

Loop Closure Detection Using the NDT

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Outline

- Background introduction
- Technical Approach Explanation
- Results Presentation
- Future Expectation



Doctoral Dissertation

The Three-Dimensional Normal-Distributions Transform
— an Efficient Representation for Registration,
Surface Analysis, and Loop Detection

MARTIN MAGNUSSON
Technology

Appearance-Based Loop Detection from 3D Laser Data Using the Normal Distributions Transform

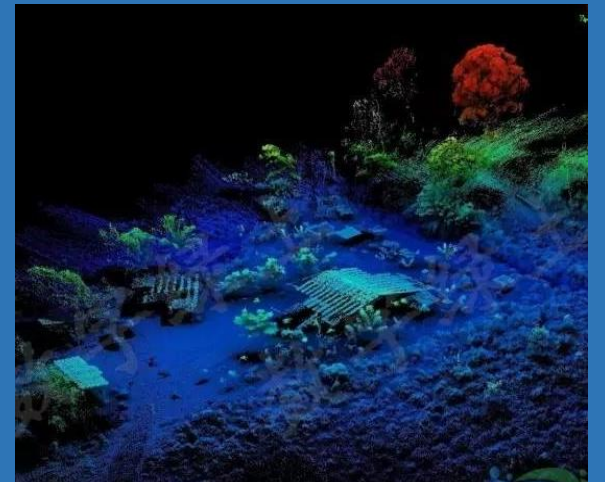
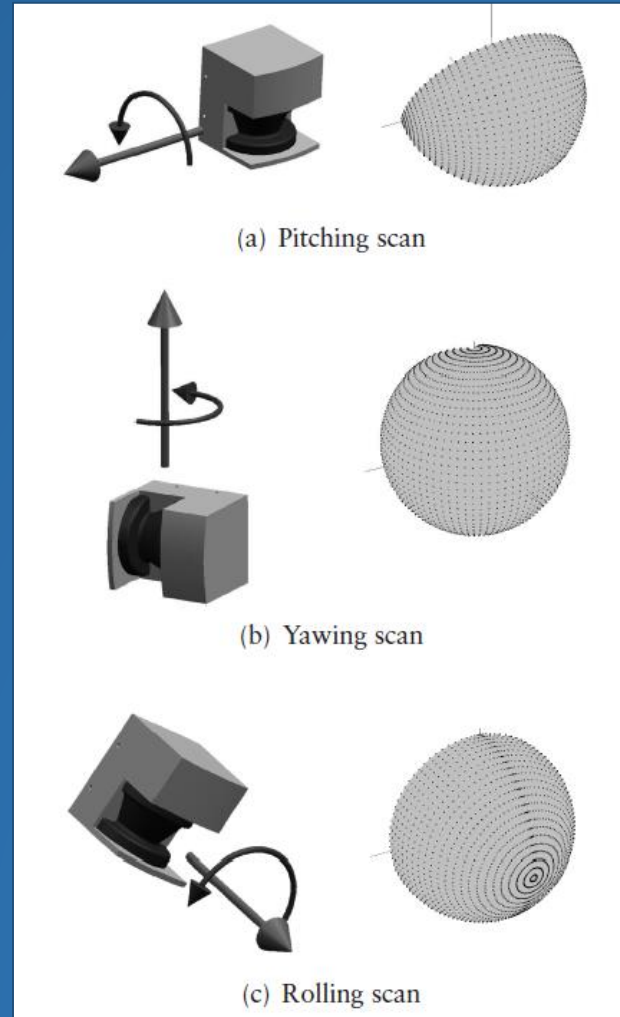
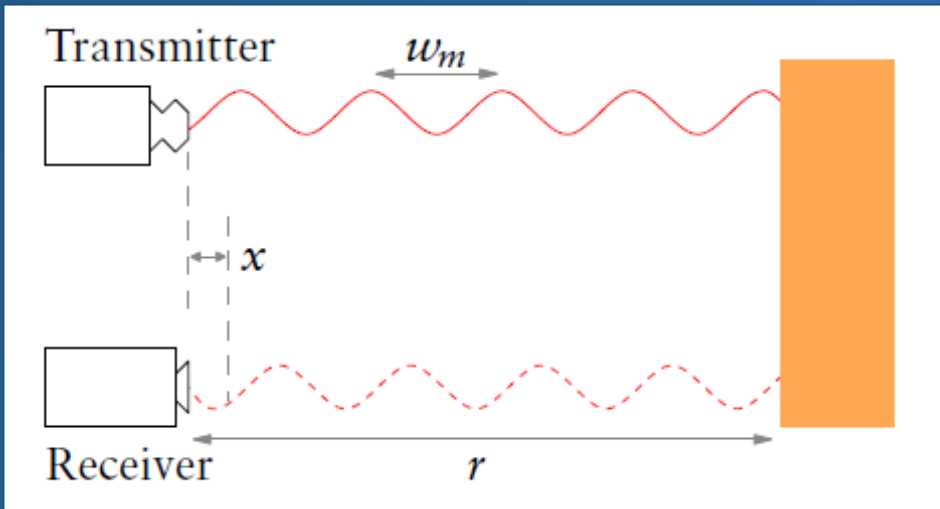
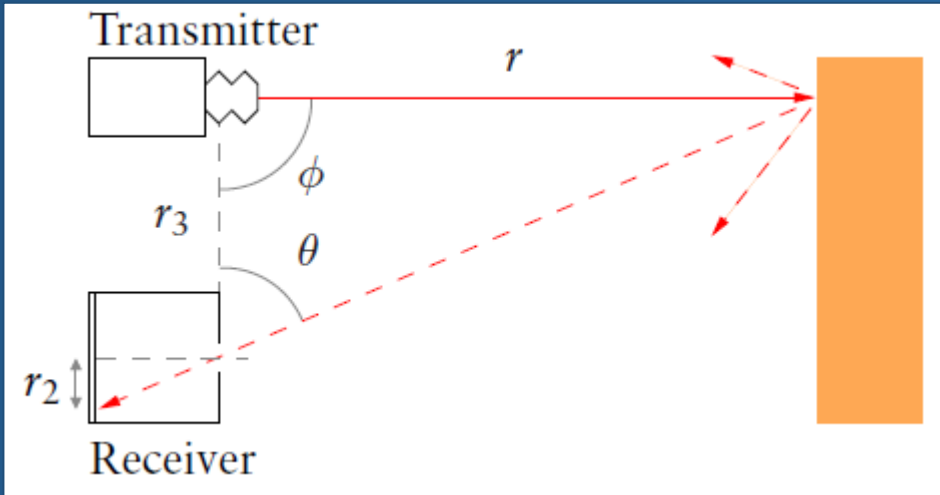
Martin Magnusson, Henrik Andreasson, Andreas Nüchter, and Achim J. Lilienthal



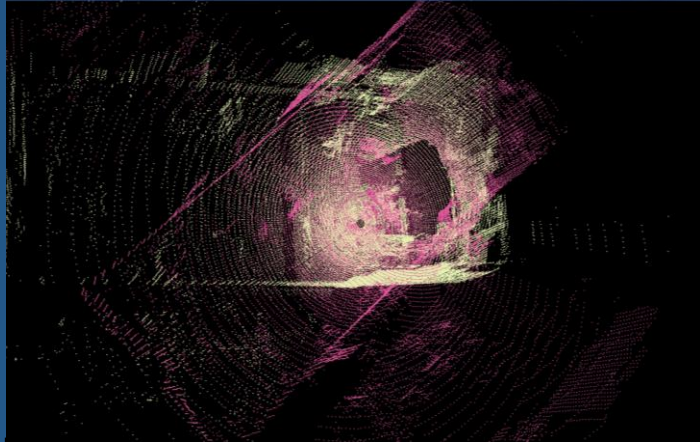
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Background

Range Sensing: Lidar



SLAM

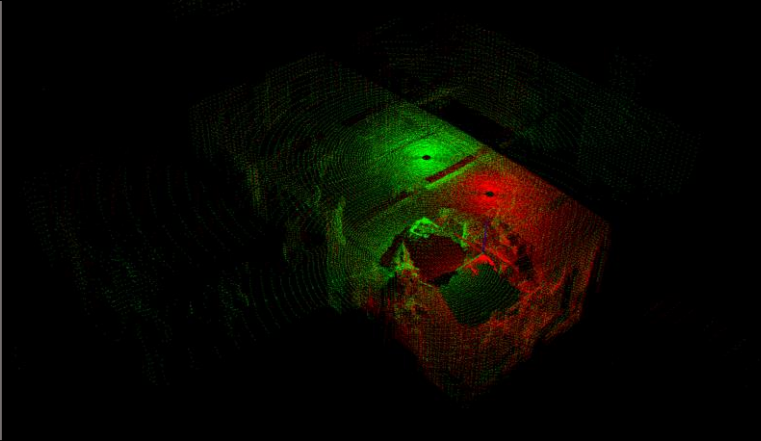


3D Scan
Point Cloud

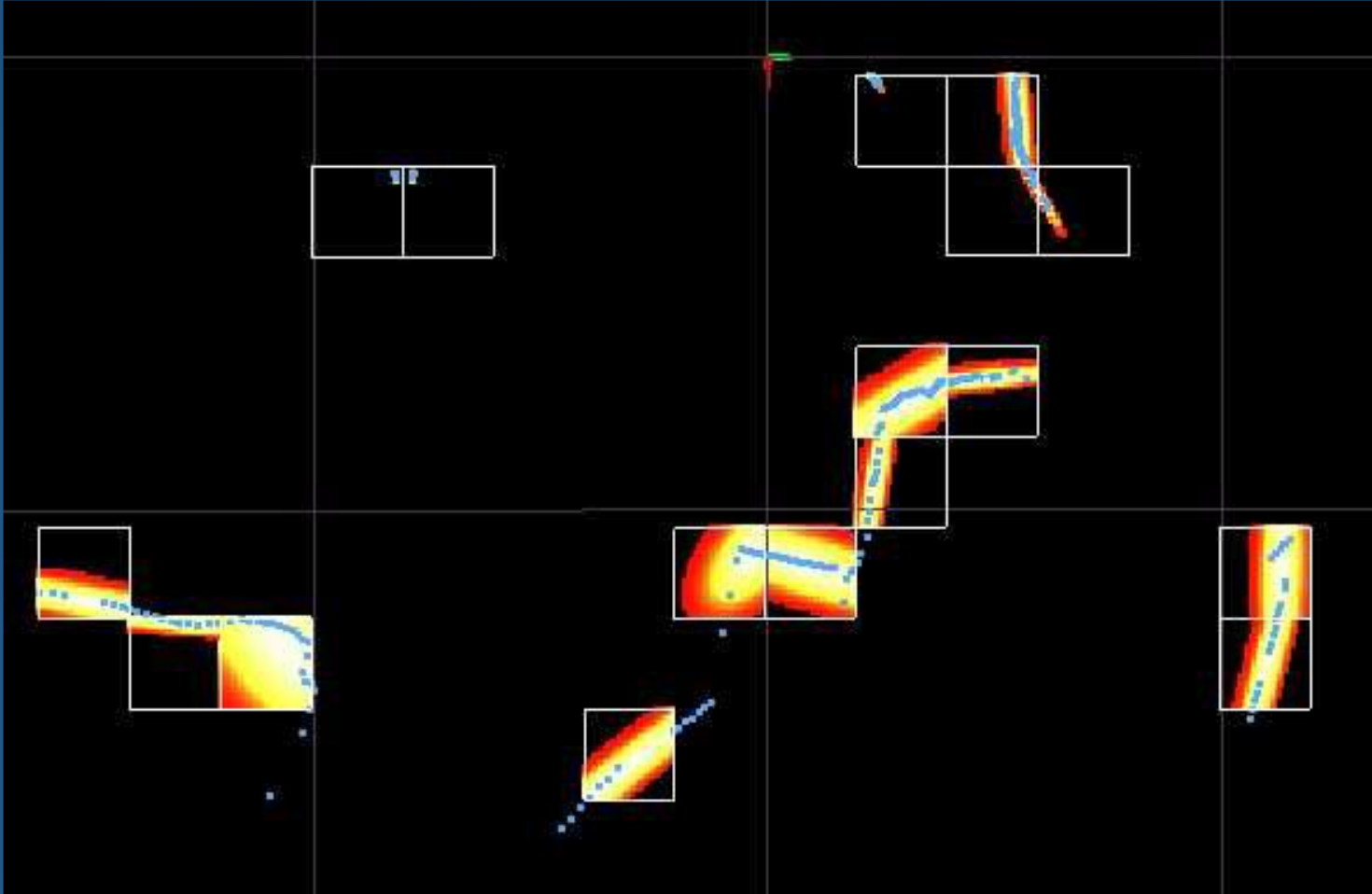
Registration



Loop Detection
& Relaxation



NDT for registration



Mean Vector

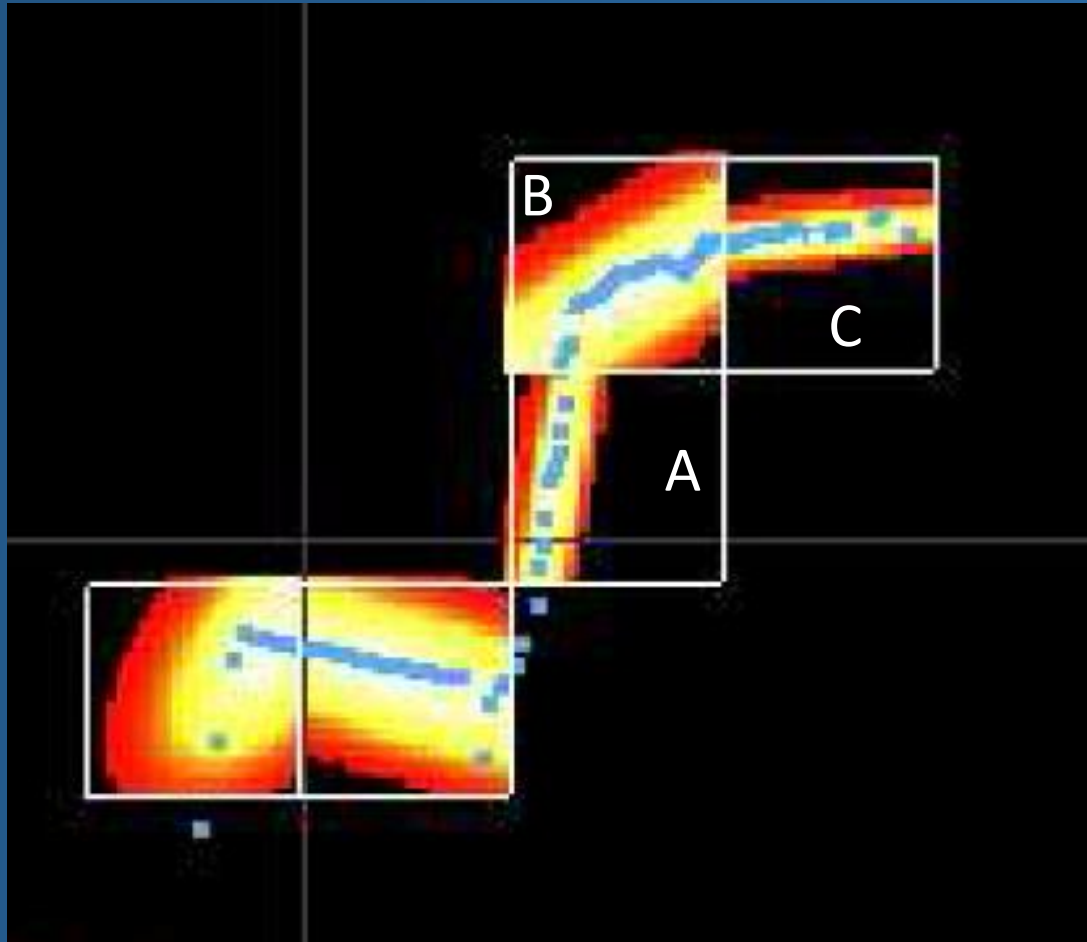
$$\vec{\mu} = \frac{1}{m} \sum_{k=1}^m \vec{y}_k,$$
$$\Sigma = \frac{1}{m-1} \sum_{k=1}^m (\vec{y}_k - \vec{\mu})(\vec{y}_k - \vec{\mu})^T,$$

Covariance Matrix

Probability Density Functions

$$p(\vec{x}) = \frac{1}{(2\pi)^{D/2} \sqrt{|\Sigma|}} \exp \left(-\frac{(\vec{x} - \vec{\mu})^T \Sigma^{-1} (\vec{x} - \vec{\mu})}{2} \right)$$

NDT for registration

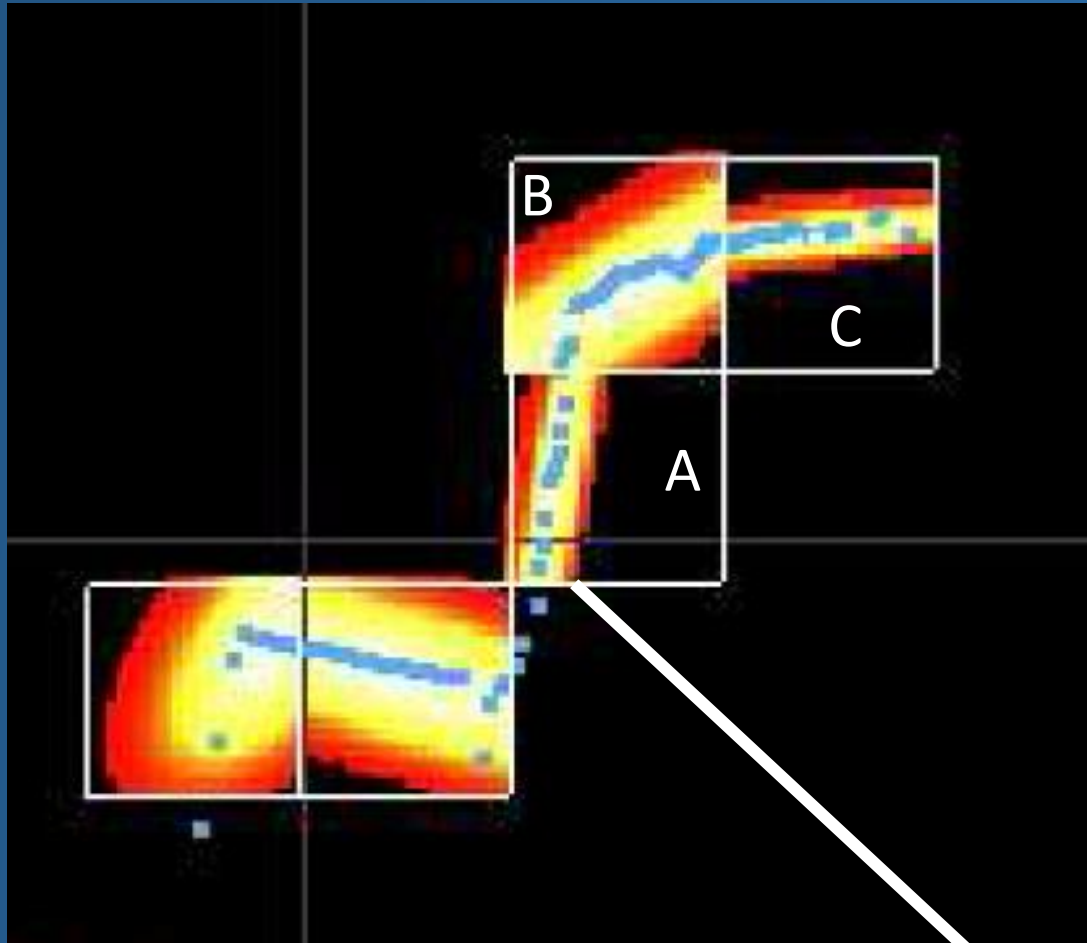


$$\Sigma = \frac{1}{m-1} \sum_{k=1}^m (\vec{y}_k - \vec{\mu})(\vec{y}_k - \vec{\mu})^T,$$

$$\begin{bmatrix} \text{cov}(X_1, X_1) & \text{cov}(X_1, X_2) & \cdots & \text{cov}(X_1, X_n) \\ \text{cov}(X_2, X_1) & \text{cov}(X_2, X_2) & \cdots & \text{cov}(X_2, X_n) \\ & & \ddots & \\ \text{cov}(X_n, X_1) & \text{cov}(X_n, X_2) & \cdots & \text{cov}(X_n, X_n) \end{bmatrix}_{n \times n}$$



NDT for registration

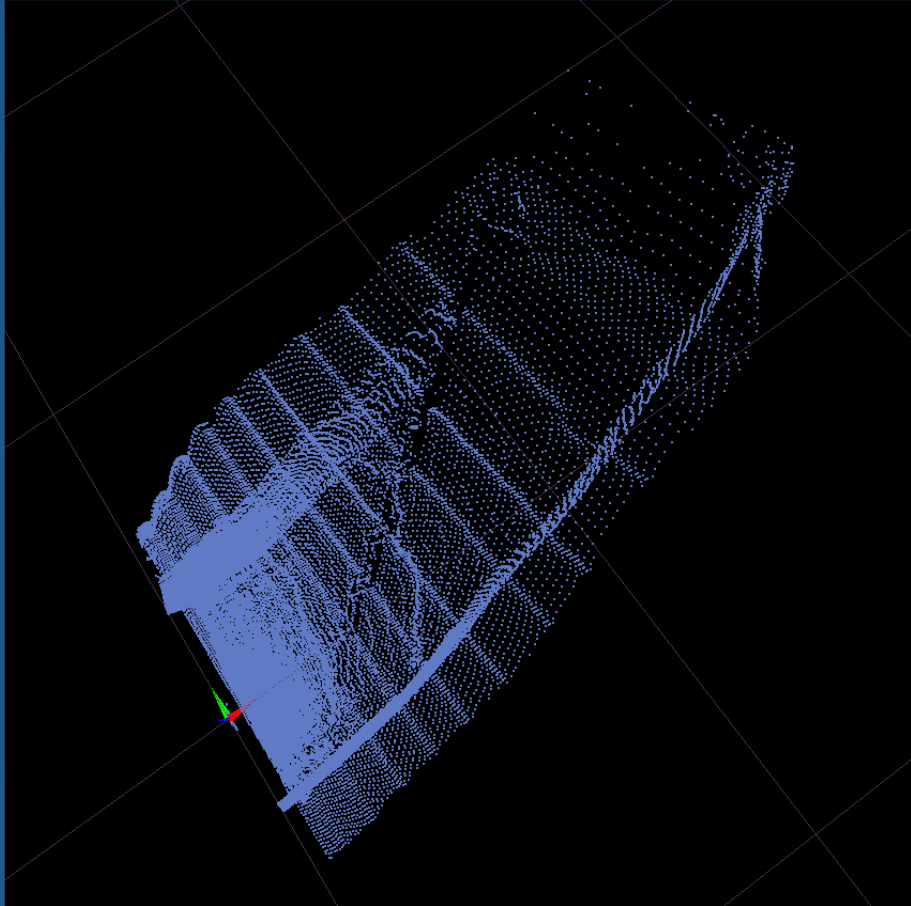


$$\Sigma = \frac{1}{m-1} \sum_{k=1}^m (\vec{y}_k - \vec{\mu})(\vec{y}_k - \vec{\mu})^T,$$

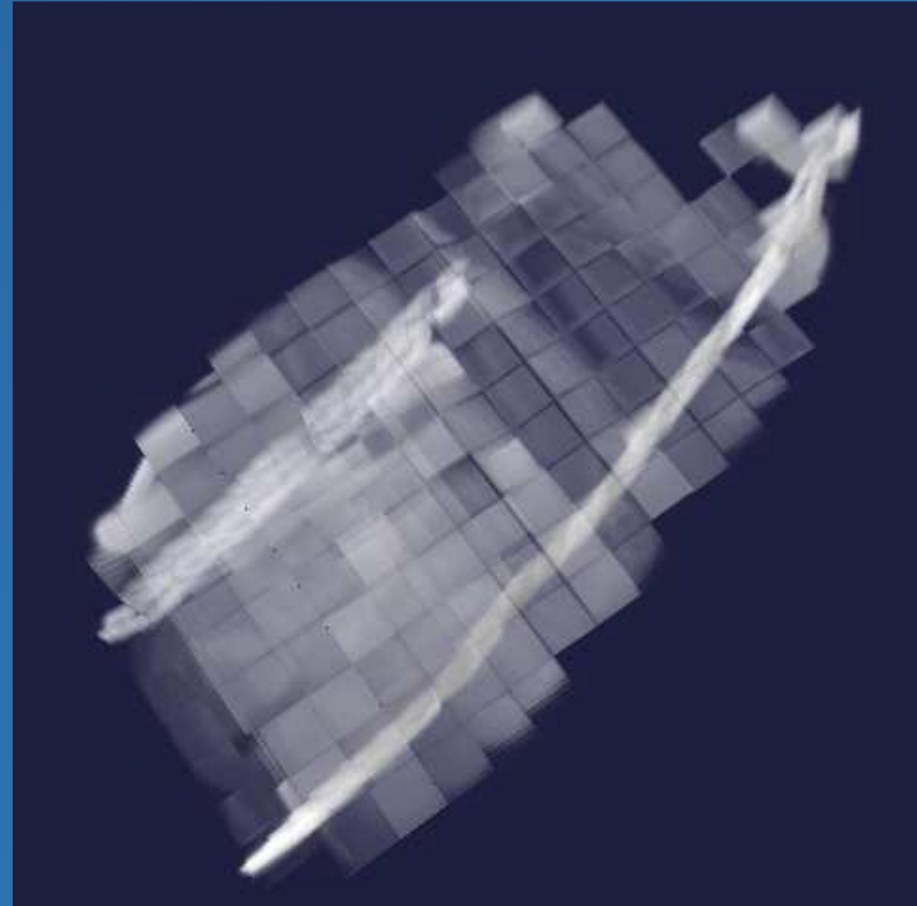
$$\begin{bmatrix} \text{cov}(X_1, X_1) & \text{cov}(X_1, X_2) & \cdots & \text{cov}(X_1, X_n) \\ \text{cov}(X_2, X_1) & \text{cov}(X_2, X_2) & \cdots & \text{cov}(X_2, X_n) \\ & & \ddots & \\ \text{cov}(X_n, X_1) & \text{cov}(X_n, X_2) & \cdots & \text{cov}(X_n, X_n) \end{bmatrix}_{n \times n}$$



3D NDT



Original point cloud



NDT representation

high compression ratio



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3D NDT

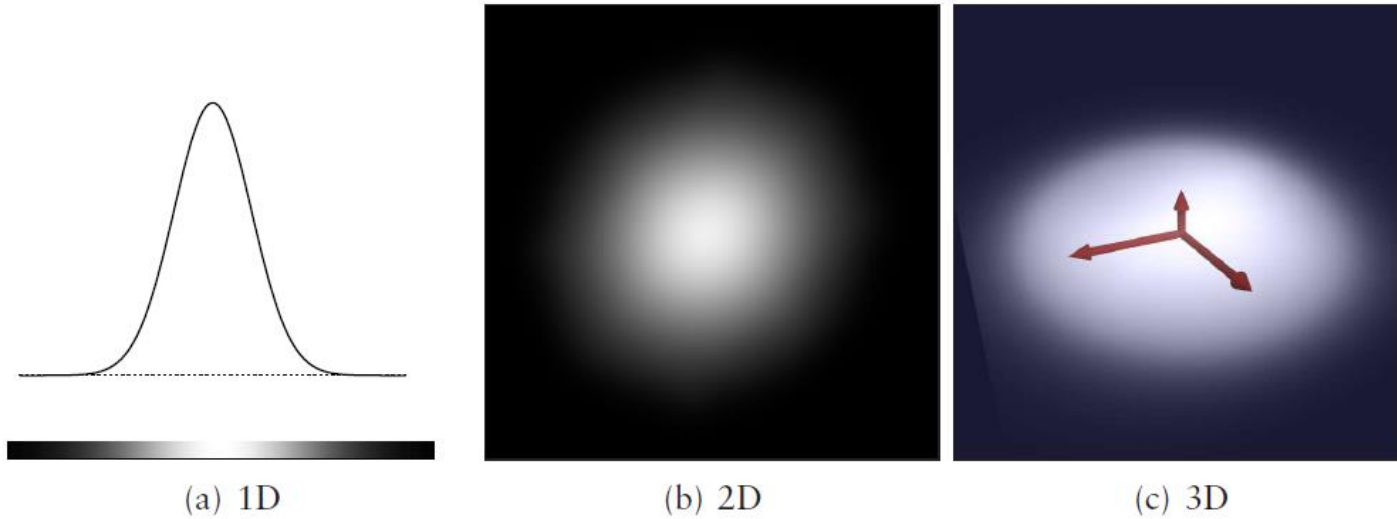
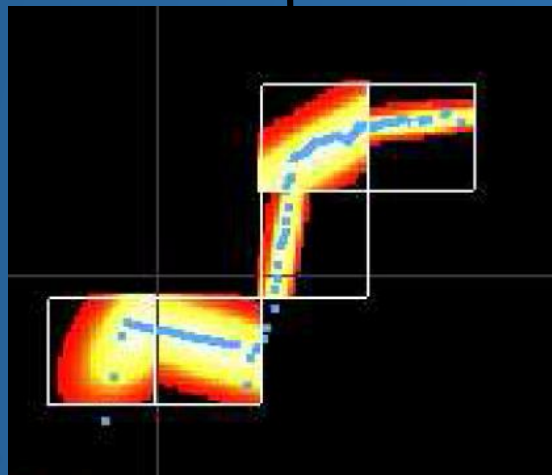


Figure 6.3: Normally-distributed PDFs in one, two, and three dimensions.

Eigenvectors & Eigenvalues
of the covariance matrix



Orientation & Smoothness



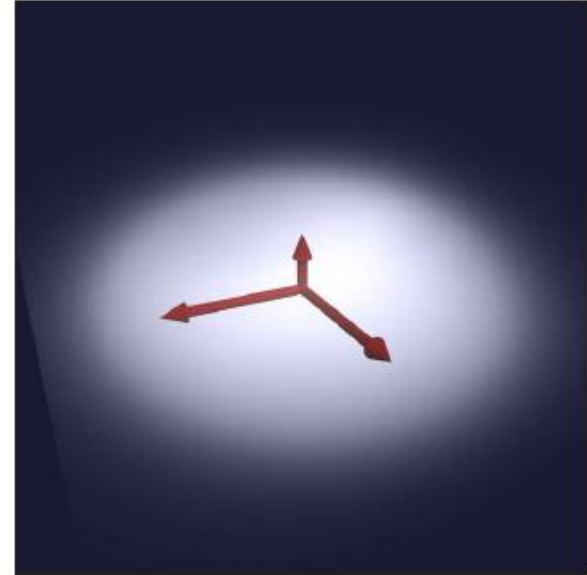
3D NDT



(a) Spherical: All eigenvalues approximately equal.



(b) Linear: One eigenvalue much larger than the other two.



(c) Planar: One eigenvalue much smaller than the others.

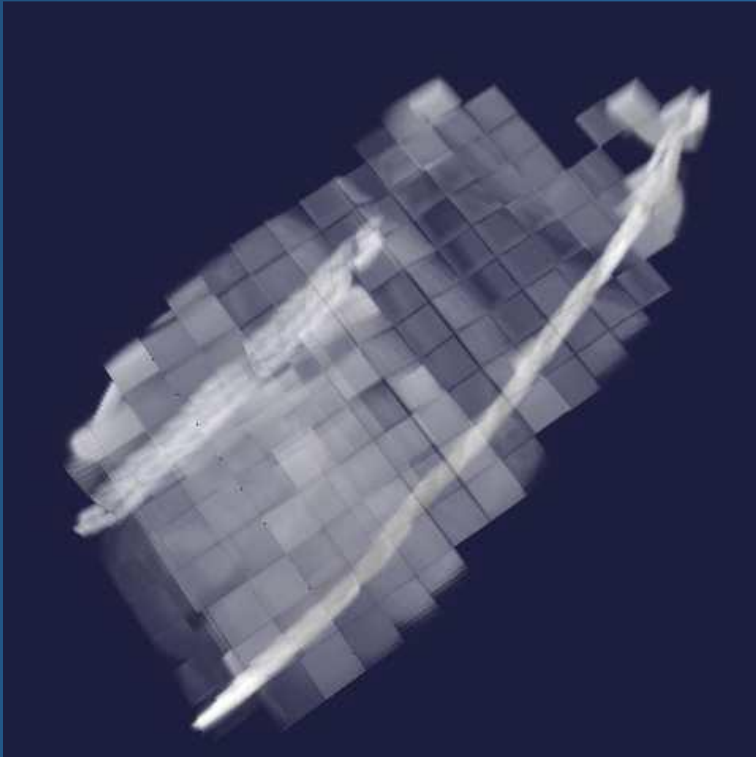


pointcloudlibrary

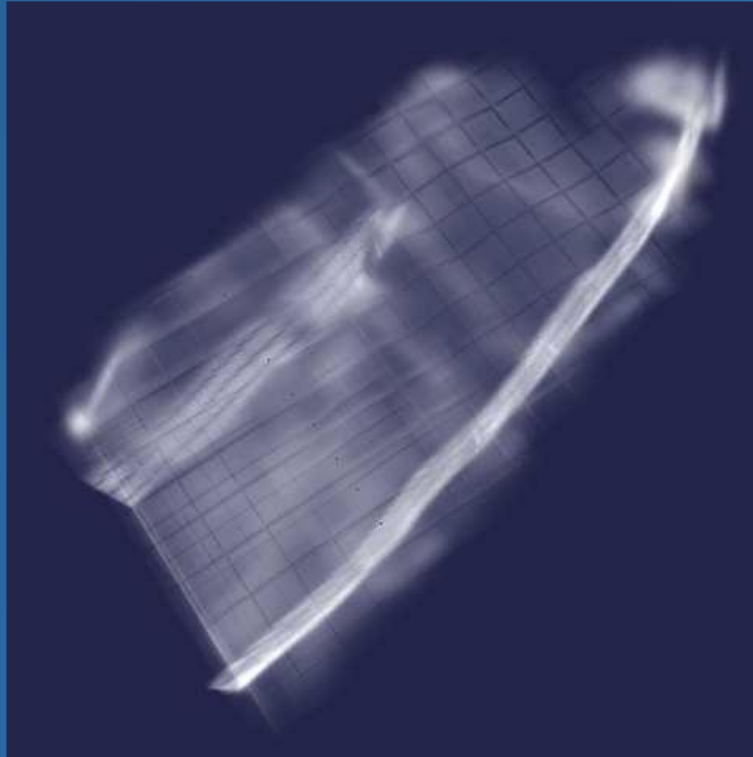


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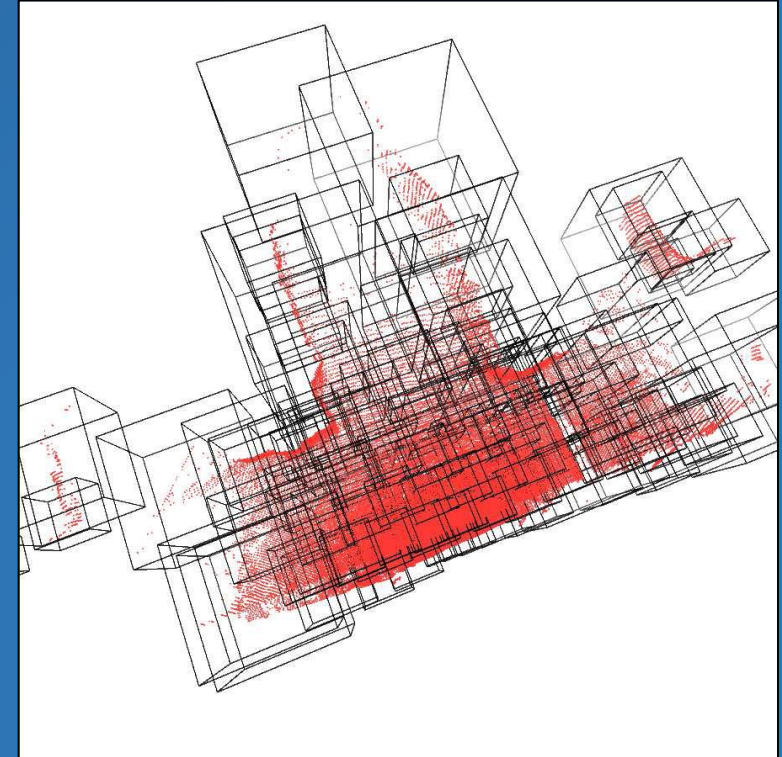
Optimization



Original NDT



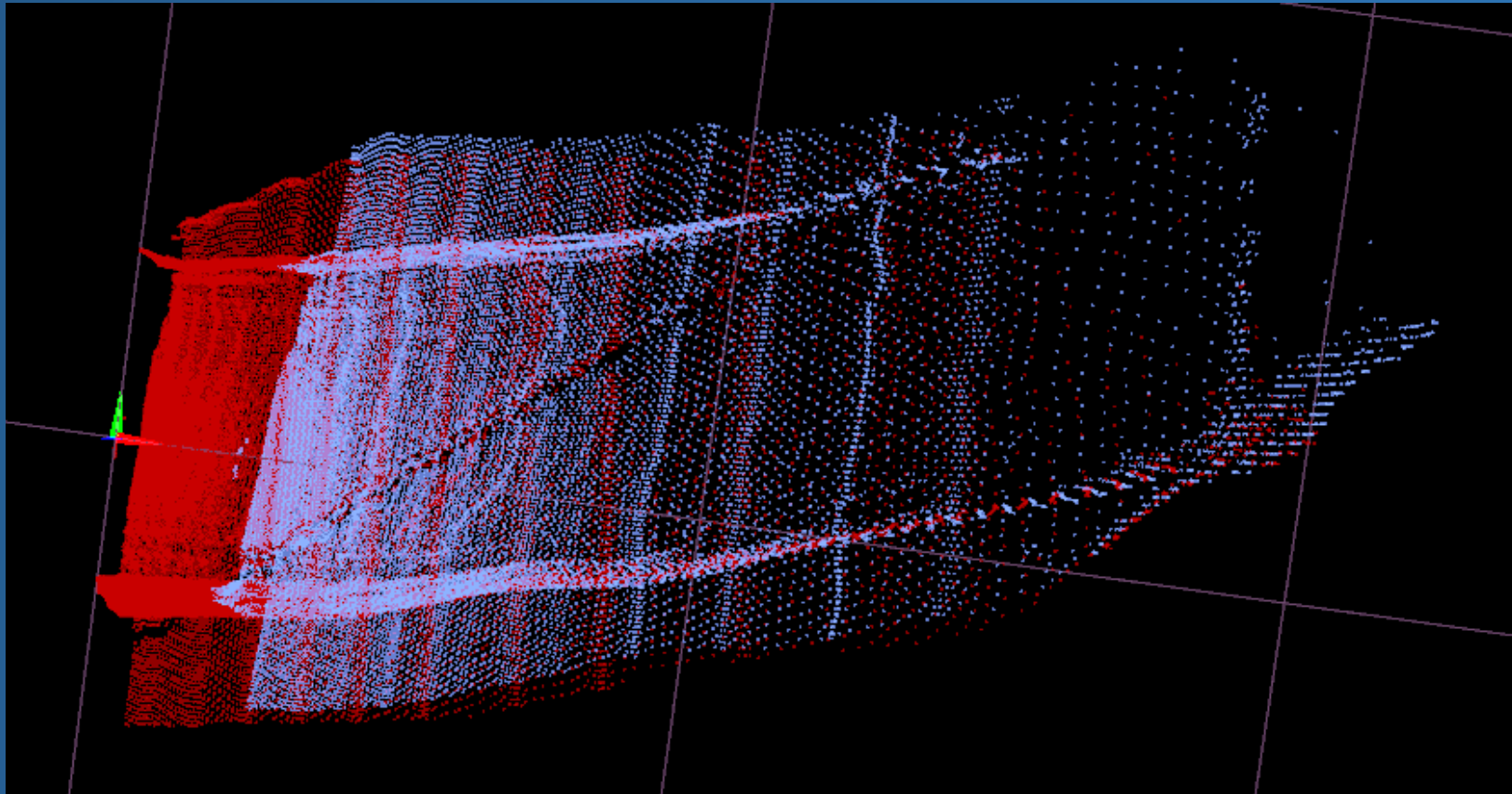
Trilinear Interpolation



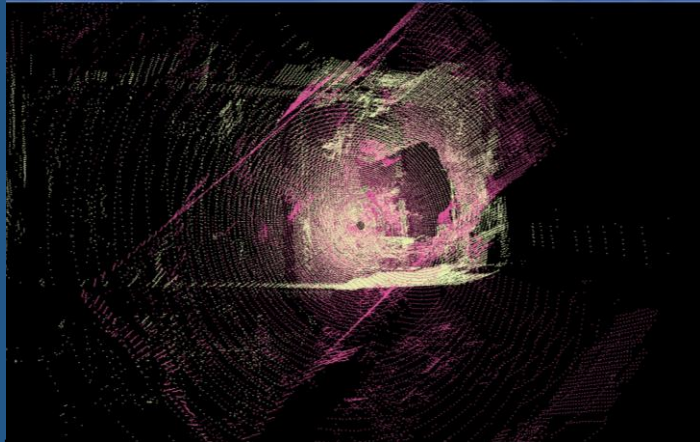
Octree discretization



Registration results



SLAM



3D Scan
Point Cloud

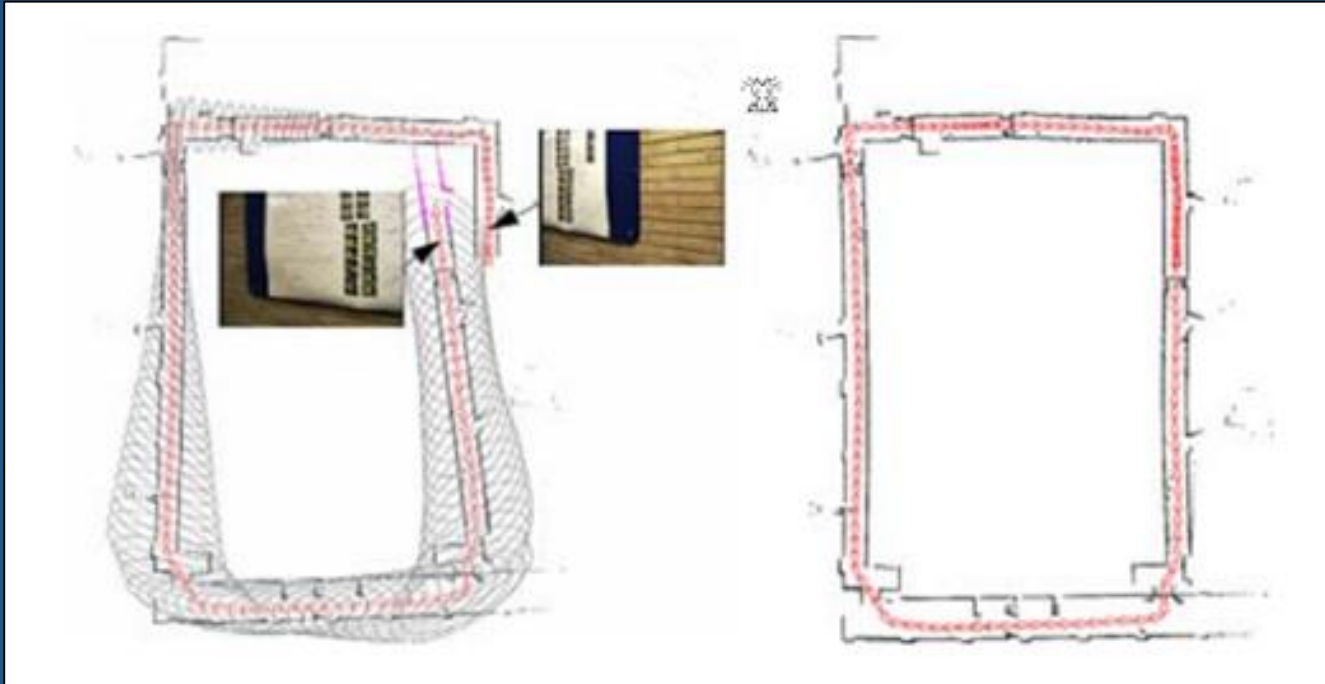
Registration



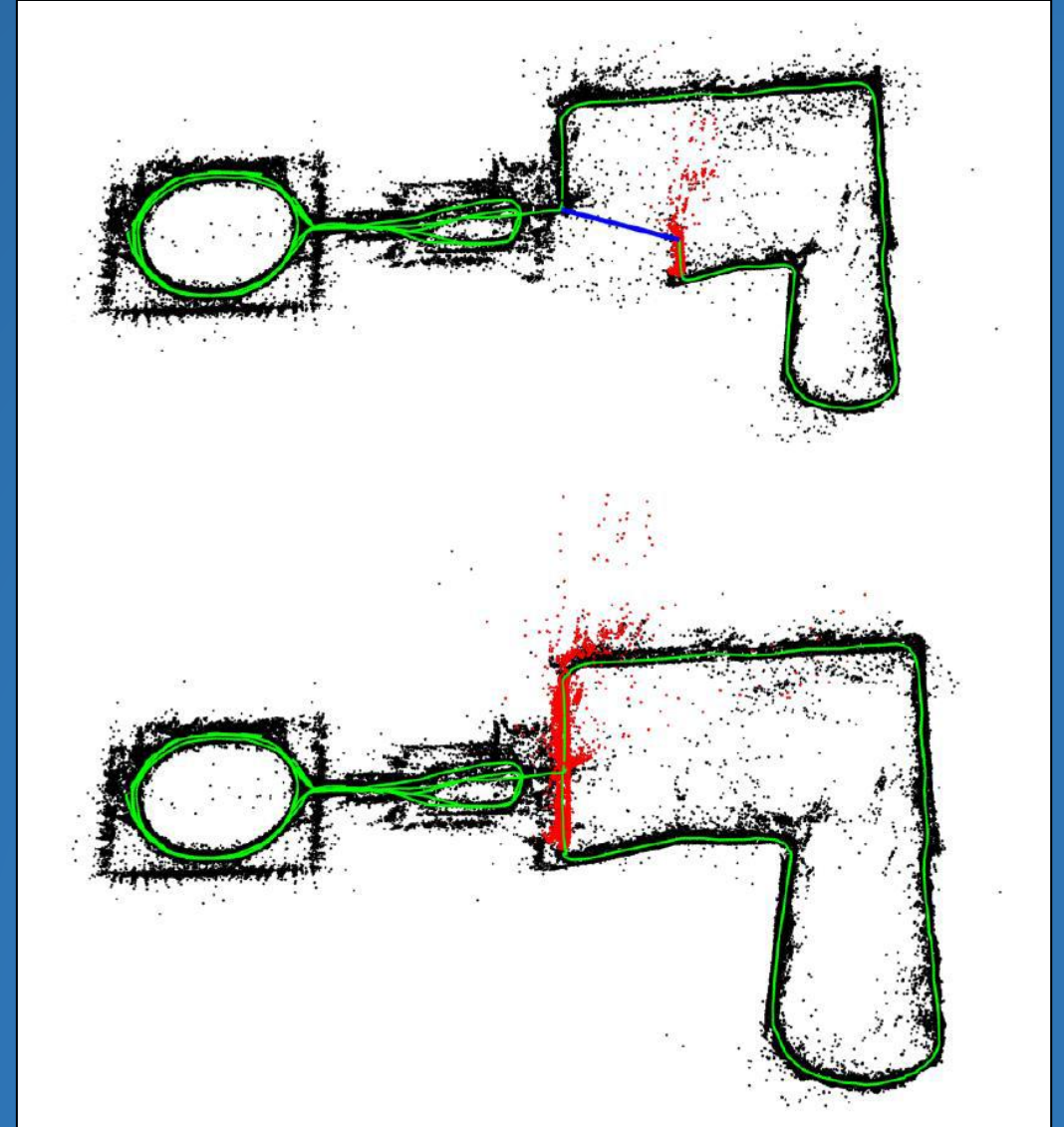
Loop Detection
& Relaxation



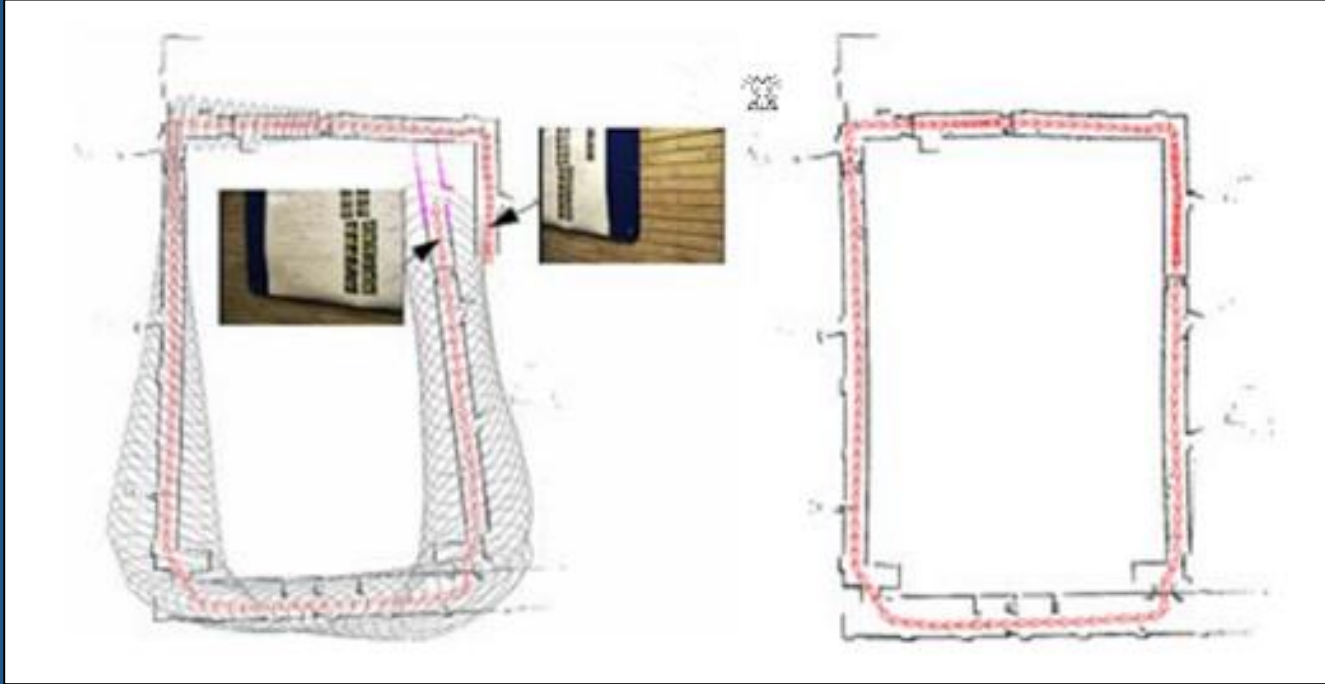
Loop Closure



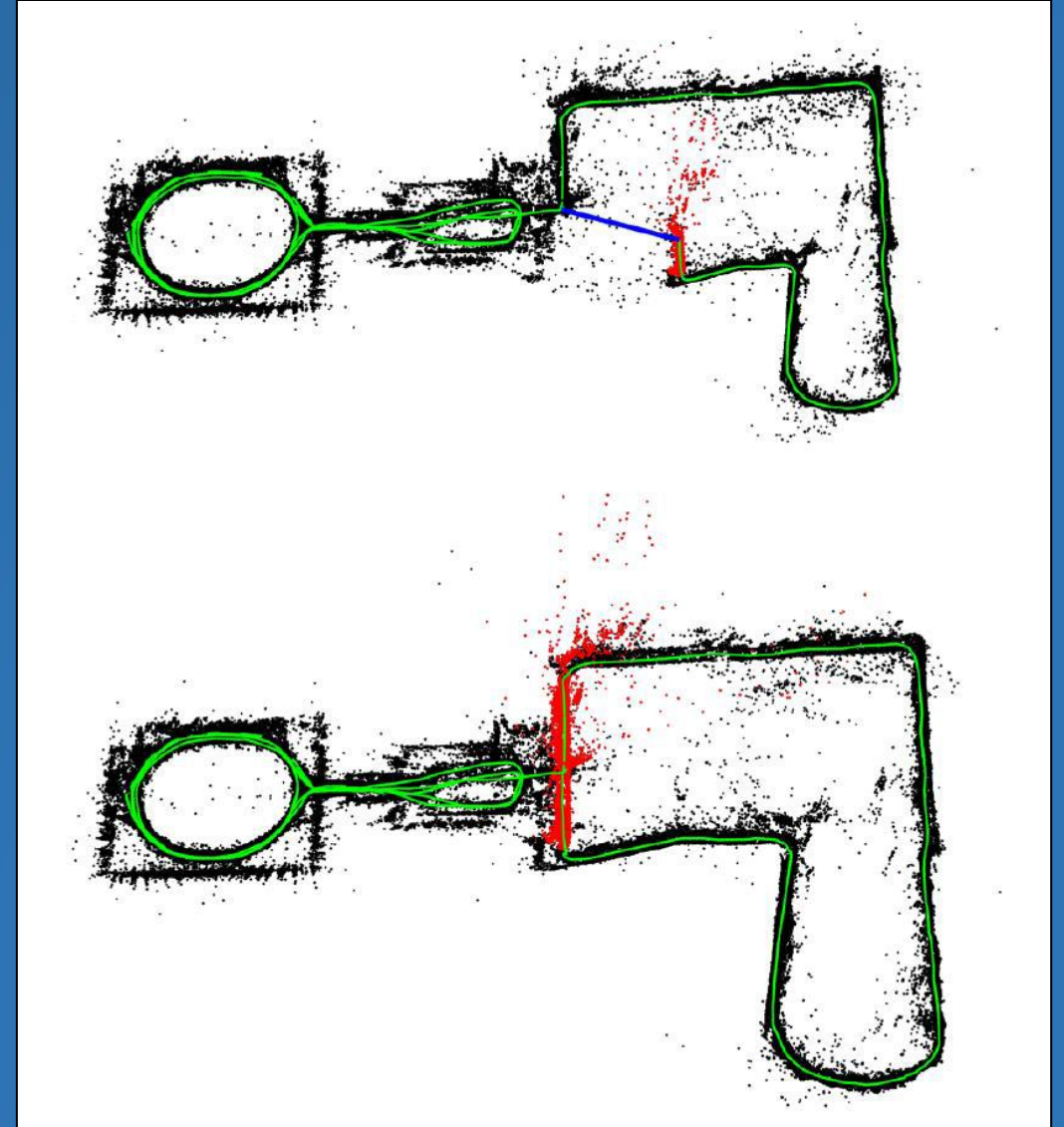
2 steps: Detection & Relaxation



Loop Closure



2 steps: **Detection** & Relaxation

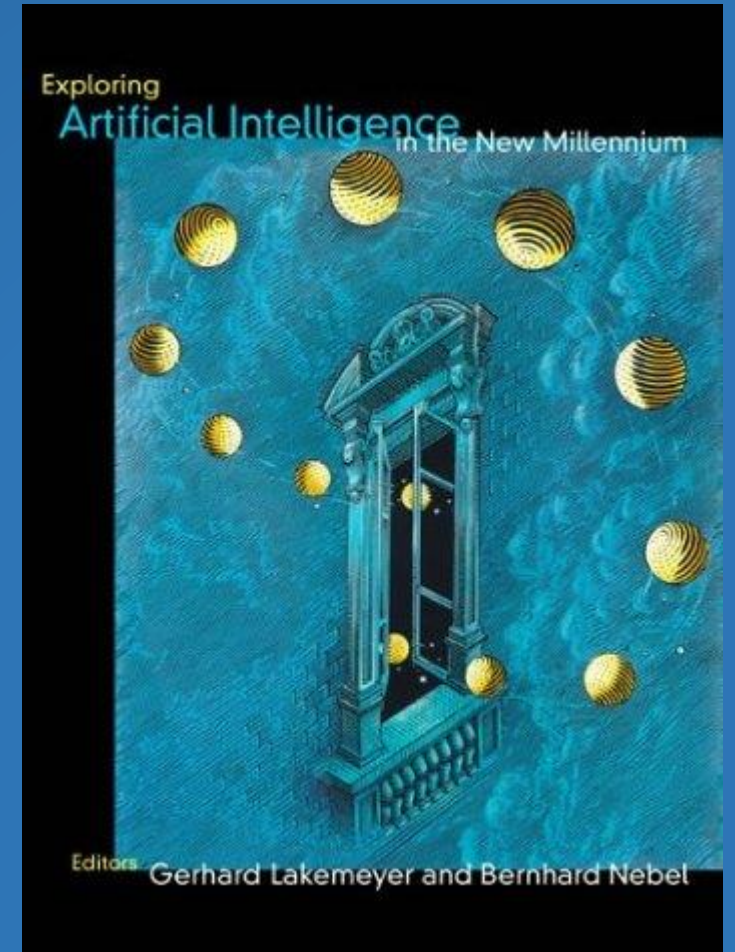


Technical Approach

“Have I seen this before?”

“Establishing the correspondence between past and present positions when closing a loop is one of the most challenging problems in robotic mapping.”

Sebastian Thrun, 2002



Appearance descriptor

The covariance matrices describe the shapes of the distributions.

the eigenvalues $\lambda_1 \leq \lambda_2 \leq \lambda_3$ and corresponding eigenvectors $\vec{e}_1, \vec{e}_2, \vec{e}_3$ of the covariance matrix

spherical

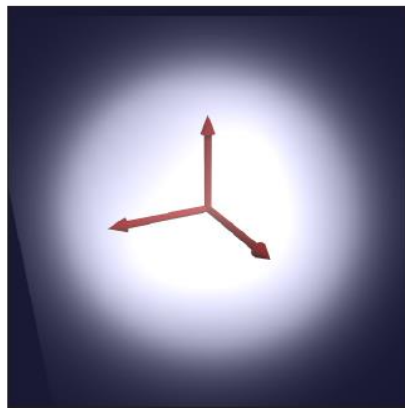
nonlinear and nonplanar

linear

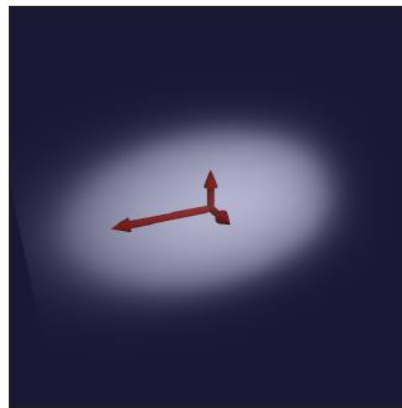
$$\lambda_2/\lambda_3 \leq t_e.$$

planar

$$\lambda_1/\lambda_2 \leq t_e.$$



(a) Spherical: All eigenvalues approximately equal.



(b) Linear: One eigenvalue much larger than the other two.

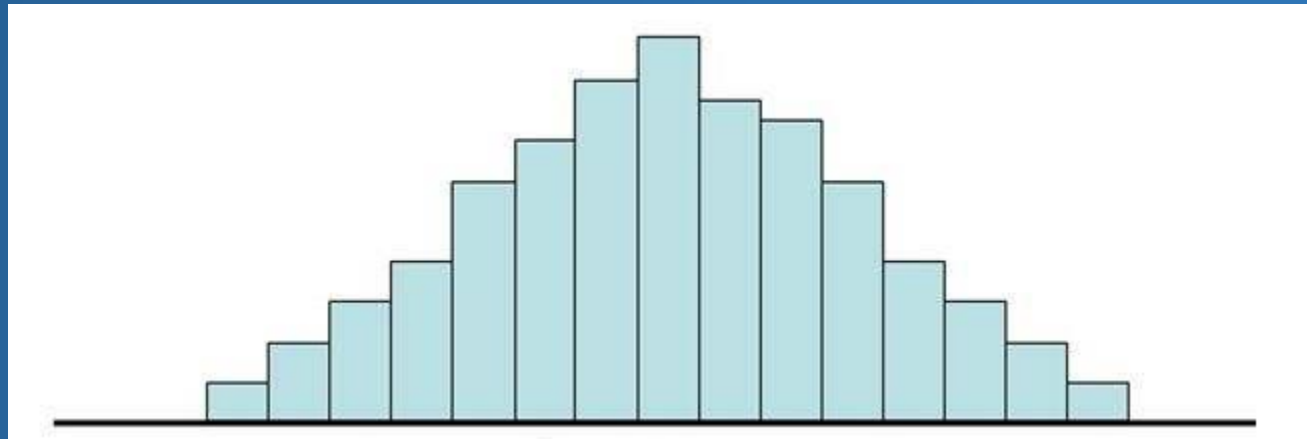


(c) Planar: One eigenvalue much smaller than the others.



Surface-shape histograms

$$\vec{f} = \left[\underbrace{f_1, \dots, f_{n_s}}_{\text{spherical classes}}, \underbrace{f_{n_s+1}, \dots, f_{n_s+n_p}}_{\text{planar classes}}, \underbrace{f_{n_s+n_p+1}, \dots, f_{n_s+n_p+n_l}}_{\text{linear classes}} \right]^T = \begin{bmatrix} \vec{S} \\ \vec{P} \\ \vec{L} \end{bmatrix},$$



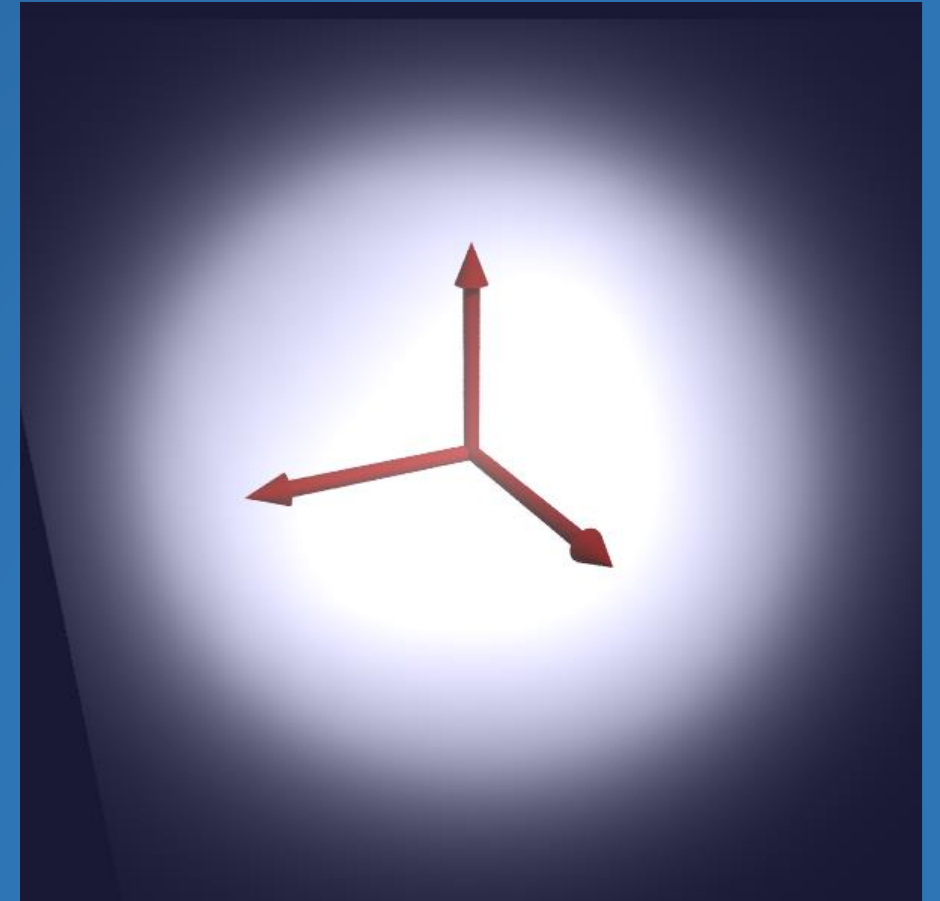
Spherical subclasses

the “roundness” ratio λ_2/λ_3

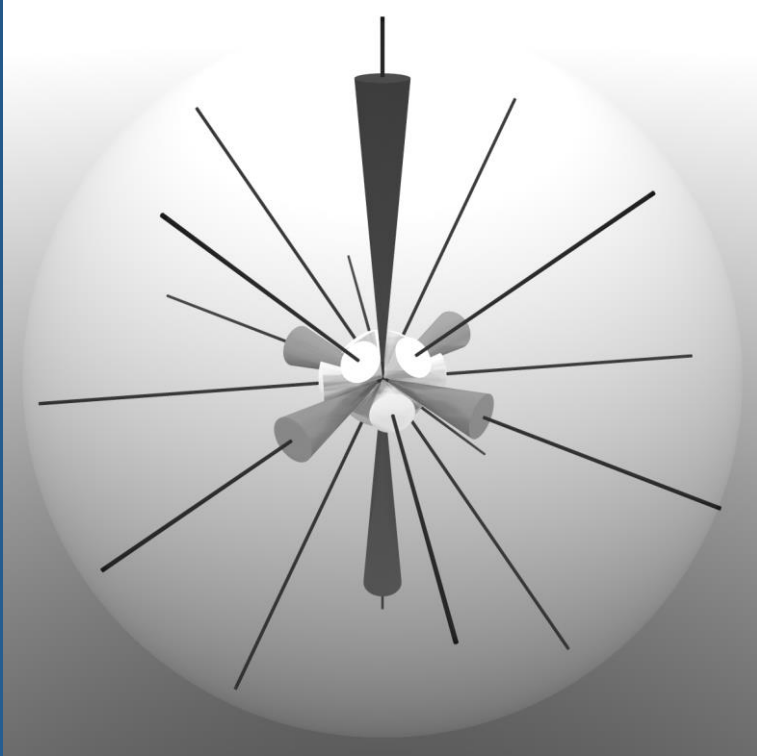
$$i = \left\lceil n_s \frac{\lambda_2/\lambda_3 - t_e}{1 - t_e} \right\rceil.$$

larger values of i = distributions with more variance

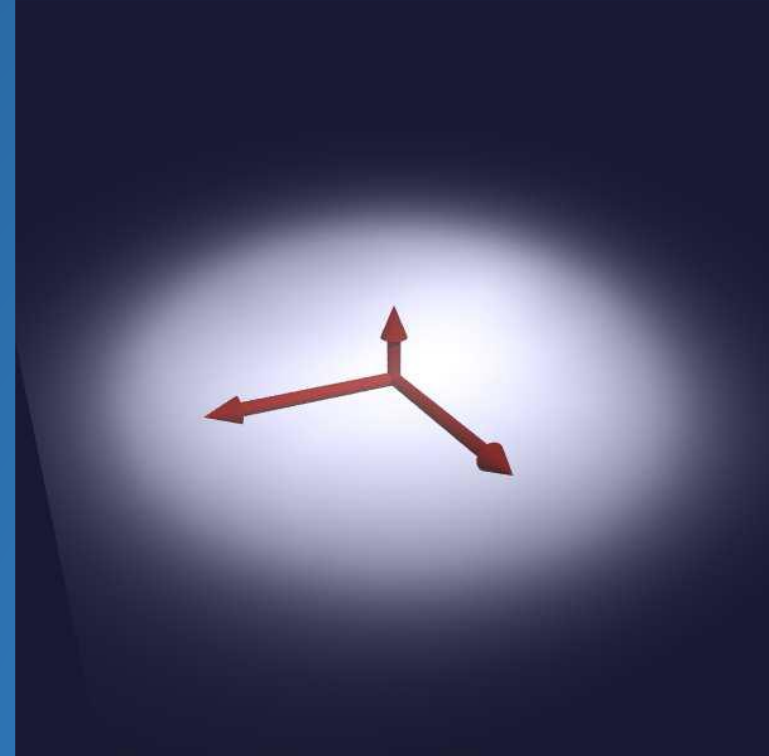
$$t_e > \lambda_2/\lambda_3 \geq 1, \text{ so } 1 \leq i \leq n_s$$



planar subclasses



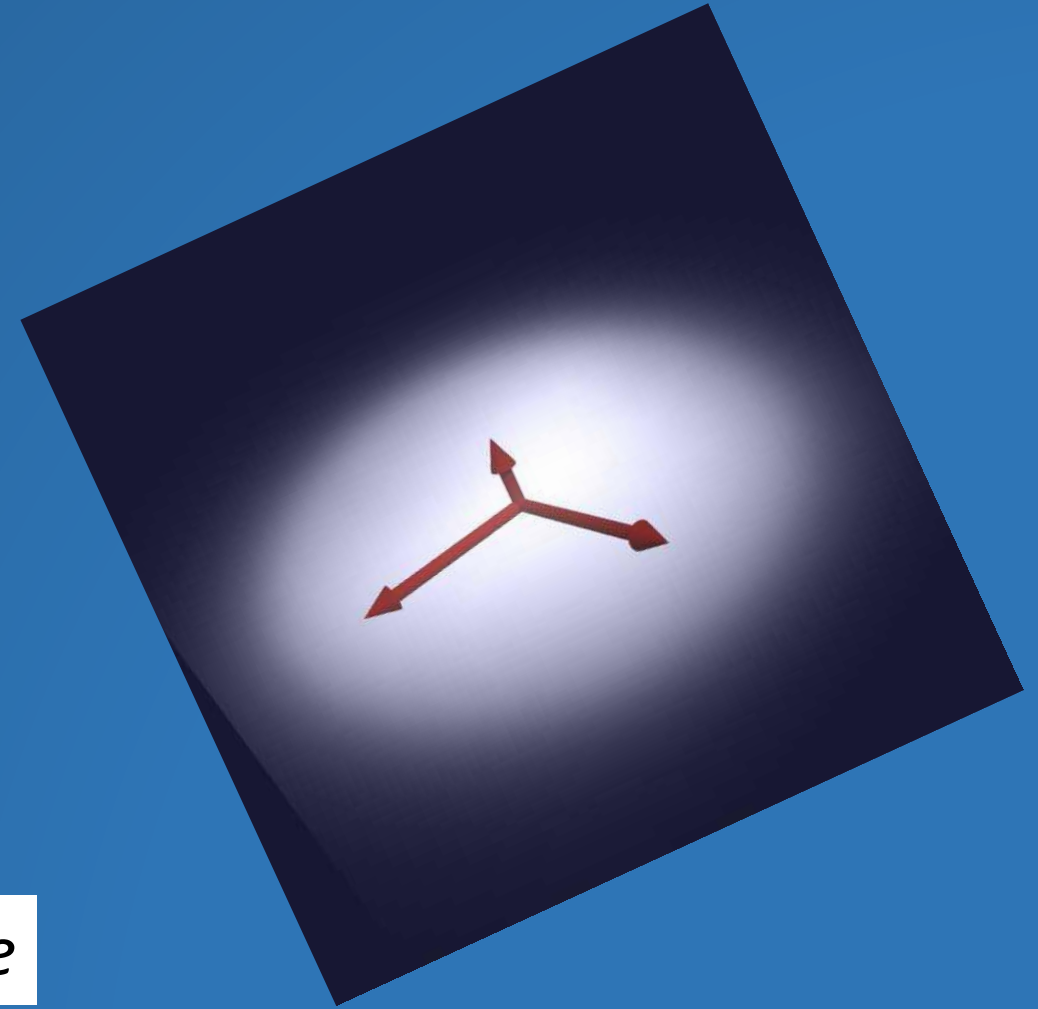
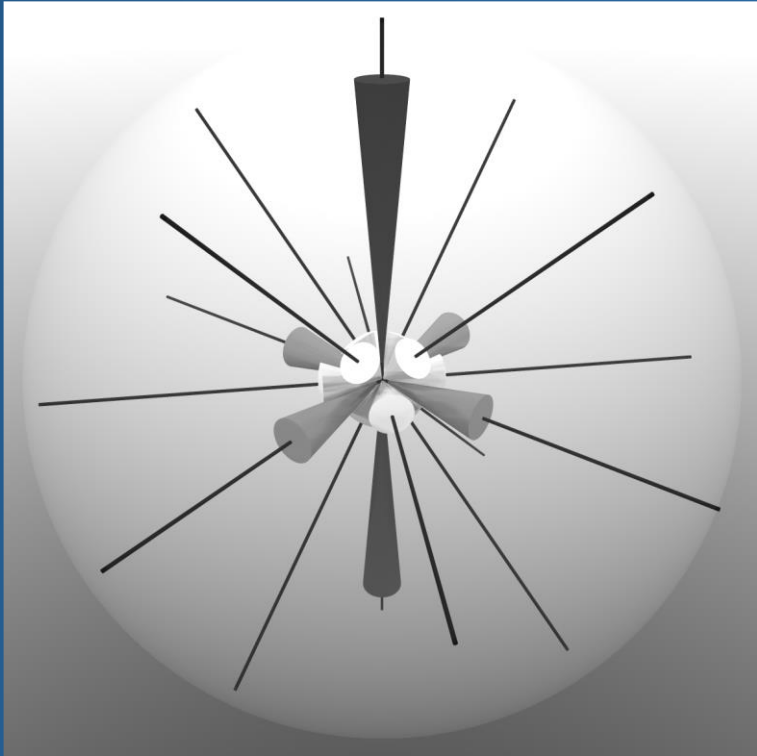
$$P = \{\pi_1, \dots, \pi_{n_p}\}$$



$$i = n_s + \arg \min_j d(\vec{e}_1, \pi_j),$$



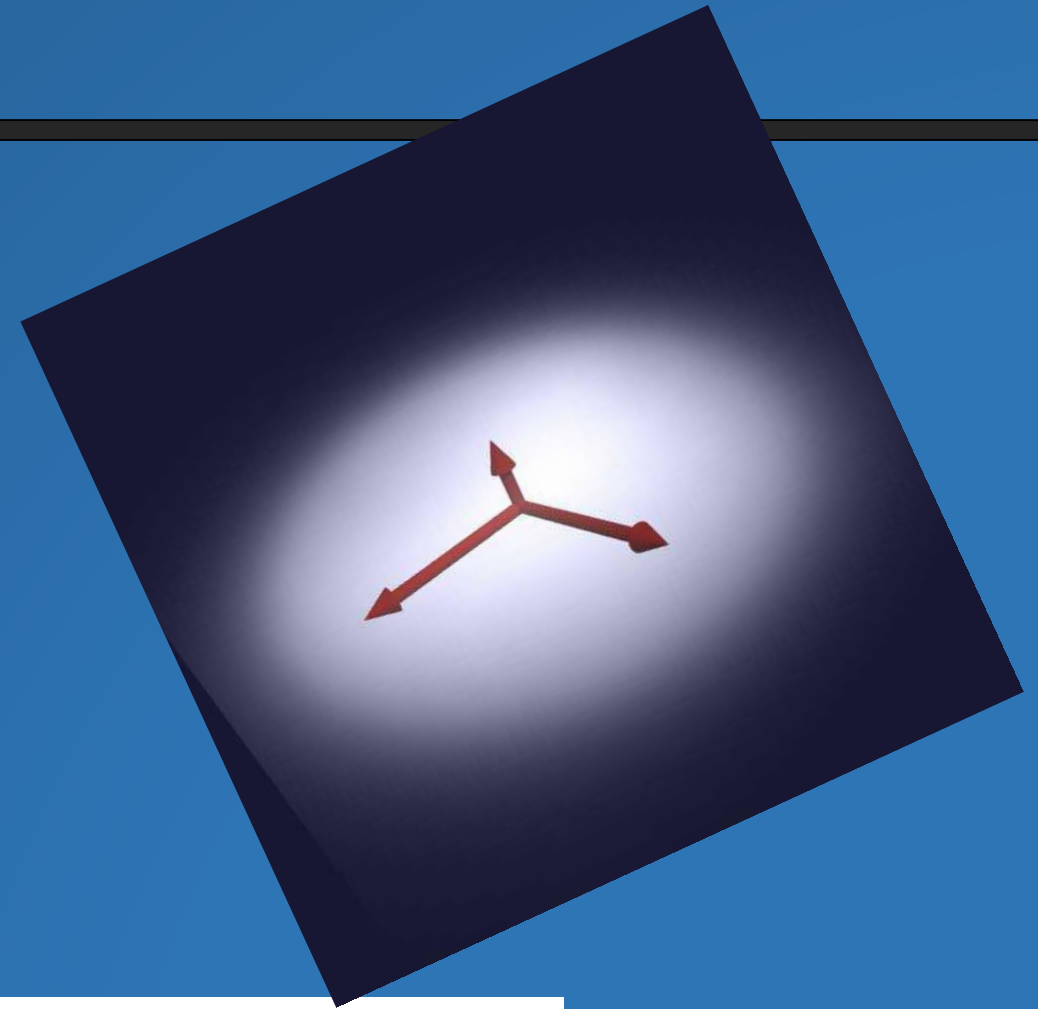
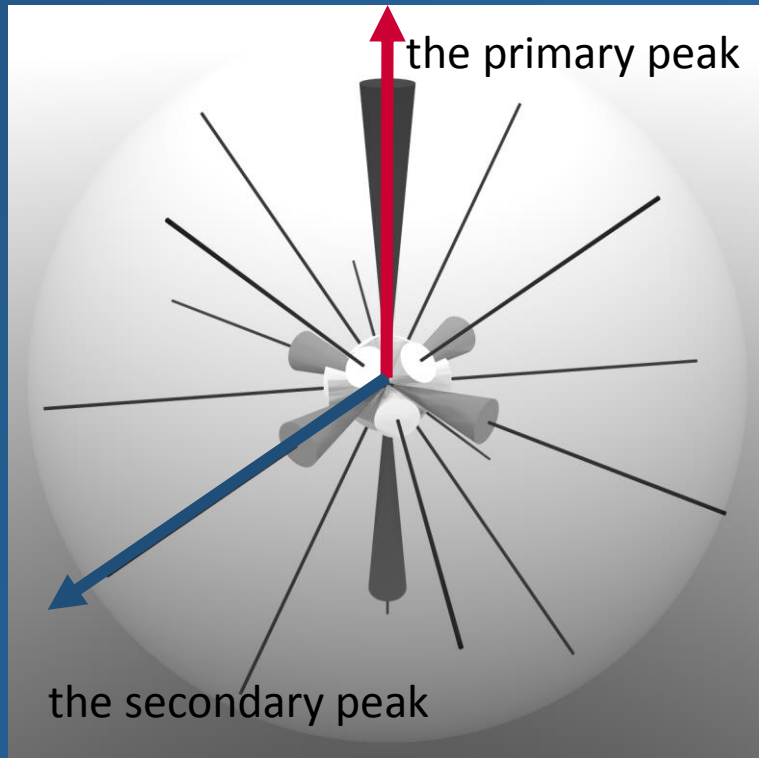
Is it rotation invariant?



Nope



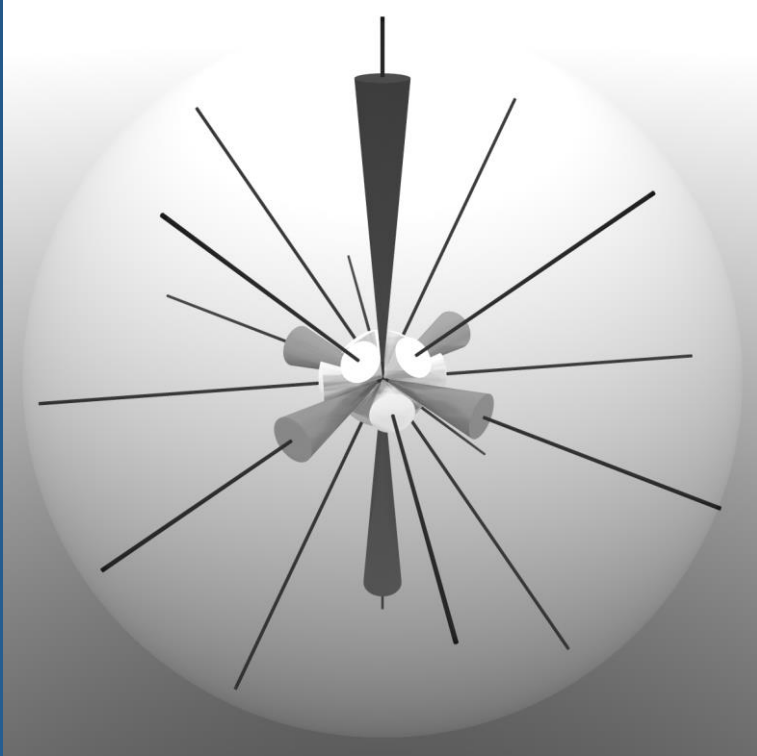
Rotation invariance



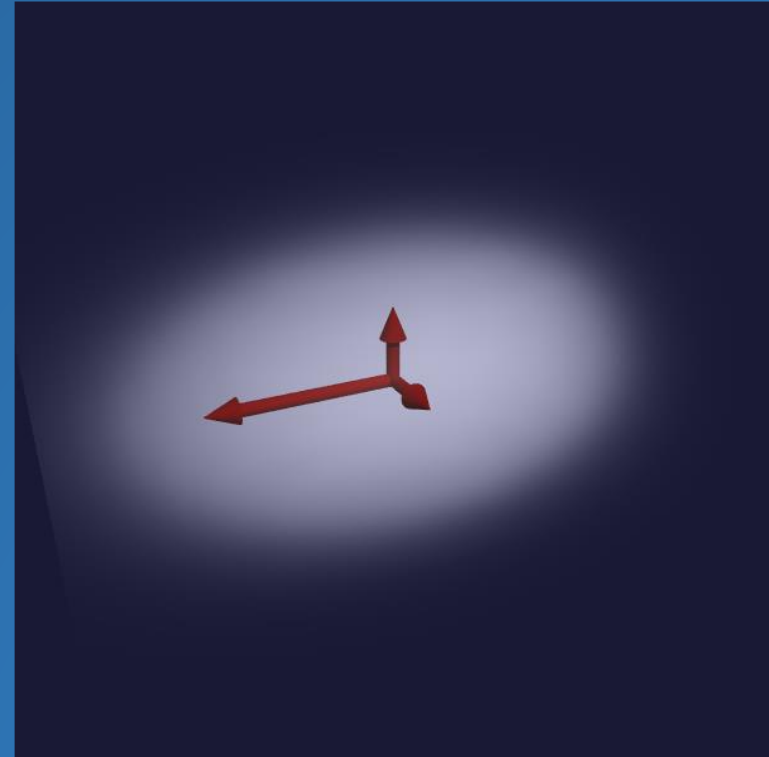
$$R_z = \left(\vec{\pi}_i \times \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, -\arccos \left(\vec{\pi}_i \cdot \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \right) \right),$$



linear subclasses



$$L = \{l_1, \dots, l_{n_l}\}$$

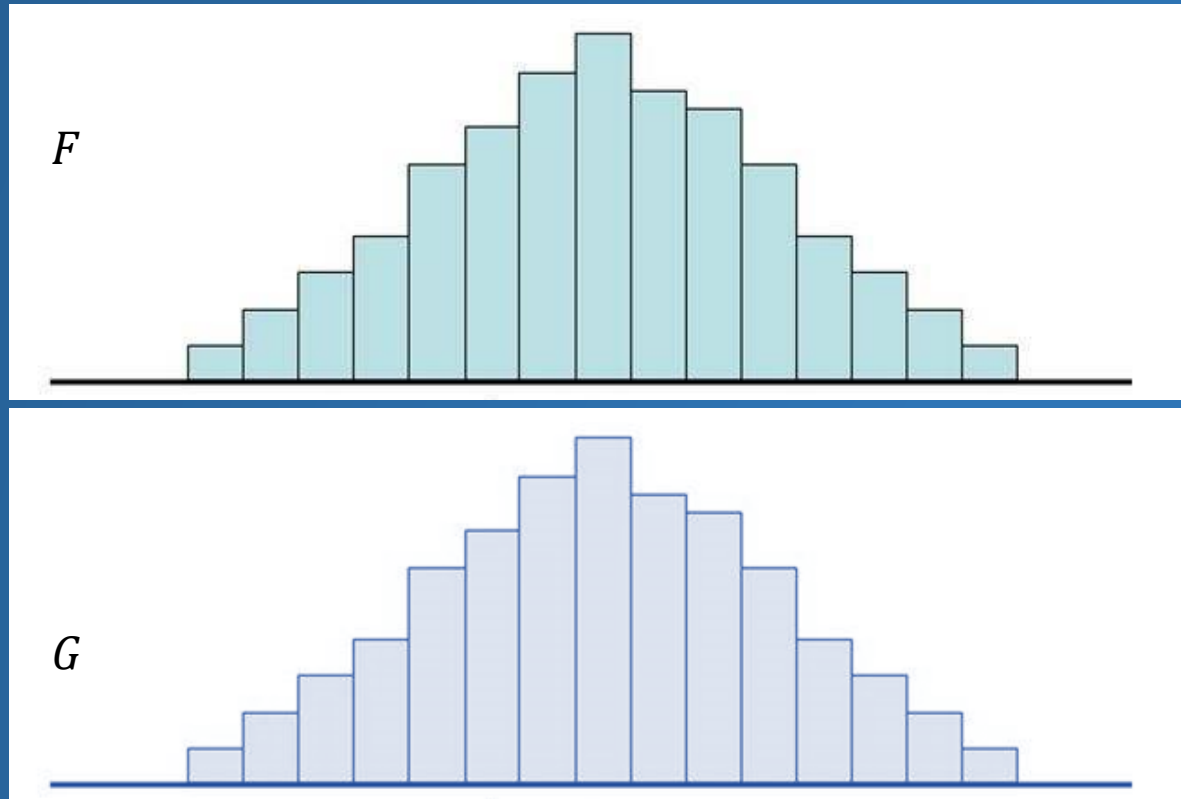


$$i = n_s + n_l + \arg \min_j d(\vec{e}_3, \lambda_j).$$



Difference measure

$$\delta(\mathbf{F}, \mathbf{G}) = \sum_{i=1}^{n_r} \left(\left\| \frac{\vec{f}_i}{\|\mathbf{F}\|_1} - \frac{\vec{g}_i}{\|\mathbf{G}\|_1} \right\|_2 \right) \frac{\max(\|\mathbf{F}\|_1, \|\mathbf{G}\|_1)}{\min(\|\mathbf{F}\|_1, \|\mathbf{G}\|_1)}$$



$$\Delta(\mathcal{X}_1, \mathcal{X}_2) = \min_{i,j} \delta(\mathbf{F}_i, \mathbf{G}_j) \quad \mathbf{F}_i \in \mathcal{F}, \mathbf{G}_j \in \mathcal{G}$$



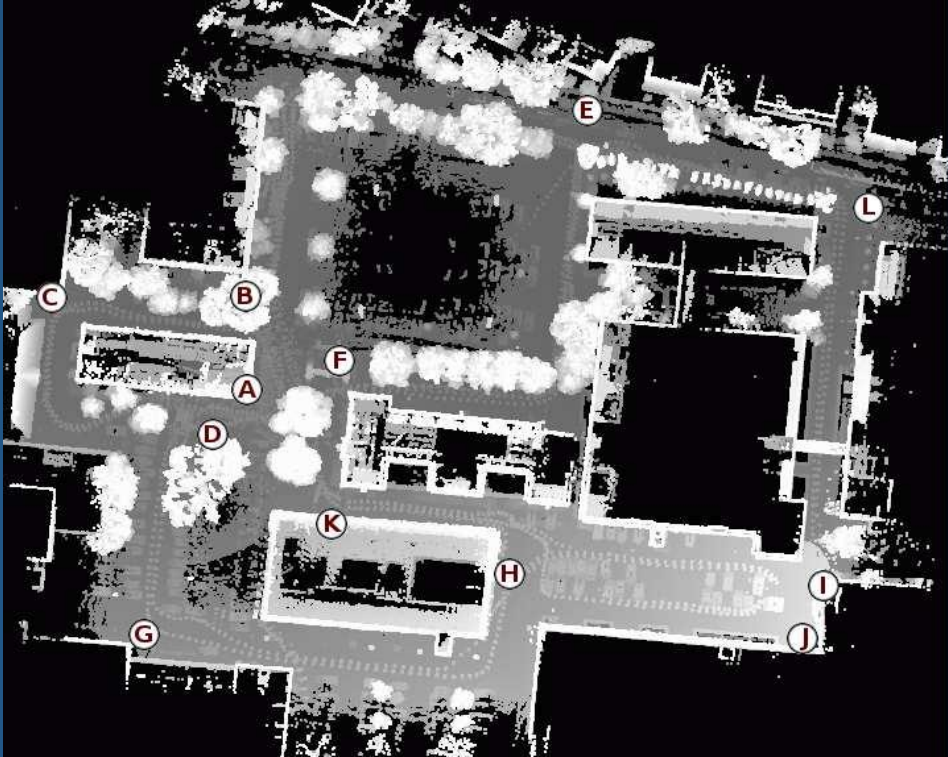
Parameters

- NDT cell size $B = 0.5$ m,
- range limits $\mathcal{R} = \{[0, 3), [3, 6), [6, 9), [9, 15), [15, \infty)\}$ m,
- spherical class count $n_s = 1$,
- planar class count $n_p = 9$,
- linear class count $n_l = 1$,
- eigenvalue-ratio threshold $t_e = 0.10$,
- ambiguity-ratio threshold $t_a = 0.60$.

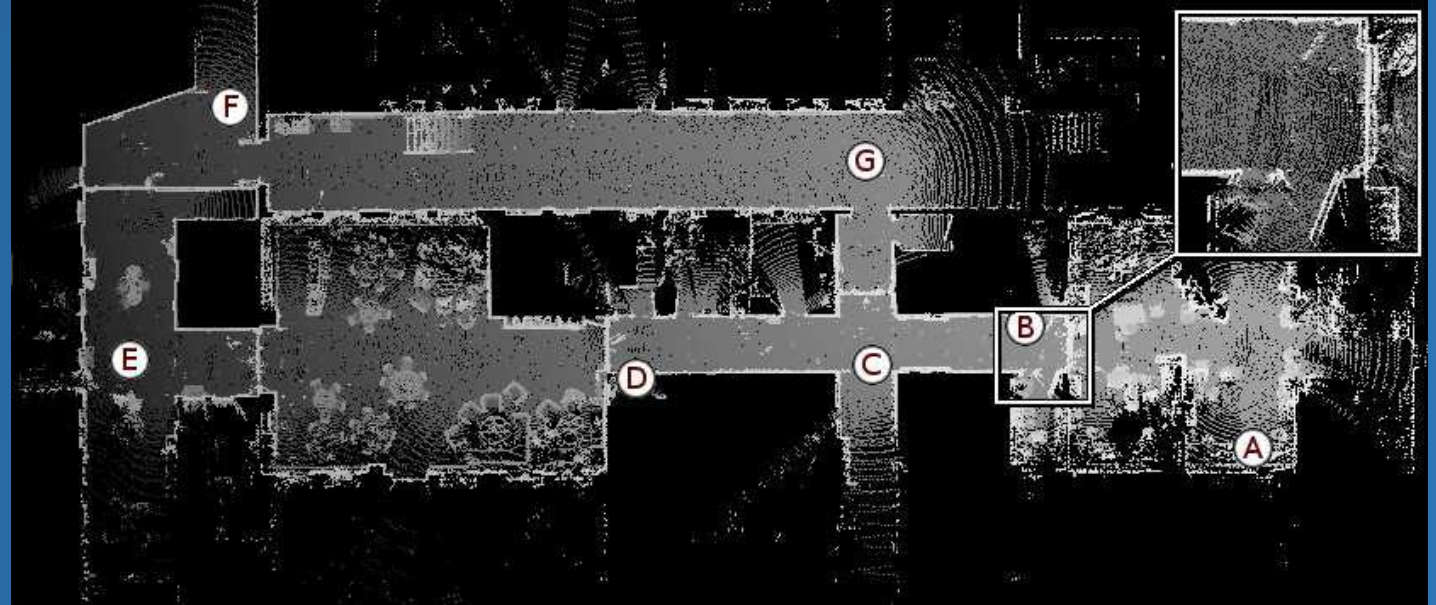


Results

Data sets



Hannover-2



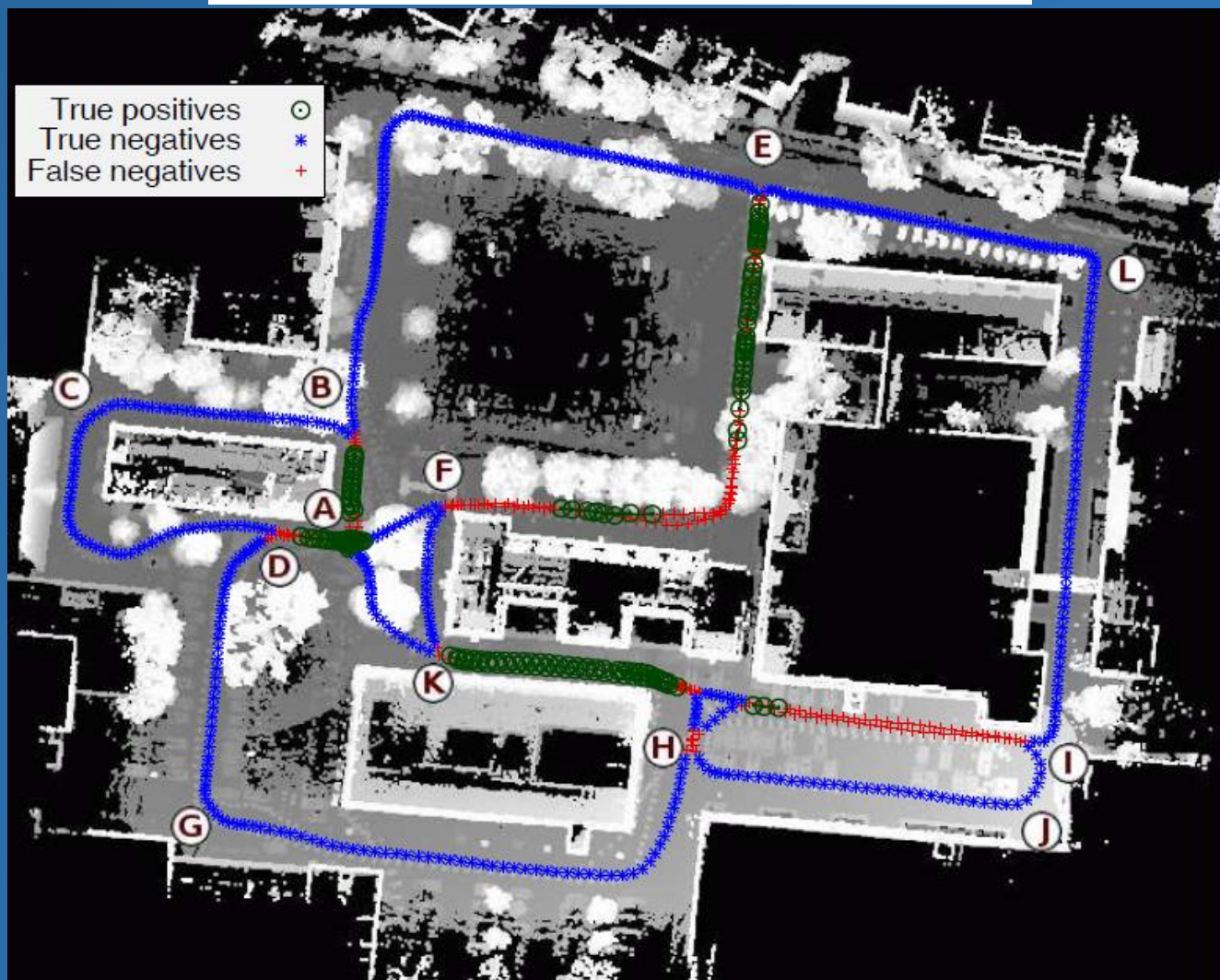
AASS-Loop



Detection Results

True positives
False positives ×
True negatives
False negatives

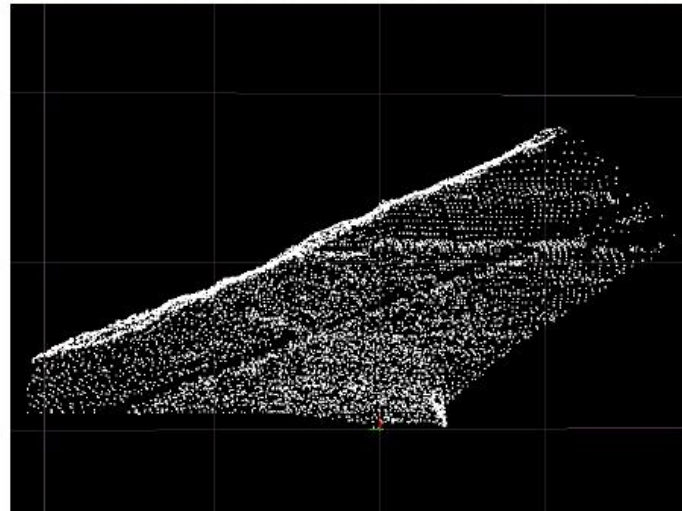
A-B-C-D-A-B-E-F-A-D-G-H-I-J-H-K-F-E-L-I-K-A



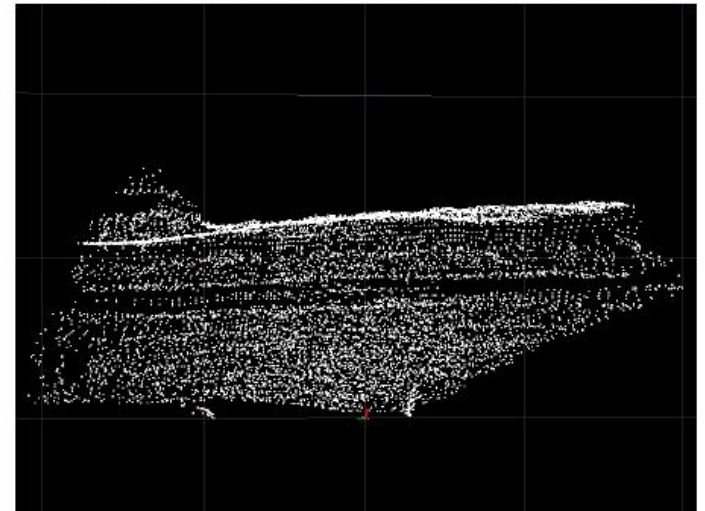
Problem encountered

$$\Delta(X, \hat{X}) < t_d$$

What is the best difference threshold?



(a) Location F



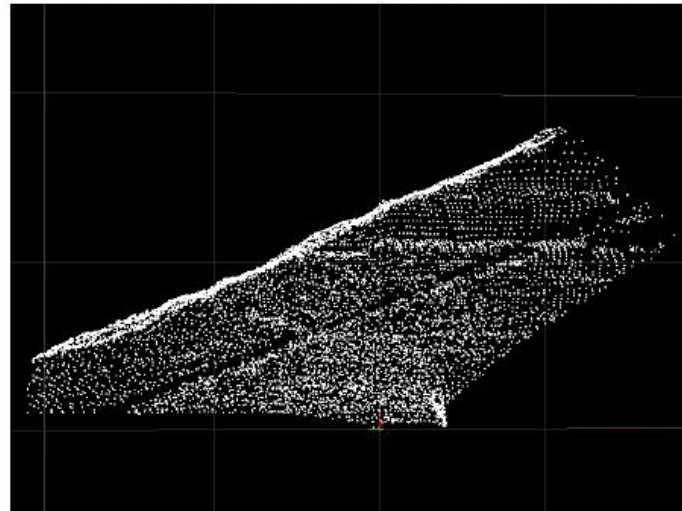
(b) Location H



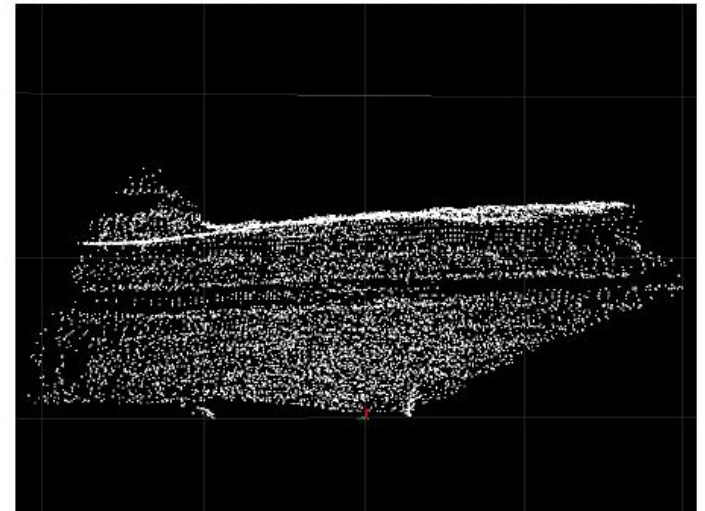
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What is the best difference threshold?



(a) Location F



(b) Location H

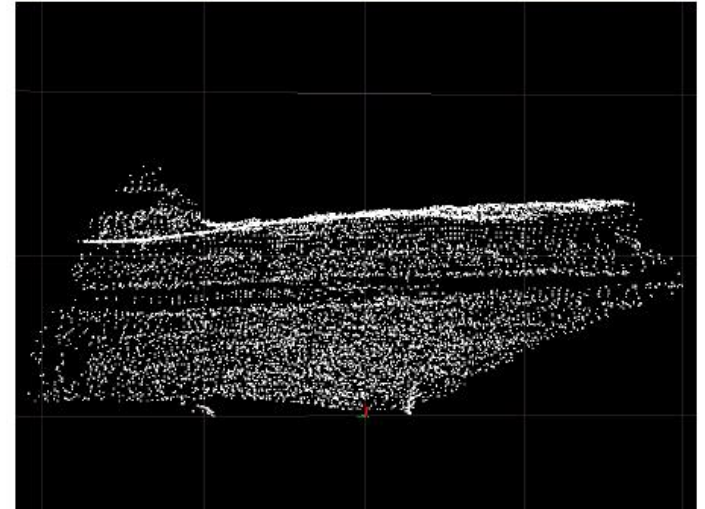
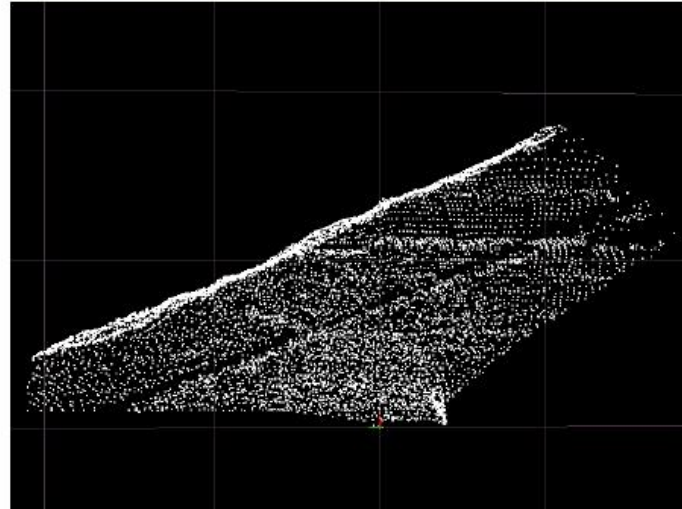


Problem encountered

$$\Delta(X, \hat{X}) < t_d$$

What is the best difference threshold?

10m below the threshold = Positive

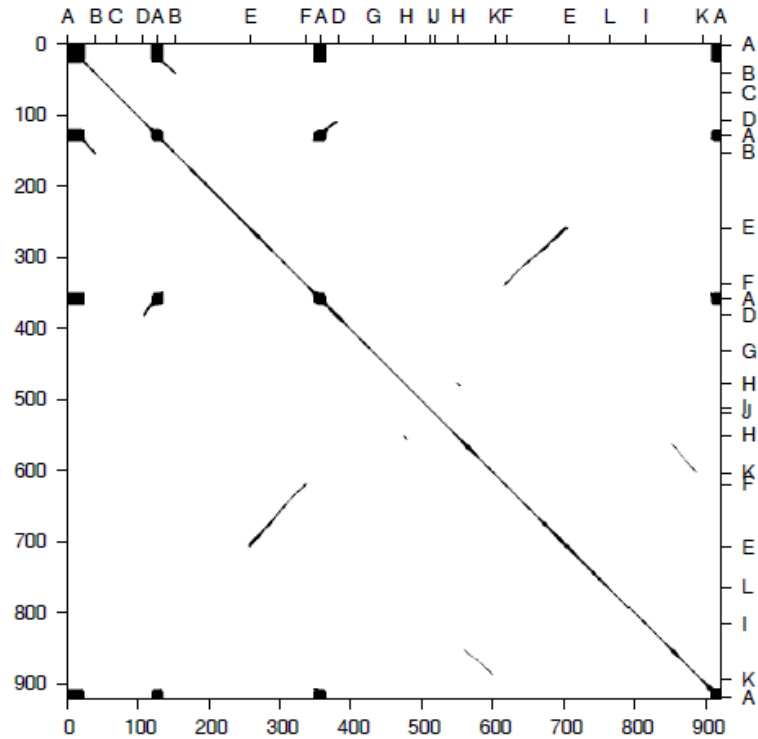


(a) Location F

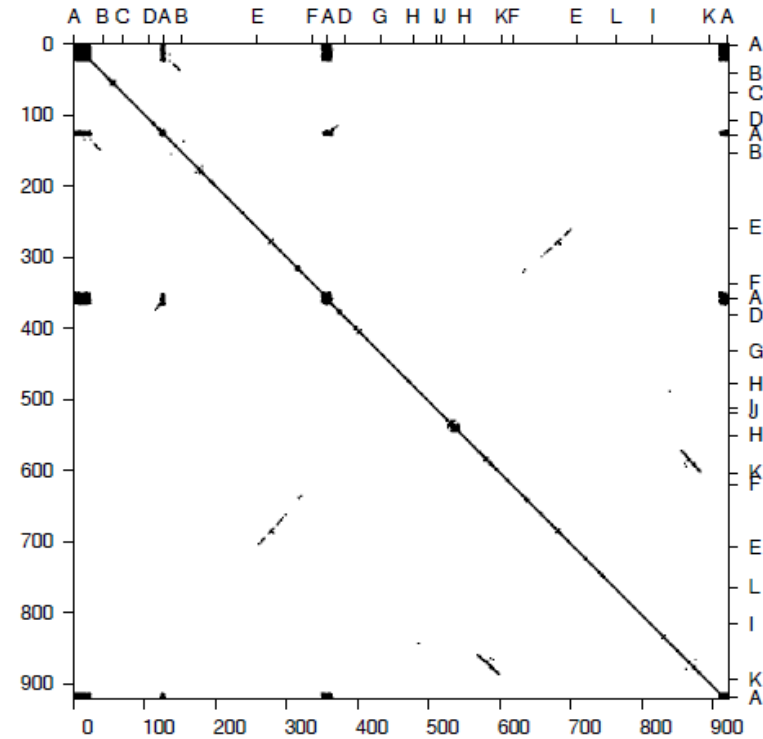
(b) Location H



Final results



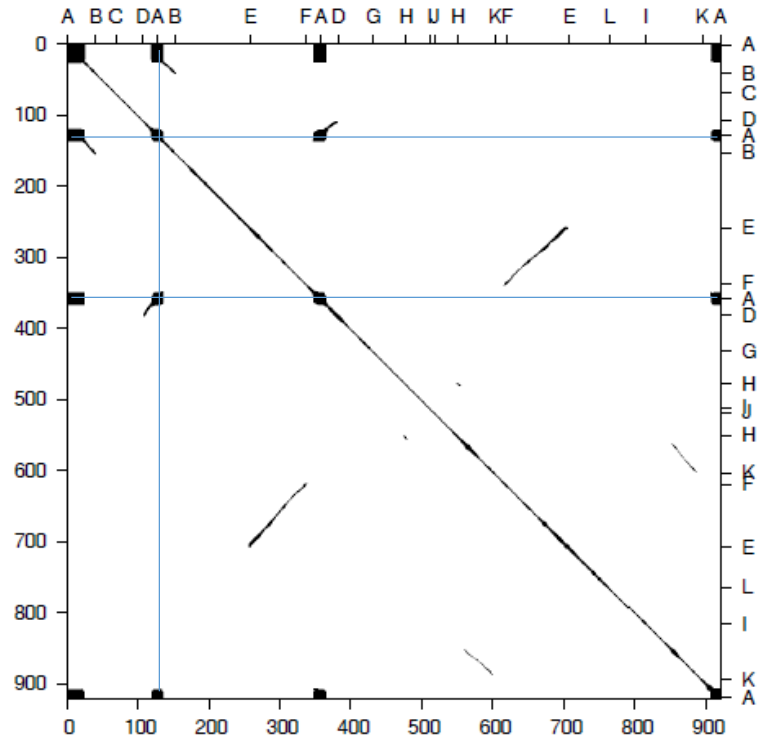
(a) Thresholded ground-truth distance matrix of Hannover-2, showing all scan pairs taken less than 3 m apart.



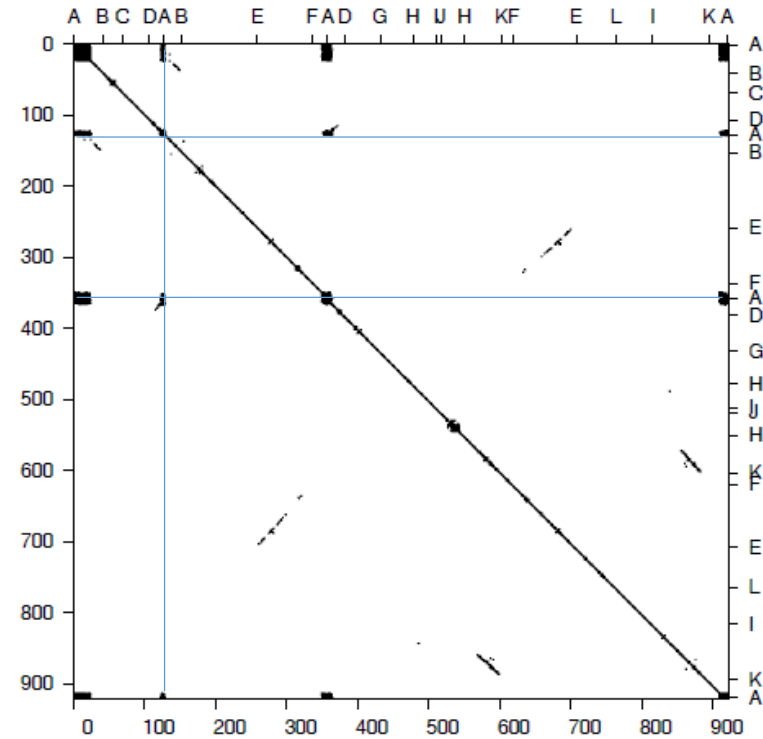
(b) Similarity matrix of Hannover-2, showing all scan pairs whose difference value $\Delta < 0.0737$.



Final results



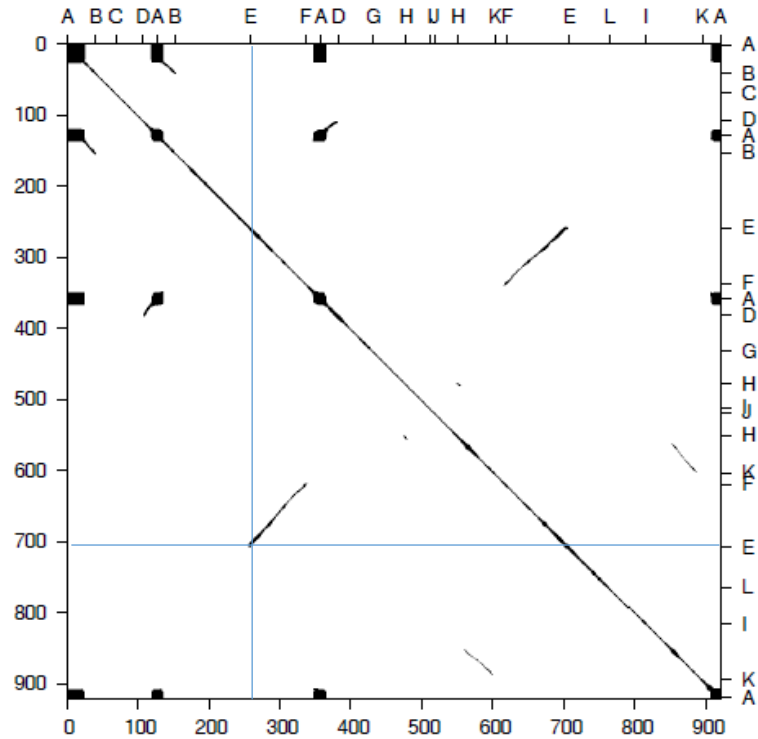
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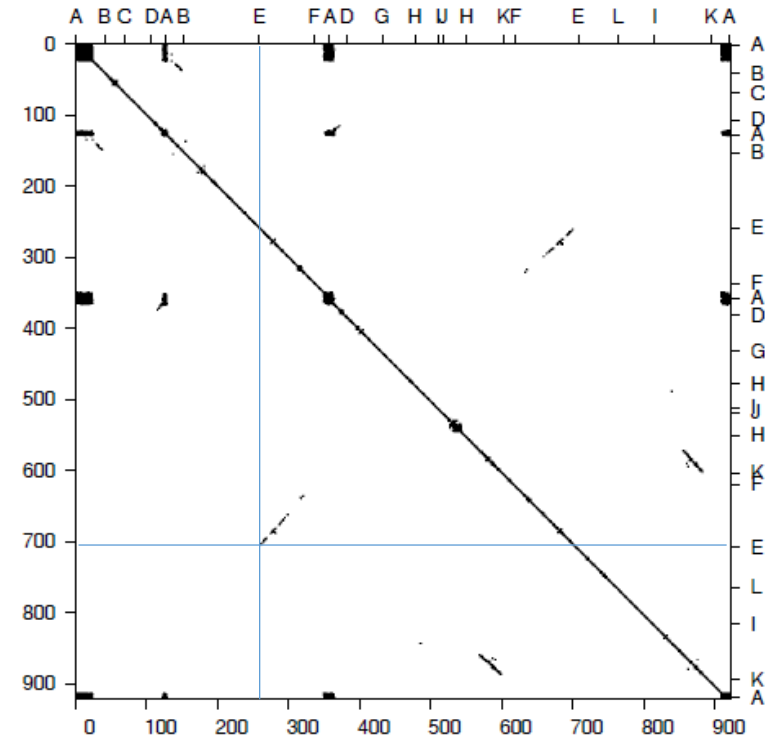
(b) Similarity matrix of Hannover-2, showing all scan pairs whose difference value $\Delta < 0.0737$.



Final results



(a) Thresholded ground-truth distance matrix of Hannover-2, showing all scan pairs taken less than 3 m apart.



(b) Similarity matrix of Hannover-2, showing all scan pairs whose difference value $\Delta < 0.0737$.



Future Expectation

The author's expectation

1. Different methods (automatic parameter)
2. Different data sets
3. Improving performance
4. Substituting a simple threshold with similarity matrix

Conclusion

1. A typical method of histogram based method
2. Main problems of loop closure detection

Tks!



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To be continued...