
vivid Documentation

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BASIC COMPONENTS

1.1 The Interval object

interval module.

class `interval.Interval` (*inf*, *sup*)

Interval class. Intervals are over natural or real values.

Variables

- **infimum** – The infimum of the interval.
- **supremum** – The supremum of the interval.
- **type** – The type of the Interval object (int, float, or long).
- **_is_Interval** – An identifier to use in place of `type` or `isinstance`.

__and__ (*other*)

Overloaded & operator; return the intersection of two Interval objects.

Raises ValueError – Intervals must overlap to take the intersection.

__contains__ (*key*)

Determine if the calling Interval contains an int, float, long, or another Interval.

Parameters key (*int|float|long|Interval*) – The value to check for membership in the calling Interval.

__deepcopy__ (*memo*)

Deepcopy an Interval object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two Interval objects are equal via the `==` operator.

__ge__ (*other*)

Overloaded `>=` operator for Interval. Determine if the calling Interval is greater than another Interval; that is, the infimum of the Interval in *other* parameter is strictly less than the calling Interval's infimum, and the supremum of the interval in *other* parameter is less than the calling Interval's supremum: (*o_{inf}*, (*s_{inf}*, *o_{sup}*), *s_{sup}*).

__getitem__ (*index*)

Retrieve the infimum or supremum of the calling Interval via indexing (e.g. `Interval[0]`).

Raises

- **IndexError** – Index must be either “0” or “1”.
- **TypeError** – Index must be an `int`.

`__gt__(other)`

Overloaded `>` operator for Interval. Determine if the calling Interval is strictly greater than another interval; that is, the infimum of the calling Interval is strictly greater than the supremum of the Interval in `other` parameter: $(o_{inf}, o_{sup})(s_{inf}, s_{sup})$.

`__hash__()`

Hash implementation for set functionality of Interval objects.

`__init__(inf, sup)`

Construct an Interval object.

Parameters

- **inf** (*int / float / long*) – The value to use as the infimum of the Interval.
- **sup** (*int / float / long*) – The value to use as the supremum of the Interval.

Raises

- **ValueError** – The infimum must be strictly less than the supremum.
- **TypeError** – The infimum and supremum provided must be ints, floats, or longs and their types must match.

`__le__(other)`

Overloaded `<=` operator for Interval. Determine if the calling Interval is less than another Interval; that is, the supremum of the calling Interval is greater than the Interval in `other`'s infimum, less than the Interval in `other`'s supremum and the infimum of the calling Interval is strictly less than the infimum of the Interval in `other` parameter: $(s_{inf}, (o_{inf}, s_{sup}), o_{sup})$.

`__lt__(other)`

Overloaded `<` operator for Interval. Determine if the calling Interval is strictly less than another interval; that is, the supremum of the calling Interval is strictly less than the infimum of the Interval in `other` parameter: $(s_{inf}, s_{sup})(o_{inf}, o_{sup})$.

`__ne__(other)`

Determine if two Interval objects are not equal via the `!=` operator.

`__or__(other)`

Overloaded `|` operator; return the union of two Interval objects.

Raises ValueError – Intervals must overlap to take the union.

`__repr__()`

Return a string representation of the Interval object.

`__str__()`

Return a readable string representation of the Interval object.

`_key()`

Private key function for hashing.

Returns 2-tuple consisting of (infimum, supremum).

Return type tuple

static collapse_intervals (*intervals*)

Collapse a list of overlapping intervals.

Parameters intervals (*list*) – A list of intervals to collapse.

Returns A new list of totally disjoint, collapsed Intervals.

Return type list

Raises **TypeError** – interval parameter must be a list containing only Interval objects.

discretize (*jump=None*)

Return all values within the range of the calling interval.

Parameters **jump** (*None/int/float/long*) – The jump to use after each value. Defaults to 1, 1.0 and 1 for int, float, and long Intervals respectively.

Returns A list of discrete values contained in the calling Interval with a step size of *jump*.

Return type list

Raises **TypeError** – If a jump is provided, it must be an int, float, or long and match the type of the calling Interval.

1.2 The Point object

point module.

class `point.Point` (**coordinates*)

Point class. Point objects represent a point of N_d cartesian space. Point objects are immutable.

Variables

- **is_generic** – Whether or not the Point object is generic (i.e., the coordinates have not been defined).
- **coordinate** – The coordinate of the Point object.
- **dimension** – The dimension of space the Point object exists in.
- **_is_Point** – An identifier to use in place of `type` or `isinstance`.

__deepcopy__ (*memo*)

Deepcopy a Point object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two Point objects are equal via the `==` operator.

__getitem__ (*key*)

Retrieve the *i*th coordinate from a Point object via indexing (e.g., `Point[i]`).

Raises

- **TypeError** – key parameter must be an int.
- **IndexError** – key parameter must be within the set $\{0, \dots, d\}$ where *d* is the dimension of the Point object.

__hash__ ()

Hash implementation for set functionality of Point objects.

__init__ (**coordinates*)

Construct a Point object.

Parameters **coordinates** (*strs/floats*) – The values to use as the coordinates of the Point object. At least one coordinate must be provided; to create a generic point object, pass values of "x".

Raises

- **ValueError** – At least one coordinate must be provided.
- **TypeError** – All coordinates must be either strings (equal to "x") or floats.

`__ne__(other)`

Determine if two Point objects are not equal via the `!=` operator.

`__repr__()`

Return a string representation of the Point object.

`__str__()`

Return a readable string representation of the Point object.

`_key()`

Private key function for hashing.

Returns *d*-tuple consisting of coordinates.

Return type `tuple`

`can_observe(spacetime_loc, worldline_start, worldline_end)`

Determine if the calling Point object can observe the spacetime location represented by the Point object in `spacetime_loc` parameter on the worldline segment determined by the Point objects in `worldline_start` and `worldline_end` parameters.

Returns Whether or not the calling Point object can observe `spacetime_loc` through the worldline defined by the Point objects in the `worldline_start` and `worldline_end` parameters.

Return type `bool`

`clocks_unequal(other)`

Determine if the clocks of two spacetime locations are unequal wherein the last coordinate of each represents time.

Returns Whether or not the calling Point object's last coordinate is equal to the last coordinate of the Point object in `other` parameter.

Return type `bool`

Raises **ValueError** – Dimensions of the Point object contained in `other` parameter and the calling Point must match.

`is_on(endpoint_1, endpoint_2)`

Determine if the calling Point object lies on line segment defined by the endpoint Point objects provided in the `endpoint_1` and `endpoint_2` parameters.

Raises **ValueError** – The calling Point object and the Point objects in the `endpoint_1` and `endpoint_2` parameters must all be in the same dimension of space and no Point object involved can be generic.

Returns Whether or not the calling Point object lies on the line segment.

Return type `bool`

`meets(worldline_1_start, worldline_1_end, worldline_2_start, worldline_2_end)`

Determine if the worldline segments defined by the Point objects in the `worldline_1_start` and `worldline_1_end` parameters and the `worldline_2_start` and `worldline_2_end` parameters meet at the calling Point object's coordinates.

Returns Whether or not worldlines meet at the calling Point object's coordinates.

Return type `bool`

Raises **ValueError** – All Point objects must have the same dimension and cannot be generic.

`not_same_point(other)`

Determine if the calling Point object and the Point object contained in `other` parameter are not the same.

Returns Whether or not the calling Point object is unequal to the Point object in other parameter.

Return type `bool`

static unstringify (*point_string*)

Reconstruct a Point object from its string representation.

Returns Point object reconstructed from string representation.

Return type *Point*

Raises ValueError – The string must match the form given by `str(Point)` or `repr(Point)`, i.e., $P(c_1, \dots, c_d)$.

1.3 The LineSegment object

line module.

class `line_segment.LineSegment` (*start_point, end_point*)

LineSegment class. Each LineSegment object represents a line segment in N_d cartesian space. LineSegment objects are immutable.

Variables

- **is_generic** – Whether or not the LineSegment object is generic (i.e., the set of coordinates have not been defined).
- **start_point** – The first endpoint of the LineSegment.
- **end_point** – The second endpoint of the LineSegment.
- **dimension** – The dimension of space the LineSegment object exists in.
- **_is_LineSegment** – An identifier to use in place of `type` or `isinstance`.

__contains__ (*key*)

Determine if a Point object or LineSegment object given in the *key* parameter is on the calling LineSegment object via the `in` operator.

Parameters *key* (*Point* | *LineSegment*) – The Point or LineSegment to check for membership in the calling LineSegment.

Raises TypeError – *key* parameter must be a Point or LineSegment object.

__deepcopy__ (*memo*)

Deepcopy a LineSegment object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two LineSegment objects are equal via the `==` operator.

__ge__ (*other*)

Overloaded `>=` operator for LineSegment object. Determine if the calling LineSegment object is a superset of the LineSegment object contained in *other* parameter where we view both LineSegment as a set of possible Point objects.

__getitem__ (*key*)

Retrieve the *i*th endpoint from a LineSegment object via indexing (e.g., `LineSegment[i]`).

Raises

- **TypeError** – *key* parameter must be an `int`.

- **IndexError** – key parameter must be either 0 or 1.

__gt__ (*other*)

Overloaded > operator for LineSegment object. Determine if the calling LineSegment object is a strict superset of the LineSegment object contained in *other* parameter where we view both LineSegment as a set of possible Point objects.

__hash__ ()

Hash implementation for set functionality of LineSegment objects.

__init__ (*start_point*, *end_point*)

Construct a LineSegment object.

Parameters

- **start_point** (Point) – The starting point of the LineSegment object.
- **end_point** (Point) – The end point of the LineSegment object.

Raises ValueError – both *start_point* and *end_point* parameters must be Point objects, agree on their gnerality, share the same dimension and be unequal.

__le__ (*other*)

Overloaded <= operator for LineSegment object. Determine if the calling LineSegment object is a subset of the LineSegment object contained in *other* parameter where we view both LineSegment as a set of possible Point objects.

__lt__ (*other*)

Overloaded < operator for LineSegment object. Determine if the calling LineSegment object is a strict subset of the LineSegment object contained in *other* parameter where we view both LineSegment as a set of possible Point objects.

__ne__ (*other*)

Determine if two LineSegment objects are not equal via the != operator.

__repr__ ()

Return a string representation of the LineSegment object.

__str__ ()

Return a readable string representation of the LineSegment object.

_key ()

Private key function for hashing.

Returns 2-tuple consisting of Point objects.

Return type tuple

static meets (*point*, *line_1*, *line_2*)

Determine if LineSegment objects given by the *line_1* and *line_2* parameters meet at the Point object given by *point* parameter.

Parameters

- **point** (Point) – The potential intersection point of the two LineSegment objects.
- **line_1** (LineSegment) – The first LineSegment of the possible intersecting pair of line segments.
- **line_2** (LineSegment) – The second LineSegment of the possible intersecting pair of line segments.

static unstringify (*line_segment_string*)

Reconstruct a LineSegment object from its string representation.

Returns LineSegment object reconstructed from string representation.

Return type *LineSegment*

Raises **ValueError** – The string must match the form given by `str(LineSegment)` or `repr(LineSegment)`.

1.4 The ValueSet object

valueset module.

Supports any object provided they implement `__deepcopy__`, `__eq__`, `__str__`, `__hash__`, and provide a parser for truth value evaluation. Additionally, `__le__` in ValueSet class must be extended to support the object if the object uses a non-standard form of equality, (e.g. Point objects are subset of generic Point of same dimension).

class `valueset.ValueSet` (*valueset*)
ValueSet class.

The ValueSet class uses the `total_ordering` decorator so strict subsets, supersets and strict supersets are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **`_base_types`** – The literal types supported by the ValueSet class.
- **`_object_types`** – The object types supported by the ValueSet class.
- **`values`** – The values contained in the ValueSet object.
- **`_is_ValueSet`** – An identifier to use in place of `type` or `isinstance`.

`__add__` (*other*)

Overloaded `+` operator for ValueSet. Take the union of two ValueSet objects or add a single element to the calling Valueset object. If adding an object, the object must be within `_object_types`.

`__contains__` (*key*)

Overloaded `in` operator for ValueSet. Determine if a value is contained in the calling ValueSet object.

Parameters **key** – The item to test for membership in the calling ValueSet object.

`__deepcopy__` (*memo*)

Deepcopy a ValueSet object via the `copy.deepcopy` method.

`__eq__` (*other*)

Determine if two ValueSet objects are equal via the `==` operator.

`__getitem__` (*key*)

Retrive the value located at the index given by `key` parameter via indexing (e.g. `ValueSet[key]`).

Parameters **key** (*int*) – The index to use for retrieval.

Raises

- **IndexError** – `key` index must be in $\{0, \dots, n - 1\}$ where n is the number of values contained in the calling ValueSet object.
- **TypeError** – `key` must be an int.

`__iadd__` (*other*)

Overloaded `+=` operator for ValueSet. Take the union of two ValueSet objects or add a single element to the calling Valueset object. If adding an object, the object must be within `_object_types`.

`__init__` (*valueset*)

Construct a ValueSet object.

Parameters **valueset** (*list/set*) – The values to place in the ValueSet object. These values are passed through the `_parse` function before being stored.

Raises **TypeError** – valueset parameter must be a list or set.

`__iter__` ()

Provide an iterator for ValueSet objects (e.g. “for value in ValueSet:”).

`__le__` (*other*)

Overloaded `<=` operator for ValueSet object. Determine if the calling ValueSet object is a subset of the ValueSet object contained in *other* parameter.

`__len__` ()

Determine the length of a ValueSet object via the `len` built-in function e.g.(`len(ValueSet)`).

`__ne__` (*other*)

Determine if two ValueSet objects are not equal via the `!=` operator.

`__nonzero__` ()

Determine if a ValueSet object is falsy (e.g. `if ValueSet` or `if not ValueSet`).

`__repr__` ()

Return a string representation of the ValueSet object.

`__setitem__` (*key, value*)

Assign a value in *value* parameter to a ValueSet object at the index given by *key* parameter (e.g. `ValueSet[key] = value`).

Parameters

- **key** (*int*) – The index to use for assignment.
- **value** – The value to assign at index given by *key*.

Raises

- **AttributeError** – An invalid/unsupported object is given as *value* parameter.
- **IndexError** – *key* index must be in $\{0, \dots, n - 1\}$ where *n* is the number of values contained in the ValueSet object.
- **TypeError** – *key* must be an `int` and *value* in *value* parameter must be in `ValueSet._base_types` or `ValueSet._object_types`.
- **ValueError** – Duplicate values are not allowed in a ValueSet object.

`__str__` ()

Return a readable string representation of the ValueSet object.

`__sub__` (*other*)

Overloaded `-` operator for ValueSet. The `-` operator functions as the set-theoretic difference.

static **`_parse`** (*values*)

Parse a *list* into the standard format used by ValueSet objects. Any `ints`, `longs`, and `floats` are absorbed into an `Interval` object if they are contained by that `Interval` and the base types contained in *values* are sorted.

Returns Filtered, sorted values in the ValueSet standard format.

Return type `list`

Raises **TypeError** – *values* parameter must be either a `list` or `set`.

static `_split_by_types` (*values*)

Split an iterable object by the types of elements within it and return a defaultdict where keys are the types composing the iterable object and the values are lists of the values of the iterable object falling into those types.

Parameters **values** (*list/set/ValueSet/...*) – An iterable object to split.

Returns A defaultdict of lists where keys correspond to `ValueSet._base_type` and `ValueSet._object_types` present in **values** parameter.

Return type `defaultdict(list)`

Raises

- **AttributeError** – Only objects containing a single identifier in `_object_types` are supported.
- **TypeError** – An invalid type exists in the iterable object.

classmethod `add_object_type` (*object_identifier*)

Add compatibility for an object to the `ValueSet` class. This is part of the vivid object extension protocol.

Parameters **object_identifier** (*str*) – The identifier used by each instance of the new class. This must be of the form: `"_is_Object"` (e.g. `"_is_Point"` or `"_is_Interval"`).

ATTRIBUTES AND RELATIONS

2.1 The Attribute object

attribute module.

class `attribute.Attribute` (*label*, *value_set*)

Attribute Class. An Attribute is a finite set A with an associated label l .

Variables

- **label** – The associated label l of the Attribute A .
- **value_set** – A ValueSet object functioning as the set of values that the attribute can take on (e.g {small,large}).
- **_is_Attribute** – An identifier to use in place of `type` or `isinstance`.

__add__ (*other*)

Combine an Attribute object with another Attribute object, a Relation object, an AttributeStructure object or an AttributeSystem object via the `+` operator.

Parameters *other* (*Attribute/Relation/AttributeStructure/AttributeSystem*)

– The object to combine with the Attribute. If an Attribute, Relation, or AttributeStructure object is provided, an AttributeStructure object is returned; if an AttributeSystem object is provided, an AttributeSystem object is returned.

Raises **TypeError** – *other* parameter must be an Attribute, Relation, AttributeStructure, or AttributeSystem object.

__deepcopy__ (*memo*)

Deepcopy an Attribute object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two Attribute objects are equal via the `==` operator.

__hash__ ()

Hash implementation for set functionality of Attribute objects.

__init__ (*label*, *value_set*)

Construct an Attribute object.

Parameters

- **label** (*str*) – The label l to associate with the Attribute object.
- **value_set** (*list/ValueSet*) – The set of values the Attribute object can take on.

Raises **TypeError** – *label* parameter must be a string and *value_set* parameter must be either a ValueSet object or a list.

__ne__(*other*)
Determine if two Attribute objects are not equal via the != operator.

__repr__()
Return a string representation of the Attribute object.

__str__()
Return a readable string representation of the Attribute object.

_key()
Private key function for hashing.

Returns 2-tuple consisting of (label, valueset)

Return type tuple

2.2 The Relation object

relation module.

class `relation.Relation`(*definition, D_of_r, subscript*)
Relation class. Relation objects represent logical relations used in AttributeStructure objects.

Variables

- **definition** – A string representation of the Relation object’s definition with form $R_n(a, \dots) \Leftarrow \dots$ where n is a positive integer; whitespace is ignored.
- **DR** – DR represents $D(R) \subseteq \{A_1, \dots, A_n\}$; held as a list of strings corresponding to the labels of some set of Attributes objects; no assumptions are made on the labels of the attributes.
- **subscript** – The subscript of the relation.
- **_is_Relation** – An identifier to use in place of `type` or `isinstance`.

__add__(*other*)
Combine a Relation object with an Attribute object, an AttributeStructure object or an AttributeSystem object via the + operator.

Parameters *other* (*Attribute/AttributeStructure/AttributeSystem*) – The object to combine with the Attribute. If an Attribute or AttributeStructure object is provided, an AttributeStructure object is returned; if an AttributeSystem object is provided, an AttributeSystem is returned.

Raises **TypeError** – *other* parameter must be an Attribute, AttributeStructure, or AttributeSystem object.

__deepcopy__(*memo*)
Deepcopy a Relation object via the `copy.deepcopy` method.

__eq__(*other*)
Determine if two Relation objects are equal via the == operator.

__init__(*definition, D_of_r, subscript*)
Construct a Relation object.

Parameters

- **definition** (*str*) – The definition of the logical relation; valid definitions have the form: $R_n(a, \dots) \Leftarrow \dots$ where all whitespace is ignored.

- **D_of_r** (*list*) – A list of strings representing $D(R) \subseteq \{A_1, \dots, A_n\}$.
- **subscript** (*int*) – The subscript of the relation; must match subscript in definition.

Raises

- **TypeError** – definition parameter must be a str, D_of_r parameter must be a list containing only strs and subscript parameter must be an int.
- **ValueError** – definition parameter must be correctly formatted, the number of parameters provided in definition must match the length of D_of_r and subscript parameter must match subscript provided in definition parameter.

__ne__ (*other*)

Determine if two Relation objects are not equal via the != operator.

__repr__ ()

Return a string representation of the Relation object.

__str__ ()

Return a readable string representation of the Relation object.

get_DR (*string=False*)

Return $D(R)$ of the calling Relation object. If *string* parameter is set to True, return a str representation of $D(R)$.

Parameters *string* (*boolean*) – A boolean value for whether or not to return a string representation of $D(R)$.

Returns A representation of $D(R)$.

Return type str|list

get_arity ()

Return the arity of the calling Relation object.

Returns The length of $D(R)$.

Return type int

static is_valid_definition (*definition*)

Determine if a given definition in *definition* parameter is valid. A definition is valid when it is of the form $R_s(x_1, \dots, x_n) \Leftrightarrow \langle \text{expression} \rangle$.

The important thing here is the left hand side and the marker " \Leftrightarrow ". Everything on the right hand side of " \Leftrightarrow " is ignored as far as the definition's validity is concerned; whether or not it is evaluatable is left to `Formula.assign_truth_value()` as it is only during the assignment of a truth value that the expression comes into play. All whitespace is trimmed immediately so arbitrary spacing is allowed.

Parameters *definition* (*str*) – The definition to verify.

Returns Whether or not *definition* is valid.

Return type bool

set_DR (*DR*)

Set $D(R)$ to DR parameter.

Parameters *DR* (*list*) – The list of strings to set the calling Relation object's $D(R)$ to.

Raises

- **TypeError** – $D(R)$ is not a list of strs.
- **ValueError** – The cardinality of $D(R)$ must match argument cardinality in Relation object's definition member.

set_definition (*definition*)

Set the definition of the Relation object to *definition* parameter after ensuring that it conforms to required format.

Parameters *definition* (*str*) – The new definition of the Relation object.

Raises

- **TypeError** – *definition* parameter must be a `str`.
- **ValueError** – *definition* must conform to valid definition rules.

ATTRIBUTE STRUCTURES

3.1 The AttributeStructure object

attribute_structure module.

class attribute_structure.**AttributeStructure**(*args)

AttributeStructure class. An AttributeStructure object consists of a finite set of Attribute objects A_1, \dots, A_k ; and a countable collection \mathcal{R} of computable Relation objects with $D(R) \subseteq \{A_1, \dots, A_k\}$ for each $R \in \mathcal{R}$. i.e.,

$$\mathcal{A} = (\{A_1, \dots, A_k\}; \mathcal{R})$$

The AttributeStructure class uses the `total_ordering` decorator so strict subsets, supersets and strict supersets are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **attributes** – A list of Attribute objects (i.e., A_1, \dots, A_k); always maintained as a list.
- **relations** – A dictionary of relations (i.e., \mathcal{R}).
- **_is_AttributeStructure** – An identifier to use in place of `type` or `isinstance`.

__add__(other)

Add an Attribute, Relation, AttributeStructure, or AttributeSystem object via the `+` operator.

Parameters **other** (Attribute/Relation/AttributeStructure/AttributeSystem)

– The object to combine with the AttributeStructure. If an Attribute, Relation, or AttributeStructure object is provided, an AttributeStructure object is returned; if an AttributeSystem object is provided, an AttributeSystem object is returned.

Raises

- **TypeError** – `other` parameter must be an Attribute, Relation, AttributeStructure, or AttributeSystem object.
- **ValueError** – Duplicate Attribute labels are not permitted, duplicate subscripts are not permitted and every Relation's $D(R)$ must be a subset of Attribute labels in the AttributeStructure.

__contains__(key)

Determine if Attribute, Relation, Attribute corresponding to a label in the `key` parameter, or Relation corresponding to a subscript in the `key` parameter is contained by AttributeStructure via `in` operator.

Parameters **key** (Attribute/Relation/str/int) – The key to use when checking for membership.

Raises **TypeError** – `key` must be an Attribute object, Relation object, `str`, or `int`.

`__deepcopy__ (memo)`

Deepcopy an AttributeStructure object via the `copy.deepcopy` method.

`__eq__ (other)`

Determine if two AttributeStructure objects are equal via the `==` operator.

`__getitem__ (key)`

Retrieve a reference to the Attribute object or Relation object in the AttributeStructure via the key provided in the `key` parameter provided.

Parameters `key` (*Attribute/Relation/str/int*) – The Attribute object, Relation object, label, or subscript to use when attempting to find the corresponding Attribute object or Relation object.

Raises

- **KeyError** – Attribute object or Relation object provided in the `key` parameter not found in the AttributeStructure, no Attribute object with label provided in the `key` parameter found in the AttributeStructure, or no Relation object with subscript provided in the `key` parameter found in the AttributeStructure.
- **TypeError** – `key` is not an Attribute object, Relation object, `int`, or `str`.

`__iadd__ (other)`

AAAdd an Attribute, Relation, AttributeStructure, or AttributeSystem object via the `+=` operator.

Parameters `other` (*Attribute/Relation/AttributeStructure/AttributeSystem*) – The object to combine with the AttributeStructure. If an Attribute, Relation, or AttributeStructure object is provided, an AttributeStructure object is returned; if an AttributeSystem object is provided, an AttributeSystem object is returned.

Raises

- **TypeError** – `other` parameter must be an Attribute, Relation, AttributeStructure, or AttributeSystem object.
- **ValueError** – Duplicate Attribute labels are not permitted, duplicate subscripts are not permitted and every Relation's $D(R)$ must be a subset of Attribute labels in the AttributeStructure.

`__init__ (*args)`

Construct an AttributeStructure object.

Parameters `args` (*Attribute/Relation*) – Any amount of Attribute and Relation objects.

Raises

- **TypeError** – all optional positional arguments provided must be Attribute or Relation objects.
- **ValueError** – Duplicate Attribute labels are not permitted, Duplicate Relation subscripts are not permitted, and each Relation object's $D(R)$ must be a subset of the cartesian product of some combination of the labels of the Attributes provided.

`__isub__ (other)`

Remove Attribute's or Relation's via `-` operator. If an AttributeStructure object is provided, all Attribute objects and Relation objects within that AttributeStructure object will be removed from the calling AttributeStructure.

Parameters `other` (*Attribute/Relation/AttributeStructure*) – The Attribute, Relation, or AttributeStructure object to remove.

Raises

- **KeyError** – Invalid Attribute or Relation object provided in `other` parameter.
- **TypeError** – Only Attribute, Relation, or AttributeStructure objects can be removed.
- **ValueError** – Some Attribute or Relation object provided in AttributeStructure object in `other` parameter not found in calling AttributeStructure object or some Relation object's $D(R)$ is invalid after an Attribute object is removed.

__le__ (*other*)

Overloaded `<=` operator. Determine if the calling AttributeStructure object is a subset of the AttributeStructure object contained in `other` parameter.

__ne__ (*other*)

Determine if two AttributeStructure objects are not equal via the `!=` operator.

__repr__ ()

Return a string representation of the AttributeStructure object.

__str__ ()

Return a readable string representation of the AttributeStructure object.

__sub__ (*other*)

Remove Attribute's or Relation's via `-` operator. If an AttributeStructure object is provided, all Attribute objects and Relation objects within that AttributeStructure object will be removed from the calling AttributeStructure.

Parameters *other* (*Attribute/Relation/AttributeStructure*) – The Attribute, Relation, or AttributeStructure object to remove.

Raises

- **KeyError** – Invalid Attribute or Relation object provided in `other` parameter.
- **TypeError** – Only Attribute, Relation, or AttributeStructure objects can be removed.
- **ValueError** – Some Attribute or Relation object provided in AttributeStructure object in `other` parameter not found in calling AttributeStructure object or some Relation object's $D(R)$ is invalid after an Attribute object is removed.

get_cardinality ()

Return the cardinality of the calling AttributeStructure object.

Returns The cardinality of the AttributeStructure object, i.e., the amount of Attribute objects contained therein.

Return type `int`

get_labels ()

Return the labels of the Attribute objects within the calling AttributeStructure object.

Returns A list of the labels of the Attribute objects in the calling AttributeStructure object.

Return type `list`

get_subscripts ()

Return the subscripts of the Relation objects within the calling AttributeStructure object.

Returns A list of the subscripts of the Relation objects in this AttributeStructure object.

Return type `list`

ATTRIBUTE SYSTEMS

4.1 The AttributeSystem object

attribute_system module.

class attribute_system.**AttributeSystem**(*attribute_structure, objects*)

AttributeSystem class. An AttributeSystem object, based on the AttributeStructure object \mathcal{A} is a pair

$$\mathcal{S} = (\{s_1, \dots, s_n\}; \mathcal{A})$$

consisting of a finite number $n > 0$ of objects s_1, \dots, s_n (represented as `strs`) and \mathcal{A} .

The AttributeSystem class uses the `total_ordering` decorator so strict subsets, supersets and strict supersets are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **attribute_structure** – The AttributeStructure of the AttributeSystem.
- **objects** – The objects of the AttributeSystem; held as a list of `strs`.
- **_is_AttributeSystem** – An identifier to use in place of `type` or `isinstance`.

__add__(*other*)

Add an Attribute, Relation, AttributeStructure, or AttributeSystem object via the `+` operator.

Parameters *other* (*Attribute/Relation/AttributeStructure/AttributeSystem*)

– The object to combine with the AttributeSystem. An AttributeSystem object is always returned regardless of the type of *other* parameter.

Raises

- **TypeError** – *other* parameter must be an Attribute, Relation, AttributeStructure, or AttributeSystem object.
- **ValueError** – Cannot add AttributeSystems with overlapping objects.

__contains__(*key*)

Determine if the Attribute object, Relation object, AttributeStructure object, or `str` in the *key* parameter is contained by the calling AttributeSystem object via `in` operator.

Parameters *key* (*Attribute/Relation/AttributeStructure/str*) – The key to use when checking for membership.

Raises **TypeError** – *key* parameter must be an Attribute object, Relation object, AttributeStructure object, or `str`.

__deepcopy__(*memo*)

Deepcopy an AttributeSystem object via the `copy.deepcopy` method.

`__eq__` (*other*)

Determine if two `AttributeSystem` objects are equal via `==` operator.

`__getitem__` (*key*)

Retrieve a reference to the `Attribute`, `Relation`, or object in the `AttributeSystem` by indexing with the key provided in `key` parameter (e.g., `"AttributeSystem[key]"`).

Parameters `key` (*Attribute/Relation/str*) – The `Attribute`, `Relation` or name of the object to get the reference of from the calling `AttributeSystem` object.

Raises **`TypeError`** – `str` in `key` does not match any object contained in the calling `AttributeSystem` object.

`__iadd__` (*other*)

Add an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object via the `+=` operator.

Parameters `other` (*Attribute/Relation/AttributeStructure/AttributeSystem*) – The object to combine with the `AttributeSystem`. An `AttributeSystem` object is always returned regardless of the type of `other` parameter.

Raises

- **`TypeError`** – `other` parameter must be an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object.
- **`ValueError`** – Cannot add `AttributeSystems` with overlapping objects.

`__init__` (*attribute_structure, objects*)

Construct `AttributeSystem` object.

Parameters

- **`attribute_structure`** (*AttributeStructure*) – an `AttributeStructure` object to use as the attribute structure \mathcal{A} of the `AttributeSystem` object.
- **`objects`** (*list*) – A list of `str`s denoting the objects of the `AttributeSystem`.

Raises

- **`TypeError`** – `objects` parameter must be a list and `attribute_structure` parameter must be an `AttributeStructure` object.
- **`ValueError`** – all objects provided in `objects` parameter must be unique non-empty `str`s.

`__isub__` (*other*)

Remove an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object via the `-=` operator. In the case of `AttributeStructure` and `AttributeSystem` objects being provided to `other` parameter, remove all of their constituent parts from the calling `AttributeSystem`.

Parameters `other` (*Attribute/Relation/AttributeStructure/AttributeSystem*) – The object to remove from the `AttributeSystem`. An `AttributeSystem` object is always returned regardless of the type of `other` parameter.

Raises

- **`TypeError`** – `other` parameter must be an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object.
- **`ValueError`** – Cannot remove objects not present in this `AttributeSystem`.

`__le__` (*other*)

Determine if the calling `AttributeSystem` object is a subset of the `AttributeSystem` object contained in the `other` parameter via `<=` operator.

`__ne__(other)`

Determine if two `AttributeSystem` objects are not equal via `!=` operator.

`__repr__()`

Return a string representation of the `AttributeSystem` object.

`__str__()`

Return a readable string representation of the `AttributeSystem` object.

`__sub__(other)`

Remove an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object via the `-` operator. In the case of `AttributeStructure` and `AttributeSystem` objects being provided to `other` parameter, remove all of their constituent parts from the calling `AttributeSystem`.

Parameters `other` (*Attribute/Relation/AttributeStructure/AttributeSystem*)

– The object to remove from the `AttributeSystem`. An `AttributeSystem` object is always returned regardless of the type of `other` parameter.

Raises

- **TypeError** – `other` parameter must be an `Attribute`, `Relation`, `AttributeStructure`, or `AttributeSystem` object.
- **ValueError** – Cannot remove objects not present in this `AttributeSystem`.

`get_power()`

Get the power of the calling `AttributeSystem` object, i.e., $n \cdot |\mathcal{A}|$.

Returns The power of the calling `AttributeSystem` object: $n \cdot |\mathcal{A}|$

Return type `int`

`is_automorphic()`

Determine if the calling `AttributeSystem` object is automorphic.

Returns Whether or not the calling `AttributeSystem` object is automorphic; i.e., some (perhaps all) of the objects s_1, \dots, s_n are contained by at least one of the `ValueSets` of the `Attribute` objects of the underlying `AttributeStructure` object \mathcal{A} .

Return type `bool`

5.1 The State object

state module.

class `state.State` (*attribute_system*, *ascriptions*={})

State class. Each State object is a state of an AttributeSystem; that is a set of functions $\sigma = \{\delta_1, \dots, \delta_k\}$, where each δ_i is a function from $\{s_1, \dots, s_n\}$ to the set of all non-empty finite subsets of A_i , i.e.,

$$\delta_i : \{s_1, \dots, s_n\} \rightarrow \mathcal{P}_{fin}(A_i) \setminus \emptyset.$$

The State class uses the `total_ordering` decorator so proper extensions, contravariant extensions and contravariant proper extensions are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **attribute_system** – A copy of the AttributeSystem object \mathcal{S} that the State object comes from.
- **ascriptions** – The ascriptions of the state (i.e., the set of attribute-object pairs and their corresponding ValueSet objects) δ_i , $i = 1, \dots, k$.
- **_is_State** – An identifier to use in place of `type` or `isinstance`.

__deepcopy__ (*memo*)

Deepcopy a State object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two State objects are equal via the `==` operator.

__getitem__ (*key*)

Retrieve the ascription δ_i or ascription of a particular object $\delta_i(s_j)$ (that is, the ValueSet corresponding to the attribute-object pair) given by *key* parameter via indexing (e.g. `State[key]`).

Raises

- **KeyError** – *key* parameter must be a valid Attribute label or valid attribute-object pair in the underlying AttributeSystem \mathcal{S} of the State object.
- **TypeError** – *key* parameter must be a `str` or `tuple` containing only `str`s.

__init__ (*attribute_system*, *ascriptions*={})

Construct a State object.

Parameters

- **attribute_system** (`AttributeSystem`) – The AttributeSystem object \mathcal{S} from which the State comes from.

- **ascriptions** (dict) – An optional dictionary of attribute-object pairs $\delta_i(s_j)$ to use as ascriptions; if some attribute-object pair is not provided, the full ValueSet of the Attribute object corresponding to the attribute label in the attribute-object pair is used.

Raises **TypeError** – `attribute_system` parameter must be an `AttributeSystem` object and `ascriptions` parameter must be a dict.

__le__ (*other*)

Overloaded `<=` operator for `State`; Determine if the calling `State` object is an extension of the `State` object in *other* parameter.

Raises

- **TypeError** – *other* parameter must be a `State` object.
- **ValueError** – The state object in the *other* parameter must share the same underlying `AttributeSystem` object \mathcal{S} as the calling `State` object.

__ne__ (*other*)

Determine if two `State` objects are not equal via the `!=` operator.

__repr__ ()

Return a string representation of the `State` object.

__str__ ()

Return a readable string representation of the `State` object.

add_object (*obj*, *ascriptions=None*)

Add an object s' to the calling `State` object's underlying `AttributeSystem` \mathcal{S} and optionally update any ascriptions of the new object $\delta_i(s')$ provided.

Parameters

- **obj** (str) – The new object s' to add to the `State`.
- **ascriptions** (dict) – The optional ValueSets to assign to the attribute-object pairs corresponding to the new object $\delta_i(s')$.

Raises

- **TypeError** – *obj* parameter must be a non-empty str and if *ascriptions* parameter is provided, it must be a dict.
- **ValueError** – Duplicate objects cannot be added and all ascriptions provided must be from an existing label of an Attribute object in the underlying `AttributeSystem` object \mathcal{S} to s' .

get_alterate_extensions (**states*)

Return all alternate extensions of the calling `State` object with respect to `State` objects $\sigma_1, \dots, \sigma_m$ provided by optional positional arguments of *states* parameter, i.e., generate $\mathbf{AE}(\{\sigma_1, \dots, \sigma_m\}, \sigma')$.

Parameters **states** (State) – The states $\{\sigma_1, \dots, \sigma_m\}$ to use for the derivation of the alternate extensions of the calling `State` object.

Returns $\mathbf{AE}(\{\sigma_1, \dots, \sigma_m\}, \sigma')$.

Return type list

Raises

- **TypeError** – all optional positional arguments must be `State` objects.
- **ValueError** – at least one `State` object must be provided in optional positional arguments and all provided `State` objects must be proper extensions of the calling `State` object.

get_worlds()

Return a list of all possible worlds $(w; \hat{\rho})$ derivable from the calling State object.

Returns all worlds $(w; \hat{\rho})$ derivable from this State object.

Return type list

is_alternate_extension(s_prime, *states)

Determine if the State object in `s_prime` parameter is an alternate extension of the calling State object w.r.t. the State objects $\sigma_1, \dots, \sigma_m$ provided by optional positional arguments of `states` parameter, i.e., evaluate $Alt(\sigma, \{\sigma_1, \dots, \sigma_m\}, \sigma')$.

Parameters

- **s_prime** (State) – The State object to verify as the alternate extension, σ'
- **states** (State) – The states $\{\sigma_1, \dots, \sigma_m\}$ to use for the derivation of the alternate extensions of the calling State object.

Returns The result of the evaluate of $Alt(\sigma, \{\sigma_1, \dots, \sigma_m\}, \sigma')$.

Return type bool

Raises **TypeError** – `s_prime` parameter must be a State object.

is_disjoint(other)

Determine if the calling State object is disjoint from the State object in the `other` parameter.

Returns Whether or not the calling State object and State object contained in the `other` parameter are disjoint.

Return type bool

is_valuation(label)

Determine if the ascription δ_i corresponding to the `label` parameter is a valuation in the calling State object; that is $|\delta_i(s_j)| = 1$ for every $j = 1, \dots, n$.

Parameters **label** (str) – The label corresponding to the ascription δ_i to check for valuation in the calling State object.

Returns Whether or not the ascription δ_i corresponding to `label` is a valuation in the calling State object.

Return type bool

is_world()

Determine if the calling State object σ is a world; that is every ascription δ_i of σ is a valuation.

Returns Whether or not the calling State object is a world.

Return type bool

static join(s1, s2)

Join two State objects if possible, i.e., return $\sigma_1 \sqcup \sigma_2$.

Parameters

- **s1** (State) – The left operand σ_1 to use for the join operation.
- **s2** (State) – The right operand σ_2 to use for the join operation.

Raises **ValueError** – `s1` and `s2` parameters must share the same underlying AttributeSystem \mathcal{S} .

set_ascription (*ao_pair*, *new_valueset*)

Set an ascription of an object (that is, $\delta_i(s_j)$) in the calling State object, given by the *ao_pair* parameter, to the ValueSet object provided in the *new_valueset* parameter.

Parameters

- **ao_pair** (tuple) – The attribute-object pair $\delta_i(s_j)$ to use as a key for the ascription dict member in the calling State object.
- **new_valueset** (ValueSet) – The new ValueSet object to assign to the corresponding attribute-object pair $\delta_i(s_j)$ given by the *ao_pair* parameter.

Raises

- **TypeError** – *ao_pair* parameter must be a tuple and *new_valueset* parameter must be a list, set, or ValueSet object.
- **ValueError** – *ao_pair* parameter must be a 2-tuple (str,str) and *new_valueset* parameter must be a non-empty subset of the ValueSet object of the Attribute object corresponding to the attribute in the *ao_pair* parameter.
- **KeyError** – *ao_pair* must be a key in the *ascriptions* member of this State object.

VOCABULARIES

6.1 The RelationSymbol object

relation_symbol module.

class relation_symbol.**RelationSymbol** (*name*, *arity*)

Relation Symbols class. The RelationSymbol class is used entirely in the Vocabulary class.

Variables

- **name** – A `str` designating the name of the RelationSymbol object.
- **arity** – An `int` designating the arity of the RelationSymbol object.
- **_is_RelationSymbol** – An identifier to use in place of `type` or `isinstance`.

__deepcopy__ (*memo*)

Deepcopy a RelationSymbol object via the `copy.deepcopy` method.

__eq__ (*other*)

Determine if two RelationSymbol objects are equal via the `==` operator.

__hash__ ()

Hash implementation for set functionality of RelationSymbol objects.

__init__ (*name*, *arity*)

Construct a RelationSymbol object.

Parameters

- **name** (`str`) – The name of the RelationSymbol object.
- **arity** (`int`) – The arity of the RelationSymbol object.

Raises

- **TypeError** – `name` parameter must be a `str` and `arity` parameter must be an `int`.
- **ValueError** – `arity` must be positive.

__ne__ (*other*)

Determine if two RelationSymbol objects are not equal via the `!=` operator.

__repr__ ()

Return a string representation of the RelationSymbol object.

__str__ ()

Return a readable string representation of the RelationSymbol object.

_key ()

Private key function for hashing.

Returns 2-tuple consisting of (name, arity)

Return type tuple

6.2 The Vocabulary object

vocabulary module.

class vocabulary.**Vocabulary** (*C, R, V*)

Vocabulary class. The Vocabulary class represents a first-order vocabulary $\Sigma = (C, R, V)$ consisting of a set of constant symbols *C*; a set of relation symbols *R*; and a set of variables *V*.

Variables

- **C** – The constants *C* of the vocabulary.
- **R** – The relation symbols *R* of the vocabulary.
- **V** – The variables *V* of the vocabulary.
- **`_is_Vocabulary`** – An identifier to use in place of `type` or `isinstance`.

`__contains__` (*key*)

Determine if the calling Vocabulary object contains the `str` or `RelationSymbol` object in the *key* parameter.

Parameters *key* (*RelationSymbol/str*) – The `str` or `RelationSymbol` object to test for membership in the calling Vocabulary object.

`__deepcopy__` (*memo*)

Deepcopy a Vocabulary object via the `copy.deepcopy` method.

`__eq__` (*other*)

Determine if two Vocabulary objects are equal via `==` operator.

`__hash__` ()

Hash implementation for set functionality of Vocabulary objects.

`__init__` (*C, R, V*)

Construct a Vocabulary object. Each parameter *C*, *R* and *V* are sorted before being stored.

Parameters

- **C** (*list*) – The constants *C* of the Vocabulary object; held as a `list` of `strs`.
- **R** (*list*) – The relation symbols *R* of the Vocabulary object; held as a `list` of `RelationSymbol` objects.
- **V** (*list*) – The variables *V* of the Vocabulary object; held as a `list` of `strs`.

Raises

- **`TypeError`** – *C*, *R*, and *V* parameters must all be lists, *C* and *V* must be contain only `strs` and *R* must contain only `RelationSymbol` objects.
- **`ValueError`** – *C* and *V* cannot overlap and duplicates are not permitted in any of the lists.

`__ne__` (*other*)

Determine if two Vocabulary objects are not equal via `!=` operator.

`__repr__` ()

Return a string representation of the Vocabulary object.

__str__()

Return a readable string representation of the Vocabulary object.

_key()

Private key function for hashing.

Returns 3-tuple consisting of (C, R, V)

Return type tuple

add_constant (*constant*)

Add a constant to this Vocabulary object's constants C.

Parameters **constant** (str) – The new constant to add to the Vocabulary's constants C.

Raises

- **TypeError** – `constant` parameter must be a `str`.
- **ValueError** – Duplicate symbols are not permitted.

add_variable (*variable*)

Add a variable to this Vocabulary object's variables V.

Parameters **variable** (str) – The new variable to add to the Vocabulary's variables V.

Raises

- **TypeError** – `variable` parameter must be a `str`.
- **ValueError** – Duplicate symbols are not permitted.

CONSTANT AND VARIABLE ASSIGNMENTS

7.1 The Assignment base class

assignment module.

class `assignment.Assignment` (*vocabulary*, *attribute_system*)

Assignment class. The Assignment class functions as a superclass for the ConstantAssignment and VariableAssignment classes.

Variables

- **vocabulary** – A reference to the Vocabulary object Σ that the Assignment is defined over.
- **attribute_system** – A copy of the AttributeSystem the Assignment originates from.
- **_is_Assignment** – An identifier to use in place of `type` or `isinstance`.

__eq__ (*other*)

Determine if two Assignment objects are equal via the `==` operator.

__init__ (*vocabulary*, *attribute_system*)

Construct a base Assignment.

Parameters

- **vocabulary** (Vocabulary) – The Vocabulary Σ the Assignment is defined over.
- **attribute_system** (AttributeSystem) – The AttributeSystem from which the objects in the Assignment come from.

Raises TypeError – `vocabulary` parameter must be a Vocabulary object and `attribute_system` parameter must be an AttributeSystem object.

__ne__ (*other*)

Determine if two Assignment objects are not equal via the `!=` operator.

7.2 The ConstantAssignment object

constant_assignment module.

class `constant_assignment.ConstantAssignment` (*vocabulary*, *attribute_system*, *mapping*)

Bases: `assignment.Assignment`

ConstantAssignment class. A ConstantAssignment is a partial function ρ from the constants C of some Vocabulary object Σ , to the objects $\{s_1, \dots, s_n\}$ of some AttributeSystem S .

The `ConstantAssignment` class uses the `total_ordering` decorator so strict subsets, supersets and strict supersets are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **vocabulary** – A reference to the `Vocabulary` object Σ the `ConstantAssignment` is defined over.
- **attribute_system** – A copy of the `AttributeSystem` object \mathcal{S} the `ConstantAssignment` originates from.
- **mapping** – The mapping $C \mapsto \{s_1, \dots, s_n\}$.
- **source** – The constants of Σ used in the partial mapping ρ .
- **target** – The objects of \mathcal{S} used in the partial mapping ρ .
- **_is_ConstantAssignment** – An identifier to use in place of `type` or `isinstance`.

`__deepcopy__` (*memo*)

Deepcopy a `ConstantAssignment` object via the `copy.deepcopy` method. This does not break the reference to the underlying `Vocabulary` object Σ .

`__eq__` (*other*)

Determine if two `ConstantAssignment` objects are equal via the `==` operator.

`__getitem__` (*key*)

Retrieve the object s_i mapped to the constant c_i given by `key` parameter via indexing (e.g. `ConstantAssignment[key]`).

Parameters `key` (*str*) – The constant c_i to use for retrieval.

Raises

- **KeyError** – The constant c_i given by the `key` parameter is not in this `ConstantAssignment`'s `source` member.
- **TypeError** – `key` parameter must be a `str`.

`__init__` (*vocabulary, attribute_system, mapping*)

Construct a `ConstantAssignment` object.

Parameters

- **vocabulary** (`Vocabulary`) – The `Vocabulary` object Σ the `ConstantAssignment` is defined over.
- **attribute_system** (`AttributeSystem`) – The `AttributeSystem` object \mathcal{S} from which the objects $\{s_1, \dots, s_n\}$ in the `ConstantAssignment` come from.
- **mapping** (`dict`) – The mapping ρ from the constants C of the `Vocabulary` object Σ in the `vocabulary` parameter to the objects $\{s_1, \dots, s_n\}$ of the `AttributeSystem` object \mathcal{A} in the `attribute_system` parameter.

Raises

- **TypeError** – `vocabulary` parameter must be a `Vocabulary` object, `attribute_system` parameter must be an `AttributeSystem` object and `mapping` parameter must be a `dict` with `str` keys and values.
- **ValueError** – All keys in the `mapping` parameter must be in the `Vocabulary` object in the `vocabulary` parameter's `C` member and all values in the `mapping` parameter must be unique and match some object in the `object` member of the `AttributeSystem` object in the `attribute_system` parameter.

`__lt__(other)`

Overloaded `<` operator for ConstantAssignment. Determine if the calling ConstantAssignment object is a subset of the ConstantAssignment object in the `other` parameter.

Raises **TypeError** – `other` parameter must be a ConstantAssignment object.

`__ne__(other)`

Determine if two ConstantAssignment objects are not equal via the `!=` operator.

`__repr__()`

Return a string representation of the ConstantAssignment object.

`__str__()`

Return a readable string representation of the ConstantAssignment object.

`add_mapping(constant_symbol, obj)`

Extend the calling ConstantAssignment object by adding a new mapping from the constant c' in the `constant_symbol` parameter to the object o' in the `obj` parameter.

Raises

- **TypeError** – Both `constant_symbol` and `obj` parameters must be `strs`.
- **ValueError** – The constant c' in the `constant_symbol` parameter must be in the `C` member of the underlying Vocabulary object Σ , the object o' in the `obj` parameter must be in the objects of the `objects` member of the underlying AttributeSystem object \mathcal{S} and neither the constant c' nor the object o' may be a duplicate.

`get_domain()`

Get the set of all and only those constant symbols for which the calling ConstantAssignment object ρ is defined w.r.t. the `C` member of the `vocabulary` member of ρ .

Returns The list of constants for which ρ is defined.

Return type `list`

`in_conflict(other)`

Check if the calling ConstantAssignment object ρ_1 is in conflict with the ConstantAssignment object ρ_2 provided in the `other` parameter.

Returns Whether or not ρ_1 and ρ_2 are in conflict, that is, if there is some $c \in \text{Dom}(\rho_1) \cap \text{Dom}(\rho_2)$, such that $\rho_1(c) \neq \rho_2(c)$.

Return type `bool`

Raises **TypeError** – `other` parameter must be a ConstantAssignment object.

`is_total()`

Determine if the calling ConstantAssignment object ρ is a total function $\hat{\rho}$ from $C \rightarrow \{s_1, \dots, s_n\}$.

Returns Whether or not the source of ρ spans the `C` member of Σ .

Return type `bool`

`remove_mapping(constant_symbol, obj)`

Extend the calling ConstantAssignment object by removing an existing mapping from the constant c' in the `constant_symbol` parameter to the object o' in the `obj` parameter.

Raises

- **TypeError** – both `constant_symbol` and `obj` parameters must be `strs`.
- **ValueError** – The constant c' in the `constant_symbol` parameter must be in the `C` member of the underlying Vocabulary object Σ , the object o' in the `obj` parameter must be in the objects of the `objects` member of the underlying AttributeSystem object \mathcal{S} and

the constant c' and the object o' must already be in the `source` and `target` members of the calling `ConstantAssignment` object respectively.

7.3 The VariableAssignment object

`variable_assignment` module.

class `variable_assignment.VariableAssignment` (*vocabulary*, *attribute_system*, *mapping*, *dummy=False*)

VariableAssignment class. A VariableAssignment is a total function χ from the variables V of some Vocabulary object Σ , to the objects $\{s_1, \dots, s_n\}$ of some AttributeSystem \mathcal{S} .

Variables

- **vocabulary** – A reference to the Vocabulary object Σ the ConstantAssignment is defined over.
- **attribute_system** – A copy of the AttributeSystem object \mathcal{S} the ConstantAssignment originates from.
- **mapping** – The mapping $V \longrightarrow \{s_1, \dots, s_n\}$.
- **source** – The variables of Σ used in the total mapping χ .
- **target** – The objects of \mathcal{S} used in the total mapping χ .
- **_is_VariableAssignment** – An identifier to use in place of type or `isinstance`.

The VariableAssignment class uses the `total_ordering` decorator so strict subsets, supersets and strict supersets are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

__deepcopy__ (*memo*)

Deepcopy a VariableAssignment object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

__eq__ (*other*)

Determine if two VariableAssignment objects are equal via the `==` operator.

__getitem__ (*key*)

Retrieve the object s_i mapped to the variable v_i given by `key` parameter via indexing (e.g. `VariableAssignment[key]`).

Parameters **key** (*str*) – The variable v_i to use for retrieval.

Raises

- **KeyError** – The variable v_i given by the `key` parameter is not in this VariableAssignment's `source` member.
- **TypeError** – `key` parameter must be a `str`.

__init__ (*vocabulary*, *attribute_system*, *mapping*, *dummy=False*)

Construct a VariableAssignment object.

Parameters

- **vocabulary** (*Vocabulary*) – The Vocabulary object Σ the VariableAssignment is defined over.
- **attribute_system** (*AttributeSystem*) – The AttributeSystem object \mathcal{S} from which the objects $\{s_1, \dots, s_n\}$ in the VariableAssignment come from.

- **mapping** (dict) – The mapping χ from the variables V of the Vocabulary object Σ in the `vocabulary` parameter to the objects $\{s_1, \dots, s_n\}$ of the AttributeSystem object \mathcal{A} in the `attribute_system` parameter.
- **dummy** (bool) – A flag for creating a dummy (i.e., empty) VariableAssignment object χ_{dummy} .

Raises

- **TypeError** – `vocabulary` parameter must be a Vocabulary object, `attribute_system` parameter must be an AttributeSystem object and `mapping` parameter must be a dict with str keys and values.
- **ValueError** – All keys in the `mapping` parameter must be in the Vocabulary object in the `vocabulary` parameter's `V` member and all values in the `mapping` parameter must be unique and match some object in the `object` member of the AttributeSystem object in the `attribute_system` parameter.

`__ne__` (*other*)

Determine if two VariableAssignment objects are not equal via the `!=` operator.

`__repr__` ()

Return a string representation of the VariableAssignment object.

`__str__` ()

Return a readable string representation of the VariableAssignment object.

NAMED STATES

8.1 The NamedState object

named_state module.

```
class named_state.NamedState (attribute_system, p, ascriptions={})  
    Bases: state.State
```

NamedState class. Each state is a pair $(\sigma; \rho)$ consisting of a state σ and a constant assignment ρ .

The NamedState class uses the `total_ordering` decorator so proper extensions, contravariant extensions and contravariant proper extensions are also available via the `<`, `>=`, and `>` operators respectively, despite the lack of magic functions for them.

Variables

- **attribute_system** – A copy of the AttributeSystem object \mathcal{S} that the NamedState object comes from.
- **ascriptions** – The ascriptions of the named state (i.e., the set of attribute-object pairs and their corresponding ValueSet objects) δ_i , $i = 1, \dots, k$.
- **p** – The ConstantAssignment object ρ of the named state.
- **_is_NamedState** – An identifier to use in place of `type` or `isinstance`.

`__deepcopy__` (memo)

Deepcopy a NamedState object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

`__eq__` (other)

Determine if two NamedState objects are equal via the `==` operator.

`__init__` (attribute_system, p, ascriptions={})

Construct a NamedState object.

Parameters

- **attribute_system** (AttributeSystem) – The AttributeSystem object \mathcal{S} from which the NamedState object comes from.
- **p** (ConstantAssignment) – The ConstantAssignment object ρ of the NamedState object.
- **ascriptions** (dict) – An optional dictionary of attribute-object pairs $\delta_i(s_j)$ to use as ascriptions; if some attribute-object pair is not provided, the full ValueSet of the Attribute object corresponding to the attribute label in the attribute-object pair is used.

Raises

- **TypeError** – `p` parameter must be a `ConstantAssignment` object.
- **ValueError** – The `AttributeSystem` object provided in the `attribute_system` parameter and the `AttributeSystem` object of the `ConstantAssignment` object in the `p` parameter must match.

`__le__` (*other*)

Overloaded `<=` operator for `NamedState`; Determine if the calling `NamedState` object $(\sigma; \rho)$ is an extension of the `NamedState` object $(\sigma'; \rho')$ in the `other` parameter; that is, if $(\sigma; \rho) \sqsubseteq (\sigma'; \rho')$.

Raises **TypeError** – `other` parameter must be a `NamedState` object.

`__ne__` (*other*)

Determine if two `NamedState` objects are not equal via the `!=` operator.

`__repr__` ()

Return a string representation of the `NamedState` object.

`__str__` ()

Return a readable string representation of the `NamedState` object.

`_generate_variable_assignments` ()

Generate all possible `VariableAssignment` objects χ derivable from the calling `NamedState` object i.e., find all combinations of objects not in the calling `NamedState` object's `ConstantAssignment` ρ and variables in the underlying `Vocabulary` Σ object (a reference to it is held by ρ). If no `VariableAssignments` can be created, a dummy `VariableAssignment` χ_{dummy} is returned.

Returns A generator for all derivable `VariableAssignment` objects χ .

Return type `generator`

`add_object` (*obj*, *ascriptions=None*, *constant_symbol=None*)

Add an object s' to the calling `NamedState` object's underlying `AttributeSystem` S , optionally update any ascriptions of the new object $\delta_i(s')$ provided and optionally bind it to a constant c' given by the `constant_symbol` parameter (if c' does not exist in the underlying `Vocabulary` object Σ , it will be added to Σ and furthermore all objects holding a reference to Σ will receive the update).

Parameters

- **obj** (`str`) – The new object s' to add to the `NamedState`.
- **ascriptions** (`dict`) – The optional `ValueSets` to assign to the attribute-object pairs corresponding to the new object $\delta_i(s')$.
- **constant_symbol** (`str`) – The optional constant c' to bind to the new object s' .

Raises

- **TypeError** – `obj` parameter must be a non-empty `str`, if `ascriptions` parameter is provided, it must be a `dict` and if `constant_symbol` parameter is provided, it must be a `str`.
- **ValueError** – Duplicate objects cannot be added, c' cannot be bound already and all ascriptions provided must be from an existing label of an `Attribute` object in the underlying `AttributeSystem` object S to s' .

`get_named_alternate_extensions` (**named_states*)

Obtain all alternate extensions of the calling `NamedState` object w.r.t. the `NamedState` objects $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$ provided in the `named_states` parameter, i.e., compute $\mathbf{AE}(\Sigma_i, \sigma)$ for the various applicable i according to algorithm.

Returns all alternative extensions of this NamedState object $(\sigma; \rho)$ w.r.t. the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$ provided as optional positional arguments in the `named_states` parameter.

Return type `list`

Raises

- **TypeError** – `ns_prime` and all arguments provided as optional positional arguments to the `named_states` parameter must be NamedState objects.
- **ValueError** – At least one NamedState object must be provided in `named_states` parameter and all NamedState objects in `ns_prime` and `named_states` parameters must be proper extensions of this NamedState.

get_worlds()

Return a generator for the generation of all possible worlds $(w; \hat{\rho})$ derivable from the calling NamedState object.

Returns A generator for the generation of all possible worlds $(w; \hat{\rho})$ derivable from this NamedState object.

Return type `generator`

is_exhaustive (*basis*, **named_states*)

Determine if on some basis (i.e., a set of attribute-object pairs $\delta_i(s_j)$), a set of NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ is exhaustive w.r.t the calling NamedState object $(\sigma; \rho)$, that is, if the ascriptions (ob objects in the basis) of the states $\sigma_1, \dots, \sigma_n$ span the ascriptions of σ .

Parameters

- **basis** (`list`) – A list of attribute-object pairs $\delta_i(s_j)$.
- **named_states** (`NamedState`) – Any positive amount of NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$.

Returns Whether or not the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ provided as optional positional arguments are exhaustive w.r.t. the calling NamedState object $(\sigma; \rho)$ on the basis provided in the `basis` parameter.

Return type `bool`

Raises **ValueError** – `basis` parameter cannot be empty and at least one NamedState object must be provided to `named_states` parameter.

is_named_alternate_extension (*ns_prime*, **named_states*)

Determine if the NamedState object in the `ns_prime` parameter $(\sigma'; \rho')$ is an alternate extension of the calling NamedState object $(\sigma; \rho)$ w.r.t. the NamedState objects provided in the `named_states` parameter $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$, i.e., evaluate $Alt((\sigma; \rho), \{(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)\}, (\sigma'; \rho'))$

Returns The result of the evaluation of $Alt((\sigma; \rho), \{(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)\}, (\sigma'; \rho'))$

Return type `bool`

Raises

- **TypeError** – `ns_prime` and all arguments provided as optional positional arguments to `named_states` parameter must be NamedState objects.
- **ValueError** – At least one NamedState object must be provided to `named_states` parameter and all NamedState objects in `ns_prime` and `named_states` parameters must be proper extensions of the calling NamedState object.

is_named_entailment (*assumption_base*, *attribute_interpretation*, **named_states*)

Determine if the calling NamedState object $(\sigma; \rho)$ entails the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$ provided as optional positional arguments to the *named_states* parameter w.r.t. the AssumptionBase object β in the *assumption_base* parameter, using the AttributeInterpretation object I provided in the *attribute_interpretation* parameter to resolve truth values of the Formula objects contained therein, i.e., evaluate $(\sigma; \rho) \Vdash_{\beta} \{(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)\}$.

Parameters

- **assumption_base** (AssumptionBase) – The AssumptionBase object β to use when evaluating $I_{(\sigma'; \rho')/\chi} \left(\bigwedge_{F \in \beta} F \right) = \text{false}$ for all χ .
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use to resolve the truth values of Formula objects in the AssumptionBase object β in *assumption_base* parameter.
- **named_states** (NamedState) – Any amount of NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$ to check for entailment.

Returns Whether or not $(\sigma; \rho) \Vdash_{\beta} \{(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)\}$

Return type bool

Raises

- **TypeError** – *assumption_base* parameter must be an AssumptionBase object, *attribute_interpretation* parameter must be an AttributeInterpretation object, and all optional positional arguments in *named_states* parameter must be NamedState objects.
- **ValueError** – All NamedState objects provided as optional positional arguments to the *named_states* parameter $(\sigma_1; \rho_1), \dots, (\sigma_m; \rho_m)$ must share the same underlying Vocabulary object Σ , have equivalent AttributeSystem objects \mathcal{S} and be proper extensions of the calling NamedState object $(\sigma; \rho)$, that is, $(\sigma_i; \rho_i) \sqsubset (\sigma; \rho)$ for $i = 1, \dots, m$.

is_world ()

Determine if the calling NamedState object $(\sigma; \rho)$ is a world; that is every ascription δ_i of σ is a valuation and ρ is total (that is, $\rho \rightarrow \hat{\rho}$ holds).

Returns Whether or not the calling NamedState object is a world.

Return type bool

satisfies_context (*context*, *X*, *attribute_interpretation*)

Determine if this NamedState object $(w; \hat{\rho})$ (which must be a world) satisfies the given Context object in the *context* parameter $\gamma = (\beta; (\sigma; \rho))$ w.r.t. a given VariableAssignment object χ and given AttributeInterpretation object I , i.e., $(w; \hat{\rho}) \models_{\chi} \gamma$ (the calling NamedState object $(w; \hat{\rho})$ satisfies every Formula object in the AssumptionBase object of the Context object β and the calling NamedState object satisfies the NamedState object of the Context object $(\sigma; \rho)$, that is, $(w; \hat{\rho}) \models_{\chi} F$ for every $F \in \beta$ and $(w; \hat{\rho}) \models (\sigma; \rho)$).

Parameters

- **context** (Context) – The context γ to check for satisfaction.
- **X** (VariableAssignment) – The variable assignment χ
- **attribute_interpretation** (AttributeInterpretation) – The fixed attribute interpretation I to use for interpreting which constants and variables are substituted into the formula for evaluation.

Returns Whether or not $(w; \hat{\rho}) \models_{\chi} \gamma$.

Return type `bool`

Raises

- **TypeError** – `context` parameter must be a Context object, `X` parameter must be a VariableAssignment object and `attribute_interpretation` must be an AttributeInterpretation object.
- **ValueError** – The calling NamedState object must be a world.

satisfies_formula (*formula*, *X*, *attribute_interpretation*)

Determine if the calling NamedState object $(w; \hat{\rho})$ (which must be a world) satisfies the given Formula object F in the `formula` parameter w.r.t. the VariableAssignment object χ in the `X` parameter and given AttributeInterpretation I in the `attribute_interpretation` parameter, i.e., $(w; \hat{\rho}) \models_{\chi} F$.

Parameters

- **formula** (Formula) – The formula F to check for satisfaction.
- **X** (VariableAssignment) – The variable assignment χ
- **attribute_interpretation** (AttributeInterpretation) – The fixed attribute interpretation I to use for interpreting which constants and variables are substituted into the formula F for evaluation.

Returns Whether or not $(w; \hat{\rho}) \models_{\chi} F$.

Return type `bool`

Raises

- **TypeError** – `formula` parameter must be a Formula object, `X` parameter must be a VariableAssignment object and `attribute_interpretation` parameter must be an AttributeInterpretation object.
- **ValueError** – The calling NamedState object must be a world.

satisfies_named_state (*named_state*)

Determine if the calling NamedState object $(w; \hat{\rho})$ (which must be a world) satisfies the given NamedState object $(\sigma; \rho)$ i.e., $(w; \hat{\rho}) \models (\sigma; \rho)$.

Parameters **named_state** (NamedState) – The named state $(\sigma; \rho)$ to check for satisfaction.

Returns Whether or not $(w; \hat{\rho}) \models (\sigma; \rho)$.

Return type `bool`

Raises

- **TypeError** – `named_state` parameter must be a NamedState object.
- **ValueError** – The calling NamedState object must be a world.

ATTRIBUTE INTERPRETATIONS

9.1 The AttributeInterpretation object

attribute_interpretation module.

class attribute_interpretation.**AttributeInterpretation** (*vocabulary, attribute_structure, mapping, profiles*)

AttributeInterpretation class. Build an interpretation table; that is, a mapping I that assigns, to each Relation-Symbol object of a Vocabulary object Σ , $R \in \mathcal{R}$ of arity n :

1. a relation $R^I \in \mathcal{R}$ of some arity m , called the **realization** of R :

$$R^I \subset A_{i_1} \times \cdots \times A_{i_m}$$

(where we might have $m \neq n$); and

2. a list of m pairs

$$[(l_{i_1}; j_1) \cdots (l_{i_m}; j_m)]$$

called the **profile** of R and denoted by $Prof(R)$, with $1 \leq j_x \leq n$ for $x = 1, \dots, m$

Variables

- **vocabulary** – The Vocabulary object Σ of the interpretation.
- **attribute_structure** – The AttributeStructure object the interpretation is into.
- **mapping** – The mapping $\mathcal{R} \rightarrow \mathcal{R}$.
- **profiles** – A list of profiles $[(l_{i_1}; j_1) \cdots (l_{i_m}; j_m)]$; one for each realization.
- **table** – The interpretation table of the attribute interpretation.
- **relation_symbols** – A copy of the RelationSymbol objects from Σ (for convenient access).
- **is_AttributeInterpretation** – An identifier to use in place of `type` or `isinstance`.

__deepcopy__ (*memo*)

Deepcopy an AttributeInterpretation object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

__eq__ (*other*)

Determine if two AttributeInterpretation objects are equal via the `==` operator.

__init__ (*vocabulary, attribute_structure, mapping, profiles*)

Construct an AttributeInterpretation object.

Parameters

- **vocabulary** (Vocabulary) – The Vocabulary object Σ to define the AttributeInterpretation over.
- **attribute_structure** (AttributeStructure) – The AttributeStructure object for which to define the AttributeInterpretation into.
- **mapping** (dict) – The mapping from the RelationSymbol objects of the Vocabulary object Σ in the `vocabulary` parameter to the Relation objects of the AttributeStructure object in the `attribute_structure` parameter; the keys being RelationSymbol objects and values being ints corresponding to the subscripts of the AttributeStructure Relation objects.
- **profiles** (list) – A list of realizations corresponding to the mapping wherein each element is a list where the first element is the RelationSymbol and the following elements are 2-tuples $(l_{i_k}; j_k)$.

Raises

- **TypeError** – `vocabulary` parameter must be a Vocabulary object, `attribute_structure` parameter must be an AttributeStructure object, `mapping` parameter must be a dict and `profile` parameter must be a list.
- **ValueError** – All keys in the `mapping` parameter must be RelationSymbol objects and all values must be unique ints, duplicate profiles are not permitted (determined by repeated RelationSymbol objects), the set of RelationSymbol's provided in the `mapping` parameter and the set of RelationSymbol's in the `vocabulary` parameter and the set of RelationSymbol's provided in the `profile` parameter must all be equal, all subscripts provided in the `mapping` parameter keys must be valid subscripts of Relation objects in the `attribute_structure` parameter, all l_{i_k} in $(l_{i_k}; j_k)$ 2-tuples provided in each realization of the `profile` parameter must be a label of some Attribute object in the `attribute_structure` parameter, and all j_k in $(l_{i_k}; j_k)$ 2-tuples provided in each realization of the `profile` parameter must be between 1 and the arity of the RelationSymbol object of the realization.

`__iter__()`

Provide an iterator for the interpretation table of AttributeInterpretation objects.

(e.g. “for entry in `attribute_interpretation`:”)

`__ne__(other)`

Determine if two AttributeInterpretation objects are not equal via the `!=` operator.

`__repr__()`

Return a string representation of the AttributeInterpretation object.

`__str__()`

Return a readable string representation of the AttributeInterpretation object.

FORMULAE AND ASSUMPTION BASES

10.1 The Formula object

formula module.

class `formula.Formula` (*vocabulary*, *name*, **terms*)

Formula class. Formula objects are defined over some Vocabulary Σ . Formula objects are immutable.

Variables

- **vocabulary** – The underlying Vocabulary object Σ the Formula is defined over.
- **name** – The name of the Formula object.
- **terms** – The terms of the Formula object.
- **is_Formula** – An identifier to use in place of `type` or `isinstance`.

`__add__` (*other*)

Combine a Formula object and another Formula object or an AssumptionBase object into an AssumptionBase object via the `+` operator.

Raises

- **TypeError** – Only a Formula object or AssumptionBase object can be combined with a Formula object.
- **ValueError** – This Formula and `other` parameter must share the same underlying Vocabulary object Σ and duplicate Formula objects are not permitted (determined by name of the Formula object only).

`__deepcopy__` (*memo*)

Deepcopy a Formula object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

`__eq__` (*other*)

Determine if two Formula objects are equal via the `==` operator.

`__hash__` ()

Hash implementation for set functionality of Formula objects.

`__init__` (*vocabulary*, *name*, **terms*)

Construct a Formula object.

Parameters

- **vocabulary** (Vocabulary) – The underlying Vocabulary object Σ the Formula is defined over.
- **name** (`str`) – The name (identifier) of the formula.

- **terms** (*str*) – Any amount of *str* constants and variables representing the terms of the formula.

Raises

- **TypeError** – *vocabulary* parameter must be a Vocabulary object.
- **ValueError** – *name* parameter must match some RelationSymbol object in the *vocabulary* parameter, at least one term must be provided and all terms provided must be in either the constants or variables of the *vocabulary* parameter Σ .

__ne__ (*other*)

Determine if two Formula objects are not equal via the \neq operator.

__repr__ ()

Return a string representation of the NamedState object.

__str__ ()

Return a readable string representation of the NamedState object.

_key ()

Private key function for hashing.

Returns tuple consisting of (*name*, t_1, \dots, t_n)

Return type tuple

assign_truth_value (*attribute_interpretation*, *named_state*, *X*)

Assign a truth value in $\{\mathbf{true}, \mathbf{false}, \mathbf{unknown}\}$ to the calling Formula object F given an arbitrary NamedState object $(\sigma; \rho)$ in the *named_state* parameter and VariableAssignment object χ in the *X* parameter w.r.t. an AttributeInterpretation object I .

This function makes use of the ParserSet object; the ParserSet object is a key part in the vivid object extension protocol.

The *assign_truth_value* function works as follows:

1. Find the entry in the interpretation table of the AttributeInterpretation object I in the *attribute_interpretation* parameter and extract the corresponding profile and Relation object (the 3rd element of the corresponding row of the table is the identifier for the Relation object; e.g. $R_{\text{subscript}}$).
2. Substitute the terms of the Formula object F into the profile (the 2nd element of each pair in the profile corresponds to the index of the term in the F to use, shifted down by 1).
3. Using the ConstantAssignment object of the *named_state* parameter ρ and the VariableAssignment in the *X* parameter χ , substitute for each term now in the profile, the object corresponding to that term given by the mapping in ρ or χ (if the term is in neither ρ nor χ , “unknown” is returned as the truth value).
4. The profile now consists of the attribute-object pairs $(\delta_i(s_j))$ for some set of the possible values of i and j to use in the Relation object’s definition when creating the evaluable expression. Now, all worlds $(w; \hat{\rho})$ derivable from the NamedState are generated and the ValueSets of the attribute-object pairs in the profile (consisting of single elements) are extracted from the ascriptions of these worlds.
5. The single element ValueSets are zipped together with the arguments in the Relation object definition (the i th attribute-object pair of the profile is zipped with the i th argument of the definition) and these new argument-ValueSet pairs are used to substitute every occurrence of each argument in the definition with the corresponding single element ValueSet creating a (hopefully) evaluable expression (the RHS of the substituted definition) for each world $(w; \hat{\rho})$.
6. Each parser in the ParserSet object will then try to evaluate the expression and save the truth value for each $(w; \hat{\rho})$. If some expression is unevaluable for all parsers in the ParserSet a ValueError is raised.

7. If the expression of every world $(w; \hat{\rho})$ evaluates to True, the truth value returned is **true**, if the expression of every world evaluates to False, the truth value returned is **false** and if the expressions of any two worlds evaluate to different values, the truth value returned is **unknown**.

Returns A truth value in the set **{true, false, unknown}**

Return type bool|str

Raises

- **TypeError** – `attribute_interpretation` parameter must be an `AttributeInterpretation` object, `named_state` parameter must be a `NamedState` object and `X` parameter must be a `VariableAssignment` object.
- **ValueError** – This `Formula` object, the `AttributeInterpretation` object in the `attribute_interpretation` parameter, the `NamedState` object in the `named_state` parameter and the `VariableAssignment` object in the `X` parameter must all share the same underlying `Vocabulary` object (that is $F, I, (\sigma; \rho)$ and χ must all share the same Σ), the `Formula` object must match an entry in the interpretation table of the `AttributeInterpretation` I in the

`attribute_interpretation` parameter, the number of attribute-object pairs in the profile corresponding to the `Formula` must match the arity of the corresponding `Relation` object found in the table (where the `Relation` object is found in the `AttributeStructure` object in the `AttributeSystem` member of the `named_state` parameter), $1 \leq j_x \leq n$ for each j_x in the profile (where n is the arity of the `RelationSymbol` corresponding to the `RelationSymbol` object matching the `Formula` in the interpretation table, or equivalently, the number of terms in the `Formula` object) and a parser in the `ParserSet` object must be able to evaluate the expression obtained after substituting the objects of the `AttributeSystem` in the `named_state` parameter, corresponding to the terms of the `Formula`, into the `Relation` object's definition.

static get_basis (*constant_assignment, variable_assignment, attribute_interpretation, *formulae*)

Get the basis of the `Formula` objects F_1, \dots, F_k provided as optional positional arguments in the `formulae` parameter w.r.t. the `ConstantAssignment` object ρ provided in the `constant_assignment` parameter, `VariableAssignment` object χ provided in the `variable_assignment` parameter, and the `AttributeInterpretation` object I provided in the `attribute_interpretation` parameter, i.e., compute $\mathcal{B}(F_1, \rho, \chi) \cup \dots \cup \mathcal{B}(F_k, \rho, \chi)$.

Parameters

- **constant_assignment** (`ConstantAssignment`) – The `ConstantAssignment` object ρ to use to compile the profile corresponding to each `Formula` object $F_i, i = 1, \dots, k$ into attribute-object pairs to consider for the basis.
- **variable_assignment** (`VariableAssignment` | `None`) – The `VariableAssignment` object χ to use to compile the profile corresponding to each `Formula` object $F_i, i = 1, \dots, k$ into attribute-object pairs to consider for the basis or `None`.
- **attribute_interpretation** (`AttributeInterpretation`) – The `AttributeInterpretation` object I to use to determine the profiles corresponding to the `Formula` objects F_1, \dots, F_k provided (the profile is extracted from the interpretation table when the `RelationSymbol` matching the `Formula` object's name is found).
- **formulae** (`Formula`) – Any positive amount of `Formula` objects F_1, \dots, F_k to consider in the basis.

Returns A list of attribute-object pairs comprising the basis of the `Formula` objects F_1, \dots, F_k provided w.r.t. ρ and χ .

Return type list

Raises

- **TypeError** – `constant_assignment` parameter must be a `ConstantAssignment` object, and all optional positional arguments provided in the `formulae` parameter must be `Formula` objects.
- **ValueError** – At least one `Formula` object must be provided and all `Formula` objects provided must match some entry in the interpretation table of the `AttributeInterpretation` object I .

10.2 The AssumptionBase object

`assumption_base` module.

class `assumption_base.AssumptionBase(*formulae)`
 AssumptionBase class.

An `AssumptionBase` object functions as a container for a finite set of `Formula` objects F_1, \dots, F_k over a single underlying Vocabulary Σ , denoted β .

Variables

- **formulae** – The set of `Formula` objects F_1, \dots, F_k contained in the `AssumptionBase` object β .
- **vocabulary** – The underlying Vocabulary object Σ the `AssumptionBase` object β is defined over.
- **_is_AssumptionBase** – An identifier to use in place of `type` or `isinstance`.

__add__ (*other*)

Add all `Formula` objects in another `AssumptionBase` object or a single `Formula` object to the calling `AssumptionBase` object via the `+` operator.

Raises

- **TypeError** – Only `Formula` objects or `AssumptionBase` objects can be added to the calling `AssumptionBase` object.
- **ValueError** – Cannot add objects with different underlying Vocabulary objects and duplicate `Formula` objects are not permitted.

__contains__ (*item*)

Overloaded `in` operator for `AssumptionBase`. Determine if a `Formula` object is contained in the calling `AssumptionBase` object.

Parameters **key** (`Formula` | `str`) – The `Formula` object or the name of a `Formula` object to test for membership in the calling `AssumptionBase` object.

__deepcopy__ (*memo*)

Deepcopy an `AssumptionBase` object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

__eq__ (*other*)

Determine if two `AssumptionBase` objects are equal via the `==` operator.

__getitem__ (*key*)

Retrieve the `Formula` object corresponding to the key given by the `key` parameter via indexing (e.g. `AssumptionBase[key]`).

Parameters **key** (`int` | `str` | `Formula`) – The key to use for indexing in the calling `AssumptionBase` object.

Raises

- **IndexError** – `int` key is out of range.
- **KeyError** – key parameter does not correspond to any `Formula` object in the `AssumptionBase`.
- **TypeError** – key parameter must be an `int`, `str`, or `Formula` object.

__iadd__ (*other*)

Add all `Formula` objects in another `AssumptionBase` object or a single `Formula` object to the calling `AssumptionBase` object via the `+` operator.

Raises

- **TypeError** – Only `Formula` objects or `AssumptionBase` objects can be added to the calling `AssumptionBase` object.
- **ValueError** – Cannot add objects with different underlying `Vocabulary` objects and duplicate `Formula` objects are not permitted.

__init__ (**formulae*)

Construct an `AssumptionBase` object.

Parameters **formulae** (*Formula* | *Vocabulary*) – Any amount of `Formula` objects F_1, \dots, F_k or a single `Vocabulary` object Σ no `Formula` objects are provided.

Raises

- **TypeError** – All optional positional arguments provided must be `Formula` objects or a single `Vocabulary` object Σ .
- **ValueError** – All `Formula` objects provided as optional positional arguments must share the same `Vocabulary` object Σ .

__iter__ ()

Provide an iterator for `AssumptionBase` objects (e.g. “for formula in `AssumptionBase`:”).

__len__ ()

Determine the length of an `AssumptionBase` object β (i.e., the amount of `Formula` objects contained in β) via the `len` built-in function e.g. (`len (AssumptionBase)`).

__ne__ (*other*)

Determine if two `AssumptionBase` objects are not equal via the `!=` operator.

__repr__ ()

Return a string representation of the `AssumptionBase` object.

__str__ ()

Return a readable string representation of the `AssumptionBase` object.

CONTEXTS

11.1 The Context object

context module.

class `context.Context` (*assumption_base, named_state*)

Context class. A Context is a pair composed of an AssumptionBase object β and a NamedState object $(\sigma; \rho)$, i.e., $\gamma = (\beta; (\sigma; \rho))$.

Variables

- **`assumption_base`** – The AssumptionBase object β of the Context object.
- **`named_state`** – The NamedState object $(\sigma; \rho)$ of the Context object.
- **`is_Context`** – An identifier to use in place of `type` or `isinstance`.

`__deepcopy__` (*memo*)

Deepcopy a Context object via the `copy.deepcopy` method. This does not break the reference to the underlying Vocabulary object Σ .

`__eq__` (*other*)

Determine if two Context objects are equal via the `==` operator.

`__init__` (*assumption_base, named_state*)

Construct a Context object.

Parameters

- **`assumption_base`** (AssumptionBase) – The AssumptionBase object β to use in the Context object.
- **`named_state`** (NamedState) – The NamedState object $(\sigma; \rho)$ to use in the Context object.

Raises

- **`TypeError`** – `assumption_base` parameter must be an AssumptionBase object and `named_state` parameter must be a NamedState object.
- **`ValueError`** – The underlying Vocabulary objects of the `assumption_base` and `named_state` parameters must be the same Vocabulary object Σ .

`__ne__` (*other*)

Determine if two Context objects are not equal via the `!=` operator.

`__repr__` ()

Return a string representation of the Context object.

`__str__()`

Return a readable string representation of the Context object.

entails_formula (*formula*, *attribute_interpretation*)

Determine if the calling Context object $\gamma = (\beta; (\sigma; \rho))$ entails the Formula object F provided in the *formula* parameter, using the AttributeInterpretation object I provided in the *attribute_interpretation* parameter to interpret truth values, i.e., determine if $\gamma \models F$.

Parameters

- **formula** (Formula) – The Formula object F to check for entailment.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use for the interpretation of truth values during the evaluation of $\gamma \models F$.

Returns Whether or not $\gamma \models F$, that is, whether or not $(w; \hat{\rho}) \models_{\chi} \gamma$ implies $(w; \hat{\rho}) \models_{\chi} F$ for all worlds $(w; \hat{\rho})$ and variable assignments χ .

Return type bool

Raises

- **TypeError** – *formula* parameter must be a Formula object and *attribute_interpretation* parameter must be an AttributeInterpretation object.
- **ValueError** – The calling Context object and the Formula object F provided in the *formula* parameter must share the same underlying Vocabulary object Σ .

entails_named_state (*named_state*, *attribute_interpretation*)

Determine if the calling Context object $\gamma = (\beta; (\sigma; \rho))$ entails the NamedState object $(\sigma'; \rho')$ provided in the *named_state* parameter, using the AttributeInterpretation object I provided in the *attribute_interpretation* parameter to interpret truth values, i.e., determine if $\gamma \models (\sigma'; \rho')$.

Parameters

- **named_state** (NamedState) – The NamedState object $(\sigma'; \rho')$ to check for entailment.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use for the interpretation of truth values during the evaluation of $\gamma \models (\sigma'; \rho')$.

Returns Whether or not $\gamma \models (\sigma'; \rho')$, that is for all worlds $(w; \hat{\rho})$ and variable assignments χ , $(w; \hat{\rho}) \models (\sigma'; \rho')$ whenever $(w; \hat{\rho}) \models_{\chi} \gamma$.

Return type bool

Raises

- **TypeError** – *named_state* parameter must be a NamedState object and *attribute_interpretation* parameter must be an AttributeInterpretation object.
- **ValueError** – The calling Context object and the NamedState object $(\sigma'; \rho')$ provided in the *named_state* parameter must share the same underlying Vocabulary object Σ .

RULES OF INFERENCE FOR DIAGRAMMATIC DEDUCTIONS

12.1 The [Thinning] rule

`inference_rules.thinning` (*context*, *named_state*, *assumption_base=*`None`, *attribute_interpretation=*`None`)

Verify that the `NamedState` object $(\sigma'; \rho')$ in the `named_state` parameter can be obtained by thinning from the `NamedState` object $(\sigma; \rho)$ contained in the `Context` object $(\beta; (\sigma; \rho))$ in the `context` parameter w.r.t. the `AssumptionBase` object $\{F_1, \dots, F_n\}$ given by the `assumption_base` parameter, using the `AttributeInterpretation` object I in the `attribute_interpretation` parameter to interpret truth values.

By Corollary 26, if $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_n\}} (\sigma'; \rho')$ then $(\{F_1, \dots, F_n\}; (\sigma; \rho)) \models (\sigma'; \rho')$.

Then, by weakening, $(\beta \cup \{F_1, \dots, F_n\}; (\sigma; \rho)) \models (\sigma'; \rho')$ and thinning holds, thus it suffices to show that a call to `entails_named_state` with context $(\{F_1, \dots, F_n\}; (\sigma; \rho))$ and named state $(\sigma'; \rho')$, that is $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_n\}} (\sigma'; \rho')$, holds to show that thinning holds.

Parameters

- **context** (`Context`) – The `Context` object $(\beta; (\sigma; \rho))$.
- **named_state** (`NamedState`) – The `NamedState` object $(\sigma'; \rho')$
- **assumption_base** (`AssumptionBase` | `None`) – The set of `Formula` objects to thin with $\{F_1, \dots, F_n\}$ if thinning is to be done with any `Formula` (i.e., $n > 0$), otherwise `None`.
- **attribute_interpretation** (`AttributeInterpretation` | `None`) – The `AttributeInterpretation` object I to use to interpret truth values if $n > 0$, otherwise `None`.

Returns Whether or not thinning holds, i.e., the result of $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_n\}} (\sigma'; \rho')$

Return type `bool`

Raises **TypeError** – `context` parameter must be a `Context` object and `named_state` parameter must be a `NamedState` object.

12.2 The [Widening] rule

`inference_rules.widening` (*context*, *named_state*, *attribute_interpretation=*`None`)

Verify that the `NamedState` object $(\sigma'; \rho')$ in the `named_state` parameter can be obtained from the `Context` object $(\beta; (\sigma; \rho))$ in the `context` parameter by widening, using the `AttributeInterpretation` object I in the `attribute_interpretation` parameter to interpret truth values.

Parameters

- **context** (`Context`) – The `Context` object $(\beta; (\sigma; \rho))$.

- **named_state** (NamedState) – The NamedState object $(\sigma'; \rho')$
- **attribute_interpretation** (AttributeInterpretation | None) – The AttributeInterpretation object I to use to interpret truth values if widening should consider the AssumptionBase object of the context parameter, otherwise None.

Returns Whether or not the NamedState object $(\sigma'; \rho')$ in the `named_state` parameter can be obtained from the Context object $(\beta; (\sigma; \rho))$ in the `context` parameter by widening, i.e., whether or not $(\beta; (\sigma; \rho)) \models (\sigma'; \rho')$

Return type bool

Raises **TypeError** – context parameter must be a Context object and named_state parameter must be a NamedState object.

12.3 The [Observe] rule

`inference_rules.observe(context, formula, attribute_interpretation)`

Determine if the Formula object F given by the `formula` parameter can be observed in the Context object $(\beta; (\sigma; \rho))$ given by the `context` parameter, using the AttributeInterpretation object I in the `attribute_interpretation` parameter to interpret truth values, i.e., determine if **observe** F holds in $(\beta; (\sigma; \rho))$.

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ in which the Formula object F can potentially be observed.
- **formula** (Formula) – The (potentially) observable Formula object F .
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use to interpret truth values in the context and formula parameters.

Returns Whether or not **observe** F holds in $(\beta; (\sigma; \rho))$, that is, whether or not $(\beta; (\sigma; \rho)) \models F$.

Return type bool

12.4 The [Absurdity] rule

`inference_rules.diagrammatic_absurdity(context, named_state, attribute_interpretation)`

Verify that the NamedState object $(\sigma'; \rho')$ in the `named_state` parameter can be obtained from the Context object $(\beta; (\sigma; \rho))$ in the `context` parameter by absurdity, using the AttributeInterpretation object I provided in the `attribute_interpretation` parameter to interpret truth values.

To show $(\sigma'; \rho')$ **by absurdity**, we must show $(\beta \cup \{\mathbf{false}\}; (\sigma; \rho)) \models (\sigma'; \rho')$.

By lemma 20, $(\beta \cup \{\mathbf{false}\}; (\sigma; \rho)) \models (\sigma'; \rho')$, thus it suffices to show that a call to `entails_named_state` with context $(\beta; (\sigma; \rho))$ and named state $(\sigma'; \rho')$, that is, $(\beta; (\sigma; \rho)) \models (\sigma'; \rho')$ holds, implicitly assuming that some $F \in \beta$ evaluates to **false** (as then no world can satisfy the context, i.e., for any world $(w; \hat{\rho})$ derivable from the context $(\beta; (\sigma; \rho))$, $(w; \hat{\rho}) \not\models_{\chi} (\beta; (\sigma; \rho))$ and thus `entails_named_state` will always hold yielding $(\sigma'; \rho')$ **by absurdity** regardless of the NamedState object $(\sigma'; \rho')$ provided in the `named_state` parameter)

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$.
- **named_state** (NamedState) – The NamedState object $(\sigma'; \rho')$.

- **attribute_interpretation** (AttributeInterpretation) –

Returns Whether or not $(\sigma'; \rho')$ **by absurdity**, that is, whether or not $(\beta; (\sigma; \rho)) \models (\sigma'; \rho')$ holds.

Return type bool

Raises **TypeError** – context parameter must be a Context object, named_state parameter must be a NamedState object and attribute_interpretation parameter must be an AttributeInterpretation object.

12.5 The [Diagram-Reiteration] rule

`inference_rules.diagram_reiteration` (context)

Perform *[Diagram – Reiteration]* to retrieve the current diagram of the Context object $(\beta; (\sigma; \rho))$ provided in the context parameter, i.e., from lemma 19: $(\beta; (\sigma; \rho)) \models (\sigma; \rho)$.

Parameters **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ from which to retrieve the current NamedState object $(\sigma; \rho)$.

Returns The NamedState object $(\sigma; \rho)$ of the Context object $(\beta; (\sigma; \rho))$ in context parameter.

Return type NamedState

12.6 The [Sentential-to-Sentential] rule

`inference_rules.sentential_to_sentential` (context, F1, F2, G, attribute_interpretation, variable_assignment=None)

Verify that a disjunction $F_1 \vee F_2$ holds in the Context object $(\beta; (\sigma; \rho))$ in the context parameter and that the Formula object G in the G parameter follows in either case, using the AttributeInterpretation object I in the attribute_interpretation parameter to interpret truth values.

To perform the **sentential-to-sentential** inference, first the disjunction $F_1 \vee F_2$ is verified. Then the truth values of $F_1 \Rightarrow G$ and $F_2 \Rightarrow G$ are determined. If either $F_1 \Rightarrow G$ or $F_2 \Rightarrow G$ do not hold, then **sentential-to-sentential** does not hold, otherwise, **sentential-to-sentential** holds.

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ in which the the Formula objects in the parameters F1, F2 apply and in which the Formula object in the G parameter would follow.
- **F1** (Formula) – The left operand of the disjunction F_1 .
- **F2** (Formula) – The right operand of the disjunction F_2 .
- **G** (Formula) – The Formula object G potentially following the disjunction in either case.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use for interpreting truth values.
- **variable_assignment** (VariableAssignment | None) – The optional VariableAssignment object χ to consider in the interpretation of truth values.

Returns Whether or not **sentential-to-sentential** holds.

Return type bool

Raises **ValueError** – The disjunction $F_1 \vee F_2$ does not hold.

12.7 The [Diagrammatic-to-Diagrammatic] rule

`inference_rules.diagrammatic_to_diagrammatic` (*context*, *inferred_named_state*,
named_states, *attribute_interpretation*,
variable_assignment, **formulae*)

Verify that on the basis of the present diagram $(\sigma; \rho)$ of the Context object $(\beta; (\sigma; \rho))$ in the `context` parameter and some set of Formula objects $F_1, \dots, F_k, k \geq 0$ provided as optional positional arguments in the `formulae` parameter, that for each NamedState object $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n), n > 0$, contained in the `named_states` parameter, a NamedState object $(\sigma'; \rho')$ provided in the `inferred_named_state` parameter can be derived in every one of these n cases.

This is rule $[C_1]$.

This function works as follows:

1. If $k > 0$ (i.e., if at least one Formula object is provided as an optional positional argument to the `formulae` parameter), compute the basis $\mathcal{B}(F_1, \rho, \chi) \cup \dots \cup \mathcal{B}(F_k, \rho, \chi)$ of F_1, \dots, F_k and determine if the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ provided in the `named_states` parameter form an exhaustive set of possibilities on this basis.
2. Determine if the proviso $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_k\}} \{(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)\}$ (where $k \geq 0$) holds.
3. Return the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models (\sigma'; \rho')$.

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ from which the present diagram $(\sigma; \rho)$ comes from.
- **inferred_named_state** (NamedState) – The NamedState object $(\sigma'; \rho')$ derivable in the $n > 0$ cases provided by the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ in the `named_states` parameter.
- **named_states** (list) – The NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n), n > 0$ functioning as the set of n exhaustive cases from which F can be derived.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use for the interpretation of truth values and the computation of the basis of F_1, \dots, F_k .
- **variable_assignment** (VariableAssignment | None) – The VariableAssignment object χ to consider when computing the basis $\mathcal{B}(F_1, \rho, \chi) \cup \dots \cup \mathcal{B}(F_k, \rho, \chi)$ of F_1, \dots, F_k or None if all terms of the F_1, \dots, F_k are in ρ .
- **formulae** (Formula) – The $k \geq 0$ Formula objects F_1, \dots, F_k to use in the computation of the basis, computation of the proviso and the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models (\sigma'; \rho')$.

Returns The result of the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models (\sigma'; \rho')$.

Return type `bool`

Raises ValueError – If $k > 0$, the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n), n > 0$ are not exhaustive on the basis of the Formula objects F_1, \dots, F_k or the proviso $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_k\}} \{(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)\}$ (where $k \geq 0$) does not hold.

12.8 The [Sentential-to-Diagrammatic] rule

`inference_rules.sentential_to_diagrammatic` (*context*, *F1*, *F2*, *named_state*,
attribute_interpretation, *variable_assignment=None*)

Verify that a disjunction $F_1 \vee F_2$ holds in the Context object $(\beta; (\sigma; \rho))$ in the `context` parameter and that the NamedState object $(\sigma'; \rho')$ in the `named_state` parameter follows in either case, using the AttributeInterpretation object *I* in the `attribute_interpretation` parameter to interpret truth values.

This is rule $[C_2]$.

This function works as follows:

1. Verify that the disjunction $F_1 \cup F_2$ given by `F1` and `F2` parameters holds in the Context object $(\beta; (\sigma; \rho))$ given by `context` parameter.
2. Generate two new Context objects $\gamma_1 = (\beta_1; (\sigma; \rho))$ where $\beta_1 = \beta \cup F_1$ and $\gamma_2 = (\beta_2; (\sigma; \rho))$ where $\beta_2 = \beta \cup F_2$.
3. For all possible worlds $(w'; \hat{\rho}')$ and variable assignments χ of the NamedState object $(\sigma'; \rho')$, determine if the world $(w'; \hat{\rho}')$ satisfies both Context objects γ_1 and γ_2 , that is $(w'; \hat{\rho}') \models \gamma_1 \wedge (w'; \hat{\rho}') \models \gamma_2$.
4. If any world $(w'; \hat{\rho}')$ and variable assignments χ of the NamedState object $(\sigma'; \rho')$ does not satisfy both γ_1 and γ_2 , then **sentential-to-diagrammatic** does not hold, otherwise, **sentential-to-diagrammatic** holds.

In this way, we capture the idea that any world $(w'; \hat{\rho}')$ and variable assignments χ of the NamedState object $(\sigma'; \rho')$ (and thus the NamedState object $(\sigma'; \rho')$ itself) follows from the context $(\beta \cup \{F_1 \vee F_2\}; (\sigma; \rho))$ in either case of the disjunction $F_1 \vee F_2$.

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ in which the Formula objects in the parameters `F1` and `F2` apply and in which the NamedState object $(\sigma'; \rho')$ in `named_state` parameter would follow.
- **F1** (Formula) – The left operand of the disjunction F_1 .
- **F2** (Formula) – The right operand of the disjunction F_2 .
- **named_state** (NamedState) – The NamedState object $(\sigma'; \rho')$ potentially following the disjunction in either case.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object *I* to use for the interpretation of truth values.
- **variable_assignment** (VariableAssignment | None) – The optional VariableAssignment object χ to consider in the interpretation of truth values.

Returns Whether or not **sentential-to-diagrammatic** holds.

Return type `bool`

Raises **ValueError** – The disjunction $F_1 \vee F_2$ does not hold.

12.9 The [Diagrammatic-to-Sentential] rule

`inference_rules.diagrammatic_to_sentential` (*context*, *F*, *named_states*, *attribute_interpretation*, *variable_assignment*, **formulae*)

Verify that on the basis of the present diagram $(\sigma; \rho)$ of the Context object $(\beta; (\sigma; \rho))$ in the `context` parameter and some set of Formula objects F_1, \dots, F_k , $k \geq 0$ provided as optional positional arguments in the `formulae` parameter, that for each NamedState object $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$, $n > 0$, contained in the `named_states` parameter, a Formula object F provided in the `F` parameter can be derived in every one of these n cases.

This is rule $[C_3]$.

This function works as follows:

1. If $k > 0$ (i.e., if at least one Formula object is provided as an optional positional argument to the `formulae` parameter), compute the basis $\mathcal{B}(F_1, \rho, \chi) \cup \dots \cup \mathcal{B}(F_k, \rho, \chi)$ of F_1, \dots, F_k and determine if the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ provided in the `named_states` parameter form an exhaustive set of possibilities on this basis.
2. Determine if the proviso $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_k\}} \{(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)\}$ (where $k \geq 0$) holds.
3. Return the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models F$.

Parameters

- **context** (Context) – The Context object $(\beta; (\sigma; \rho))$ from which the present diagram $(\sigma; \rho)$ comes from.
- **F** (Formula) – The Formula object F derivable in the $n > 0$ cases provided by the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$ in the `named_state` parameter.
- **named_states** (list) – The NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$, $n > 0$ functioning as the set of n exhaustive cases from which F can be derived.
- **attribute_interpretation** (AttributeInterpretation) – The AttributeInterpretation object I to use for the interpretation of truth values and the computation of the basis of F_1, \dots, F_k .
- **variable_assignment** (VariableAssignment | None) – The VariableAssignment object χ to consider when computing the basis $\mathcal{B}(F_1, \rho, \chi) \cup \dots \cup \mathcal{B}(F_k, \rho, \chi)$ of F_1, \dots, F_k or None if all terms of the F_1, \dots, F_k are in ρ .
- **formulae** (Formula) – The $k \geq 0$ Formula objects F_1, \dots, F_k to use in the computation of the basis, computation of the proviso and the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models F$.

Returns The result of the evaluation of $(\beta \cup \{F_1, \dots, F_k\}; (\sigma; \rho)) \models F$.

Return type `bool`

Raises ValueError – If $k > 0$, the NamedState objects $(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)$, $n > 0$ are not exhaustive on the basis of the Formula objects F_1, \dots, F_k or the proviso $(\sigma; \rho) \Vdash_{\{F_1, \dots, F_k\}} \{(\sigma_1; \rho_1), \dots, (\sigma_n; \rho_n)\}$ (where $k \geq 0$) does not hold.

PARSERS

13.1 The ParserSet object

parser_set module.

class parser_set.ParserSet

ParserSet class. The ParserSet object functions as a sequence/collection. The ParserSet class is part of the vivid object extension protocol.

Variables

- **parsers** – The parsers contained in the ParserSet object.
- **_is_ParserSet** – An identifier to use in place of `type` or `isinstance`.

__getitem__ (*key*)

Retrieve the parser located at the index given by `key` parameter via indexing (e.g. `ParserSet[key]`).

Parameters **key** (*int*) – The index to use for retrieval.

Raises **TypeError** – `key` parameter must be an index.

__init__ ()

Construct a ParserSet object.

__iter__ ()

Provides an iterator for ParserSet (e.g. “for parser in ParserSet:”).

__len__ ()

Determine the length of the ParserSet object via the `len` built-in function e.g. (`len(ParserSet)`).

13.2 The PointParser object

point_parser module.

class point_parser.PointParser

PointParser class. The PointParser class is used for parsing Point object related expressions.

Variables **_is_Parser** – An identifier to use in place of `type` or `isinstance`.

__call__ (*args)

Call PointParser object (e.g., `PointParser(expression)`).

__init__ ()

Construct a PointParser object.

`_eval` (*string*)

Try to evaluate given string (e.g., “`is_on(P(2.0,2.0),P(1.0,1.0),P(3.0,3.0))`”).

Parameters **string** (*str*) – The expression to evaluate; the `PointParser` object unstringifies `Point` objects in *string* parameter and tries to call a function of the `Point` object (also given by *string* parameter) with unstringified `Points` as arguments.

Raises **ValueError** – Function provided in *string* parameter is not a function in the `Point` class, some argument is not a `Point` after trying to unstringify or the *string* parameter is improperly formatted.

13.3 The `TruthValueParser` object

`truth_value_parser` module.

class `truth_value_parser.TruthValueParser`

`TruthValueParser` class. `TruthValueParser` provides parsing functionality for entirely mathematical/logical strings.

Variables **`_is_Parser`** – An identifier to use in place of `type` or `isinstance`.

`__call__` (**args*)

Call `TruthValueParser` object (e.g., `TruthValueParser(expression)`).

`__init__` ()

Construct a `TruthValueParser` object.

`_eval` (*string*)

Try to evaluate given string in *string* parameter. (e.g., “`(4 < 5 * cos(2 * PI) and 4*e^3 > 3 *(3 + 3))and!(2 < 3)`”).

Parameters **string** (*str*) – The expression to evaluate.

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