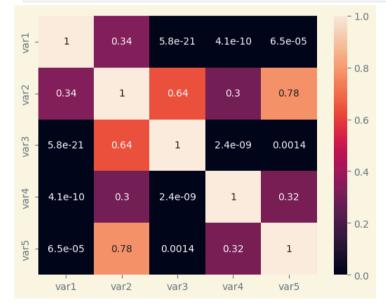
Алешко Альберт Вариант 1

Задание 3

```
In [1]: import pandas as pd
        import numpy as np
        import seaborn as sns
        \textbf{from} \ \texttt{matplotlib} \ \textbf{import} \ \texttt{pyplot} \ \textbf{as} \ \texttt{plt}
        from scipy.stats import pearsonr, spearmanr
        import pingouin as pg
        import tqdm
        from statsmodels.formula.api import ols
        plt.style.use('Solarize_Light2') # Функция для задания стиля графикам
In [2]: sheet_name = '2-1'
         # sheet_name = '1вар-адекв'
        data = pd.read_excel('data2.xlsx', sheet_name=sheet_name,
                              header=None, names=['var1', 'var2', 'var3', 'var4', 'var5']) # читаем из файла все выборки
        # data# выводим их
In [3]: length = len(data.T)
In [4]: def get_correlation(df, corr_func):
            names = df.columns
             correlation = np.zeros((length, length))
            correlation[range(length), range(length)] = 1
            p_values = np.zeros((length, length))
            p_values[range(length), range(length)] = 1
            for i in range(len(names)):
                 for j in range(i + 1, len(names)):
                     res = corr_func(df[names[i]], df[names[j]])
                     correlation[i, j] = correlation[j, i] = res[0]
                     p_values[i, j] = p_values[j, i] = res[1]
            df_correlation = pd.DataFrame(correlation)
            df_p_values = pd.DataFrame(p_values)
            df_correlation.columns = df_p_values.columns = names
            df_correlation.index = df_p_values.index = names
            return df_correlation, df_p_values
In [5]: corr, p_vals = get_correlation(data, pearsonr)
In [6]: sns.heatmap(corr, annot=True, vmin=-1, vmax=1);
```

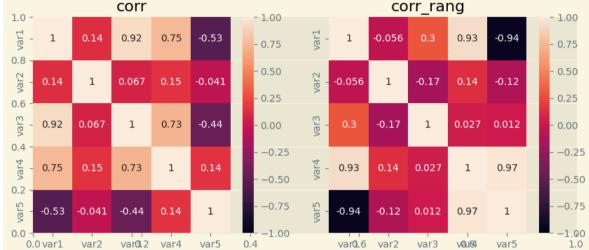


In [7]: sns.heatmap(p_vals, annot=True, vmin=0, vmax=1);



```
In [8]: def get_part_corr(df):
             names = df.columns
             correlation = np.zeros((length, length))
             correlation[range(length), range(length)] = 1
p_values = np.zeros((length, length))
             p_values[range(length), range(length)] = 1
             for i in range(len(names)):
                  for j in range(i+1, len(names)):
    co_names = list(df.columns)
                      co_names.remove(names[i])
                      if names[j] in co_names:
                          co_names.remove(names[j])
                      # print((names[i],names[j]),co_names)
                      res = pg.partial_corr(data=df, x=names[i], y=names[j], covar=co_names)
                      correlation[i, j] = correlation[j, i] = res['r'].iloc[0]
                      p_values[i, j] = p_values[j, i] = res['p-val'].iloc[0]
             df_correlation = pd.DataFrame(correlation)
             df_p_values = pd.DataFrame(p_values)
             df_correlation.columns = df_p_values.columns = names
```

```
df_correlation.index = df_p_values.index = names
              return df_correlation, df_p_values
In [9]: # partial_corr = pg.partial_corr(data=data, x='1', y='2', covar=['3','4','5'])
corr_part, p_vals = get_part_corr(data)
         # print(partial_corr)
In [10]: fig = plt.subplots(figsize=(10, 4))
         plt.subplot(121)
         plt.title('corr')
         sns.heatmap(corr, annot=True, vmin=-1, vmax=1);
         plt.subplot(122)
         plt.title('corr_rang')
         sns.heatmap(corr_part, annot=True, vmin=-1, vmax=1);
                                                                                         corr_rang
                               corr
         1.0 -
                                                            - 1.00
                                                                                                                           - 1.00
         varl
                                0.92
                                        0.75
                                                                                                       0.93
                                                                                                               -0.94
                                                -0.53
                                                                               1
                                                                                      -0.056
                                                             0.75
                                                                                                                            0.75
         0.8
```



In [11]: sns.heatmap(p_vals, annot=True, vmin=0, vmax=1);



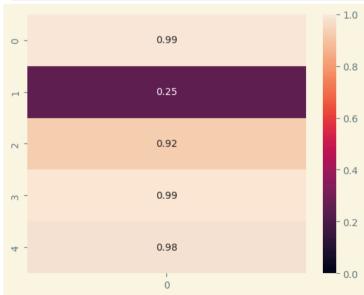
```
In [12]: def multiple_correlation(df):
    names = df.columns
    length = len(names)
    correlation = np.zeros((length))
    p_values = np.zeros((length))

    for i, name in enumerate(names):
        formula = name + ' ~ ' + ' + '.join([n for j, n in enumerate(names) if j != i])
        mod = ols(formula=formula, data=df)
        res = mod.fit()
        correlation[i] = res.rsquared ** 0.5
        p_values[i] = res.f_pvalue

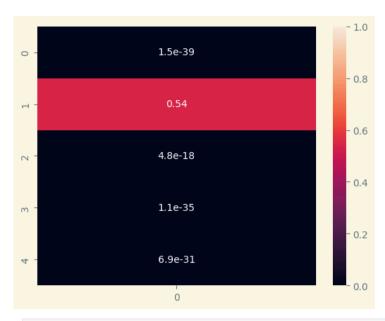
    return correlation, p_values
```

In [13]: multi_corr, p_vals = multiple_correlation(data)

In [14]: sns.heatmap(multi_corr[..., None], annot=True, vmin=0, vmax=1);



In [15]: sns.heatmap(p_vals[..., None], annot=True, vmin=0, vmax=1);



```
In [16]: corr_rang, p_vals = get_correlation(data, spearmanr)
```

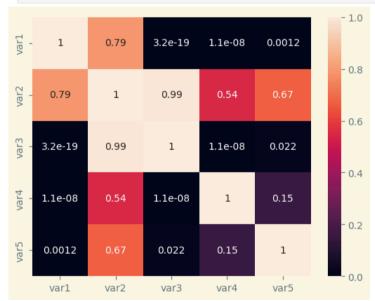
```
In [17]: fig = plt.subplots(figsize=(10, 4))

plt.subplot(121)
sns.heatmap(corr, annot=True, vmin=-1, vmax=1);
plt.title('corr')

plt.subplot(122)
plt.title('corr_rang')
sns.heatmap(corr_rang, annot=True, vmin=-1, vmax=1);
```



In [18]: sns.heatmap(p_vals, annot=True, vmin=0, vmax=1);



```
In [19]: from math import *
   import scipy as sci
```

```
In [20]: def Cheddock_scale_check(r, name='r'):
               # задаем шкалу Чеддока
                   # no correlation (n <= 0.1)'
                   # very weak (0.1 < n <= 0.2)'
                   # weak (0.2 < n <= 0.3)'
# moderate (0.3 < n <= 0.5)'
                   # perceptible (0.5 < n <= 0.7)'
                   # high (0.7 < n <= 0.9)'
                   # very high (0.9 < n <= 0.99)'
              # functional (n > 0.99)'
Cheddock_scale = {
                   f'no correlation': 0.1,
                   f'very weak': 0.2,
                   f'weak ': 0.3, f'moderate': 0.5,
                   f'perceptible': 0.7,
                   f'high': 0.9,
f'very high': 0.99,
                   f'functional': 1.0}
               r_scale = list(Cheddock_scale.values())
               for i, elem in enumerate(r_scale):
                   if abs(r) <= elem:</pre>
                       conclusion_Cheddock_scale = list(Cheddock_scale.keys())[i]
               {\bf return} \ \ {\bf conclusion\_Cheddock\_scale}
```

```
matrix_XY_df = pd.DataFrame({
                                          'X': X,
                                          'Y': Y})
                               # число интервалов группировки
                               group\_int\_number = lambda \ n: \ round \ (3.31*log(n_X, \ 10)+1) \ if \ round \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ (3.31*log(n_X, \ 10)+1) \ >= 2 \ else \ 2 \ else \
                               K_X = group_int_number(n_X)
                               K_Y = group_int_number(n_Y)
                               # группировка данных и формирование корреляционной таблицы
                               cut_X = pd.cut(X, bins=K_X)
                               cut_Y = pd.cut(Y, bins=K_Y)
                               matrix_XY_df['cut_X'] = cut_X
                              matrix_XY_df['cut_Y'] = cut_Y
CorrTable_df = pd.crosstab(
                                         index=matrix_XY_df['cut_X'],
                                        columns=matrix_XY_df['cut_Y'],
                                         rownames=['cut_X'],
                                        colnames=['cut_Y'])
                               CorrTable_np = np.array(CorrTable_df)
                               K_X = len(CorrTable_np)
                               K_Y = len(CorrTable_np[0])
                                # итоги корреляционной таблицы по строкам и столбцам
                               n_group_X = [np.sum(CorrTable_np[i]) for i in range(K_X)]
                               n_group_Y = [np.sum(CorrTable_np[:,j]) for j in range(len(CorrTable_np[0]))]
                               Xboun\_mean = [(CorrTable\_df.index[i].left + CorrTable\_df.index[i].right)/2 \ \ for \ i \ in \ range(K\_X)]
                               Xboun_mean[0] = (np.min(X) + CorrTable_df.index[0].right)/2 # исправляем значения в крайних интервалах
                               \label{eq:local_control} Xboun\_mean[K\_X-1] = (CorrTable\_df.index[K\_X-1].left + np.max(X))/2
                                # среднегрупповые значения переменной Ү
                               Yboun_mean = [(CorrTable_df.columns[j].left + CorrTable_df.columns[j].right)/2 for j in range(K_Y)]
                               Yboun_mean[0] = (np.min(Y) + CorrTable_df.columns[0].right)/2 # исправляем значения в крайних интервалах
                               Yboun\_mean[K\_Y-1] = (CorrTable\_df.columns[K\_Y-1].left + np.max(Y))/2
                                # средневзевешенные значения Х и Ү для каждой группы
                               \label{thm:mean_group} \textbf{Xmean\_group = [np.sum(CorrTable\_np[:,j] * Xboun\_mean) / n\_group\_Y[j] for j in range(K\_Y)]}
                               Ymean_group = [np.sum(CorrTable_np[i] * Yboun_mean) / n_group_X[i] for i in range(K_X)]
                                # общая дисперсия Х и Ү
                               Sum2\_total_X = np.sum(n\_group_X * (Xboun\_mean - np.mean(X))**2)
                               Sum2\_total_Y = np.sum(n\_group_Y * (Yboun_mean - np.mean(Y))**2)
                                # межгрупповая дисперсия Х и Ү (дисперсия групповых средних)
                              Sum2_between_group_X = np.sum(n_group_Y * (Xmean_group - np.mean(X))**2)
Sum2_between_group_Y = np.sum(n_group_X * (Ymean_group - np.mean(Y))**2)
                                # эмпирическое корреляционное отношение
                               corr_ratio_XY = sqrt(Sum2_between_group_Y / Sum2_total_Y)
                               corr_ratio_YX = sqrt(Sum2_between_group_X / Sum2_total_X)
                               try:
                                        if orientation!='XY' and orientation!='YX':
                                                 raise ValueError("Error! Incorrect orientation!")
                                         if orientation=='XY':
                                                 corr_ratio = corr_ratio_XY
                                         elif orientation=='YX':
                                                corr ratio = corr_ratio_YX
                               except ValueError as err:
                                       print(err)
                                # проверка гипотезы о значимости корреляционного отношения
                                F\_corr\_ratio\_calc = (n\_X - K\_X)/(K\_X - 1) * corr\_ratio**2 / (1 - corr\_ratio**2) 
                               dfn = K_X - 1
                               dfd = n_X - K_X
                               F_corr_ratio_table = sci.stats.f.ppf(p_level, dfn, dfd, loc=0, scale=1)
                               a_corr_ratio_calc = 1 - sci.stats.f.cdf(F_corr_ratio_calc, dfn, dfd, loc=0, scale=1)
                               conclusion_corr_ratio_sign = 'significance' if F_corr_ratio_calc >= F_corr_ratio_table else 'not significance'
                                # доверительный интервал корреляционного отношения
                               if F_corr_ratio_calc >= F_corr_ratio_table:
                                         f1 = round ((K_X - 1 + n_X * corr_ratio**2)**2 / (K_X - 1 + 2 * n_X * corr_ratio**2))
                                         f2 = n_X - K_X
                                         z1 = (\bar{n}_X - \bar{k}_X) / n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(p_level, f1, f2, loc=0, scale=1) - (\bar{k}_X - 1)/n_X * (\bar{
                                         z2 = (n_X - K_X) / n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) - (K_X - 1)/n_X * corr_ratio**2 / (1 - corr_ratio**2) * 1/sci.stats.f.ppf(1 - p_level, f1, f2, loc=0, scale=1) * (1 - corr_ratio**2) 
                                         corr_ratio_conf_int_low = sqrt(z1) if sqrt(z1) >= 0 else 0
                                         corr_ratio_conf_int_high = sqrt(z2) if sqrt(z2) <= 1 else 1</pre>
                                        corr_ratio_conf_int_low = corr_ratio_conf_int_high = '-'
                                # оценка тесноты связи
                               if scale=='Cheddok':
                                         conclusion_corr_ratio_scale = scale + ': ' + Cheddock_scale_check(corr_ratio, name=chr(951))
                                         conclusion_corr_ratio_scale = scale + ': ' + Evans_scale_check(corr_ratio, name=chr(951))
                                # формируем результо
                               result = pd.DataFrame({
                                          'notation': (chr(951)),
                                          'coef_value': (corr_ratio),
                                          'c_v_squared': (corr_ratio**2),
                                          'p_level': (p_level),
                                          'a_level': (a_level),
                                          'F_calc': (F_corr_ratio_calc),
                                          'F_table': (F_corr_ratio_table),
                                          'F_calc >= F_table': (F_corr_ratio_calc >= F_corr_ratio_table),
                                          'a_calc': (a_corr_ratio_calc),
                                          'a_calc <= a_level': (a_corr_ratio_calc <= a_level),</pre>
                                          'significance': (conclusion_corr_ratio_sign),
                                         'conf_int_low': (corr_ratio_conf_int_low),
'conf_int_high': (corr_ratio_conf_int_high),
                                          'scale': (conclusion_corr_ratio_scale)
                                         index=[name])
                               return result
In [22]: names = data.columns
                     new_df = pd.DataFrame({
                                          'notation': (),
                                          'coef_value': (),
                                          'c_v_squared': (),
                                          'p_level': (),
                                          'a_level': (),
                                          'F_calc': (),
                                          'F_table': (),
                                          'F_calc >= F_table': (),
                                          'a_calc': (),
                                          'a_calc <= a_level': (),</pre>
                                          'significance': (),
                                          'conf_int_low': (),
                                          'conf_int_high': (),
                                          'scale': ()
                                         })
                      for one in names:
                               for two in names:
                                       if(one!=two):
                                                  try:
                                                           res = corr_ratio_check(data[one], data[two])
                                                           new_df = pd.concat([new_df, res])
                                                  except:
                                                           print('error')
```

 $n_Y = len(Y)$

запишем данные в DataFrame

				-	_		_				3			
var1 var2	η	0.406018	0.164851	0.95	0.05	1.414632	2.318498	0.0	2.311710e-01	0.0	not significance	-	-	Cheddok: moderate
var1 var3	η	0.920520	0.847357	0.95	0.05	39.783996	2.318498	True	5.551115e-16	True	significance	1.612586	1	Cheddok: very high
var1 var4	η	0.702272	0.493185	0.95	0.05	6.973938	2.318498	True	3.177223e-05	True	significance	0.57308	1	Cheddok: high
var1 var5	η	0.618713	0.382805	0.95	0.05	4.445013	2.318498	True	1.393598e-03	True	significance	0.395595	1	Cheddok: perceptible
var2 var1	η	0.404477	0.163602	0.95	0.05	1.401822	2.318498	False	2.360105e-01	False	not significance	-	-	Cheddok: moderate
var2 var3	η	0.476072	0.226645	0.95	0.05	2.100309	2.318498	False	7.286889e-02	False	not significance	-	-	Cheddok: moderate
var2 var4	η	0.481702	0.232037	0.95	0.05	2.165375	2.318498	False	6.513877e-02	False	not significance	-	-	Cheddok: moderate
var2 var5	η	0.272468	0.074239	0.95	0.05	0.574711	2.318498	False	7.482250e-01	False	not significance	-	-	Cheddok: weak
var3 var1	η	0.909746	0.827638	0.95	0.05	34.412455	2.318498	True	7.105427e-15	True	significance	1.490374	1	Cheddok: very high
var3 var2	η	0.336767	0.113412	0.95	0.05	0.916756	2.318498	False	4.922925e-01	False	not significance	-	-	Cheddok: moderate
var3 var4	η	0.756170	0.571794	0.95	0.05	9.569807	2.318498	True	1.111974e-06	True	significance	0.711491	1	Cheddok: high
var3 var5	η	0.468123	0.219139	0.95	0.05	2.011242	2.318498	False	8.492764e-02	False	not significance	-	-	Cheddok: moderate
var4 var1	η	0.695733	0.484045	0.95	0.05	8.255744	2.427040	True	1.447203e-05	True	significance	0.582481	1	Cheddok: perceptible
var4 var2	η	0.320314	0.102601	0.95	0.05	1.006118	2.427040	False	4.254677e-01	False	not significance	-	-	Cheddok: moderate
var4 var3	η	0.736718	0.542754	0.95	0.05	10.445655	2.427040	True	1.187842e-06	True	significance	0.67928	1	Cheddok: high
var4 var5	η	0.266963	0.071269	0.95	0.05	0.675296	2.427040	False	6.443645e-01	False	not significance	-	-	Cheddok: weak
var5 var1	η	0.592440	0.350985	0.95	0.05	3.875701	2.318498	True	3.525059e-03	True	significance	0.343286	0.981747	Cheddok: perceptible
var5 var2	η	0.329227	0.108391	0.95	0.05	0.871233	2.318498	False	5.238241e-01	False	not significance	-	-	Cheddok: moderate
var5 var3	η	0.492239	0.242300	0.95	0.05	2.291777	2.318498	False	5.236408e-02	False	not significance	-	-	Cheddok: moderate
var5 var4	η	0.354154	0.125425	0.95	0.05	1.027787	2.318498	False	4.205297e-01	False	not significance	-	-	Cheddok: moderate