# **Syntax-based Statistical Machine Translation**

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- Part I Introduction
- Part II Rule Extraction
- Part III Decoding
- Part IV Extensions

### What Do We Mean by Syntax-based SMT?

- "Syntax-based" is a very inclusive term. It refers to a large family of approaches:
  - Hiero, syntax-directed MT, syntax-augmented MT, syntactified phrasebased MT, tree-to-string, string-to-dependency, dependency tree-let-based, soft syntax, fuzzy tree-to-tree, tree-based, . . .
- We mean that the translation model uses a tree-based representation of language.
  - We don't count syntax-based preordering or syntactic LMs.
- We will focus on four widely-used approaches:
  - 1. Hierarchical phrase-based
  - 2. Tree-to-string

- 3. String-to-tree
- 4. Tree-to-tree

### Why Use Syntax?

- Many translation problems can be best explained by pointing to syntax
  - reordering, e.g., verb movement in German–English translation
  - long distance agreement (e.g., subject-verb) in output
- Encourage grammatically coherent output
- Important step towards more linguistically motivated models (semantics)
- State-of-the art for some language pairs
  - Chinese-English (NIST 2008)
  - English-German (WMT 2012)
  - German-English (WMT 2013)

### **Statistical Machine Translation**

Given a source string, s, find the target string,  $t^*$ , with the highest probability according to a distribution p(t|s):

$$t^* = \arg\max_t p(t|s)$$

- 1. Model a probability distribution p(t|s)
- 2. Learn the parameters for the model
- 3. Find or approximate the highest probability string  $t^*$

### **Statistical Machine Translation**

- 1. Model a probability distribution p(t|s)
  - How is syntax used in modelling?
- 2. Learn the parameters for the model
  - What are the parameters of a syntax-based model?
- 3. Find or approximate the highest probability string  $t^*$ 
  - How do we decode with a syntax-based model?

# Modelling p(t|s)

• Most SMT models use Och and Ney's (2002) log-linear formulation:

$$p(t|s) = \frac{\exp\left(\sum_{m=1}^{M} \lambda_m h_m(t,s)\right)}{\sum_{t'} \exp\left(\sum_{m=1}^{M} \lambda_m h_m(t',s)\right)}$$

 $h_1, \ldots, h_M$  are real-valued functions and  $\lambda_1, \ldots, \lambda_M$  are real-valued constants

• Denominator can be ignored during search:

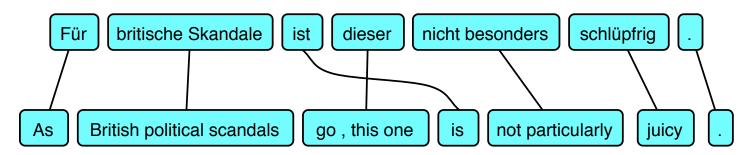
$$t^* = \arg \max_{t} p(t|s)$$
$$= \arg \max_{t} \sum_{m=1}^{M} \lambda_m h_m(t,s)$$

# Modelling p(t|s)

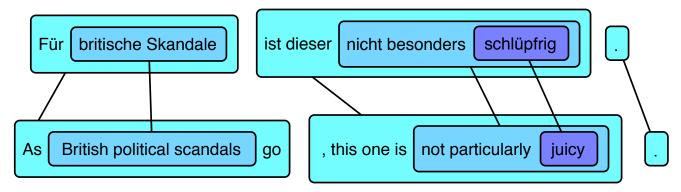
$$t^* = \arg\max_{t} \sum_{m=1}^{M} \lambda_m h_m(t, s) \tag{1}$$

- ullet In word-based models, s and t are modelled as sequences of words.
- ullet In phrase-based models, s and t are modelled as sequences of phrases.
- So what about syntax-based models?

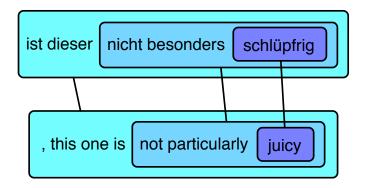
Like phrase pairs. . .



#### But with nesting:



Hierarchical phrase pairs:

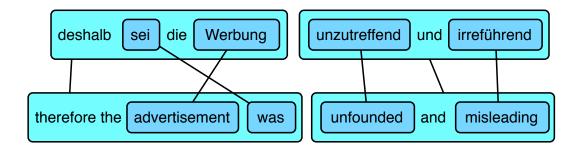


are modelled using Synchronous Context-Free Grammar (SCFG):

```
X \rightarrow ist \ dieser \ X_1 \mid , \ this \ one \ is \ X_1
```

 $\mathbf{X} \rightarrow nicht\ besonders\ \mathbf{X}_1 \mid not\ particularly\ \mathbf{X}_1$ 

 $\mathbf{x} \rightarrow schl\ddot{u}pfrig \mid juicy$ 



Rules can include up to two non-terminals:

$$X \rightarrow deshalb X_1 die X_2 \mid therefore the X_2 X_1 \ X \rightarrow X_1 und X_2 \mid X_1 and X_2$$

Glue rules concatenate hierarchical phrases:

$$S \rightarrow X_1 \mid X_1$$

$$S \rightarrow S_1 X_2 \mid S_1 X_2$$

- Synchronous Context-Free Grammar:
  - Rewrite rules of the form  $\langle A, B \rangle \to \langle \alpha, \beta, \sim \rangle$
  - -A and B are source and target non-terminals, respectively
  - $\alpha$  and  $\beta$  are strings of terminals and non-terminals for the source and target sides, respectively.
  - $-\sim$  is a one-to-one correspondence between source and target non-terminals.
- Hiero grammars are a special case of SCFG:
  - One non-terminal type, X, on source side
  - Two non-terminal types,  $\boldsymbol{x}$  and  $\boldsymbol{s}$ , on target side
  - Various restrictions on rule form (see Chiang (2007))

 $S_1 \mid S_1$ 

• Derivation starts with pair of linked S symbols.

$$S_1 \mid S_1$$

$$\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3$$

• 
$$s \rightarrow s_1 x_2 \mid s_1 x_2$$
 (glue rule)

$$S_1 \mid S_1$$

$$\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3$$

$$\Rightarrow S_2 \mid X_4 \mid Und \mid X_5 \mid S_2 \mid X_4 \mid Und \mid$$

•  $X \rightarrow X_1 \ und \ X_2 \mid X_1 \ and \ X_2$ 

```
S_1 \mid S_1
\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3
\Rightarrow S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid X_4 \mid und \mid X_5
\Rightarrow S_2 \mid unzut reffend \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid X_5 \mid S_3 \mid unfounded \mid und \mid X_5 \mid S_3 \mid unfounded \mid und \mid X_5 \mid S_4 \mid unfounded \mid und \mid X_5 \mid S_5 \mid unfounded \mid und \mid X_5 \mid unfounded \mid und \mid
```

 $\bullet$  X  $\rightarrow$  unzutreffend | unfounded

```
S_1 \mid S_1
\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3
\Rightarrow S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid X_4 \mid und \mid X_5
\Rightarrow S_2 \mid unzut reffend \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid unfounded \mid
```

•  $x \rightarrow irref\"{u}hrend \mid misleading$ 

```
S_1 \mid S_1
\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3
\Rightarrow S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid unfounded \mid unfoun
```

•  $s \rightarrow x_1 \mid x_1$  (glue rule)

```
S_1 \mid S_1
\Rightarrow S_2 \mid X_3 \mid S_2 \mid X_3
\Rightarrow S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid X_4 \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid X_5 \mid S_2 \mid unfounded \mid und \mid x_5 \mid S_2 \mid unfounded \mid und \mid unfounded \mid
```

•  $x \rightarrow deshalb x_1 die x_2 \mid therefore the x_2 x_1$  (non-terminal reordering)

```
\begin{array}{l} \mathbf{S}_{1} \ | \ \mathbf{S}_{1} \\ \Rightarrow \ \mathbf{S}_{2} \ \mathbf{X}_{3} \ | \ \mathbf{S}_{2} \ \mathbf{X}_{3} \\ \Rightarrow \ \mathbf{S}_{2} \ \mathbf{X}_{4} \ und \ \mathbf{X}_{5} \ | \ \mathbf{S}_{2} \ \mathbf{X}_{4} \ and \ \mathbf{X}_{5} \\ \Rightarrow \ \mathbf{S}_{2} \ unzutreffend \ und \ \mathbf{X}_{5} \ | \ \mathbf{S}_{2} \ unfounded \ and \ \mathbf{X}_{5} \\ \Rightarrow \ \mathbf{S}_{2} \ unzutreffend \ und \ irref\"{u}hrend \ | \ \mathbf{S}_{2} \ unfounded \ and \ misleading} \\ \Rightarrow \ \mathbf{X}_{6} \ unzutreffend \ und \ irref\"{u}hrend \ | \ \mathbf{X}_{6} \ unfounded \ and \ misleading} \\ \Rightarrow \ deshalb \ \mathbf{X}_{7} \ die \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ \mathbf{X}_{7} \ unfounded \ and \ misleading} \\ \Rightarrow \ deshalb \ sei \ die \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\"{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\ddot{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\ddot{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\ddot{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \ irref\ddot{u}hrend \ | \ therefore \ the \ \mathbf{X}_{8} \ unzutreffend \ und \
```

 $\bullet$  X  $\rightarrow$  sei | was

```
S_1 \mid S_1
    \Rightarrow S<sub>2</sub> X<sub>3</sub> | S<sub>2</sub> X<sub>3</sub>
    \Rightarrow S<sub>2</sub> X<sub>4</sub> und X<sub>5</sub> | S<sub>2</sub> X<sub>4</sub> and X<sub>5</sub>
    \Rightarrow S<sub>2</sub> unzutreffend und X<sub>5</sub> | S<sub>2</sub> unfounded and X<sub>5</sub>
    \Rightarrow S<sub>2</sub> unzutreffend und irreführend | S<sub>2</sub> unfounded and misleading
    \Rightarrow X<sub>6</sub> unzutreffend und irreführend | X<sub>6</sub> unfounded and misleading
    \Rightarrow deshalb x_7 die x_8 unzutreffend und irreführend
               therefore the X<sub>8</sub> X<sub>7</sub> unfounded and misleading
    \Rightarrow deshalb sei die x_8 unzutreffend und irreführend
               therefore the x_8 was unfounded and misleading
    ⇒ deshalb sei die Werbung unzutreffend und irreführend
               therefore the advertisement was unfounded and misleading
```

 $\bullet$  X  $\rightarrow$  Werbung | advertisement

We can now define the search in terms of SCFG derivations

$$t^* = \arg\max_{t} \sum_{m=1}^{M} \lambda_m h_m(t, s) \tag{1}$$

$$= \arg\max_{t} \sum_{m=1}^{M} \lambda_{m} h_{m}(t, s, d) \tag{2}$$

 $d \in D$ , the set of synchronous derivations with source s and yield t.

• In practice, approximated with search for single-best derivation:

$$d^* = \arg\max_{d} \sum_{m=1}^{M} \lambda_m h_m(t, s, d)$$
 (3)

• Search for single-best derivation:

$$d^* = \arg\max_{d} \sum_{m=1}^{M} \lambda_m h_m(t, s, d)$$
 (3)

• Rule-local feature functions allow decomposition of derivation scores:

$$h_m(d) = \sum_{r_i} h_m(r_i)$$

ullet But n-gram language model can't be decomposed this way. . .

$$d^* = \arg\max_{d} \left( \lambda_1 \log p_{LM}(d) + \sum_{r_i} \sum_{m=2}^{M} \lambda_m h_m(r_i) \right) \tag{4}$$

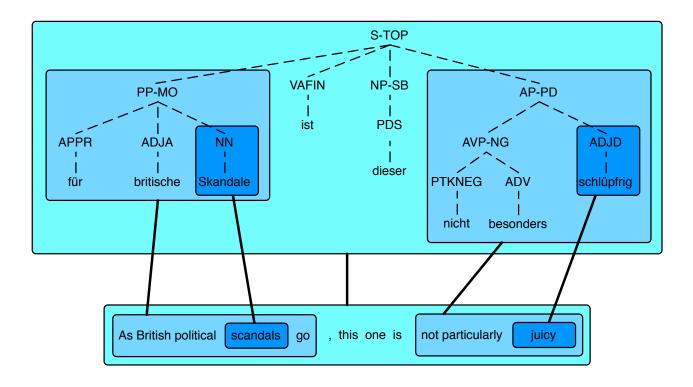
#### • Summary so far:

- Generalizes concept of phrase pair to allow nested phrases
- Formalized using SCFG
- No use of linguistic annotation: syntactic in a purely formal sense
- Model uses standard SMT log-linear formulation
- Search over derivations

#### • Later:

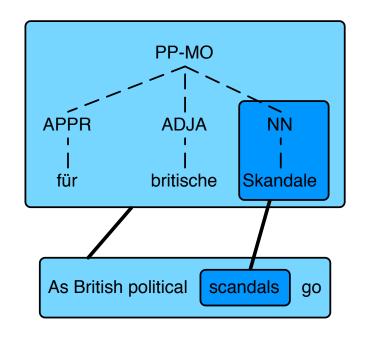
- Rule extraction and scoring
- Decoding (search for best derivation)
- k-best extraction

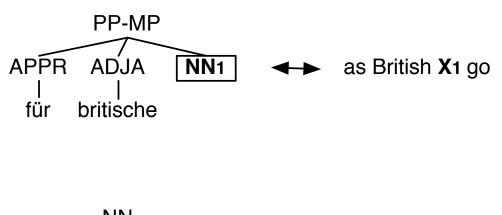
Hierarchical phrase pairs but with embedded tree fragments on the source side:



Each source subphrase is a complete subtree.

Formalized using Synchronous Tree-Substitution Grammar (STSG):





- Synchronous Tree Substitution Grammar (STSG):
  - Grammar rules have the form  $\langle \pi, \gamma, \sim \rangle$
  - $-\pi$  is a tree with source terminal and non-terminal leaves
  - $-\gamma$  is a string<sup>1</sup> of target terminals and non-terminals
  - $-\sim$  is a one-to-one correspondence between source and target non-terminals.

#### Unlike Hiero:

- Linguistic-annotation (on source-side)
- No limit to number of substitution sites (non-terminals)
- No reordering limit during decoding

 $<sup>^1 \</sup>text{Technically, a 1-level tree formed by adding X as the root and the symbols from } \gamma$  as children.

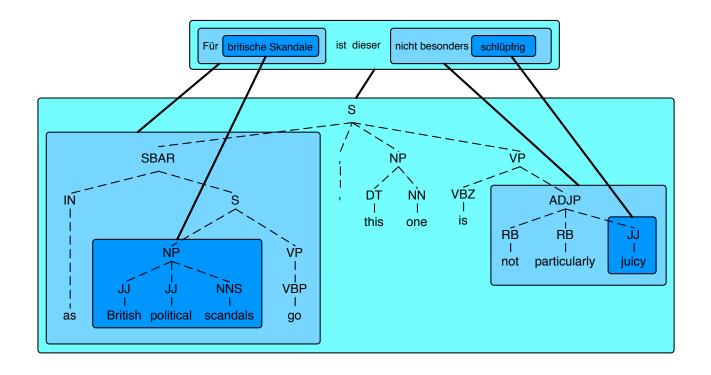
- Derivation involves synchronous rewrites (like SCFG)
- Tree fragments required to match input parse tree.
  - Motivation: tree provides context for rule selection ("syntax-directed")
- Efficient decoding algorithms available: source tree constrains rule options
- Search for single-best derivation:

$$d^* = \arg\max_{d} \left( \lambda_1 \log p_{LM}(d) + \sum_{r_i} \sum_{m=2}^{M} \lambda_m h_m(r_i) \right)$$

where source-side of d must match input tree

## **String-to-Tree**

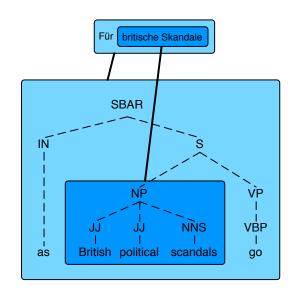
Hierarchical phrase pairs but with embedded tree fragments on the target side:

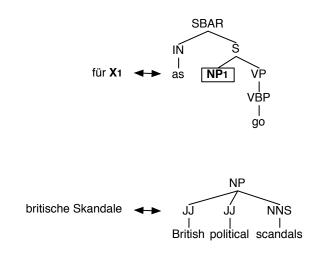


Each target subphrase is a complete subtree.

### **String-to-Tree**

#### Formalized using STSG:





#### Or SCFG:

SBAR 
$$\rightarrow f\ddot{u}r X_1 \mid as NP_1 go$$

NP  $\rightarrow britische Skandale \mid British political scandals$ 

## String-to-Tree

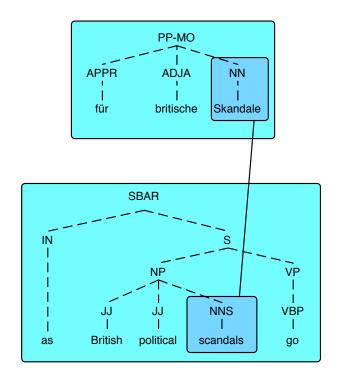
- Derivation is a rewriting process, like hierarchical phrase-based and tree-to-string
  - Rewrites only allowed if target labels match at substitution sites
  - Internal tree structure not used in derivation (hence frequent use of SCFG)
  - Motivation: constraints provided by target syntax lead to more fluent output

#### • Later:

- Rule extraction and scoring
- Decoding (Hiero will be special case of S2T)
- k-best extraction (likewise)

### Tree-to-Tree

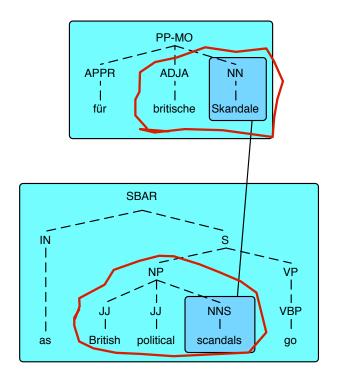
Hierarchical phrase pairs but with embedded tree fragments on both sides:



Formalized using STSG

#### Tree-to-Tree

Differences in source and target syntactic structure increasingly important



Can be differences in treebank annotation style or simply differences in language choice

# **Summary So Far**

• We have introduced four models:

Model	<b>Formalism</b>	Source Syntax	Target Syntax	Input
Hiero	SCFG	N	N	string
T2S	STSG	Y	N	tree
S2T	STSG or SCFG	N	Υ	string
T2T	STSG	Υ	Υ	tree

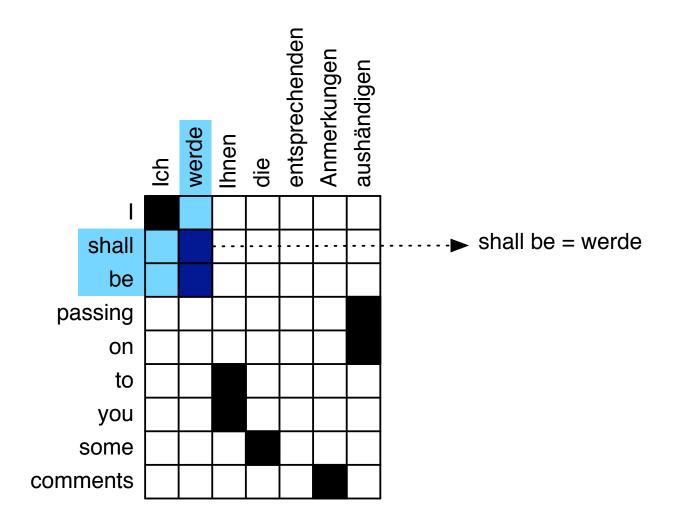
- Next:
  - Rule extraction

- Part I Introduction
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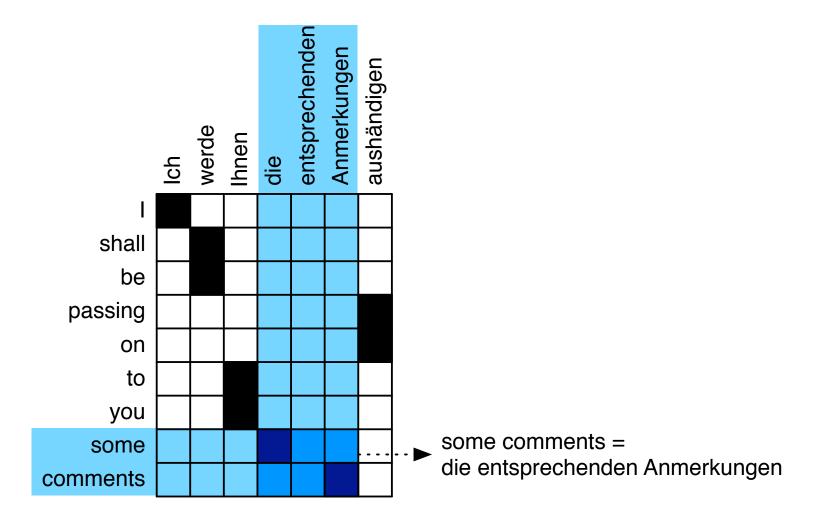
## **Learning Synchronous Grammars**

- Extracting rules from a word-aligned parallel corpus
- First: Hierarchical phrase-based model
  - only one non-terminal symbol x
  - no linguistic syntax, just a formally syntactic model
- Then: Synchronous phrase structure model
  - non-terminals for words and phrases: NP, VP, PP, ADJ, ...
  - corpus must also be parsed with syntactic parser

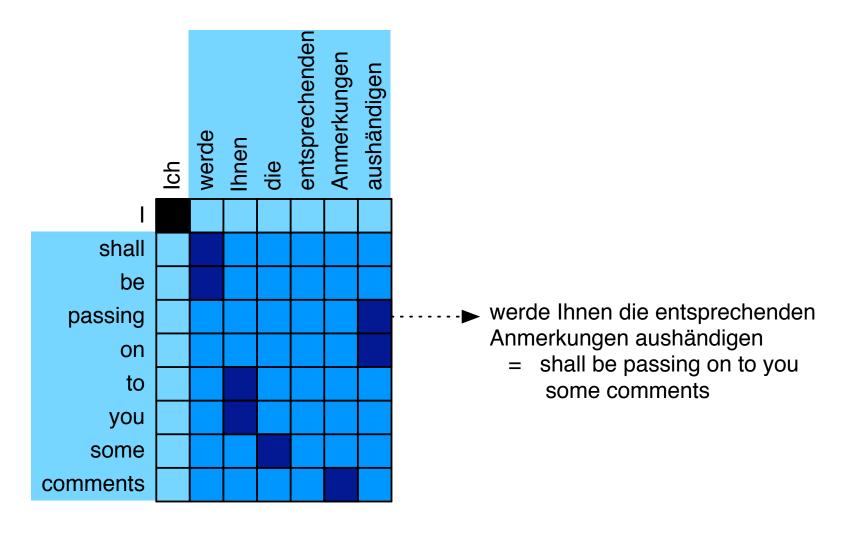
# **Extracting Phrase Translation Rules**



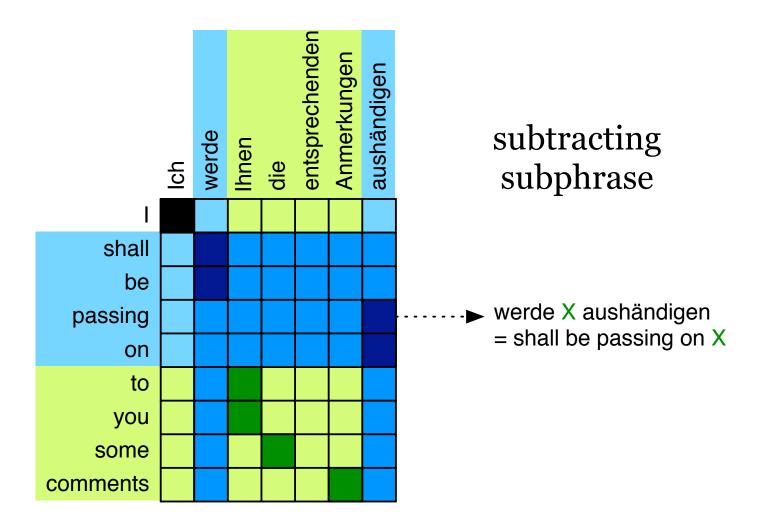
## **Extracting Phrase Translation Rules**



## **Extracting Phrase Translation Rules**



## **Extracting Hierarchical Phrase Translation Rules**



### **Formal Definition**

Recall: consistent phrase pairs

$$(ar{e},ar{f})$$
 consistent with  $A\Leftrightarrow$  
$$\forall e_i\in ar{e}:(e_i,f_j)\in A o f_j\in ar{f}$$
 and  $\forall f_j\in ar{f}:(e_i,f_j)\in A o e_i\in ar{e}$  and  $\exists e_i\in ar{e},f_j\in ar{f}:(e_i,f_j)\in A$ 

ullet Let P be the set of all extracted phrase pairs  $(\bar{e},\bar{f})$ 

#### **Formal Definition**

• Extend recursively:

$$\begin{split} \text{if } (\bar{e},\bar{f}) \in P \text{ and } (\bar{e}_{\text{SUB}},\bar{f}_{\text{SUB}}) \in P \\ \text{and } \bar{e} &= \bar{e}_{\text{PRE}} + \bar{e}_{\text{SUB}} + \bar{e}_{\text{POST}} \\ \text{and } \bar{f} &= \bar{f}_{\text{PRE}} + \bar{f}_{\text{SUB}} + \bar{f}_{\text{POST}} \\ \text{and } \bar{e} &\neq \bar{e}_{\text{SUB}} \text{ and } \bar{f} \neq \bar{f}_{\text{SUB}} \end{split}$$
 
$$\text{add } (e_{\text{PRE}} + \mathbf{X} + e_{\text{POST}}, f_{\text{PRE}} + \mathbf{X} + f_{\text{POST}}) \text{ to } P \end{split}$$

(note: any of  $e_{\mathrm{PRE}}$ ,  $e_{\mathrm{POST}}$ ,  $f_{\mathrm{PRE}}$ , or  $f_{\mathrm{POST}}$  may be empty)

• Set of hierarchical phrase pairs is the closure under this extension mechanism

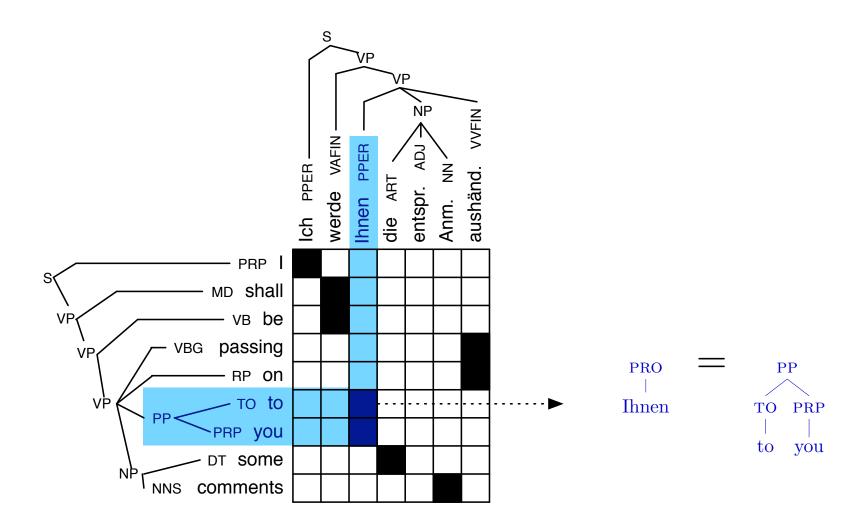
#### **Comments**

 Removal of multiple sub-phrases leads to rules with multiple non-terminals, such as:

$$Y \rightarrow X_1 X_2 \mid X_2 \text{ of } X_1$$

- Typical restrictions to limit complexity [Chiang, 2005]
  - at most 2 nonterminal symbols
  - at least 1 but at most 5 words per language
  - span at most 15 words (counting gaps)

# **Learning Syntactic Translation Rules**

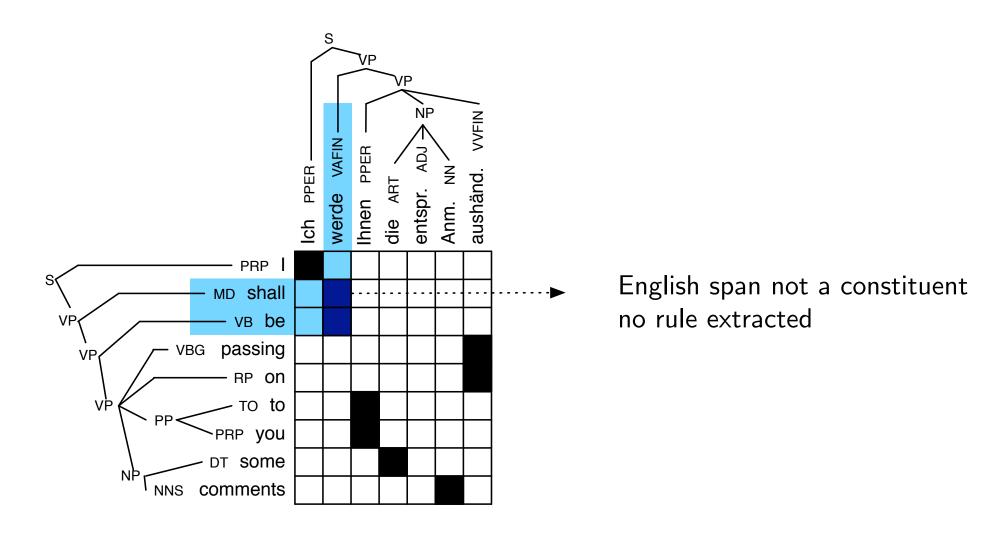


# **Constraints on Syntactic Rules**

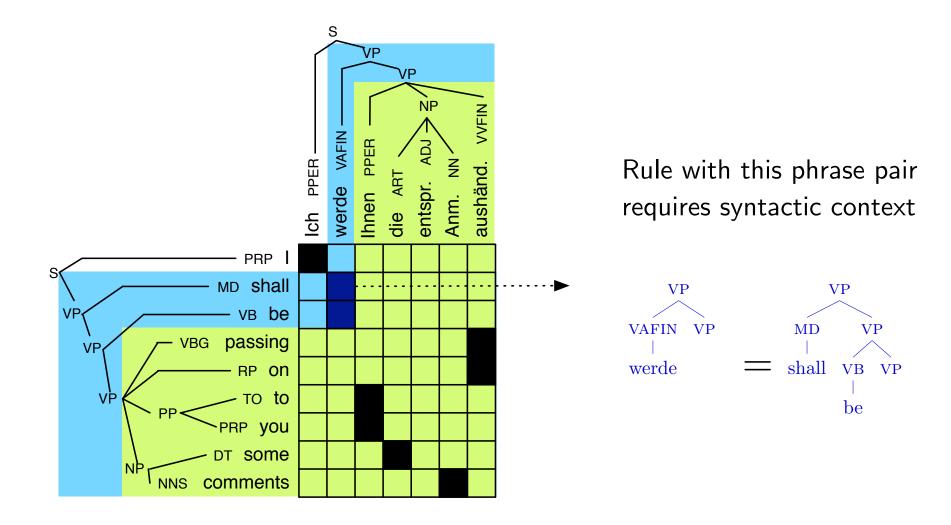
- Same word alignment constraints as hierarchical models
- Hierarchical: rule can cover any span
   syntactic rules must cover constituents in the tree
- ◆ Hierarchical: gaps may cover any span
   ⇒ gaps must cover constituents in the tree

Much fewer rules are extracted (all things being equal)

## Impossible Rules



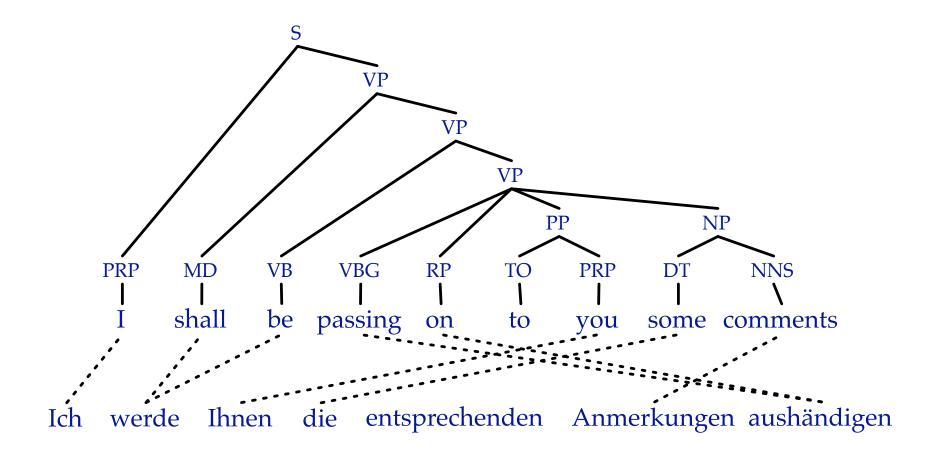
### **Rules with Context**



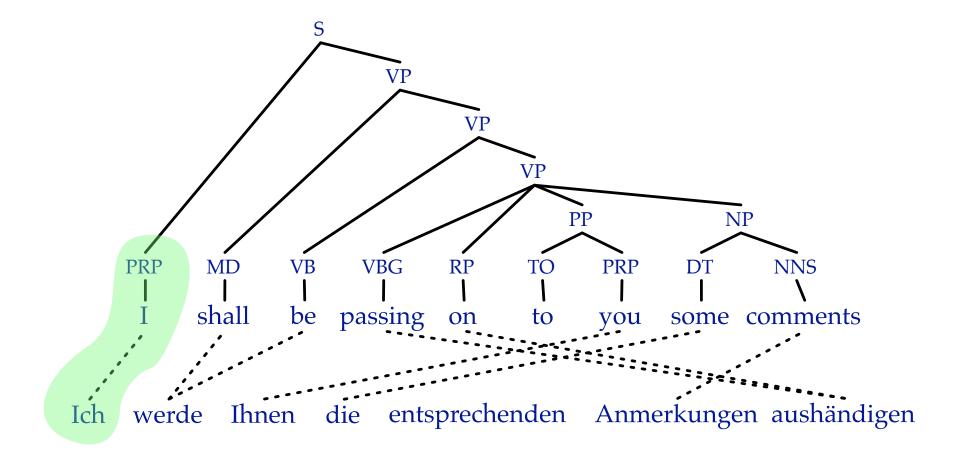
# **Too Many Rules Extractable**

- Huge number of rules can be extracted
   (every alignable node may or may not be part of a rule → exponential number of rules)
- Need to limit which rules to extract
- Option 1: similar restriction as for hierarchical model (maximum span size, maximum number of terminals and non-terminals, etc.)
- Option 2: only extract minimal rules ("GHKM" rules)

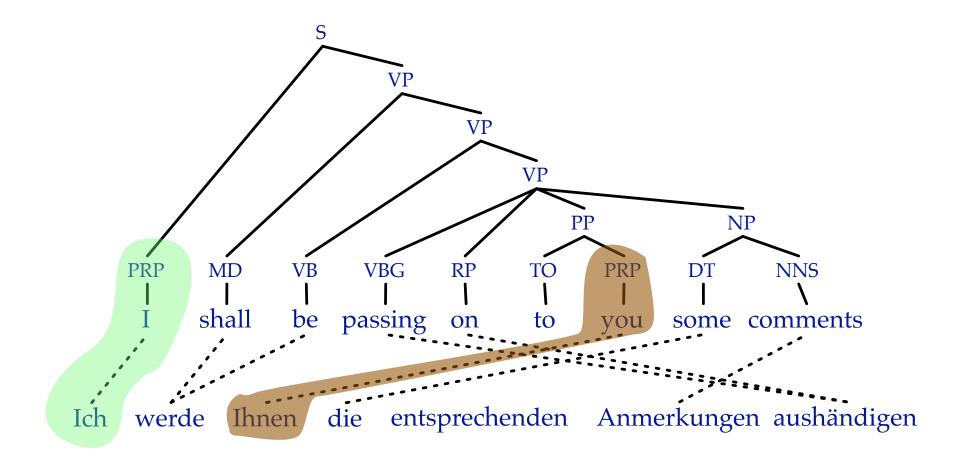
### **Minimal Rules**



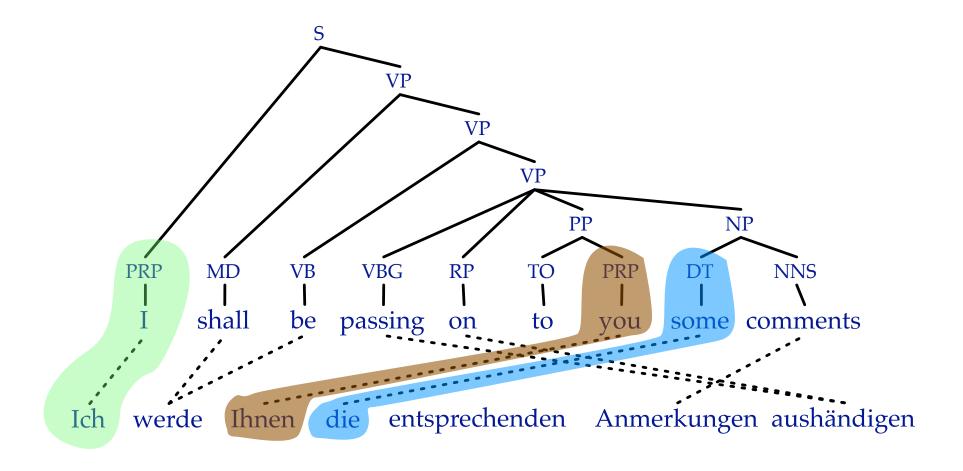
Extract: set of smallest rules required to explain the sentence pair



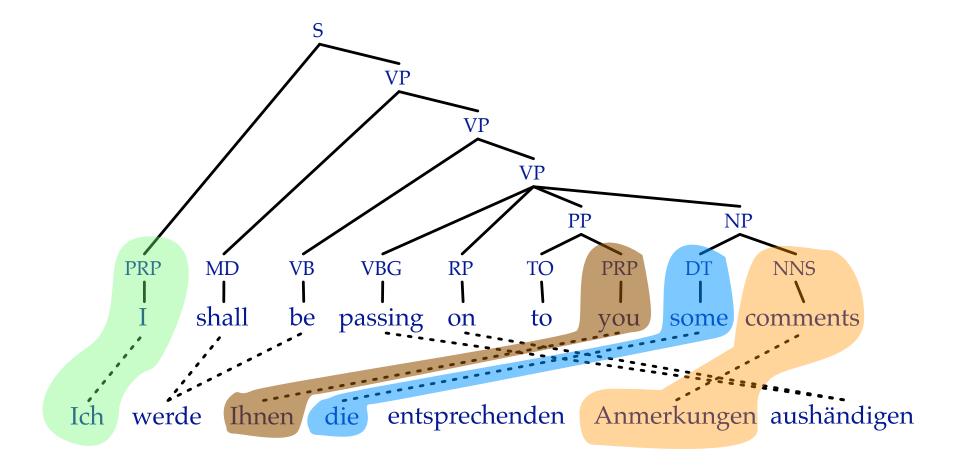
Extracted rule:  $PRP \rightarrow Ich \mid I$ 



Extracted rule:  $PRP \rightarrow Ihnen \mid you$ 

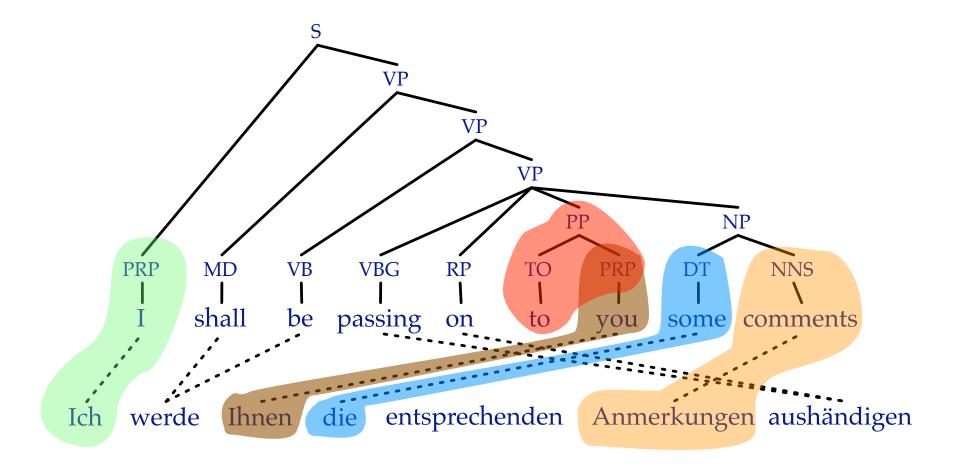


Extracted rule: DT  $\rightarrow$  die | some



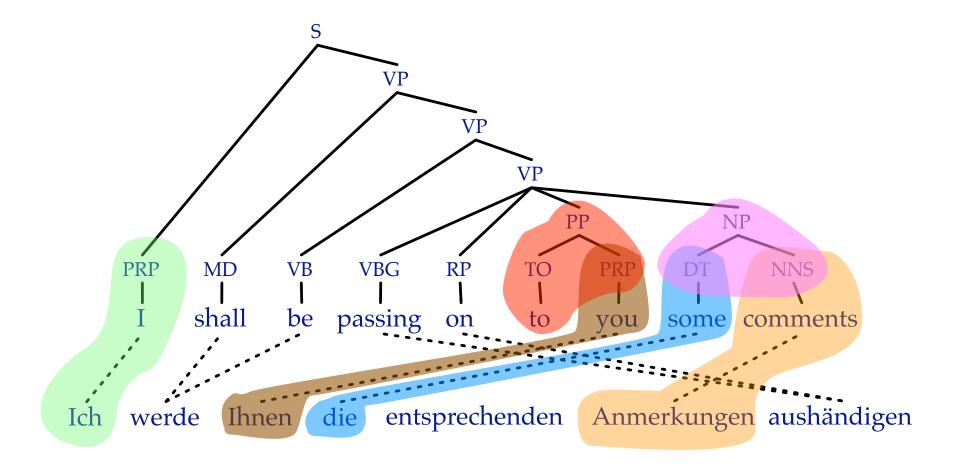
Extracted rule: NNS → Anmerkungen | comments

### **Insertion Rule**



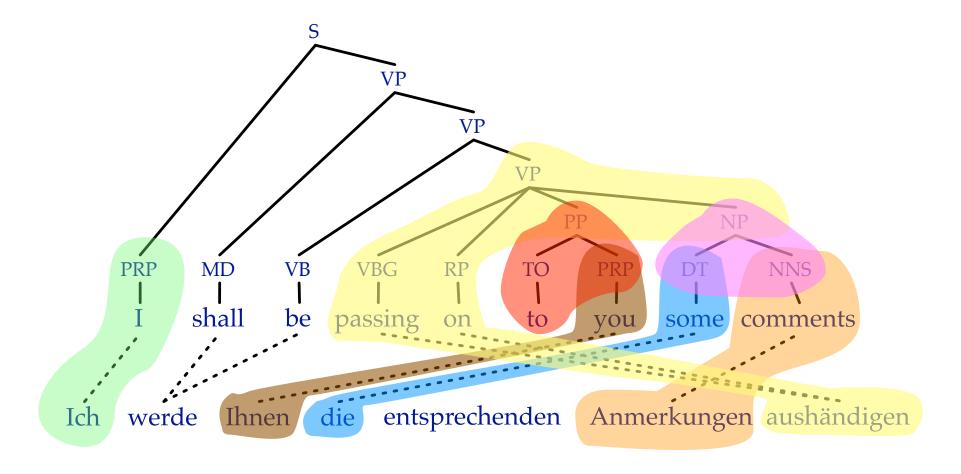
Extracted rule:  $PP \rightarrow X \mid to PRP$ 

## **Non-Lexical Rule**



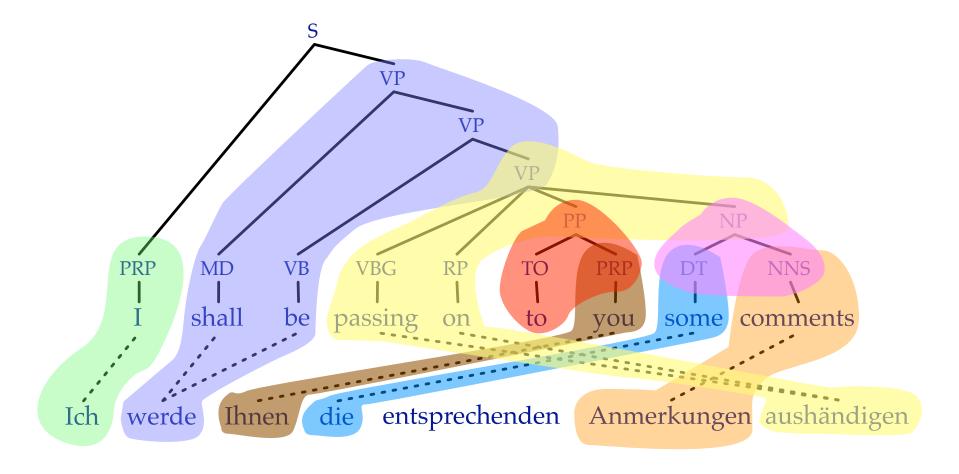
Extracted rule: NP  $\rightarrow$  X<sub>1</sub> X<sub>2</sub> | DT<sub>1</sub> NNS<sub>2</sub>

## **Lexical Rule with Syntactic Context**



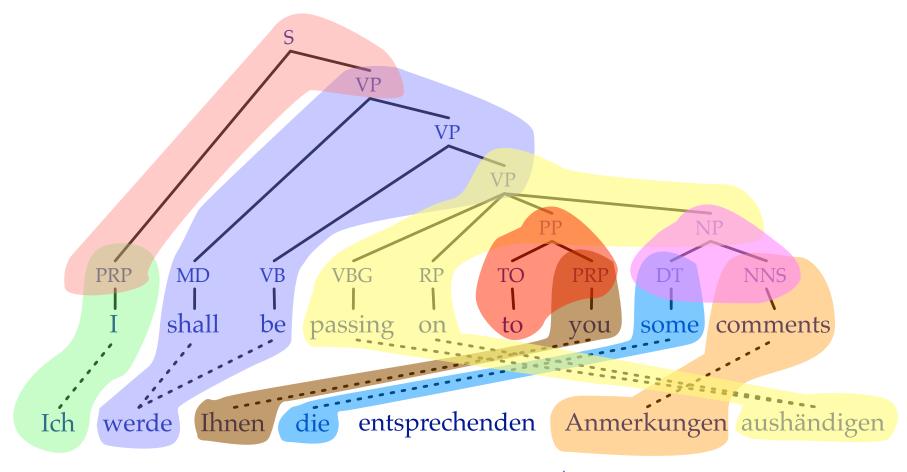
Extracted rule:  $VP \rightarrow X_1 X_2$  aushändigen | passing on  $PP_1 NP_2$ 

## **Lexical Rule with Syntactic Context**



Extracted rule:  $VP \rightarrow werde \ X \mid shall \ be \ VP$  (ignoring internal structure)

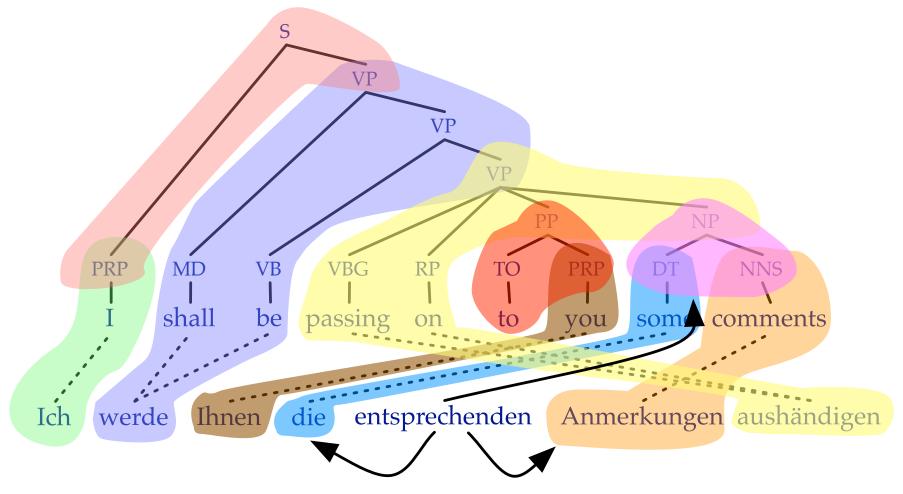
### **Non-Lexical Rule**



Extracted rule:  $S \rightarrow X_1 X_2 \mid PRP_1 VP_2$ 

DONE — note: one rule per alignable constituent

## **Unaligned Source Words**



Attach to neighboring words or higher nodes  $\rightarrow$  additional rules

#### **Too Few Phrasal Rules?**

- Lexical rules will be 1-to-1 mappings (unless word alignment requires otherwise)
- But: phrasal rules very beneficial in phrase-based models
- Solutions
  - combine rules that contain a maximum number of symbols (as in hierarchical models, recall: "Option 1")
  - compose minimal rules to cover a maximum number of non-leaf nodes

## **Composed Rules**

• Current rules

$$X_1 X_2 = NP$$

$$\widehat{DT_1 NNS_1}$$

$$die = DT$$
 $some$ 

• Composed rule

(1 non-leaf node: NP)

## **Composed Rules**

• Minimal rule:  $X_1 \ X_2 \ aushändigen = VP$ 3 non-leaf nodes:  $VP, \ PP, \ NP$ PRP PRP PP1 NP2

passing on

• Composed rule: Ihnen  $x_1$  aushändigen = VP 3 non-leaf nodes:  $v_{PRP}$  PRP  $v_{PRP}$  PP  $v_{PRP}$   $v_{PRP}$  v

# **Relaxing Tree Constraints**

• Impossible rule

$$X = MD VB$$
 werde shall be

- Create new non-terminal label: MD+VB
- $\Rightarrow$  New rule

$$\begin{array}{rcl}
x & = & MD + VB \\
\text{werde} & & \widehat{MD} & VB \\
& & \text{shall be}
\end{array}$$

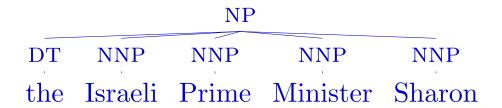
# **Zollmann Venugopal Relaxation**

- If span consists of two constituents, join them: X+Y
- If span conststs of three constituents, join them: X+Y+Z
- If span covers constituents with the same parent x and include
  - every but the first child Y, label as  $X \setminus Y$
  - every but the last child Y, label as X/Y
- For all other cases, label as FAIL

⇒ More rules can be extracted, but number of non-terminals blows up

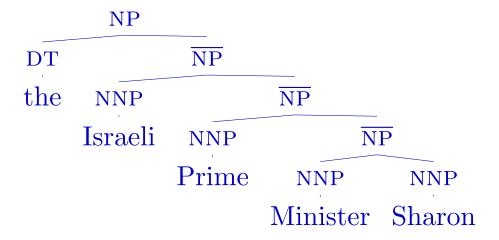
## **Special Problem: Flat Structures**

• Flat structures severely limit rule extraction



• Can only extract rules for individual words or entire phrase

# Relaxation by Tree Binarization



More rules can be extracted Left-binarization or right-binarization?

## **Scoring Translation Rules**

- Extract all rules from corpus
- Score based on counts
  - joint rule probability:  $p(LHS, RHS_f, RHS_e)$
  - rule application probability:  $p(RHS_f, RHS_e|LHS)$
  - direct translation probability:  $p(RHS_e|RHS_f, LHS)$
  - noisy channel translation probability:  $p(RHS_f|RHS_e, LHS)$
  - lexical translation probability:  $\prod_{e_i \in RHS_e} p(e_i | RHS_f, a)$
- Edinburgh's WMT System:
  - $p(RHS_e, LHS|RHS_f)$  and  $p(RHS_f|RHS_e, LHS)$
  - lexical translation probability:  $\prod_{e_i \in RHS_e} p(e_i | RHS_f, a)$
  - PCFG probability of tree fragment:  $p_{pefq}\left(\pi\right)$
  - rule rareness and rule count penalties:  $\exp(-1/count(r))$  and  $\exp(1)$

- Part I Introduction
- Part II Rule Extraction
- Part III Decoding
- Part IV Extensions

#### **Outline**

- 1. Hiero/S2T decoding (SCFG with string input)
  - Viterbi decoding with local features (-LM)
  - k-best extraction
  - LM integration (cube pruning)
  - The S2T algorithm, as implemented in Moses
- 2. T2S decoding (STSG with tree input)
  - Vanilla T2S: non-directional, cube pruning
- 3. T2T decoding (STSG with tree input)
  - Included for completeness better alternatives explored later

# Viterbi S2T Decoding (-LM)

Find the highest-scoring synchronous derivation  $d^*$ **Objective** 

- $C_i$ ,  $\alpha_i$  and  $\beta_i$  are LHS, source RHS, target RHS of rule  $r_i$ , respectively.
- $w_i$  is weight of rule  $r_i$  (weighted product of rule-local feature functions).
- $\bullet$  |G| is the number of rules in the grammar G.

 $w_{|G|}$ 

# Viterbi S2T Decoding (-LM)

**Objective** Find the highest-scoring synchronous derivation  $d^*$ 

#### **Solution**

#### 1. Project grammar

Project weighted SCFG to weighted CFG  $f: G \rightarrow G'$  (many-to-one rule mapping)

#### 2. Parse

Find Viterbi parse of sentence wrt G'

#### 3. Translate

Produce synchronous tree pair by applying inverse projection f'

## **Example**

#### **Input** jemand mußte Josef K. verleumdet haben

someone must Josef K. slandered have

#### Grammar

```
\rightarrow Josef K. | Josef K.
                                                                                                        0.90
r_1:
              \rightarrow verleumdet | slandered
                                                                                                        0.40
      VBN
              \rightarrow verleumdet | defamed
                                                                                                        0.20
      VBN
              \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                        0.10
r_{4}:
       VP
              \rightarrow jemand X_1 | someone VP_1
                                                                                                        0.60
r_5:
              \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1
                                                                                                        0.80
r_6:
              \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                        0.05
r_7:
```

(Six derivations in total)

#### jemand mußte Josef K. verleumdet haben Input

Source

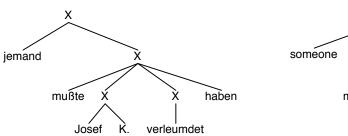
someone must Josef K. slandered have

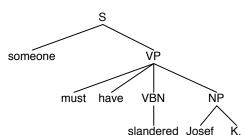
## Grammar

```
NP \rightarrow Josef K. | Josef K.
\Rightarrow r_1:
                 \rightarrow verleumdet | slandered
                                                                                                                   0.40
\Rightarrow r_2:
          VBN
                   \rightarrow verleumdet | defamed
                                                                                                                   0.20
          VBN
\Rightarrow r_4:
                 \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                   0.10
         VP
\Rightarrow r_5: S \rightarrow jemand X_1 \mid someone VP_1
                                                                                                                   0.60
        S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid someone \ must \ have \ VBN_2 \ NP_1
                                                                                                                   0.80
   r_6:
                   \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                                   0.05
   r_7:
```

Target

## Derivation 1





0.90

## **Input** jemand mußte Josef K. verleumdet haben

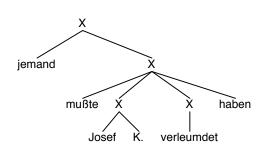
someone must Josef K. slandered have

## **Grammar**

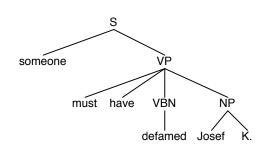
```
NP \rightarrow Josef K. | Josef K.
                                                                                                                   0.90
\Rightarrow r_1:
                 \rightarrow verleumdet | slandered
                                                                                                                   0.40
          VBN
                   \rightarrow verleumdet | defamed
                                                                                                                   0.20
\Rightarrow r_3:
          VBN
         VP \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                   0.10
\Rightarrow r_4:
\Rightarrow r_5: S \rightarrow jemand X_1 \mid someone VP_1
                                                                                                                   0.60
        S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid someone \ must \ have \ VBN_2 \ NP_1
                                                                                                                   0.80
   r_6:
                   \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                                   0.05
   r_7:
```

Target

## Derivation 2



Source



## **Input** jemand mußte Josef K. verleumdet haben

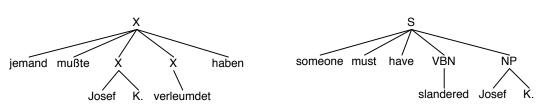
someone must Josef K. slandered have

## Grammar

```
NP \rightarrow Josef K. | Josef K.
                                                                                                                   0.90
\Rightarrow r_1:
                 \rightarrow verleumdet | slandered
                                                                                                                   0.40
\Rightarrow r_2:
          VBN
                   \rightarrow verleumdet | defamed
                                                                                                                   0.20
          VBN
                   \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                   0.10
         S \rightarrow jemand X_1 \mid someone VP_1
   r_5:
                                                                                                                   0.60
\Rightarrow r_6: S \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN<sub>2</sub> NP<sub>1</sub>
                                                                                                                   0.80
              S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \ | \ NP_1 \ must \ have \ been \ VBN_1 \ by \ someone
                                                                                                                   0.05
```

Source Target

**Derivation 3** 



## **Input** jemand mußte Josef K. verleumdet haben

someone must Josef K. slandered have

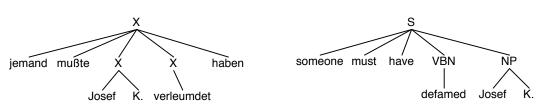
 $NP \rightarrow Iosef K \mid Iosef K$ 

## **Grammar**

<b>→</b> / 1.	111	/		0.50
$r_2$ :	VBN	$\rightarrow$	$verleumdet \mid slandered$	0.40
$\Rightarrow r_3$ :	VBN	$\rightarrow$	$verleumdet \mid defamed$	0.20
$r_4$ :	VP	$\rightarrow$	$mu\beta te \ X_1 \ X_2 \ haben \mid must \ have \ VBN_2 \ NP_1$	0.10
$r_5$ :	$\mathbf{S}$	$\rightarrow$	$jemand X_1 \mid someone VP_1$	0.60
$\Rightarrow r_6$ :	$\mathbf{S}$	$\rightarrow$	$jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid someone \ must \ have \ VBN_2 \ NP_1$	0.80
$r_7$ :	$\mathbf{S}$	$\rightarrow$	jemand mußte X <sub>1</sub> X <sub>2</sub> haben   NP <sub>1</sub> must have been VBN <sub>1</sub> by someone	0.05

Source Target

Derivation 4



0.90

## **Input** jemand mußte Josef K. verleumdet haben

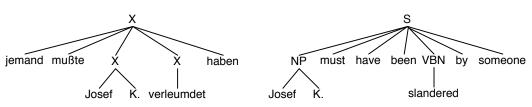
someone must Josef K. slandered have

### Grammar

```
NP \rightarrow Josef K. | Josef K.
                                                                                                                      0.90
\Rightarrow r_1:
                  \rightarrow verleumdet | slandered
                                                                                                                      0.40
\Rightarrow r_2:
          VBN
                   \rightarrow verleumdet | defamed
                                                                                                                      0.20
          VBN
                   \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                      0.10
   r_{4}:
          VP
                   \rightarrow jemand X_1 | someone VP_1
                                                                                                                      0.60
   r_5:
              S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid someone \ must \ have \ VBN_2 \ NP_1
                                                                                                                      0.80
   r_6:
              S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \ | \ NP_1 \ must \ have \ been \ VBN_1 \ by \ someone
                                                                                                                      0.05
\Rightarrow r_7:
```

Source Target

### Derivation 5



#### jemand mußte Josef K. verleumdet haben Input

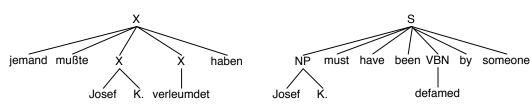
someone must Josef K. slandered have

## Grammar

$\Rightarrow r_1$ :	NP	$\rightarrow$	$Josef\ K.\  \ Josef\ K.$	0.90
$r_2$ :	VBN	$\rightarrow$	$verleumdet \mid slandered$	0.40
$\Rightarrow r_3$ :	VBN	$\rightarrow$	$verleumdet \mid defamed$	0.20
$r_4$ :	VP	$\rightarrow$	$mu\beta te \ \mathrm{X}_1 \ \mathrm{X}_2 \ haben \mid must \ have \ \mathrm{VBN}_2 \ \mathrm{NP}_1$	0.10
$r_5$ :	$\mathbf{S}$	$\rightarrow$	$jemand X_1 \mid someone VP_1$	0.60
$r_6$ :	$\mathbf{S}$	$\rightarrow$	$jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid someone \ must \ have \ VBN_2 \ NP_1$	0.80
$\Rightarrow r_7$ :	$\mathbf{S}$	$\rightarrow$	jemand mußte $X_1$ $X_2$ haben   NP <sub>1</sub> must have been VBN <sub>1</sub> by someone	0.05

Source Target

## Derivation 6



G	$egin{array}{c} r_1: & r_2: & & & & & & & & & & & & & & & & & & &$	NP VBN VP S S	$\begin{array}{c} \rightarrow \\ \rightarrow \end{array}$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0.90 0.40 0.20 0.10 0.60 0.80 0.05
G'	$q_1$ : $q_2$ : $q_3$ : $q_4$ : $q_5$ :	NP VBN VP S	$\begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \end{array}$	Josef K.  verleumdet  mußte NP VBN haben  jemand VP  jemand mußte NP VBN haben	0.90 0.40 0.10 0.60 0.80

 $\bullet$  G is original synchronous grammar, G' is monolingual projection

```
NP \rightarrow Josef K. \mid Josef K.
                                                                                                                               0.90
          \Rightarrow r_1:
                     VBN \rightarrow verleumdet \mid slandered
                                                                                                                               0.40
                     VBN \rightarrow verleumdet \mid defamed
                                                                                                                               0.20
              r_3:
G
                             \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                               0.10
              r_{4}:
                             \rightarrow jemand X_1 | someone VP_1
                                                                                                                              0.60
              r_5:
                             \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1
                                                                                                                              0.80
                             \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                                              0.05
              r_7:
                                                                                                                               0.90
                      NP \rightarrow Josef K.
          \Rightarrow q_1:
                             \rightarrow verleumdet
                                                                                                                               0.40
                     VBN
G'
                             \rightarrow mu\beta te \text{ NP VBN } haben
                                                                                                                               0.10
              q_3:
                             \rightarrow jemand VP
                                                                                                                               0.60
              q_4:
                             \rightarrow jemand mußte NP VBN haben
                                                                                                                              0.80
              q_5:
```

Projected rule gets LHS and source RHS (but with target non-terminal labels)

```
NP \rightarrow Josef K. \mid Josef K.
                                                                                                                              0.90
              r_1:
                    VBN \rightarrow verleumdet \mid slandered
                                                                                                                              0.40
                    VBN \rightarrow verleumdet \mid defamed
                                                                                                                              0.20
          \Rightarrow r_3:
G
                             \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                              0.10
              r_{4}:
                             \rightarrow jemand X_1 | someone VP_1
                                                                                                                              0.60
              r_5:
                             \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1
                                                                                                                              0.80
                             \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                                              0.05
              r_7:
                                                                                                                              0.90
                      NP
                             \rightarrow Josef K.
              q_1:
          \Rightarrow q_2:
                    VBN
                             \rightarrow verleumdet
                                                                                                                              0.40
G'
                             \rightarrow mu\beta te \text{ NP VBN } haben
                                                                                                                              0.10
                             \rightarrow jemand VP
                                                                                                                              0.60
              q_4:
                             \rightarrow jemand mußte NP VBN haben
                                                                                                                              0.80
              q_5:
```

• Many-to-one: weight of projected rule is the best from set of projecting rules

```
NP \rightarrow Josef K. \mid Josef K.
                                                                                                                               0.90
              r_1:
                     VBN \rightarrow verleumdet \mid slandered
                                                                                                                               0.40
                     VBN \rightarrow verleumdet \mid defamed
                                                                                                                               0.20
              r_3:
G
                             \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                               0.10
          \Rightarrow r_{A}:
                             \rightarrow jemand X_1 | someone VP_1
                                                                                                                              0.60
                             \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1
                                                                                                                              0.80
                             \rightarrow jemand mußte X_1 X_2 haben | NP<sub>1</sub> must have been VBN<sub>1</sub> by someone
                                                                                                                              0.05
              r_7:
                                                                                                                               0.90
                           \rightarrow Josef K.
                       NP
              q_1:
                             \rightarrow verleumdet
                                                                                                                               0.40
                     VBN
G'
                             \rightarrow mu\beta te \text{ NP VBN } haben
          \Rightarrow q_3:
                                                                                                                               0.10
                       VP
                             \rightarrow jemand VP
                                                                                                                               0.60
              q_4:
                         S \rightarrow jemand mu\beta te NP VBN haben
                                                                                                                              0.80
              q_5:
```

• Target non-terminal labels projected to monolingual rule (in source order)

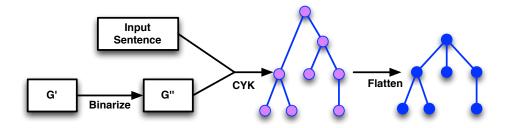
```
NP \rightarrow Josef K. \mid Josef K.
                                                                                                                              0.90
              r_1:
                     VBN \rightarrow verleumdet \mid slandered
                                                                                                                              0.40
                     VBN \rightarrow verleumdet \mid defamed
                                                                                                                             0.20
G
                             \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                             0.10
              r_{4}:
                    S \rightarrow jemand X_1 \mid someone VP_1
                                                                                                                             0.60
          \Rightarrow r_5:
                             \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1
                                                                                                                             0.80
                        S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid NP_1 \ must \ have \ been \ VBN_1 \ by \ someone
                                                                                                                             0.05
              r_7:
                                                                                                                              0.90
                           \rightarrow Josef K.
                      NP
              q_1:
                             \rightarrow verleumdet
                    VBN
                                                                                                                             0.40
G'
                             \rightarrow mu\beta te \text{ NP VBN } haben
                                                                                                                             0.10
              q_3:
                    s \rightarrow jemand VP
                                                                                                                              0.60
          \Rightarrow q_4:
                        S \rightarrow jemand mu\beta te NP VBN haben
                                                                                                                             0.80
```

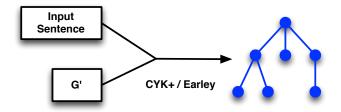
• And so on. . .

```
NP \rightarrow Josef K. \mid Josef K.
                                                                                                                               0.90
              r_1:
                                                                                                                               0.40
                     VBN \rightarrow verleumdet \mid slandered
                     VBN \rightarrow verleumdet \mid defamed
                                                                                                                               0.20
              r_3:
G
                              \rightarrow mu\beta te X_1 X_2 haben \mid must have VBN_2 NP_1
                                                                                                                               0.10
              r_{4}:
                             \rightarrow jemand X_1 | someone VP_1
                                                                                                                               0.60
           \Rightarrow r_6: S \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN<sub>2</sub> NP<sub>1</sub>
                                                                                                                               0.80
          \Rightarrow r_7:
                        S \rightarrow jemand \ mu\beta te \ X_1 \ X_2 \ haben \mid NP_1 \ must \ have \ been \ VBN_1 \ by \ someone
                                                                                                                               0.05
                                                                                                                               0.90
                            \rightarrow Josef K.
                       NP
              q_1:
                              \rightarrow verleumdet
                     VBN
                                                                                                                               0.40
G'
                             \rightarrow mu\beta te \text{ NP VBN } haben
                                                                                                                               0.10
              q_3:
                     s \rightarrow jemand VP
                                                                                                                               0.60
              q_4:
                         s \rightarrow jemand mu\beta te NP VBN haben
                                                                                                                               0.80
```

• And so on.

# **Step 2: Find Viterbi Parse**

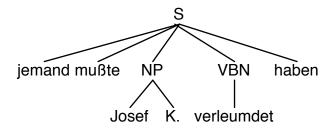




- Standard weighted parsing algorithms.
- Binarization can be explicit (like CYK) or implicit (like Earley / CYK+)

1-best parse tree

Source-side parse tree



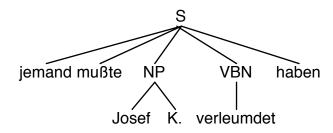
## 1-best parse tree Source-side parse tree



• Source-side: replace non-terminals with Xs

#### 1-best parse tree

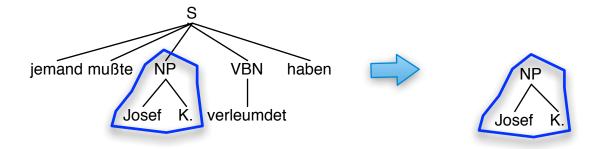
Source-side parse tree



• Target-side: invert grammar projection

#### 1-best parse tree

#### Source-side parse tree



• Target-side: invert grammar projection

$$NP \rightarrow Josef K. \mid Josef K.$$

# 1-best parse tree Source-side parse tree Source-side parse tree Josef K. verleumdet Source-side parse tree

• Target-side: invert grammar projection (multiple rules? pick highest-scoring)

```
VBN \rightarrow verleumdet | slandered 0.4

VBN \rightarrow verleumdet | defamed 0.2
```

# 1-best parse tree Source-side parse tree

Target-side: invert grammar projection (multiple rules? pick highest-scoring)

```
S \rightarrow jemand mußte X_1 X_2 haben | someone must have VBN_2 NP_1 0.80
S \rightarrow jemand mußte X_1 X_2 haben | NP_1 must have been VBN_2 by someone 0.05
```

## k-best Extraction

**Objective** Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

Well. . .

- 1. 1-best derivation is 1-best monolingual parse tree with best set of translations
- 2. 2-best is one of
  - (a) 1-best monolingual parse tree with second best set of translations, and
  - (b) 2-best monolingual parse tree with best translations
- 3. 3-best derivation is 'the other one' or one of
  - (a) 1-best monolingual parse tree with third best set of translations, and
  - (b) 2-best monolingual parse tree with second best translations, and
  - (c) 3-best monolingual parse tree with best translations
- 4. 4-best derivation is 'one of what's left' or . . .

## k-best Extraction

**Objective** Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

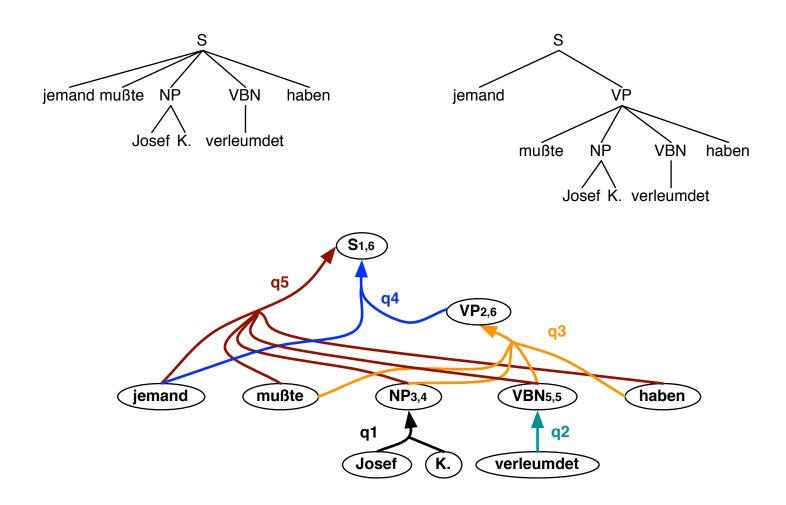
Well. . .

- 1. 1-best derivation is 1-best monolingual parse tree with best set of translations
- 2. 2-best is one of
  - (a) 1-best monolingual parse tree with second best set of translations, and
  - (b) 2-best monolingual parse tree with best translations

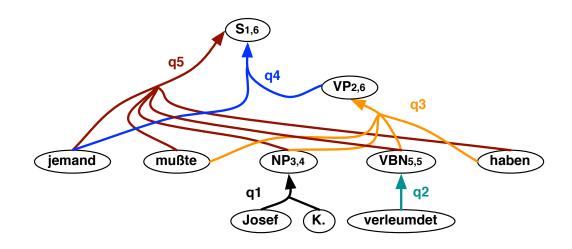
3. . . .

We know part of the solution: how to get the k-best monolingual derivations (Huang and Chiang, 2005)

# Digression: Parsing and Hypergraphs



## Digression: Parsing and Hypergraphs



- Generalization of a graph: hyperedges connect two sets of vertices
- Terminology: vertices and hyperedges (nodes and arcs)
- A parse forest can be represented by a rooted, connected, labelled, directed, acyclic hypergraph (Klein and Manning, 2001)
- Vertices represent parsing states; hyperedges represent rule applications

## Monolingual *k*-best Extraction

Huang and Chiang (2005) provide efficient algorithms for k-best extraction.

## **Objective**

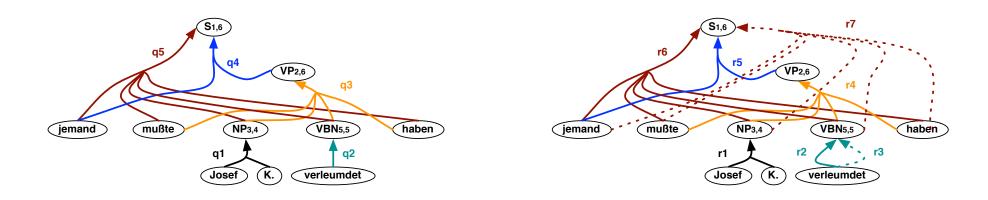
Extract the k-best monolingual derivations  $d_1, d_2, \dots d_k$  from a weighted parse forest

# Outline (alg. 3)

- 1. The 1-best subderivation for every vertex (and its incoming hyperedges) is known from the outset
- 2. Given the i-best derivation, the next best candidate along the same hyperedge is identical except for a substitution at a single incoming vertex
- 3. At the top vertex, generates candidates by recursively asking predecessors for next best subderivations.
- 4. Maintain priority queue of candidates at each vertex

# Synchronous k-best Extraction

Replace hyperedges according to f' (invert grammar projection)



- ullet The standard k-best extraction algorithm now gives the k-best synchronous derivations.
- The second hypergraph is sometimes called a "translation hypergraph".
- We'll call the first the "parse forest hypergraph" or the "parse hypergraph."

# S2T Decoding (LM-) Summary

## **Objective**

Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

#### Solution

1. Project grammar

Project weighted SCFG to unweighted CFG  $f: G \rightarrow G'$  (many-to-one)

2. Parse

Build parse hypergraph wrt G'

3. Invert projection

Expand hypergraph by replacing hyperedges according to f'

4. Extract derivations

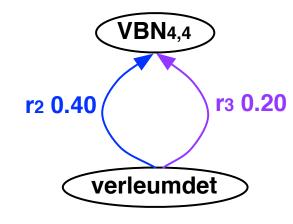
Extract k-best derivations using Huang and Chiang's (2005) algorithm

# **LM** Integration

#### Without LM

k-best derivation is k-best path through translation hypergraph

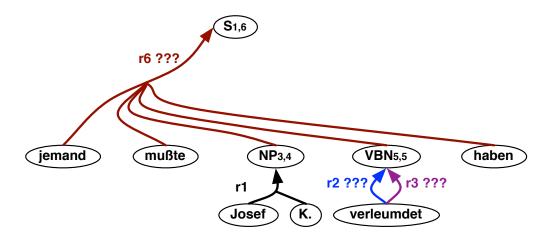
# **Optimal** substructure



If global best path includes  ${
m VBN_{4,4}}$  then best path must include hyperedge labelled  $r_2$ 

## **LM** Integration

Consider the two paths that include the hyperedge labelled  $r_6$ :

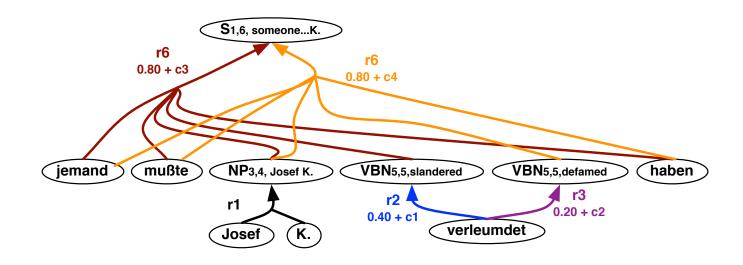


What's the best path through this hypergraph? For bi-gram LM we need to compute:

```
have slandered Josef p(\text{have} \mid \langle \mathbf{s} \rangle) \times p(\text{slandered} \mid \text{have}) \times p(\text{Josef} \mid \text{slandered}) \times \dots have defamed Josef p(\text{have} \mid \langle \mathbf{s} \rangle) \times p(\text{defamed} \mid \text{have}) \times p(\text{Josef} \mid \text{defamed}) \times \dots
```

# **State Splitting?**

Restore optimal substructure property by splitting states:



- Vertex labels include first and last words of translation.
- Hyperedges labelled with weights that incorporate LM costs.
- *k*-best derivation is *k*-best path.

# **State Splitting?**

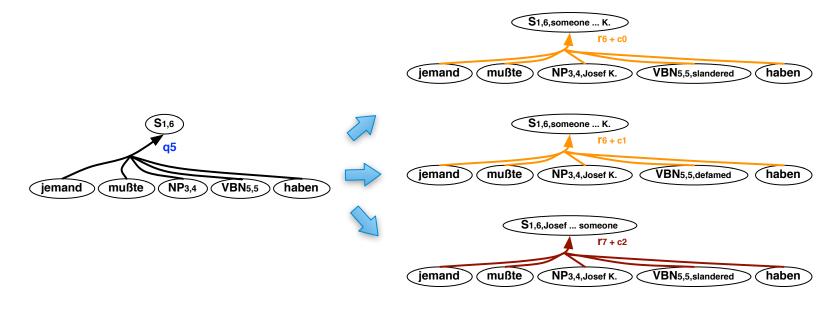
## **Objective**

Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

# Potential Solution

- 1. Project grammar Project weighted SCFG to weighted CFG  $f: G \rightarrow G'$
- 2. Parse Build parse hypergraph wrt G'
- Invert projection + split states
   Expand hypergraph by replacing hyperedges according to f'. During replacement, split states and add LM costs
- 4. Extract derivations Extract k-best derivations (Huang and Chiang, 2005)

## **State Splitting?**



- ullet Pick a search vertex for  $\left( \begin{array}{c} NP_{3,4} \end{array} \right)$  from the set  $\left\{ \begin{array}{c} \left( \begin{array}{c} NP_{3,4,Josef\ K.} \end{array} \right) \end{array} \right\}$
- ullet Pick a search vertex for  $\left( v_{BN_{5,5}} \right)$  from the set  $\left\{ \left( v_{P_{5,5,slandered}} \right), \left( v_{P_{5,5,defamed}} \right) \right\}$
- ullet Pick a synchronous rule from the set  $f'(q_5)=\{r_6,r_7\}$  (i.e. pick a target-side)

The full set is generated by taking the Cartesian product of these three sets.

## The Search Hypergraph is Too Large. . .

The parse hypergraph has  $O(n^3)$  space constraints (assuming certain grammar properties. . . )

With a m-gram LM the search hypergraph is much larger:

	Vertices	Hyperedges
Parse	$O(n^2 C )$	$O(n^3 G )$
Search	$O(n^2 C  T ^{2(m-1)})$	$O(n^3 G  T ^{2A(m-1)})$

C is the set of target non-terminals n is the input sentence length T is the set of target-side terminals m is the order of the LM A is the maximum rule arity

## **Heuristic Search**

- In practice, only part of the search hypergraph can be explored.
- During search, a partial search hypergraph is generated in topological order.
- Three main strategies for reducing search space:
  - Parse forest pruning Avoid splitting some parse forest hyperedges by prepruning the forest (methods can be exact or inexact).
  - **Heuristic best-first splitting** e.g. cube pruning. Use a splitting algorithm that finds expanded hyperedges in approximately best-first order.
  - **Beam search** Bin vertices according to source word span and category. Keep only the highest-scoring vertices for use later in the search.

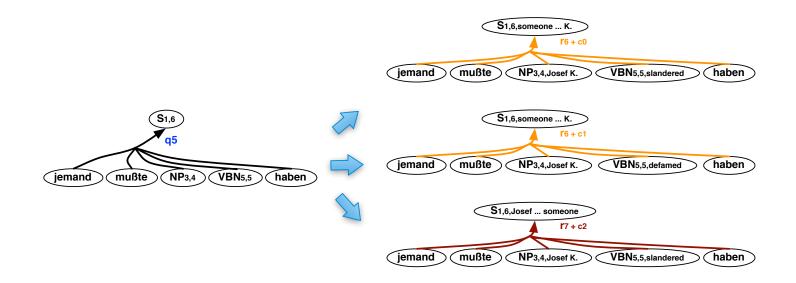
# **Strategy 1: Parse Forest Pruning**

- If parse forest is constructed in full prior to search then dead-ends can be pruned away.
- State splitting can be restricted to a small subset of promising hyperedges.
  - Moses ranks hyperedges according to -LM rule cost plus sums of incoming +LM vertex costs.
- Monolingual forest pruning methods (Inside-outside estimates, see e.g. Charniak and Johnson (2005)).

(Forest pruning methods haven't been widely explored in the MT literature.)

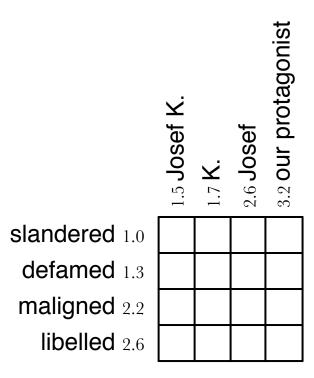
# Strategy 2: Heuristic Best-First State Splitting

• For every hyperedge in the parse hypergraph, there can be very many corresponding hyperedges in the search hypergraph.



• Cube pruning (Chiang, 2007) is most widely-used approximate algorithm but see Heafield et al. (2013) for a faster alternative.

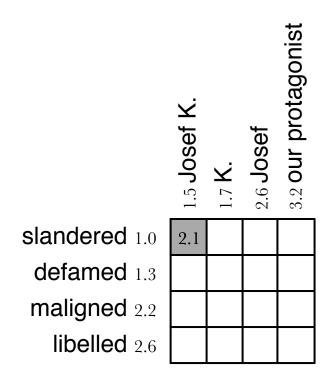
## **Cube Pruning**



Arrange all the choices in a "cube"

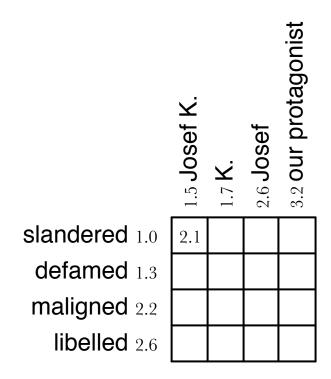
(here: a square, generally an orthotope, also called a hyperrectangle)

#### Create the First Hyperedge



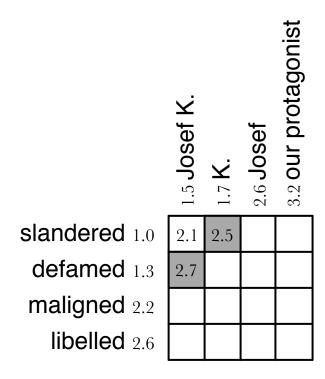
• Hyperedges created in cube: (0,0)

## "Pop" Hyperedge



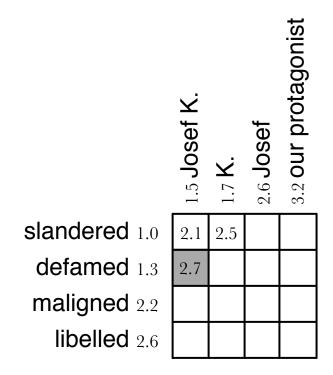
- ullet Hyperedges created in cube:  $\epsilon$
- Hyperedges popped: (0,0)

#### **Create Neighboring Hyperedges**



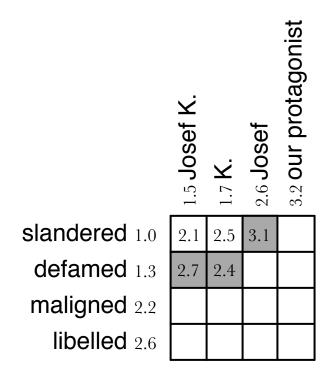
- Hyperedges created in cube: (0,1), (1,0)
- Hyperedges popped: (0,0)

#### Pop Best Hyperedge



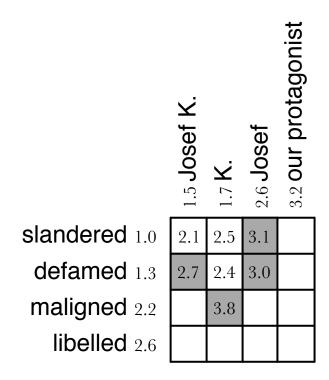
- Hyperedges created in cube: (0,1)
- Hyperedges popped: (0,0), (1,0)

# **Create Neighboring Hyperedges**



- Hyperedges created in cube: (0,1), (1,1), (2,0)
- Hyperedges popped: (0,0), (1,0)

#### More of the Same



- Hyperedges created in cube: (0,1), (1,2), (2,1), (2,0)
- Hyperedges popped: (0,0), (1,0), (1,1)

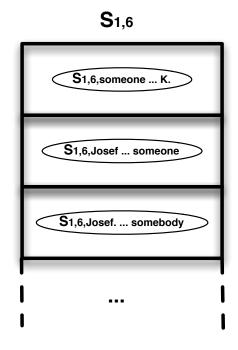
#### **Queue of Cubes**

- Many parse hyperedges for any given span
- Each of them will have a cube
- We can create a queue of cubes
- ⇒ Always pop off the most promising hyperedge, regardless of cube

• May have separate queues for different target constituent labels

#### Strategy 3: Beam search

- Bin vertices according to source word span and category.
- Keep only the highest-scoring vertices for use later in the search.



# Putting it All Together: The S2T Decoding Algorithm in Moses

**Objective** 

Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

Outline

1. Project grammar

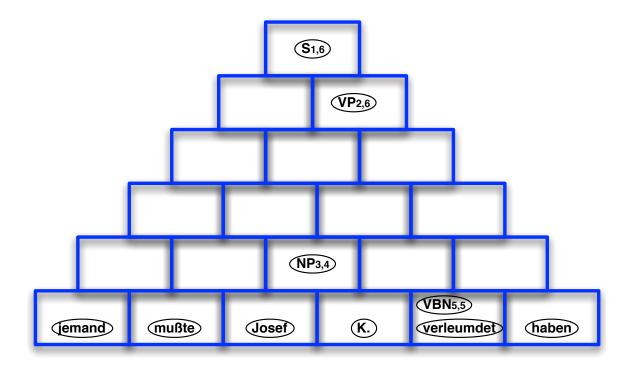
Project weighted SCFG to weighted CFG  $f: G \rightarrow G'$ 

2. Interleaved parse + search

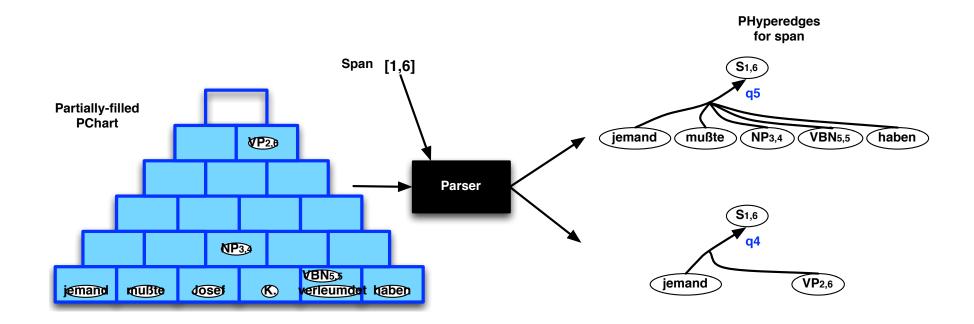
Span-by-span, build parse hypergraph wrt  $G^\prime$  and build partial search hypergraph

3. Extract derivations

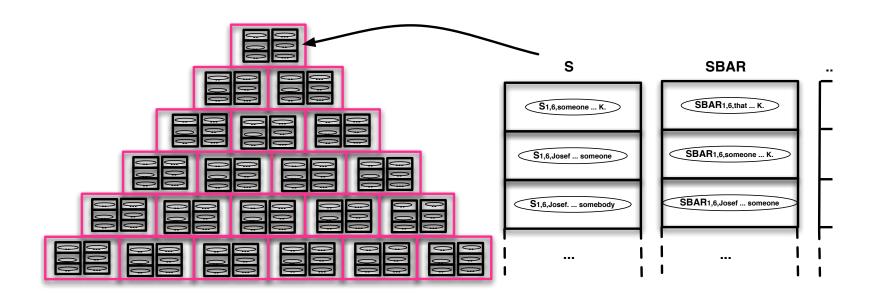
Extract k-best derivations (Huang and Chiang, 2005)



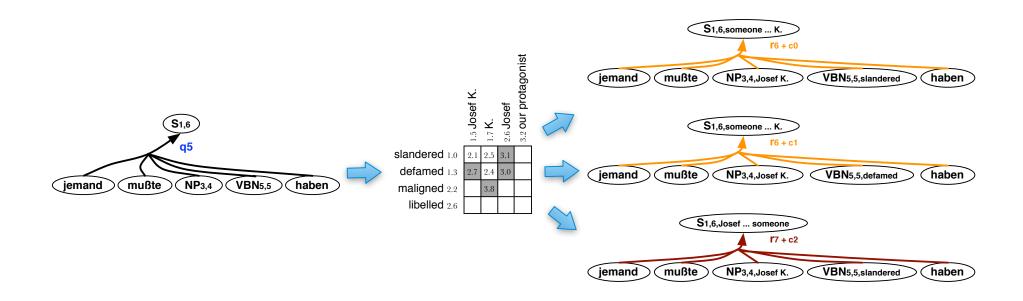
- Vertices of the parse hypergraph are stored in a chart (includes input sentence)
- Hyperedges are enumerated but not stored in chart
- Terminology: PChart, PVertex, PHyperedge



- Parser generates PHyperedges for given span of PChart
- Parser has access to partially-completed PChart
- For now, the parser is a black-box component but we'll return to parsing. . .



- Vertices of the search hypergraph are stored in a chart (includes input sentence)
- Vertices are stored in stacks (one per span + category), which are sorted
- Hyperedges are stored (unlike in PChart)
- Terminology: SChart, SVertex, SHyperedge

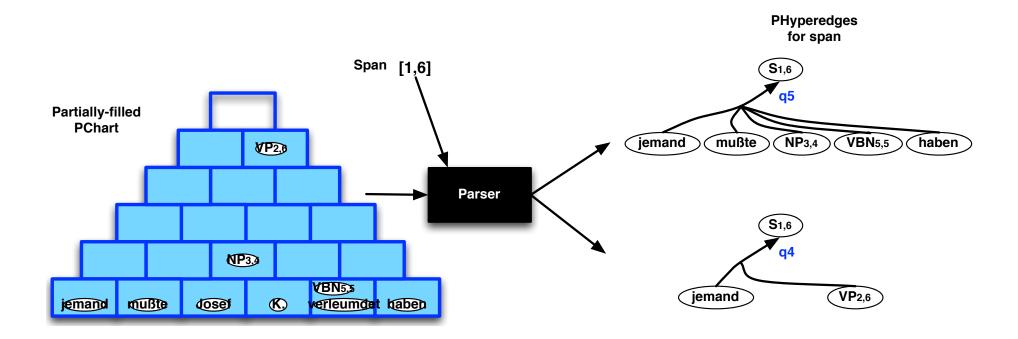


- Cube pruning algorithm (or similar) produces SHyperedges from PHyperedges
- A single SVertex can be produced multiple times so must check for this ('recombination')

#### The Moses S2T Decoding Algorithm

```
1: initialize PChart and SChart by adding vertices for input words
 2: for each span (in parser-defined order) do
      p-hyperedges = ForestPrune(parser.EnumerateHyperedges(span, p-chart), s-chart)
     for all p-hyperedges do
 4:
        create a cube for it
 5:
        create first s-hyperedge in cube
 6:
        place cube in queue
 7:
     end for
 8:
     for specified number of pops do
 9:
        pop off best s-hyperedge of any cube in queue
10:
        add it to a category-specific buffer
11:
        create its neighbors
12:
     end for
13:
     for category do
14:
        recombine s-hyperedges from buffer and move into s-chart stack
15:
        sort stack
16:
     end for
17:
18: end for
```

# Parsing for S2T Decoding



- Parser's job is to enumerate PHyperedges, span-by-span.
- Parser has access to partially-filled PChart.

#### Parsing for S2T Decoding

- Can we just use CYK / CYK+ / Earley?
  - All require binarization (implicit or explicit).
  - Wasn't a problem for Viterbi -LM case.
- **Idea 1** Binarize G'
  - Binary normal forms exist for monolingual CFG grammars.
  - But we still need to know the synchronous rules for +LM search.
- Idea 2 Binarize G before projection to CFG
  - Binarization impossible for some SCFG rules with rank  $\geq 4$
  - Not necessarily a problem: non-binarizable cases are rare in word-aligned translation data (Zhang et al., 2006)
  - But tricky in practice: how do we weight rules? And what about grammar inflation?

#### **How to Avoid Binarization**

• Hopkins and Langmead (2010) define a grammar property called scope:

Pattern	Scope	Pattern	Scope
abcde	0	a ⋄ ⋄ ⋄ e	2
a ⋄ c ⋄ e	0	♦ b c d ♦	2
a ⋄ ⋄ d e	1	♦ ♦ c d ♦	3
♦ b c d e	1	$\Diamond \Diamond \Diamond \Diamond \Diamond \Diamond$	6

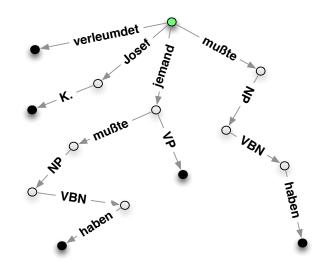
- They prove that a sentence of length n can be parsed with a scope k grammar in O(nk) chart updates without binarization.
- They demonstrate empirically that reducing a GHKM grammar to scope-3 by pruning does not harm translation quality compared to synchronous binarization (and pruning is much simpler).
- Chung et al. (2011) perform similar comparison and achieve same result.

#### **Specialized Parsing Algorithms**

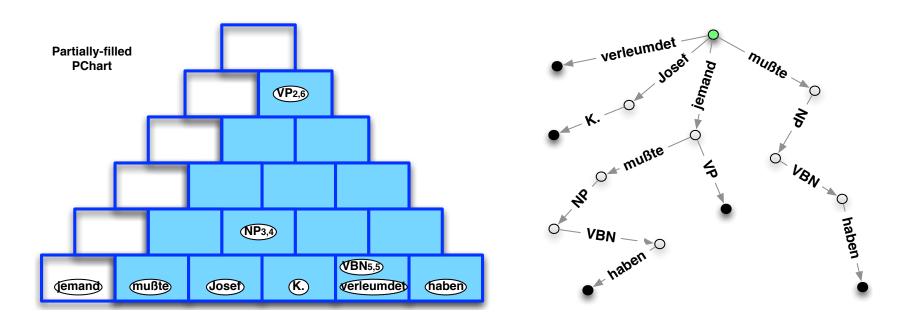
- CYK+ and Earley are popular choices for S2T decoding.
- But storing large numbers of dotted rules is problematic in practice (Chung et al. 2011 find scope-3 slower than binarized grammar with Earley parser, which they attribute to dotted rule storage).
- Several parsing algorithms have been designed specifically for synchronous translation grammars: DeNero et al. (2009), Hopkins and Langmead (2010), Sennrich (2014).
- We use Sennrich (2014)'s recursive variant of CYK+:
  - Good performance on WMT-scale task: fast, low-memory overhead
  - Simpler than CYK+ and alternatives
  - No dotted rule storage

# Parsing for S2T Decoding (Moses-style)

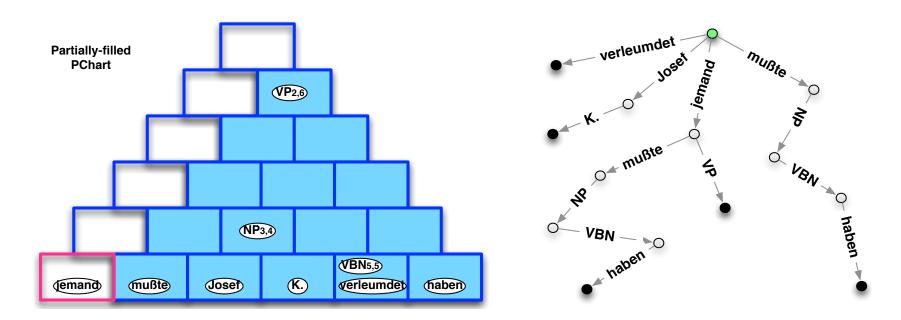
```
\begin{array}{lll} q_1\colon & \operatorname{NP} & \to & Josef \ K. \\ q_2\colon & \operatorname{VBN} & \to & verleum det \\ q_3\colon & \operatorname{VP} & \to & mu\beta te \ \operatorname{NP} \ \operatorname{VBN} \ haben \\ q_4\colon & \operatorname{S} & \to & jemand \ \operatorname{VP} \\ q_5\colon & \operatorname{S} & \to & jemand \ mu\beta te \ \operatorname{NP} \ \operatorname{VBN} \ haben \end{array}
```



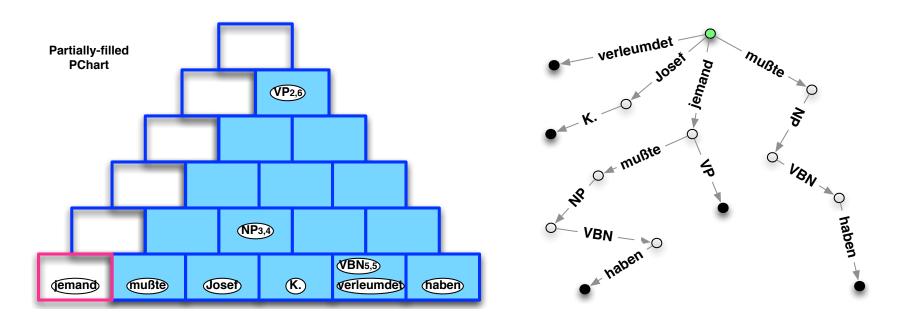
- $\bullet$  Projected grammar G' is represented as a trie (sometimes called a prefix tree)
- Edges are labelled with terminals and non-terminals
- Labels along path (from root) represent prefix of rule RHS
- ullet Vertices in black are associated with group of rules from G (sub-grouped by rule LHS)



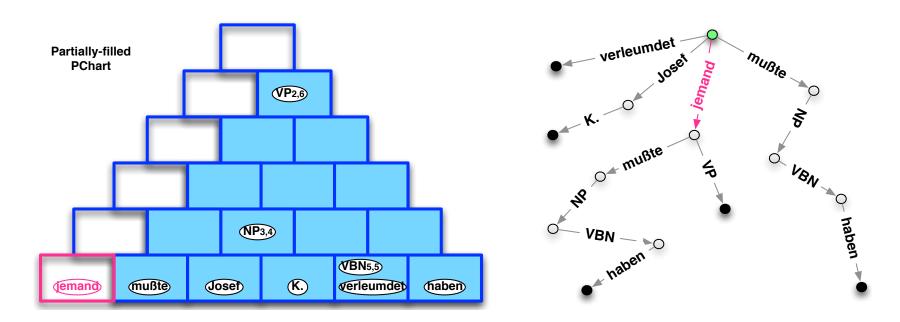
- Sennrich (2014)'s parsing algorithm visits cells in right-to-left, depth-first order.
- We consider situation where all of PChart filled except for left-most diagonal.
- Recall that PVertices are stored, but PHyperedges are not.



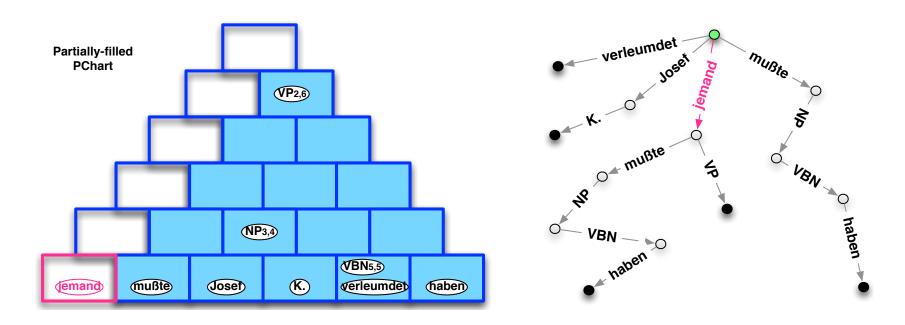
- Tail prefix: []
- Recursion level: 0



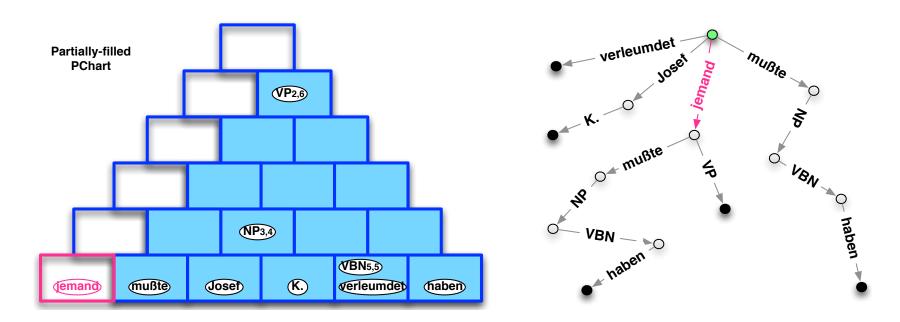
- Tail prefix: []
- Recursion level: 0
- Look for edge labelled 'jemand' at root node



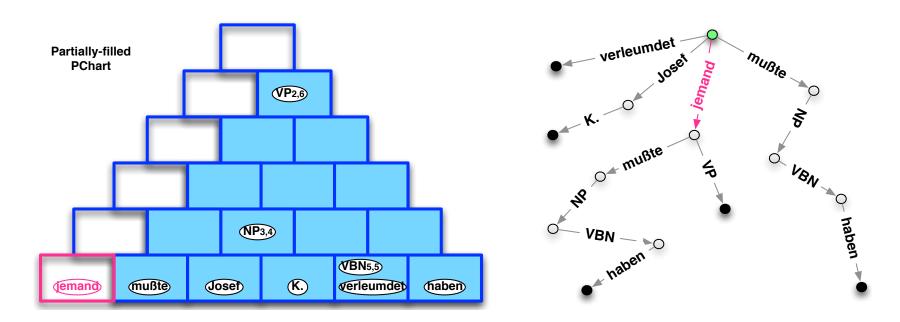
- Tail prefix:  $[jemand_{1,1}]$
- Recursion level: 0
- Look for edge labelled 'jemand' at root node found



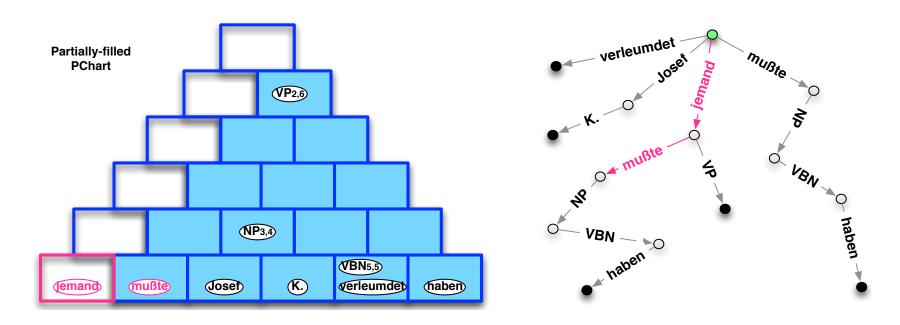
- Tail prefix:  $[jemand_{1,1}]$
- Recursion level: 0
- Check for rules at current node none



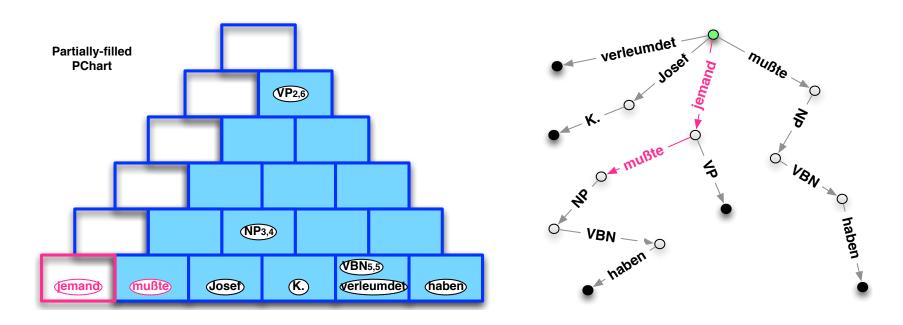
- Tail prefix:  $[jemand_{1,1}]$
- Recursion level: 0
- Now visit each cell along previous diagonal (recursive step)



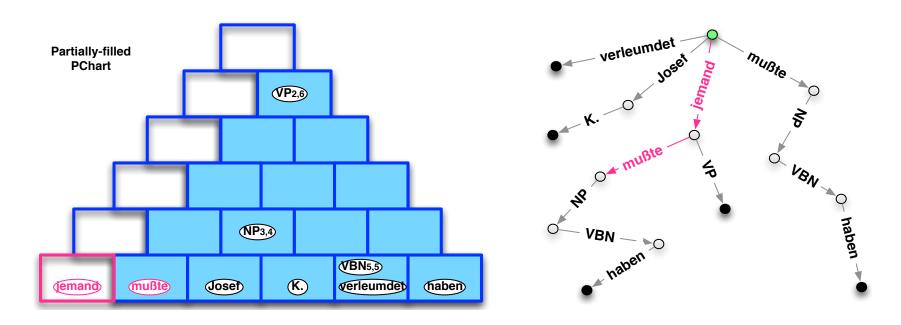
- Tail prefix:  $[jemand_{1,1}]$
- Recursion level: 1
- Look for edge labelled 'mußte' at current node



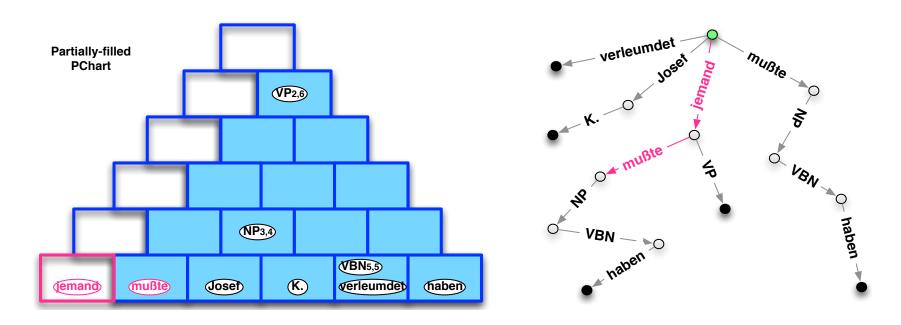
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 1
- Look for edge labelled 'mußte' at current node found



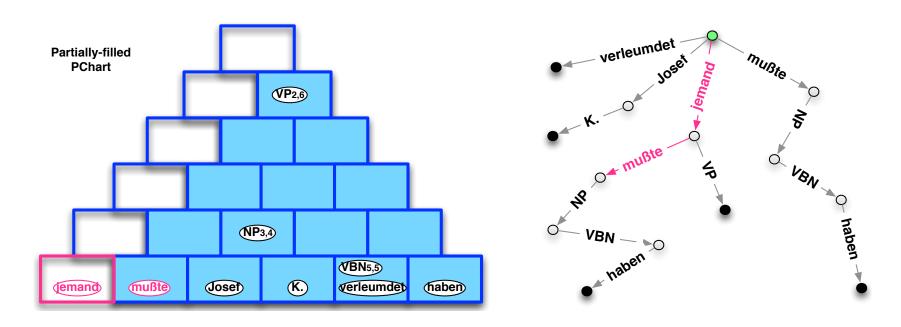
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 1
- Now visit each cell along previous diagonal



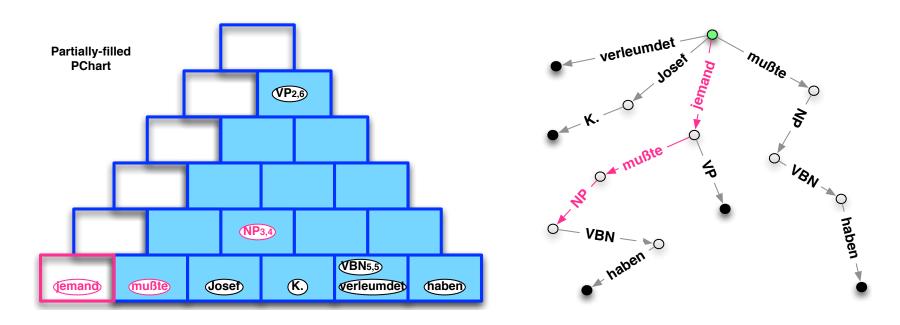
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 2
- Look for edge labelled 'Josef' at current node



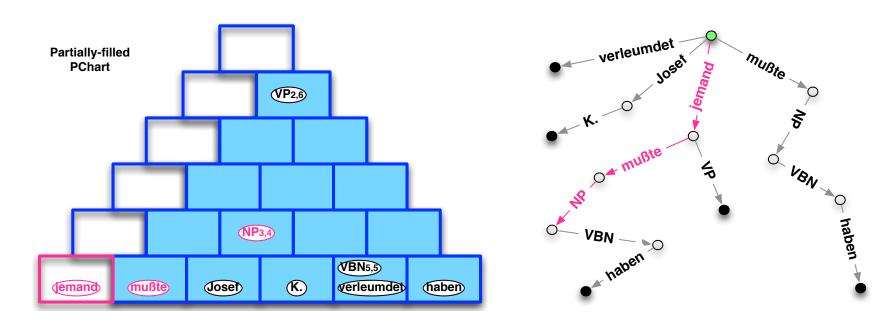
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 2
- Look for edge labelled 'Josef' at current node not found



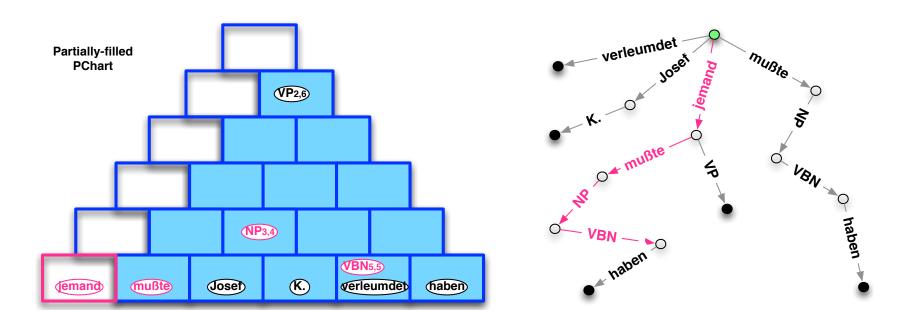
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 2
- Look for edge labelled 'NP' at current node



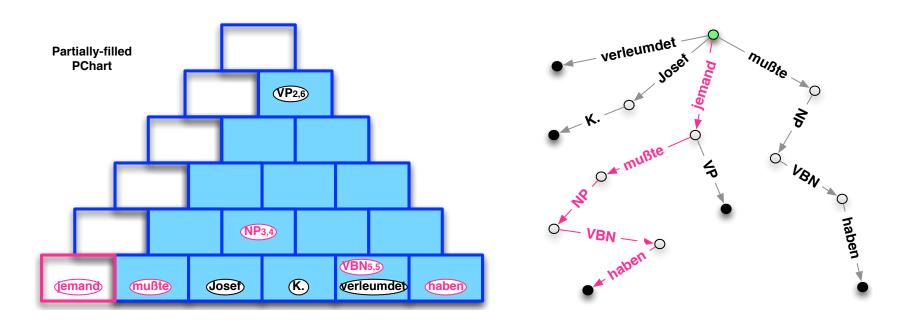
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}]$
- Recursion level: 2
- Look for edge labelled 'NP' at current node found



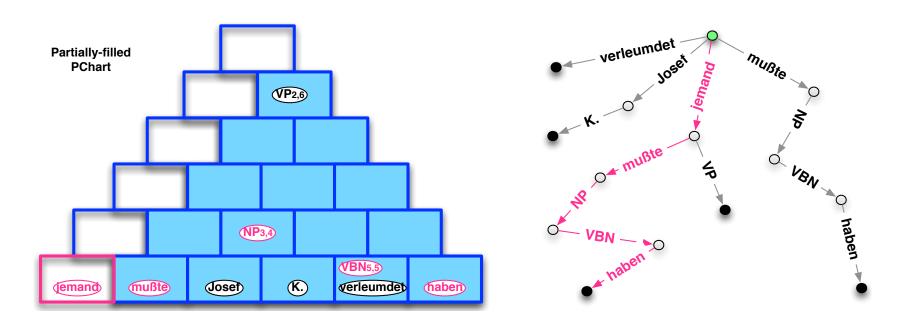
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}]$
- Recursion level: 3
- And so on...



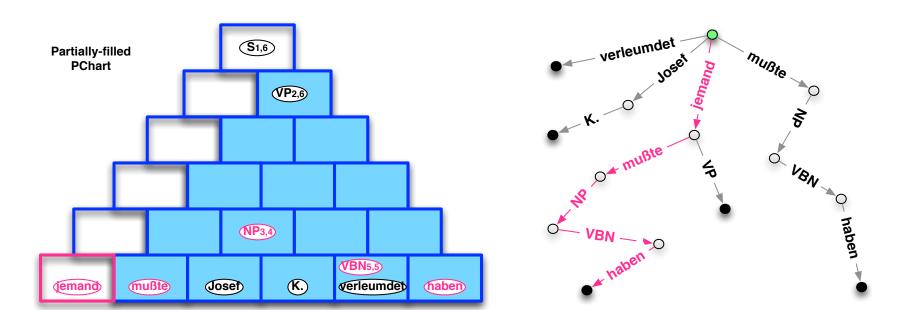
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}]$
- Recursion level: 3
- And so on...



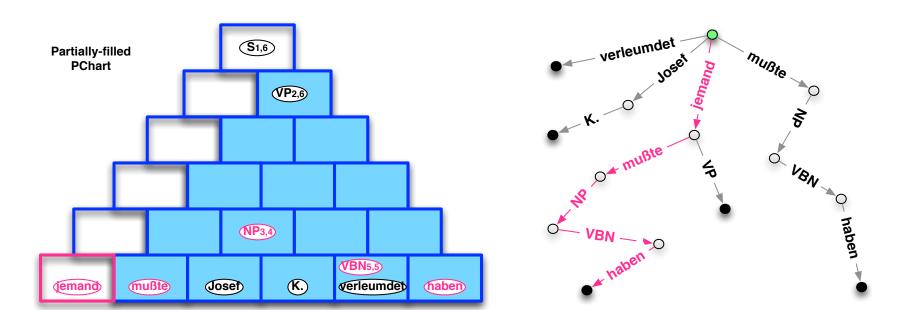
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}, haben_{6,6}]$
- Recursion level: 4
- And so on...



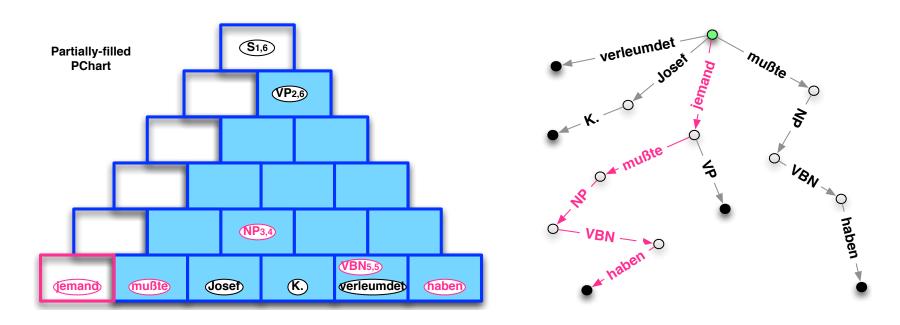
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}, haben_{6,6}]$
- Recursion level: 4
- At this point we add a PVertex for each LHS from trie node's rule group



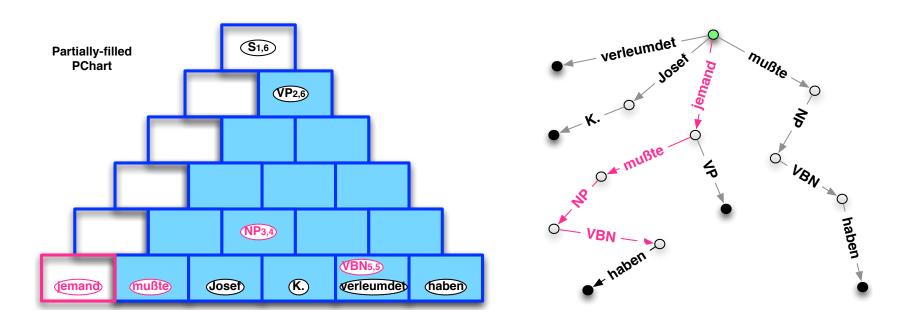
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}, haben_{6,6}]$
- Recursion level: 4
- At this point we add a PVertex for each LHS from trie node's rule group



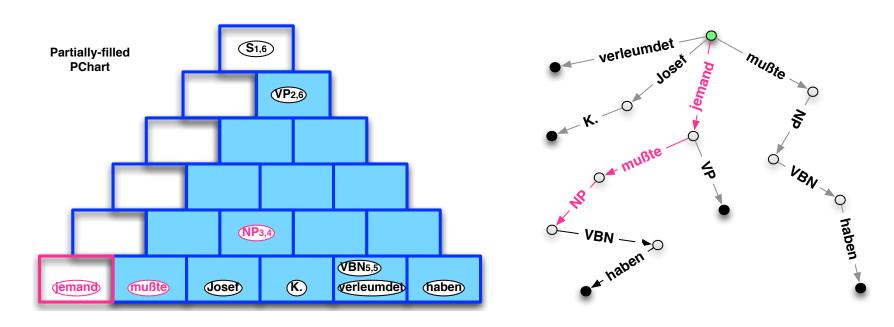
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}, haben_{6,6}]$
- Recursion level: 4
- Together the PVertex and tail prefix constitute a complete PHyperedge.



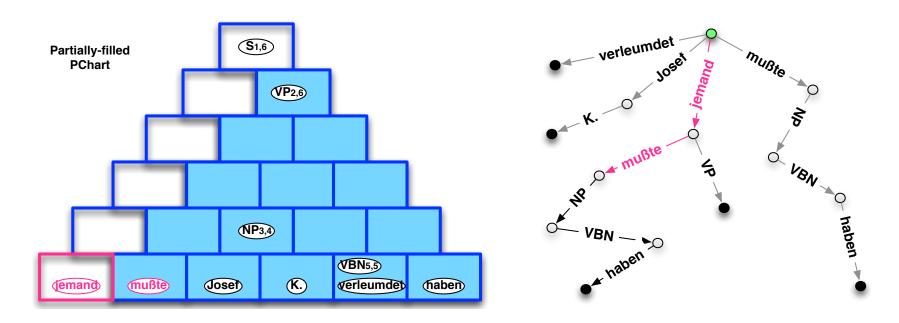
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}, haben_{6,6}]$
- Recursion level: 4
- Reached end of sentence, so now the recursion stack unwinds



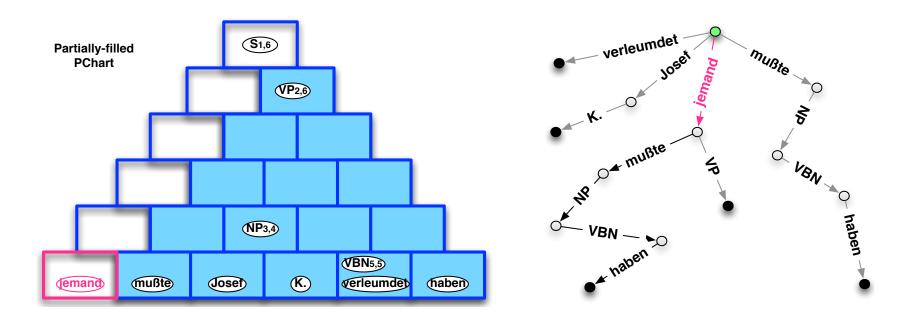
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}, VBN_{5,5}]$
- Recursion level: 3
- The recursion stack unwinds. . .



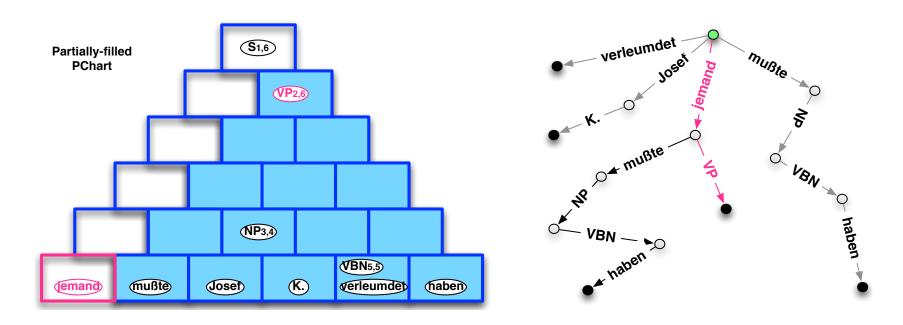
- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}, NP_{3,4}]$
- Recursion level: 2
- The recursion stack unwinds. . .



- Tail prefix:  $[jemand_{1,1}, mußte_{2,2}]$
- Recursion level: 1
- The parser continues trying to extend the tail. . .

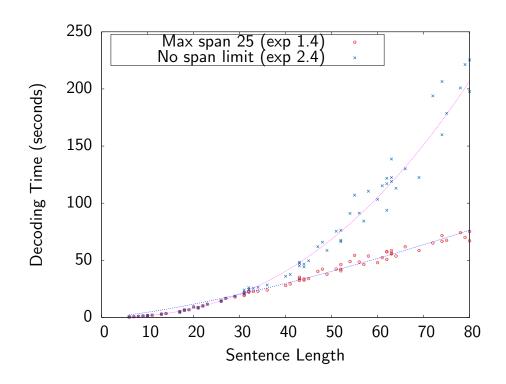


- Tail prefix:  $[jemand_{1,1}]$
- Recursion level: 1
- The parser continues trying to extend the tail. . .



- Tail prefix:  $[jemand_{1,1}, VP_{2,6}]$
- Recursion level: 1
- ullet PVertex  $S_{1,6}$  has already been added, but new tail means new PHyperedge

#### **Decoding Performance in Practice**



- S2T Moses system trained using all English-German data from WMT14
- Span limit can be used to reduce decoding time (limit is typically 10-15 for Hiero; can be higher or unlimited for S2T)

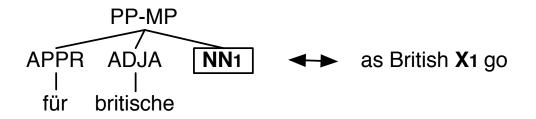
### **String-to-Tree Decoding - Summary**

- Input sentence is a string.
- Decoding algorithm based on monolingual parsing.
- Hiero decoding is special-case of S2T decoding.
- To integrate a m-gram LM, the parse forest hypergraph is expanded to a (much-larger) search hypergraph.
- Heavy pruning is required in practice.

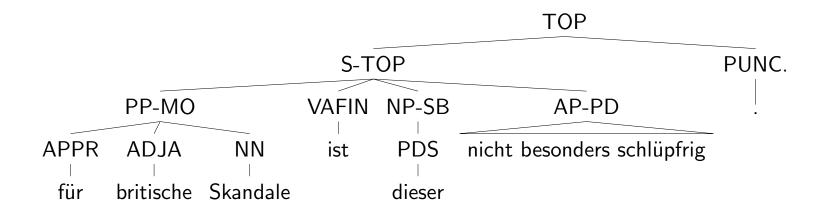
# **Tree-to-String Decoding**

#### Reminder

• Translation rules are STSG rules with source-side syntax



• Input is parse tree



#### **Outline**

**Objective** Find the k-best synchronous derivations  $d_1, d_2, \dots d_k$ 

#### Outline

1. Project grammar

Project weighted STSG to unweighted TSG  $f:G \to G'$ 

2. Match rules

Find rules from  $G^{\prime}$  that match input tree, record in match hypergraph

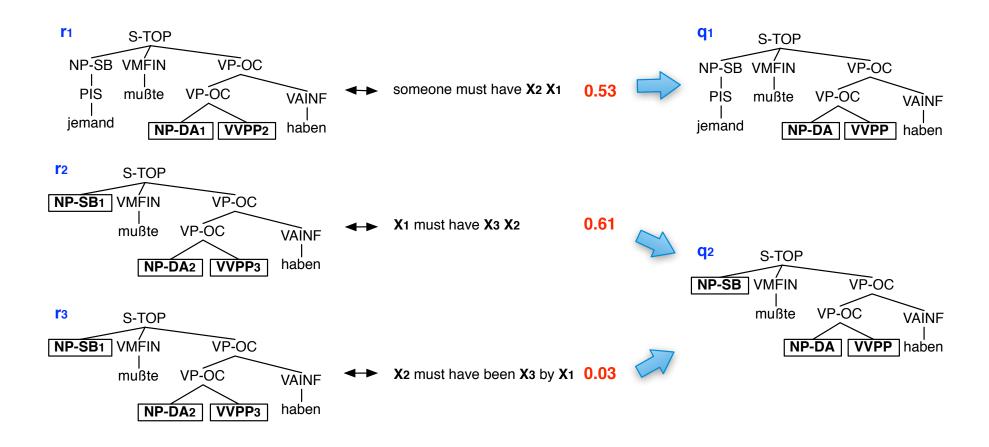
3. Search

In post-order traversal of match hypergraph, build partial search hypergraph

4. Extract derivations

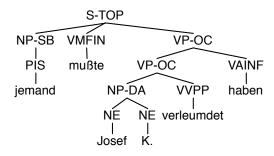
Extract k-best derivations (Huang and Chiang, 2005)

### **Step 1: Project Grammar**



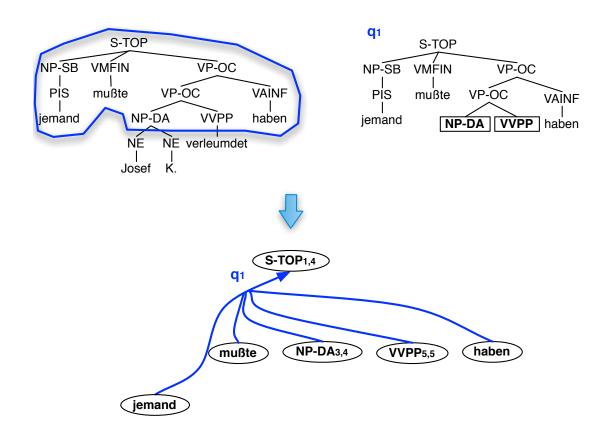
• Take source-side of rule, ignore weights.

### Step 2: Match Rules, Build Match Hypergraph



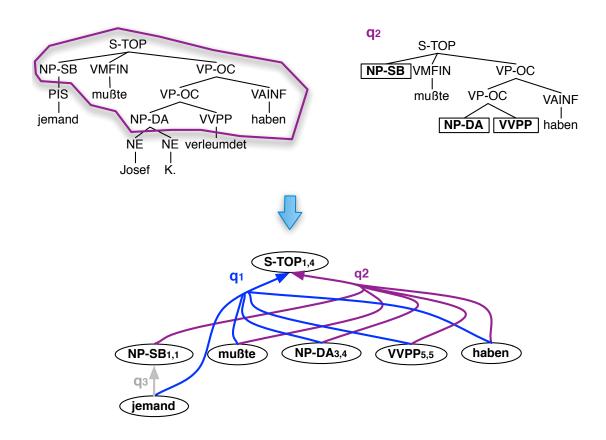
• Look for rules that match input tree

# Step 2: Match Rules, Build Match Hypergraph



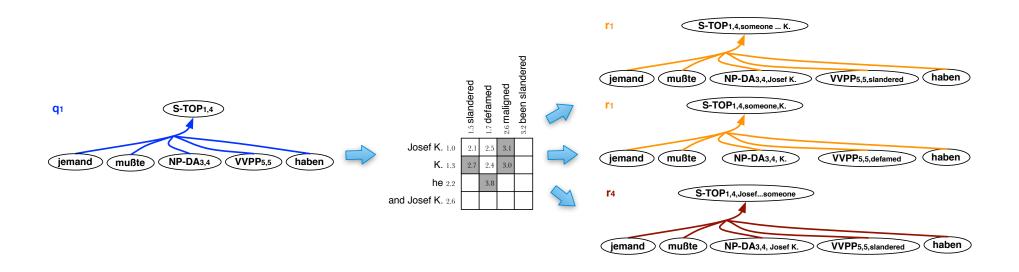
• For each matching rule, add hyperedge to match hypergraph

# Step 2: Match Rules, Build Match Hypergraph



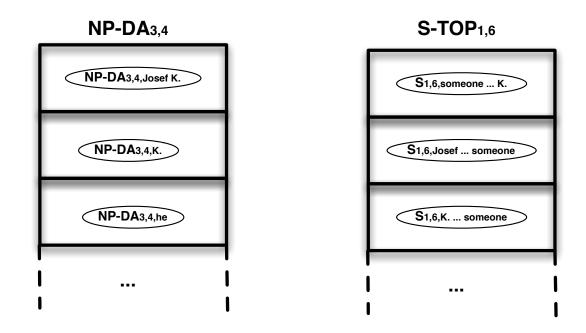
ullet Match hypergraph encodes forest of possible derivation trees from G'

### Step 3: Build Partial Search Hypergraph



- Cube pruning algorithm produces SHyperedges from MHyperedges
- Translations not necessarily constituents (unlike S2T)

# Step 3: Build Partial Search Hypergraph



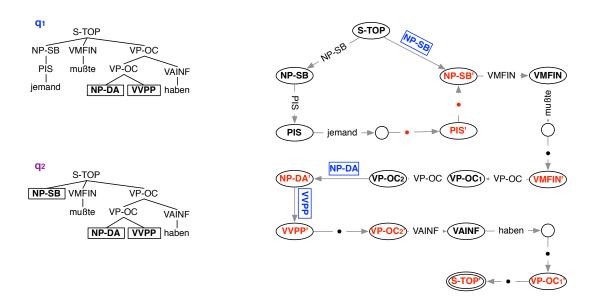
• Vertices are stored in stacks, one per input tree node

### The T2S Decoding Algorithm

```
1: build match hypergraph by matching grammar rules to input tree
 2: for each m-vertex (post-order) do
     for all incoming m-hyperedges do
        create a cube for it
 4:
        create first s-hyperedge in cube
 5:
        place cube in queue
 6:
     end for
 7:
     for specified number of pops do
 8:
        pop off best s-hyperedge of any cube in queue
 9:
        add it to a buffer
10:
        create its neighbors
11:
     end for
12:
     recombine s-hyperedges from buffer and move into stack
13:
     sort and prune stack
14:
15: end for
```

#### Rule Matching by DFA Intersection

- Rules are encoded as DFAs. Scheme here is from Matthews et al. (2014)
- Input tree encoded in same way.
- Standard DFA intersection algorithm produces rule match hypergraph.



## **Tree-to-String Decoding - Summary**

- Input sentence is a parse tree.
- Tree constrains rule choice: much smaller search space than S2T
- Decoding algorithm based on rule matching with LM integration.
- LM integration identical to S2T.

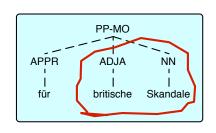
## A Sketch of Tree-to-Tree Decoding

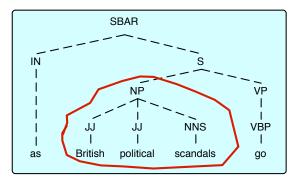
- STSG with tree input.
- T2T decoding is combination of S2T and T2S:
  - Search state expanded to include target-side category
  - Rule matching used to select rules; further constrained by target categories
  - Multiple category-specific stacks per input tree node
  - LM integration identical to S2T / T2S.
- Exact T2T not widely used in practice due to syntactic divergence.

- Part I Introduction
- Part II Rule Extraction
- Part III Decoding
- Part IV Extensions

## "Fuzzy" Syntax

- In a nutshell: move syntax out of grammar and into feature functions
  - Syntax becomes a soft constraint
  - Motivated by syntactic divergence problem in tree-to-tree model

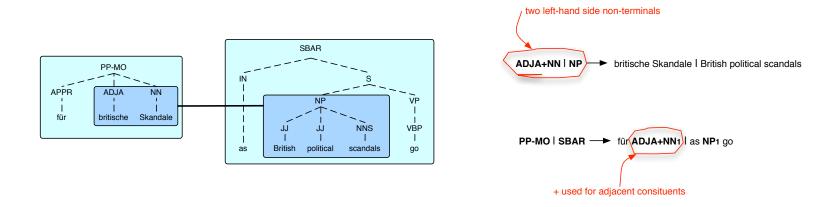




- "Learning to Translate with Source and Target Syntax" (Chiang, 2010)
  - Zhang et al (2011) use fuzzy syntax on source-side of string-to-tree model and explore alternative feature functions

### "Fuzzy" Syntax

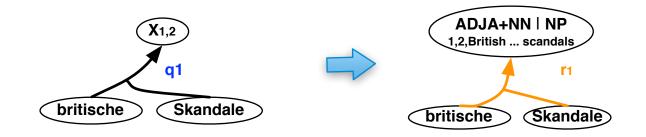
- Parse trees on both sides of training data
- Uses Hiero rule extraction but with SAMT-style labelling



- Only most frequent labelling kept (one-to-one correspondence with Hiero rules)
  - r1 ADJA+NN | NP → britische Skandale | British political scandals
    r2 PP-MO | SBAR → für ADJA+NN1 | as NP1 go
    q1 X → britische Skandale | British political scandals
    q2 X → für X1 | as X1 go

## "Fuzzy" Syntax

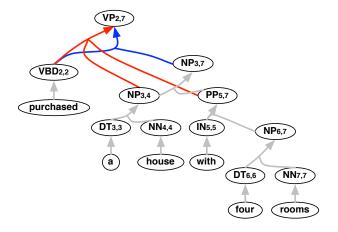
Rule labels not used during parsing but retrieved for search



- Feature functions score substitutions
  - e.g. if a NP is rewritten as a ADJA+NN on source side then the feature  ${\tt subst^s}_{\tt NP\to ADJA+NN}$  fires
- Tens of thousands of features
- Outperforms exact tree-to-tree (0.4 BLEU on Zh-En; 1.5 BLEU on Ar-En)

### Forest-to-String

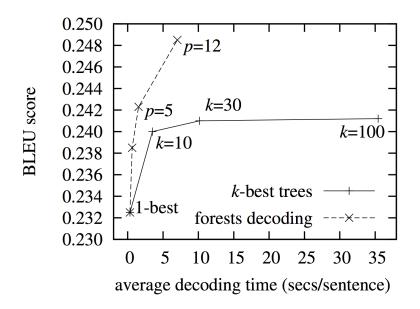
- Translation quality of T2S model depends on accuracy of 1-best (or k-best) parse tree(s) for input sentences
- Forest-to-string extends T2S by using (pruned) parse forest as input



- Algorithm is identical to T2S except for rule matching step
- "Forest-based Translation" (Mi et al., 2008)

## Forest-to-String

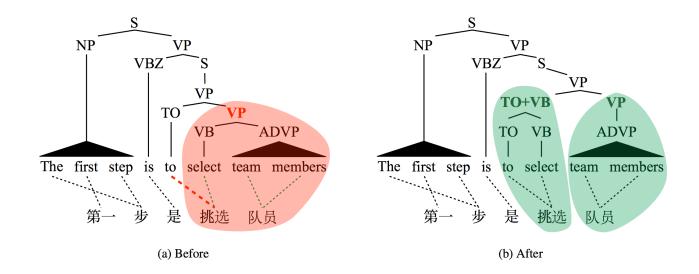
• Using forest gives better speed-quality trade-off than using k-best trees



(Figure taken from Mi et al., 2008)

#### **Tree Transformation**

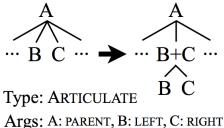
- Adapting training data for syntax-based MT is active area of research (tree binarization, label coarsening / refinement, word alignment edits)
- "Transforming Trees to Improve Syntactic Convergence" (Burkett and Klein, 2012) proposes tree restructuring method to improve rule extraction:



(Figure taken from Burkett and Klein, 2012)

#### **Tree Transformation**

• Defines six classes of transformation



A: PARENT, B: LEFT, C: RIGHT Args: A: PARENT, B: TARGET

- Error-based learning method using GHKM frontier node count as metric
- Sequence of transformations learned from subset of training data then applied to full corpus
- Gain of 0.9 BLEU over baseline on Chinese to English; outperforms simple left and right binarization

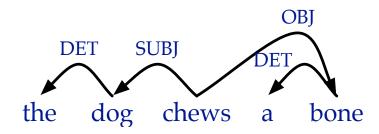
### **Dependency**

A different view on syntax

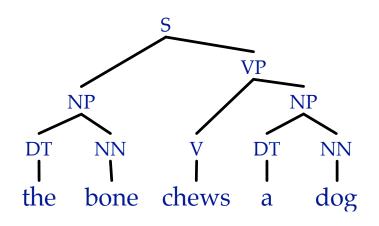
SCFG phrase structure

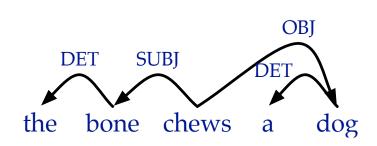
NP NP NP NP DT NN U DT NN the dog chews a bone

Syntactic dependency grammar



#### Phrase Structure is not Enough



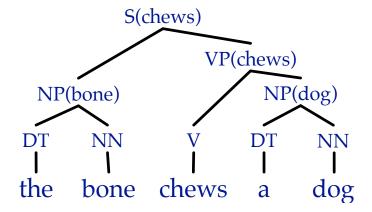


syntactically well-formed

semantically implausible

## **Dependency in SCFG**

Add head word to constituents

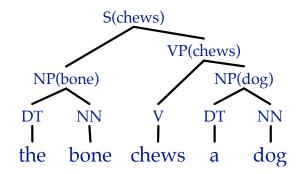


Add mapping of head words to rules

$$VP(w_1) \rightarrow V(w_1) NP(w_2)$$

requires identification of head child

#### **Semantic Plausibility**

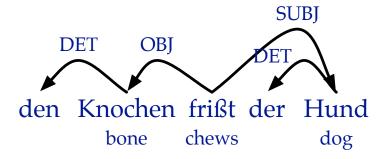


#### Score each lexical relationship

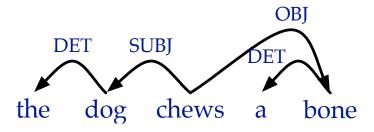
- Rule:  $VP(chews) \rightarrow V(chews) NP(dogs)$ 
  - Feature:  $VP(chews) \rightarrow V-HEAD(chews)$  **OK**
  - Feature:  $VP(chews) \rightarrow NP(dog)$  **BAD**
- Rule:  $S(chews) \rightarrow NP(bone) VP(chews)$ 
  - Feature:  $S(chews) \rightarrow NP(bone)$  BAD
  - Feature:  $S(chews) \rightarrow V-HEAD(chews)$  **OK**

#### Informed by Source

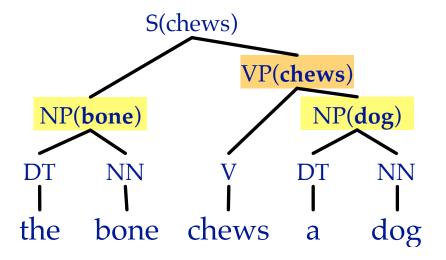
- Languages with case marking
  - different word order
  - same dependency relationships



• Give preference to translations that preserve dependency relationships



#### **Verb Frames**



- Check if full verb frame is properly filled
  - intransitive / transitive / ditransitive
  - not just binary relationships
  - appropriate type of subjects / objects
- However: tracking verb frame is not trivial

#### **Towards Semantics**

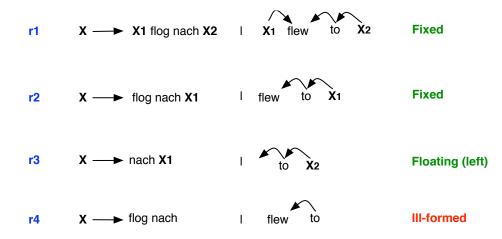
- Different syntax same verb-noun semantic relationships
  - The bone is chewed by the dog.
  - The dog chews the bone.
  - The bone, the dog chews.
  - A dog chewed a bone.
- Even more abstract representations e.g., Abstract Meaning Representation (AMR):

```
(c / chew-01
    :arg0 (d / dog)
    :arg1 (b / bone))
```

• Generation of these types of representation open research problem

# String-to-Dependency: Shen et al. (2008)

- Hiero rules but with unlabelled dependencies on target side
- Target-side allowed one head to which floating dependencies can attach



• "A New String-to-Dependency Machine Translation Algorithm with a Target Dependency Language Model" (Shen et al., 2008)

#### **String-to-Dependency**

- Decoding algorithm modified to combine dependency structures.
- Restriction to well-formed rules reduces grammar size from 140M to 26M rules (no significant effect on translation quality).
- Gains of 1.2 BLEU on Zh-En from addition of dependency LM (Markov model over dependency heads).

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