15-213 Recitation: Data Lab

Jack Biggs 25 Jan 2016

Agenda

- Introduction
- Course Details
- Data Lab
 - Getting started
 - Running your code
 - ANSI C
- Bits & Bytes
- Integers
- Floating Point

Introduction

- Welcome to 15-213/18-213/15-513!
- Recitations are for...
 - Reviewing lectures
 - Discussing homework problems
 - Interactively exploring concepts
 - Previewing future lecture material

Please, please ask questions!

Course Details

- How do I get help?
 - Course website: http://cs.cmu.edu/~213
 - Office hours: 5-9PM from Sun-Thu in Wean 5207
 - Staff mailing list: <u>15-213-staff@cs.cmu.edu</u>
 - Definitely consult the course textbook
 - Carefully read the assignment writeups!
- All labs are submitted on Autolab.
- All labs should be worked on using the shark machines.

Data Lab: Getting Started

- Download lab file (datalab-handout.tar)
 - Upload tar file to shark machine
 - cd <my course directory>
 - tar xpvf datalab-handout.tar
- <filename>: Permission denied
 - chmod +x <filename>
- Upload bits.c file to Autolab for submission

Data Lab: Running your code

- dlc: a modified C compiler that interprets ANSI C only
- btest: runs your solutions on random values
- bddcheck: exhaustively tests your solutions
 - Checks all values, formally verifying the solution
- driver.pl: Runs both dlc and bddcheck
 - Exactly matches Autolab's grading script
 - You will likely only need to submit once
- For more information, read the writeup
 - Available under assignment page as "View writeup"
 - Read it. Read the writeup... please.

Data Lab: What is ANSI C?

Within two braces, all declarations must go before any expressions.

This is *not* ANSI C.

```
unsigned int foo(unsigned int x)
   x = x * 2;
    int y = 5;
   if (x > 5) {
       x = x * 3;
       int z = 4;
       x = x * z;
    return x * y;
```

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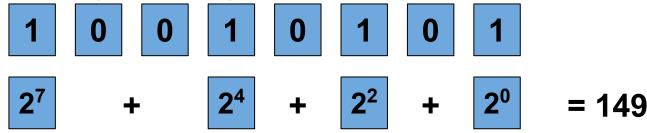
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Bits & Bytes: Unsigned integers

- An unsigned number represents positive numbers between 0 and 2^k-1, where k is the numbers of bits used.
- Subtracting 1 from 0 will underflow to the highest value.
- Adding 1 to the highest value will overflow to 0

An 8-bit unsigned integer:

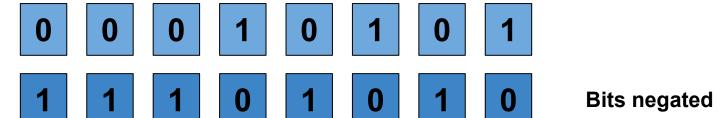


- In C, a *signed* number represents numbers between [-2 ^{k-1}, 2^{k-1}-1], where *k* is the number of bits used.
- Overflow and underflow (from max > 0 and min < 0 values) is undefined with signed numbers in C
 - Depending on the underlying architecture, signed overflow / underflow could modulo, do nothing, or even abort the program
- The highest-level bit is set to 1 in negative numbers.
- To get the negative value of a positive number x, invert the bits of x and add 1.

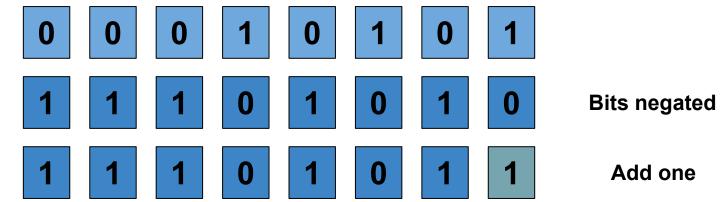
From positive to negative:

0 0 1 0 1

From positive to negative:



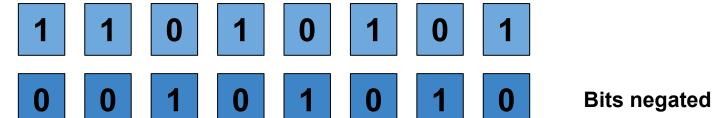
From positive to negative:



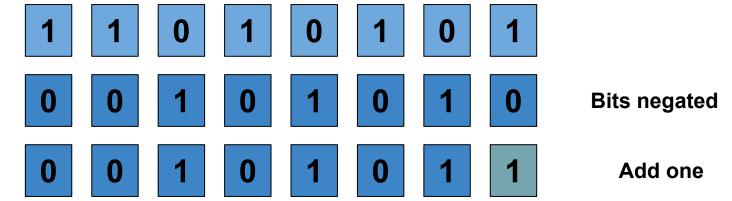
From negative to positive:

1 1 0 1 0 1

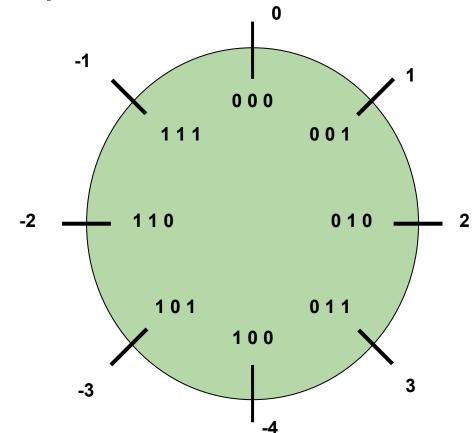
From negative to positive:



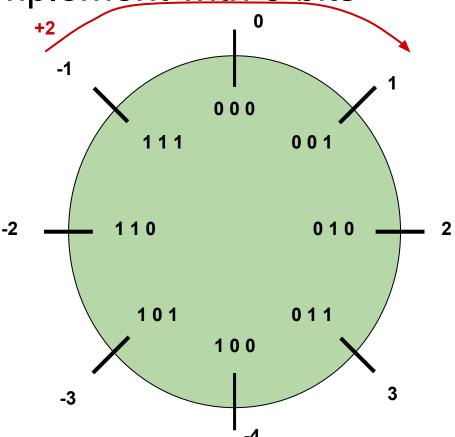
From negative to positive:



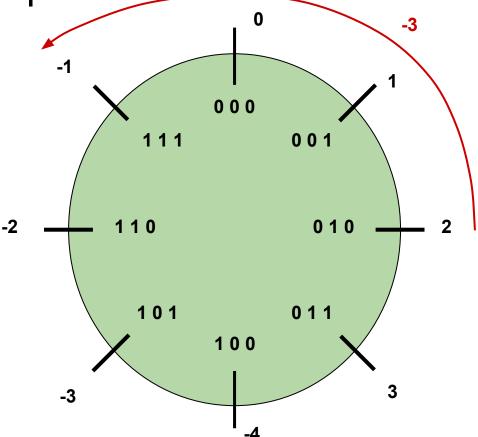
- Why would anybody want to do this?
 - Uses the same circuitry for addition and subtraction!
- Note that there is no positive 4: the two's complement of -4 with three bits is -4

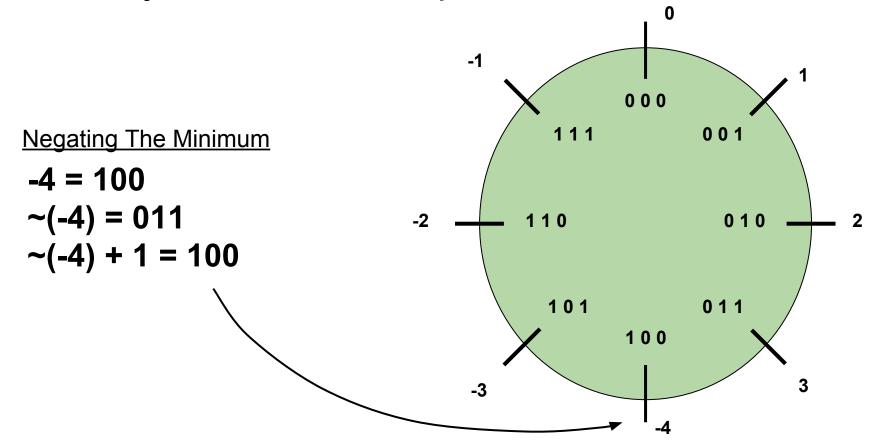


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AND: &&

<u>OR: ||</u>

EQ: ==

NOT: !

!15213 =

AND: &&

<u>OR: ||</u>

EQ: ==

NOT: !

!15213 =

$$15 == 18 = 0$$

$$15 == 18 = 0$$

$$!15213 = 0$$

<u>AND: &</u>	<u>OR: </u>	<u>XOR: ^</u>	<u>NOT: ~</u>
01100101	01100101	01100101	
& 11101101	11101101	^ 11101101	~11101101

<u>AND: &</u>	<u>OR:</u>	<u>XOR: ^</u>	<u>NOT: ∼</u>
01100101	01100101	01100101	
<u>8</u> 11101101	11101101	^ 11101101	~11101101
01100101	11101101		

<u>AND: &</u>	<u>OR:</u>	<u>XOR: ^</u>	<u>NOT: ~</u>
01100101	01100101	01100101	
<u>* 11101101</u>	11101101	<u>^ 11101101</u>	~11101101
01100101	11101101	10001000	

<u> AND: &</u>	<u>OR: </u>	<u>XOR: ^</u>	<u>NOT: ~</u>
01100101	01100101	01100101	
<u>8</u> 11101101	11101101	^ 11101101	~11101101
01100101	11101101	10001000	00010010

Bits & Bytes: Shifting

Shifting modifies the positions of bits in a number:

Shifting right on a signed number will extend the sign:

(If the sign bit is zero, it will fill in with zeroes instead.)

This is known as "arithmetic" shifting.

Bits & Bytes: Shifting

Shifting right on an unsigned number will fill in with 0.

This is known as "logical" shifting.

Arithmetic shifting is useful for preserving the sign when dividing by a power of 2. We get around this when we don't need it by using *bitmasks*.

In other languages, such as Java, it is possible to choose shifting operators, regardless of the type of integer. In C, however, it depends on the signedness.

Bits & Bytes: Endianness (Byte Order)

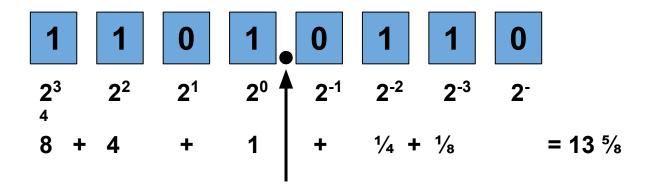
- Endianness describes which byte in a number comes first in memory. This is important for bomb lab.
- Little-Endian machines store the lowest-order byte first.
 - Intel machines (the shark machines!) are little-endian.

```
Oxdeadbeef: Ox ef be ad de
```

- Big-Endian machines store the highest-order byte first.
 - The Internet is big-endian
 - How we think about binary numbers normally

```
Oxdeadbeef: Ox de ad be ef
```

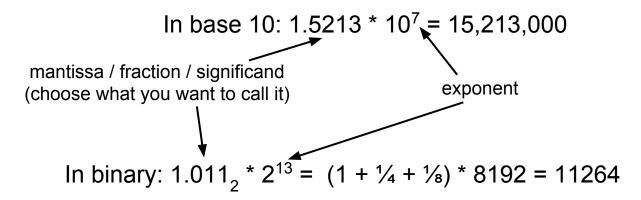
Floating Point: "Fixed" Point Representation



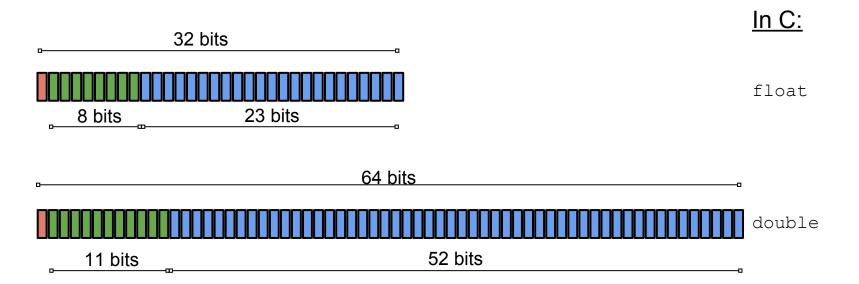
- Bits to the right of the "binary point" represent smaller fractions
- Difficult to represent a wide range of numbers
 - In this example, can't represent a number larger than 16
 - Can we sacrifice a bit of precision to accomplish this?

Floating Point: Scientific Notation

In Scientific Notation, we represent a number as a fraction multiplied by an exponentiated scaling factor.



Floating Point: IEEE Standard

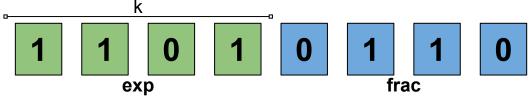


Floating Point: Sign and Exponent

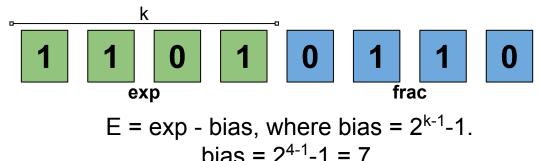
```
s exp frac
```

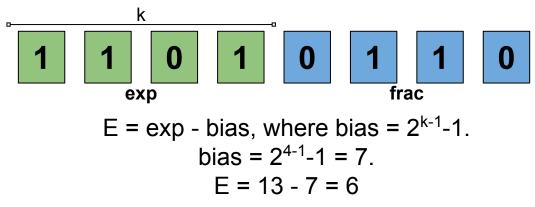
- If sign is 1, then the number is negative.
- The exponent determines three different value types.
 - Normalized: 0 != exp != 1111₂...
 - Mantissa = s * 1.frac
 - **Denormalized**: exp = 0
 - Mantissa = s * 0.frac
 - Special: $exp = 1111_2...$
- Neither exp nor frac use two's complement!

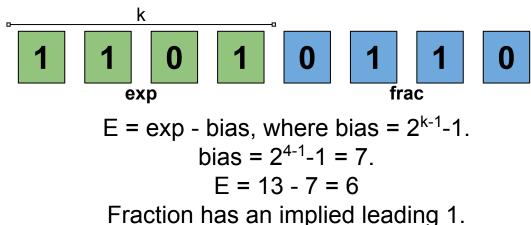
Consider a floating point implementation based on the IEEE floating point standard. This implementation omits the sign bit, and uses 4 bits for the exponent and 4 bits for the fraction.

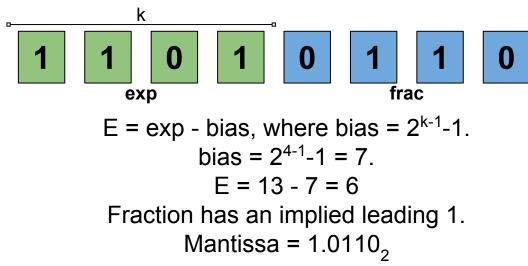


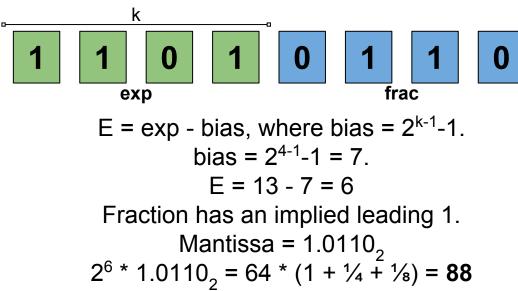
 $E = \exp - bias$, where $bias = 2^{k-1}-1$.

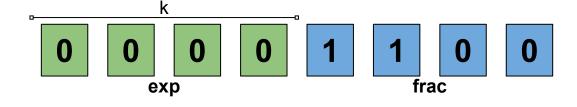




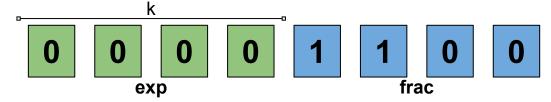




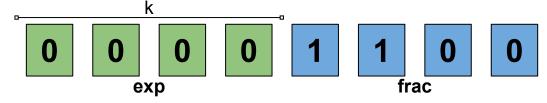




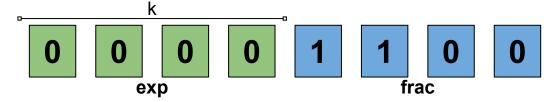
E = 1 - bias, and bias = 7 as before.



E = 1 - bias, and bias = 7 as before. Fraction has an implied leading 0.



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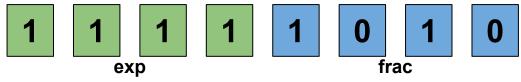


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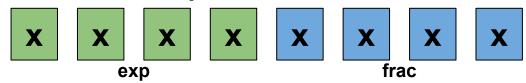
Final answer: $2^{-6} * (0 + \frac{1}{2} + \frac{1}{4}) = 0.01171875$

Floating Point Example: Special Values

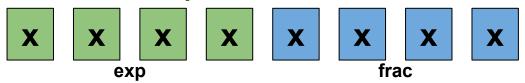
- 1 1 1 0 0 0 0 0
- Exp is all 1
- If fraction is all 0, then represents infinity
 - Also, -Infinity (if we had a sign bit)



- If fraction != 0, then represents NaN (Not a Number!)
- Sign bit doesn't really matter, but either can turn up
 - (Mostly from division errors)



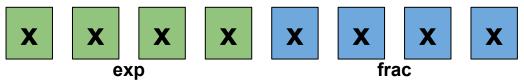
- What is the largest denormalized number?
- What is the smallest normalized number?
- What is the largest finite number it can represent?
- What is the smallest non-zero value it can represent?



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0000 1111 =
$$0.1111_2 * 2^{-6} = 0.0146484375$$

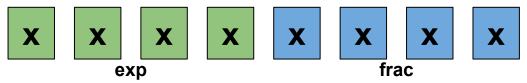
(recall that E = 1 - bias, and bias = 7 in this example)



- What is the largest denormalized number?
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$$E = 1 - 7 = -6$$

Answer:
$$1.0000_2 * 2^{-6} = 2^{-6} = 1/64$$

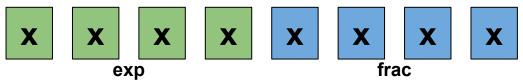


- What is the largest denormalized number?
- What is the smallest normalized number?
- What is the largest finite number it can represent?
- What is the smallest non-zero value it can represent?

1110 1111

$$E = 14 - 7 = 7$$

Answer: 1.1111₂ * 2⁷ = 248



- What is the largest denormalized number?
- What is the smallest normalized number?
- What is the largest finite number it can represent?
- What is the smallest non-zero value it can represent?

$$0000\ 0001$$
= 0.0001_2 * 2^{-6} = 0.0009765625
(recall that E = 1 - bias, and bias = 7 in this example)

Floating Point: Rounding 1.BBGRXXX

In the below examples, imagine the underlined part as a fraction.

- Guard Bit: the least significant bit of the resulting number
- Round Bit: the first bit removed from rounding
- Sticky Bits: all bits after the round bit, OR'd together

Examples of rounding cases, including rounding to nearest even number

- 1.10¦11: More than ½, round up: 1.11
- 1.10 10: Equal to 1/2, round down to even: 1.10
- 1.01 101: Less than 1/2, round down: 1.01
- 1.01 10: Equal to ½, round up to even: 1.10
- 1.01\overline{00}: Equal to 0, do nothing: 1.01
- 1.00 00: Equal to 0, do nothing: 1.00

All other cases involve either rounding up or down - try them!

Questions?

- Remember, data lab is due this Thursday!
 - You really should have started already!
- Read the lab writeup.
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 - **■** Please.:)