

Chapter 19: Binary Search Trees

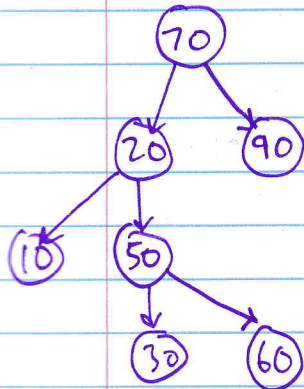
Binary Search + insertions
deletions

Find in $O(\log N)$

Basics B-tree

- must be comparable

Worst case
 $O(N)$



insert 80

- to keep sorted a LL would have to look at each place.

- 70 → 90 → left : two nodes

insert 55

- 70 → 20 → 50 → 60 → left
- not balanced

- remove 30

~~30~~

- remove 50

↑ or ↑
50 60

Big Oh

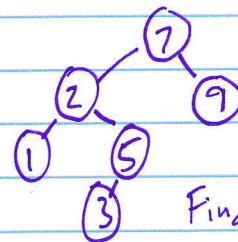
- insert
 $\log N$

- remove

$\log N$

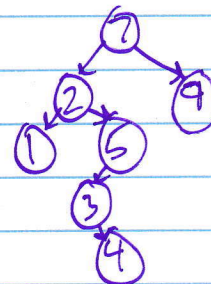
- find

$\log N$



Finding min: go down
all lefts ↓

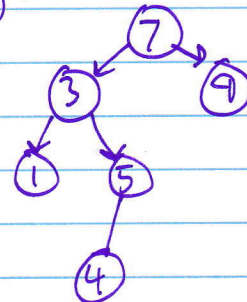
Finding max: go down
right ↓



delete 2

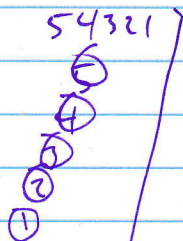
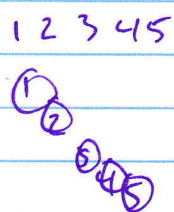
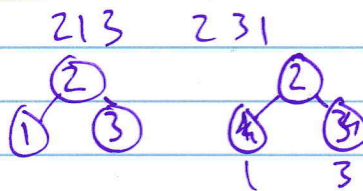
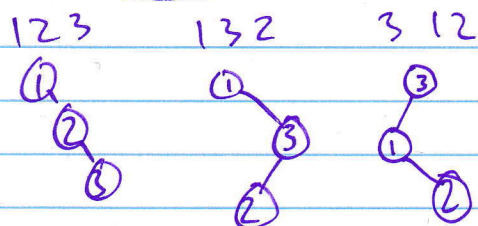
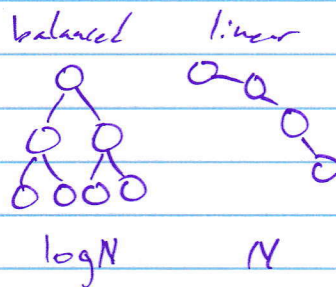
When deleting

- pick the smallest node on right
- move it to popped node



Chapter 18: Balanced vs. Unbalanced

- find the 5th element
- would be useful if each node knows # of children
- this might make it linear time
- with size or rank

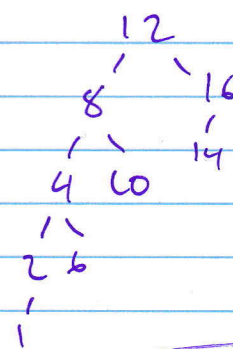
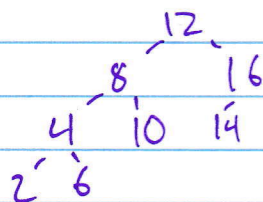


AVL Trees:

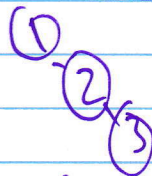
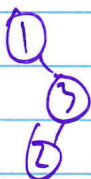
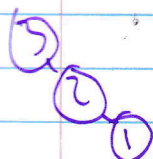
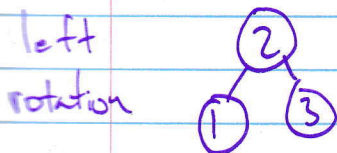
B tree with balancing, for every node the height of left & right differs by 1

is

is not

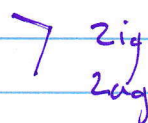
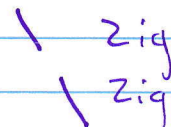


how to balance?



right

left



single rot

double rot