

Sample/practice exam 2016, questions - Class test

Theory Of Computation (Monash University)

Faculty of Information Technology Monash University

FIT2014 Theory of Computation SAMPLE MID-SEMESTER TEST

2nd Semester 2016

Working Space

Question 1 (5 marks)

A language L is called **hereditary** if it has the following property:

For every nonempty string x in L, there is a character in x which can be deleted from x to give another string in L.

 $Prove\ by\ contradiction\$ that every nonempty hereditary language contains the empty string.

Question 2 (8 marks)

In this question, we write T for True and F for False.

Let P_n be the proposition $x_1 \wedge x_2 \wedge \cdots \wedge x_n$. Note that P_1 consists just of x_1 , and P_n is equivalent to $P_{n-1} \wedge x_n$.

Prove by induction on n that, if $x_1 = F$, then P_n is False.

Question 3 (3 marks)

Write down a regular expression for the language of all binary representations of positive integers.

Your alphabet for this question is $\{0,1\}$. Leading zeros are not allowed. Do not use any signs or decimal points.

ANSWER:

Question 4 (3 marks)

Construct a Finite Automaton (FA) to recognise the language of strings consisting of an odd number of 0s followed by an even number of 1s.

(Note: zero is considered to be an even number.)

Question 5 (7 marks)

Construct a Nondeterministic Finite Automaton (NFA) to recognise the language represented by the regular expression $\,$

 $(\mathtt{aa} \cup \mathtt{b})^*\mathtt{ab}^*.$

Question 6 (4 marks)

Consider the five-state Finite Automaton represented by the following table.

state		a	Ъ
Start	1	2	3
	2	1	5
	3	1	4
Final	4	2	5
Final	5	3	5

Convert this into an equivalent FA with the minimum possible number of states. Write your answer in the following table. You may not need all the rows available.

state	a	Ъ

Working Space

END OF TEST