

# CSC 1301 – Spring 2020

## Homework #2

Due 02/11/2020

### Binary Calculation, Data Manipulation & Representation

Name Rafid Shaou Lab Time Friday - 3:00 PM

You must show all work for all problems -failure to show work results in Zero points

Complete the following problems for the other values.

	Decimal	Hexadecimal	Binary	Octal
1. $10111010_2$ $2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1$ $128 + 32 + 16 + 8 + 2 = 186$	<u>186<sub>10</sub></u>	$\begin{array}{r l} 1011 & 1010 \\ \hline 8 & 4 \end{array}$ 11 → B 10 → A <u>BA<sub>16</sub></u>	$\begin{array}{r l} 010 & 111 & 010 \\ \hline 4 & 2 & 1 \end{array}$ 2 7 2 <u>272<sub>8</sub></u>	Octal
2. $11110011_2$ $2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1$ $128 + 64 + 32 + 16 + 2 + 1 = 243$	<u>243<sub>10</sub></u>	$\begin{array}{r l} 1111 & 0011 \\ \hline 8 & 4 \end{array}$ 11 → B 10 → A <u>F3<sub>16</sub></u>	$\begin{array}{r l} 010 & 111 & 010 \\ \hline 4 & 2 & 1 \end{array}$ 2 7 2 <u>363<sub>8</sub></u>	Octal
3. $10101010_2$ $2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1$ $128 + 64 + 32 + 16 + 2 + 1 = 243$	<u>170<sub>10</sub></u>	$\begin{array}{r l} 1111 & 0011 \\ \hline 8 & 4 \end{array}$ 15 → F 3 <u>AF<sub>16</sub></u>	$\begin{array}{r l} 011 & 110 & 011 \\ \hline 4 & 2 & 1 \end{array}$ 3 6 3 <u>252<sub>8</sub></u>	Octal
4. $11111110_2$ $2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1$ $128 + 64 + 32 + 16 + 8 + 4 + 2 = 254$	<u>254<sub>10</sub></u>	$\begin{array}{r l} 1010 & 1010 \\ \hline 8 & 4 \end{array}$ 10 → A 10 → A <u>FE<sub>16</sub></u>	$\begin{array}{r l} 010 & 101 & 010 \\ \hline 4 & 2 & 1 \end{array}$ 2 5 2 <u>376<sub>8</sub></u>	Octal
5. $11011011_2$ $2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1$ $128 + 64 + 32 + 16 + 8 + 4 + 2 = 254$	<u>219<sub>10</sub></u>	$\begin{array}{r l} 1111 & 1110 \\ \hline 8 & 4 \end{array}$ 15 → F 14 → E <u>DE<sub>16</sub></u>	$\begin{array}{r l} 011 & 111 & 110 \\ \hline 4 & 2 & 1 \end{array}$ 3 7 6 <u>333<sub>8</sub></u>	Octal
6. $2E_{16}$ $\begin{array}{r} 2 \\ \swarrow \searrow \\ 8 \ 4 \end{array}$ $\begin{array}{r} E \rightarrow 14 \\ \swarrow \searrow \\ 8 \ 4 \end{array}$ $\begin{array}{r} 0010 \\ 1110 \end{array}$	<u>46<sub>10</sub></u>	$\begin{array}{r l} 1101 & 1011 \\ \hline 8 & 4 \end{array}$ 13 → D 11 → B <u>5B<sub>16</sub></u>	$\begin{array}{r l} 011 & 011 & 011 \\ \hline 4 & 2 & 1 \end{array}$ 3 3 3 <u>101110<sub>2</sub></u>	Octal
7. $16_{16}$ $\begin{array}{r} 1 \\ \swarrow \searrow \\ 8 \ 4 \end{array}$ $\begin{array}{r} 6 \\ \swarrow \searrow \\ 8 \ 4 \end{array}$ $\begin{array}{r} 0001 \\ 0110 \end{array}$	<u>22<sub>10</sub></u>	$\begin{array}{r l} 101 & 110 \\ \hline 4 & 2 \end{array}$ 5 6 <u>26<sub>8</sub></u>	$\begin{array}{r l} 101110 \\ \hline 2^5 \ 2^4 \ 2^3 \ 2^2 \end{array}$ 32 + 8 + 4 + 2 = 46 <u>101110<sub>2</sub></u>	Octal
8. $AA_{16}$ $\begin{array}{r} 8 \ 4 \end{array}$ $\begin{array}{r} 0001 \\ 0110 \end{array}$	<u>170<sub>10</sub></u>	$\begin{array}{r l} 010 & 110 \\ \hline 4 & 2 \end{array}$ 2 6 <u>252<sub>8</sub></u>	$\begin{array}{r l} 10110 \\ \hline 2^4 \ 2^3 \ 2^2 \end{array}$ 16 + 4 + 2 = 22 <u>10101010<sub>2</sub></u>	Octal

## Short Answers

1. What are the 4-bit patterns used to represent each of the characters in the string "1302"?  
\*\*\*\*\*Only represent the characters between the quotation marks.) Note: There is space between 1302.

$2^{11} \boxed{2^{10}} 2^9 \boxed{2^8} 2^7 2^6 2^5 \boxed{2^4} 2^3 \boxed{2^2} \boxed{2^1} 2^0$   
2048 1024 512 256 128 64 32 16 8 4 2 1  
10100010110

$$\begin{array}{r} 1302 \\ -1024 \\ \hline 278 \end{array} \quad \begin{array}{r} 278 \\ -256 \\ \hline 22 \end{array} \quad \begin{array}{r} 22 \\ -16 \\ \hline 6 \end{array} \quad \begin{array}{r} 6 \\ -4 \\ \hline 2 \end{array} \quad \begin{array}{r} 2 \\ -2 \\ \hline 0 \end{array}$$

2. What is the biggest value we can express in 4 bits? Express it in both binary and in decimal:

binary 1111 decimal 15

3. What is the smallest value we can express in 4 bits if we use unsigned numbers? Express it in both binary and in decimal:

binary 0000 decimal 0

## FLOATING POINT BINARY CONVERSIONS

### Sample Table

\*\*\*\* This table shows the smallest fraction that can be stored in a 23-bit mantissa. This table shows a few simple examples of binary floating-point numbers alongside their equivalent decimal fractions and decimal values:

Binary	Decimal Fraction	Decimal Value
.1	1/2	.5
.01	1/4	.25
.001	1/8	.125
.0001	1/16	.0625
.00001	1/32	.03125



### 1. Convert the following to binary:

a)  $9.027 = 1001.00000110111010011$

⑨ + 0.027

$$\begin{array}{l} 9 \div 2 = 4 \text{ R } 1 \\ 4 \div 2 = 2 \text{ R } 0 \\ 2 \div 2 = 1 \text{ R } 0 \\ 1 \div 2 = 0 \text{ R } 1 \end{array}$$

$9 = 1001$

$$\begin{array}{l} 0.027 \times 2 = 0.054 \\ 0.054 \times 2 = 0.108 \\ 0.108 \times 2 = 0.216 \\ 0.216 \times 2 = 0.432 \\ 0.432 \times 2 = 0.864 \\ 0.864 \times 2 = 1.728 \end{array}$$

0  
0  
0  
0  
0  
1

→ cont...

b)  $13.0920 =$

⑬ + 0.0920

$$13 \div 2 = 6 \text{ R } 1$$

$$6 \div 2 = 3 \text{ R } 0$$

$$3 \div 2 = 1 \text{ R } 1$$

$$1 \div 2 = 0 \text{ R } 1$$

$13 = 1101$

$$\begin{array}{l} 0.0920 \times 2 = 0.184 \\ 0.184 \times 2 = 0.368 \\ 0.368 \times 2 = 0.736 \\ 0.736 \times 2 = 1.472 \end{array}$$

0  
0  
0  
1

→ cont...

### 2. Find and bring in a URL that explains floating point representation

if URL works, 3 points - only 1 if it's just present but doesn't work

[geckstorgeeks.org/floating-point-representation-basics/](http://geckstorgeeks.org/floating-point-representation-basics/)

### 3. Convert the following to decimal

a)  $0110.01001$

$$4 + 2 + \frac{1}{4} + \frac{1}{32} = 6.28125$$

b)  $1010.10001$

$$8 + 2 + \frac{1}{2} + \frac{1}{32} = 10.53125$$

$$1+2+9 = 12 \rightarrow C_{16}$$

$$8+1 = 9_{16}$$

## Bonus

1) Demonstrate how to solve the hexadecimal Arithmetic (Show work)

$\begin{array}{r} \overset{1}{a) \ 82CD} \\ + 1982 \\ \hline 9C4F_{16} \end{array}$	$\begin{array}{l} D+2 = 13+2 \\ = 15 \\ = F_{16} \\ \hline C+8 = 12+8 \\ = 20 \\ = 16+4 \\ = 14_{16} \end{array}$	$\begin{array}{r} b) \ A31 \\ + E2C \\ \hline 1185D_{16} \end{array}$	$\begin{array}{l} 1+C = 1+12 \\ = 13 \\ = D_{16} \\ \hline 3+2 = 5_{16} \\ \hline A+E = 10+14 \\ = 24 \\ = 16+8 \\ = 18_{16} \end{array}$
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2) Show the unsigned binary number 1010 1010 1010.1010 in decimal? (Show work)

$$2048 + 512 + 128 + 32 + 8 + 2 + \frac{1}{2} + \frac{1}{8} = 2730.625$$