modifies the other

```
t.zero_()
print(t_np)
```

Output >>>

```
tensor([[0., 0., 0.],
       [0., 0., 0.]])
[[0. 0. 0.]
 [0. 0. 0.]]
```

Notes about conversion without copy

Lastly, as NumPy only works on CPU, to convert a PyTorch tensor allocated to the GPU, the content will have to be copied to the CPU first

- What is a PyTorch tensor?
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`torch.linalg` module

- All functions from `numpy.linalg` implemented
(with accelerator & automatic differentiation support)
- Some additional functions

Requires `torch >= 1.9`

Linear algebra support was less developed before the introduction of this module

System of linear equations solver

Let's have a look at an extremely basic example:

$$2x + 3y - z = 5$$

$$x - 2y + 8z = 21$$

$$6x + y - 3z = -1$$

We are looking for the values of x , y , and z that would satisfy this system

System of linear equations solver

We create a 2D tensor `A` of size `(3, 3)` with the coefficients of the equations & a 1D tensor `b` of size `3` with the right hand sides values of the equations

```
A = torch.tensor([[2., 3., -1.], [1., -2., 8.], [6., 1., -3.]])  
b = torch.tensor([5., 21., -1.]); print(b)
```

Output>>>

```
tensor([[ 2.,  3., -1.],  
       [ 1., -2.,  8.],  
       [ 6.,  1., -3.]])  
tensor([ 5., 21., -1.])
```

System of linear equations solver

Solving this system is as simple as running the `torch.linalg.solve` function:

```
x = torch.linalg.solve(A, b); print(x)
```

Output>>>

```
tensor([1., 2., 3.])
```

Our solution is:

x = 1

y = 2

z = 3

Verify our result

```
torch.allclose(A @ x, b)
```

Output>>>

```
True
```

System of linear equations solver

Here is another simple example:

```
# Create a square normal random matrix
A = torch.randn(4, 4); print(A)
# Create a tensor of right hand side values
b = torch.randn(4); print(b)

# Solve the system
x = torch.linalg.solve(A, b); print(x)

# Verify
torch.allclose(A @ x, b)
```

System of linear equations solver

Output >>>

With 2 multidimensional tensors

```
A = torch.randn(2, 3, 3)                      # Must be batches of square matrices
B = torch.randn(2, 3, 5)                      # Dimensions must be compatible
X = torch.linalg.solve(A, B); print(X)
torch.allclose(A @ X, B)
```

Output>>>

```
tensor([[[ -0.0545,  -0.1012,   0.7863,  -0.0806,  -0.0191],
         [ -0.9846,  -0.0137,  -1.7521,  -0.4579,  -0.8178],
         [ -1.9142,  -0.6225,  -1.9239,  -0.6972,   0.7011]],
        [[  3.2094,    0.3432,  -1.6604,  -0.7885,   0.0088],
         [  7.9852,    1.4605,  -1.7037,  -0.7713,   2.7319],
         [ -4.1979,    0.0849,   1.0864,   0.3098,  -1.0347]]])
```

True

Matrix inversions

| It is faster and more numerically stable to solve a system of linear equations directly than to compute the inverse matrix first

**Limit matrix inversions to situations where it is
truly necessary**

Matrix inversions

```
A = torch.rand(2, 3, 3)      # Batch of square matrices
A_inv = torch.linalg.inv(A)  # Batch of inverse matrices
A @ A_inv                   # Batch of identity matrices
```

Output>>>

```
tensor([[[ 1.0000e+00, -6.0486e-07,  1.3859e-06],
         [ 5.5627e-08,  1.0000e+00,  1.0795e-06],
         [-1.4133e-07,  7.9992e-08,  1.0000e+00]],

        [[[ 1.0000e+00,  4.3329e-08, -3.6741e-09],
          [-7.4627e-08,  1.0000e+00,  1.4579e-07],
          [-6.3580e-08,  8.2354e-08,  1.0000e+00]]])
```

Other linear algebra functions

`torch.linalg` contains many more functions, including for instance:

- `torch.tensordot` which generalizes matrix products
- `torch.linalg.tensorsolve` which computes the solution \mathbf{x} to the system
$$\text{torch.tensordot}(\mathbf{A}, \mathbf{x}) = \mathbf{B}$$
- `torch.linalg.eigvals` which computes the eigenvalues of a square matrix

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Device attribute

Tensor data can be placed in the memory of various processor types:

- the RAM of CPU
- the RAM of a GPU with CUDA support
- the RAM of a GPU with **AMD's ROCm support**
- the RAM of an **XLA device** (e.g. **Cloud TPU**) with the **torch_xla package**

Device attribute

The values for the device attributes are:

- CPU: 'cpu'
- GPU (CUDA and AMD's ROCm): 'cuda'
- XLA: xm.xla_device()

This last option requires to load the **torch_xla package** first:

```
import torch_xla
import torch_xla.core.xla_model as xm
```

Creating a tensor on a specific device

By default, tensors are created on the CPU

```
t1 = torch.rand(2); print(t1)
```

Output>>>

```
tensor([0.1606, 0.9771]) # Implicit: device='cpu'
```

| Printing a tensor only displays attributes \neq default values

Creating a tensor on a specific device

You can create a tensor on an accelerator by specifying the device attribute

```
t2_gpu = torch.rand(2, device='cuda'); print(t2_gpu)
```

Output>>>

```
tensor([0.0664, 0.7829], device='cuda:0') # :0 means the 1st GPU
```

Copying a tensor to a specific device

You can also make copies of a tensor on other devices

```
# Make a copy of t1 on the GPU
t1_gpu = t1.to(device='cuda'); print(t1_gpu)
t1_gpu = t1.cuda() # Same as above written differently

# Make a copy of t2_gpu on the CPU
t2 = t2_gpu.to(device='cpu'); print(t2)
t2 = t2_gpu.cpu() # For the alternative form
```

Output>>>

```
tensor([0.1606, 0.9771], device='cuda:0')
tensor([0.0664, 0.7829]) # Implicit: device='cpu'
```

Multiple GPUs

If you have multiple GPUs, you can optionally specify which GPU a tensor should be created on or copied to

```
t3_gpu = torch.rand(2, device='cuda:0')      # Create a tensor on 1st GPU
t4_gpu = t1.to(device='cuda:0')                # Make a copy of t1 on 1st GPU
t5_gpu = t1.to(device='cuda:1')                # Make a copy of t1 on 2nd GPU
```

Or the equivalent short forms for the last two:

```
t4_gpu = t1.cuda(0)
t5_gpu = t1.cuda(1)
```

Timing

Let's compare the timing of some matrix multiplications on CPU & GPU with PyTorch built-in benchmark utility

```
# Load utility
import torch.utils.benchmark as benchmark
# Define tensors on the CPU
A = torch.randn(500, 500)
B = torch.randn(500, 500)
# Define tensors on the GPU
A_gpu = torch.randn(500, 500, device='cuda')
B_gpu = torch.randn(500, 500, device='cuda')
```

I ran the code on my laptop with a dedicated GPU & 32GB RAM

Timing

Let's time 100 runs

```
t0 = benchmark.Timer(  
    stmt='A @ B',  
    globals={'A': A, 'B': B})  
  
t1 = benchmark.Timer(  
    stmt='A_gpu @ B_gpu',  
    globals={'A_gpu': A_gpu, 'B_gpu': B_gpu})  
  
print(t0.timeit(100))  
print(t1.timeit(100))
```

Timing

Output >>>

```
A @ B  
2.29 ms  
1 measurement, 100 runs , 1 thread
```

```
A_gpu @ B_gpu  
108.02 us  
1 measurement, 100 runs , 1 thread
```

Speedup:

$$(2.29 * 10^{**-3}) / (108.02 * 10^{**-6}) = 21$$

Timing

By replacing 500 with 5000, we get:

```
A @ B  
2.21 s  
1 measurement, 100 runs , 1 thread
```

```
A_gpu @ B_gpu  
57.88 ms  
1 measurement, 100 runs , 1 thread
```

Speedup:

```
2.21/(57.88 * 10**-3) = 38
```

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Parallel tensor operations

PyTorch already allows for **distributed training** of ML models

The implementation of distributed tensor operations—for instance for linear algebra—is **in the work through the use of a ShardedTensor primitive** that can be sharded across nodes

See also **this issue** for more comments about upcoming developments on (among other things) tensor sharding

Questions?