



# Hyperspherical Consistency Regularization

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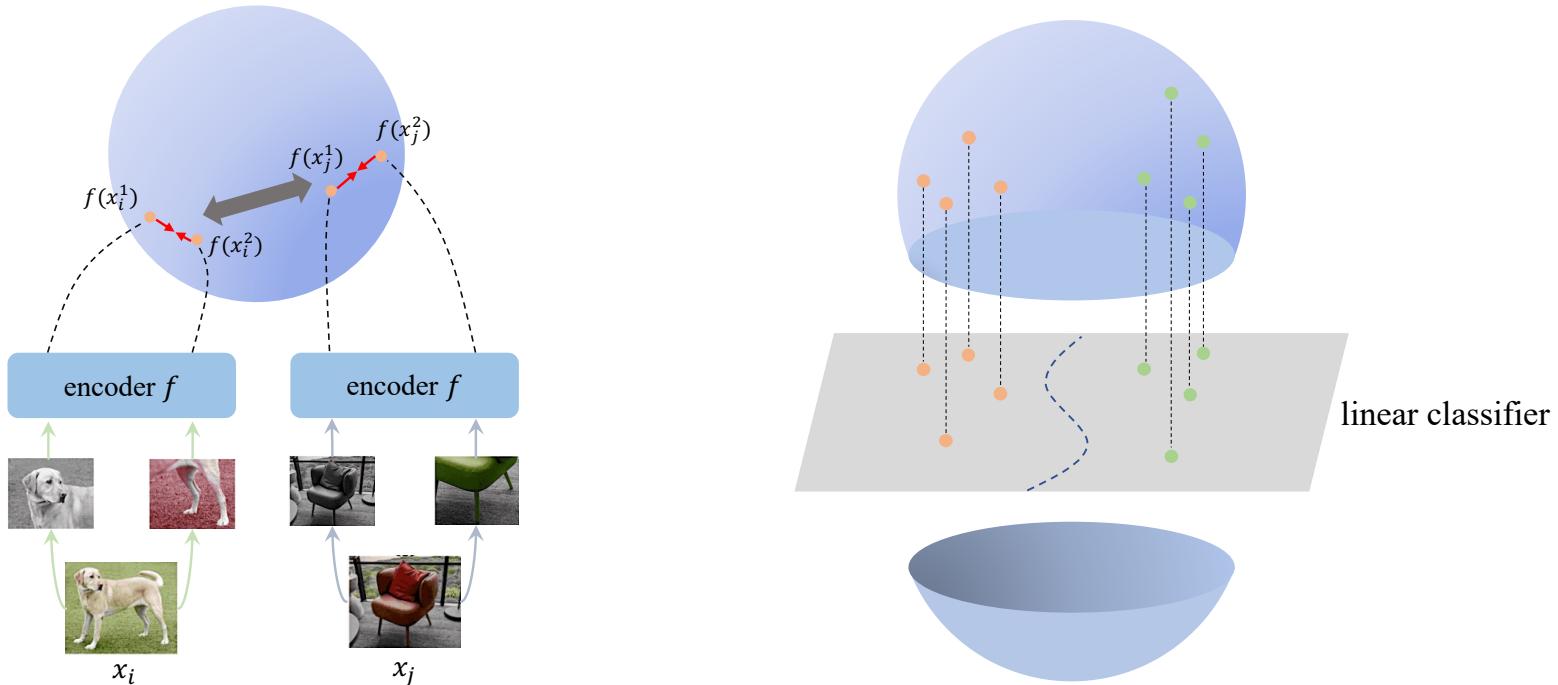
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CVPR, 2022

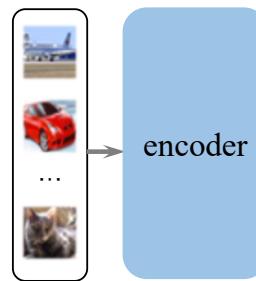
# Contrastive learning on the hypersphere



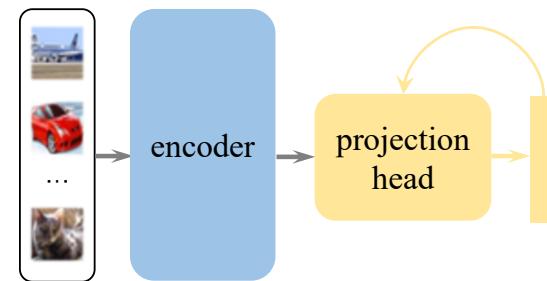
Linear classifier learns to separate the hypersphere through the hypersphere.



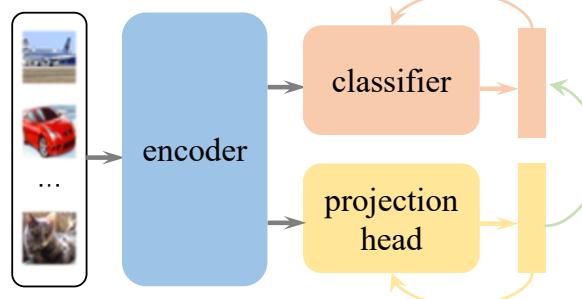
# Learning paradigms



(a) supervised learning



(b) self-supervised learning

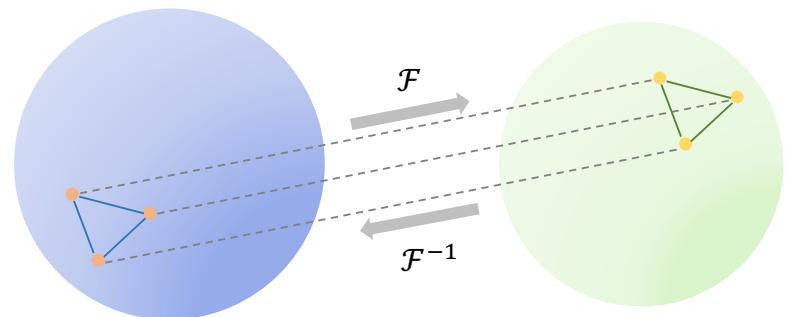
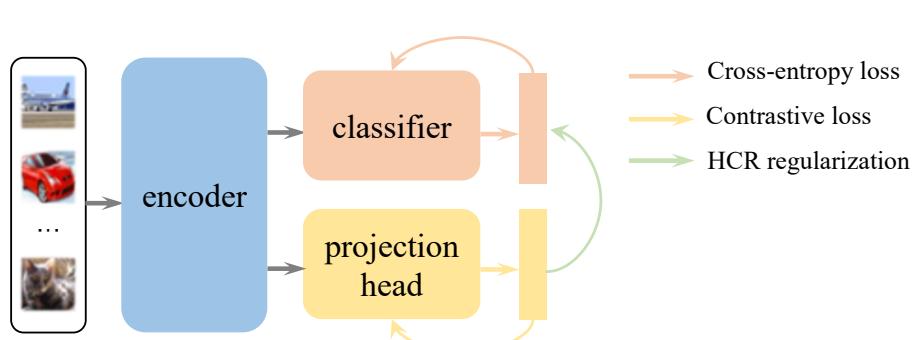


(c) learning with HCR

- > Cross-entropy loss
- > Contrastive loss
- > HCR regularization

HCR takes supervised learning as the primary task and forces self-supervised learning to assist it from another perspective.

# Hypersphere consistency regularization



projection head's hypersphere      classifier's hypersphere

Define the objective of HCR:

$$\begin{aligned} HCR(p(d_g), q(d_h)) \\ = -p(d_g)\log(q(d_h)) - (1 - p(d_g))\log(1 - q(d_h)) \end{aligned}$$

where,

$$\begin{aligned} p(d_g) &= C_g \frac{1}{\sigma_g \sqrt{2\pi}} \exp\left[-\frac{1}{2} \frac{(d_g - \mu_g)^2}{\sigma_g^2}\right], \\ q(d_h) &= C_h \frac{1}{\sigma_h \sqrt{2\pi}} \exp\left[-\frac{1}{2} \frac{(d_h - \mu_h)^2}{\sigma_h^2}\right]. \end{aligned}$$

# Experiments – Semi-supervised learning



Classification accuracy (%) on Stanford Cars dataset.

Method	Label Proportion		
	15%	30%	50%
Pseudo-Labeling	40.93±0.23	67.02±0.19	78.71±0.30
Π-model	45.19±0.21	57.29±0.26	64.18±0.29
Mean Teacher	54.28±0.14	66.02±0.21	74.24±0.23
UDA	39.90±0.43	64.16±0.40	71.86±0.56
FixMatch	49.86±0.27	77.54±0.29	84.78±0.33
SimCLRv2	45.74±0.16	61.70±0.18	77.49±0.24
Self-Tuning	74.99±0.11	85.87±0.04	89.83±0.01
Self-Tuning+HCR	<b>78.76±0.08</b>	<b>87.70±0.07</b>	<b>91.14±0.06</b>

Classification accuracy (%) on FGVC Aircraft dataset.

Method	Label Proportion		
	15%	30%	50%
Pseudo-Labeling	46.83±0.30	62.77±0.31	73.21±0.39
Π-model	37.72±0.25	58.49±0.26	65.63±0.36
Mean Teacher	51.59±0.23	71.62±0.29	80.31±0.32
UDA	43.96±0.45	64.17±0.49	67.42±0.53
FixMatch	55.53±0.26	71.35±0.35	78.34±0.43
SimCLRv2	40.78±0.21	59.03±0.29	68.54±0.30
Self-Tuning	66.68±0.17	79.94±0.09	84.35±0.08
Self-Tuning+HCR	<b>70.54±0.02</b>	<b>82.64±0.04</b>	<b>86.89±0.15</b>

Classification accuracy (%) on CUB-200-2011 dataset.

Method	Label Proportion		
	15%	30%	50%
Pseudo-Labeling	45.33±0.23	56.20±0.29	64.07±0.32
Π-model	45.20±0.25	58.49±0.26	65.63±0.36
Mean Teacher	53.26±0.19	66.66±0.20	74.37±0.30
UDA	46.90±0.31	61.16±0.35	71.86±0.43
FixMatch	44.06±0.23	63.54±0.18	75.96±0.29
SimCLRv2	45.74±0.15	62.70±0.24	71.01±0.34
Self-Tuning	64.79±0.06	74.31±0.07	78.45±0.31
Self-Tuning+HCR	<b>66.42±0.24</b>	<b>75.06±0.13</b>	<b>79.48±0.16</b>

Classification accuracy (%) of transfer learning methods.

Method	Stanford Cars	Aircraft	CUB200
Fine-Tuning	87.20±0.19	81.13±0.21	78.01±0.16
L <sup>2</sup> -SP	86.58±0.26	80.98±0.29	78.44±0.17
DELTA	86.32±0.20	80.44±0.20	78.63±0.18
BSS	87.63±0.27	81.48±0.18	78.85±0.31
Co-Tuning	89.53±0.09	83.87±0.09	81.24±0.14
Self-Tuning	92.33±0.10	88.96±0.21	81.60±0.11
Self-Tuning+HCR	<b>93.03±0.06</b>	<b>90.41±0.03</b>	<b>82.63±0.19</b>

# Experiments – Noisy label learning

CIFAR-100 with symmetric noises.

Method	sym-20%	sym-50%	sym-80%
Standrad CE	57.79±0.44	33.75±0.46	8.64±0.22
Decoupling	56.18±0.32	31.58±0.54	7.71±0.23
Co-teaching	64.28±0.32	32.62±0.51	6.65±0.71
Co-teaching+	55.40±0.71	26.49±0.45	8.57±1.55
JoCoR	62.29±0.71	30.19±0.60	6.84±0.92
Co-learning	66.58±0.15	55.54±0.43	35.45±0.79
Co-learning+HCR	<b>70.27±0.32</b>	<b>59.93±0.25</b>	<b>39.14±0.47</b>

CIFAR-100 with asymmetric noises.

Method	asym-20%	asym-30%	asym-40%
Standrad CE	59.36±0.36	51.06±0.44	42.49±0.23
Decoupling	57.97±0.24	49.86±0.54	41.51±0.67
Co-teaching	59.76±0.53	49.53±0.79	40.62±0.79
Co-teaching+	56.11±0.60	47.12±0.73	38.98±0.54
JoCoR	58.58±0.51	49.04±0.91	39.72±0.76
Co-learning	65.26±0.76	56.97±1.22	47.62±0.79
Co-learning+HCR	<b>68.85±0.22</b>	<b>61.94±0.17</b>	<b>50.29±0.69</b>

CIFAR-100 with instance-dependent noises.

Method	ins-20%	ins-30%	ins-40%
Standrad CE	55.45±0.54	48.77±0.47	41.30±0.27
Decoupling	52.20±0.48	45.32±0.83	36.33±0.47
Co-teaching	55.16±0.61	45.24±0.37	34.64±1.00
Co-teaching+	50.37±0.85	40.73±0.58	32.15±0.80
JoCoR	54.21±0.34	45.03±0.52	34.08±1.05
Co-learning	69.42±0.42	65.45±0.86	60.40±1.37
Co-learning+HCR	<b>70.03±0.31</b>	<b>66.89±0.41</b>	<b>62.91±0.84</b>

## Summary



- We propose hyperspherical consistency regularization (HCR), to encourage the pairwise distance distribution of the classifier to be similar to the distribution of the projection head in the latent space.
- Through extensive experiments on semi-supervised learning, fine-grained classification and noisy label learning, HCR shows consistent improvements on these tasks.