

$$\text{Info}(D) \cdot I(9,5) = -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \frac{5}{14} = 0.940$$

| age | income | student | credit_rating | buys_computer |
|---------|--------|---------|---------------|---------------|
| <=30 | high | no | fair | no |
| <=30 | high | no | excellent | no |
| 31...40 | high | no | fair | yes |
| >40 | medium | no | fair | yes |
| >40 | low | yes | fair | yes |
| >40 | low | yes | excellent | no |
| 31...40 | low | yes | excellent | yes |
| <=30 | medium | no | fair | no |
| <=30 | low | yes | fair | yes |
| >40 | medium | yes | fair | yes |
| <=30 | medium | yes | excellent | yes |
| 31...40 | medium | no | excellent | yes |
| 31...40 | high | yes | fair | yes |
| >40 | medium | no | excellent | no |

age

| | ≤30 | 31...40 | >40 |
|-----|-----|---------|-----|
| Yes | 2 | 4 | 3 |
| No | 3 | 0 | 2 |

$$\text{Info}_{\text{age}}(D) = \frac{5}{14} I(2,1) + \frac{9}{14} I(4,0)$$

$$= \frac{5}{14} I(1,2) = 0.694$$

$$\text{Gain}_{\text{age}} = \text{Info}(D) - \text{Info}_{\text{age}}(D)$$

$$= 0.940 - 0.694 = 0.246$$

student

| student | buys_computer |
|---------|---------------|
| no | no |
| no | no |
| no | yes |
| no | yes |
| yes | yes |
| yes | no |
| yes | yes |
| no | no |
| yes | yes |
| yes | yes |
| no | yes |
| yes | yes |
| no | no |

| | yes | no |
|-----|-----|----|
| Yes | 6 | 3 |
| No | 1 | 4 |

$$\text{Info}_{\text{student}}(D) = \frac{7}{14} I(6,1) + \frac{7}{14} I(3,4) = 0.7885$$

$$\text{Gain}_{\text{student}} = \text{Info}(D) - \text{Info}_{\text{student}}(D)$$

$$= 0.151$$

credit-rating

$$\text{Gain}_{\text{credit}} = 0.246$$

$$\text{Gain}_{\text{income}} = 0.029$$

$$\text{Gain}_{\text{student}} = 0.151$$

$$\text{Gain}_{\text{credit}} = 0.048$$

age > student > credit > income

income

| income | buys_computer |
|--------|---------------|
| high | no |
| high | no |
| high | yes |
| medium | yes |
| low | yes |
| low | no |
| medium | yes |
| medium | no |
| low | yes |
| medium | yes |
| medium | yes |
| high | yes |
| medium | no |

| | low | medium | high |
|-----|-----|--------|------|
| yes | 3 | 4 | 2 |
| no | 1 | 2 | 2 |

$$\text{Info}_{\text{income}}(D) = \frac{4}{14} I(3,1) + \frac{6}{14} I(4,2)$$

$$+ \frac{4}{14} I(2,2)$$

$$= 0.911$$

$$\text{Gain}_{\text{income}} = \text{Info}(D) - \text{Info}_{\text{income}}(D)$$

$$\text{Gain}_{\text{income}} = 0.029$$

credit-rating

| credit_rating | buys_computer |
|---------------|---------------|
| fair | no |
| excellent | no |
| fair | yes |
| fair | yes |
| fair | yes |
| excellent | no |
| excellent | yes |
| fair | no |
| fair | yes |
| fair | yes |
| excellent | yes |
| excellent | yes |
| fair | yes |
| excellent | no |

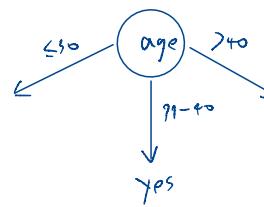
| | fair | excellent |
|-----|------|-----------|
| yes | 6 | 3 |
| no | 2 | 3 |

$$\text{Info}_{\text{credit}}(D) = \frac{8}{14} I(6,1) + \frac{6}{14} I(3,3)$$

$$= 0.842$$

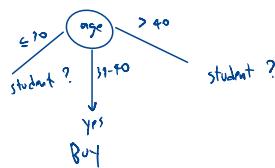
$$\text{Gain}_{\text{credit}} = \text{Info}(D) - \text{Info}_{\text{credit}}(D)$$

$$= 0.078$$



student > credit > income

| age | student | buys_computer |
|-----------|---------|---------------|
| ≤ 30 | no | no |
| ≤ 30 | no | no |
| ≤ 30 | yes | no |
| > 40 | no | yes |
| > 40 | yes | yes |
| > 40 | yes | no |
| ≤ 30 | yes | no |
| ≤ 30 | yes | yes |
| > 40 | yes | yes |
| ≤ 30 | yes | yes |
| ≤ 30 | yes | no |
| > 40 | no | no |



$$Info(C) = I(5,5) = 1$$

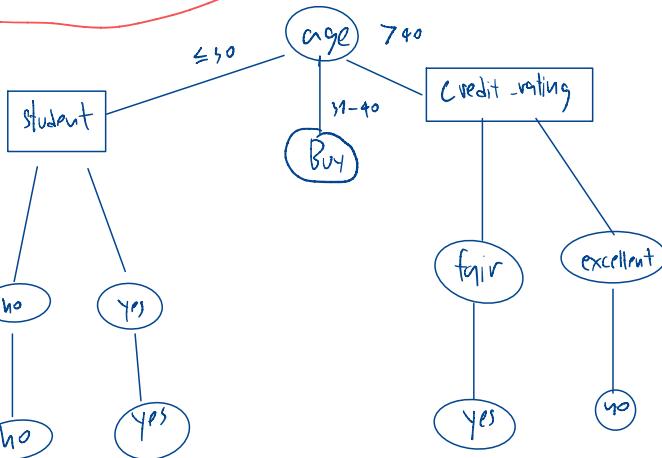
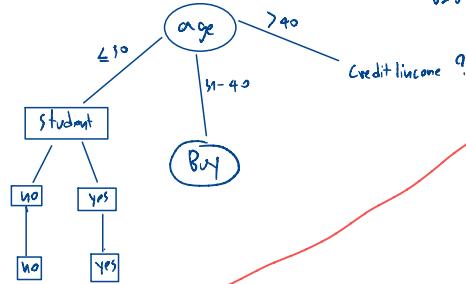
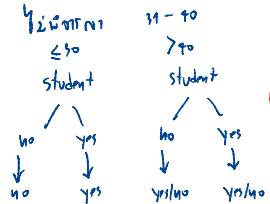
$$Info_{\leq 30}(0) = \frac{2}{5}(2,0) + \frac{3}{5}(0,1) = 0$$

$$Info_{> 40}(0) = \frac{3}{5}(2,1) + \frac{2}{5}(1,1) = 0.951$$

$$Gain(\leq 30) = 1 - 0.1$$

$$Gain(> 40) = 1 - 0.951 = 0.049$$

≤ 30 > 40
 ≤ 30 > 40



| age | income | student | credit_rating | buys_computer |
|-----------|--------|---------|---------------|---------------|
| ≤ 30 | high | no | fair | no |
| ≤ 30 | high | no | excellent | no |
| ≤ 30 | high | yes | fair | no |
| > 40 | medium | no | fair | yes |
| > 40 | low | no | fair | yes |
| > 40 | low | no | excellent | no |
| ≤ 30 | low | no | fair | no |
| ≤ 30 | medium | no | fair | no |
| ≤ 30 | medium | no | excellent | no |
| > 40 | medium | no | fair | yes |
| > 40 | medium | no | excellent | no |
| > 40 | medium | yes | fair | no |
| > 40 | medium | yes | excellent | no |

$$Info(C) = I(3,2) = -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} = 0.970$$

$$Info_{credit}(C) = \frac{3}{5} I(1,0) + \frac{2}{5} I(0,1) = 0$$

$$Info_{income}(C) = \frac{3}{5} I(2,1) + \frac{2}{5} I(1,1) = 0.951$$

$$Gain(Credit) = 0.970 - 0 = 0.970$$

$$Gain(Credit) = 0.970 - 0.951 = 0.019$$

credit > income

Gain Credit