

Problem 1

Subtract the following hexadecimal numbers:

$$7ACD - 3AFE = ?$$

$$\begin{array}{r} 7ACD \\ - 3AFE \\ \hline \end{array}$$

Step-1: D-E

Here $D = 13 < E = 14$, we take/borrow from CSo $C = 12$ becomes 11 and $D = 13$ becomes $13 + 16 = 29$

$$= 29 - 14$$

$$= 15$$

$$= F_{16}$$

$$\begin{array}{r} 7A\overset{11}{\cancel{C}}\overset{29}{\cancel{D}} \\ - 3AFE \\ \hline F \end{array}$$

Step-2: B-F

Here $B = 11 < F = 15$, we take/borrow from ASo $A = 10$ becomes 9 and $B = 11$ becomes $11 + 16 = 27$

$$= 27 - 15$$

$$= 12$$

$$= C_{16}$$

$$\begin{array}{r} 7\overset{9}{\cancel{A}}\overset{27}{\cancel{B}}\overset{29}{\cancel{C}}\overset{29}{\cancel{D}} \\ - 3AFE \\ \hline CF \end{array}$$

Step-3: 9-A

Here $9 < A = 10$, we take/borrow from 7

$\therefore 7$ becomes 6 and 9 becomes $9 + 16 = 25$

$$= 25 - 10$$

$$= 15$$

$$= F_{16}$$

$$\begin{array}{r} 25 27 \\ 6 9 4 29 \\ 7 A C D \\ - 3 A F E \\ \hline F C F \end{array}$$

Step-4: 6-3

Here $6 > 3$, so directly subtract it

$$= 6-3$$

$$= 3$$

$$= 3_{16}$$

$$\begin{array}{r} 25 27 \\ 6 9 H 29 \\ \cancel{7} \cancel{A} \cancel{L} \cancel{D} \\ - 3 A F E \\ \hline 3 F C F \end{array}$$

Problem 2

Convert 01110110 into 2's Complement form.

Convert 01110110 into 2's Complement form.

1) Flip all bits...

10001001 (This is 1's complement)

2) Add 1 to the 1's complement

$$\begin{array}{r} 10001001 \\ + \quad \quad \quad 1 \\ \hline 10001010 \end{array}$$
 (This is 2's complement)

Problem 3

Subtract the following Octal numbers:

$$765 - 377 = ?$$

$$\begin{array}{r} 765 \\ - 377 \\ \hline \end{array}$$

Step-1: $5 - 7$

Here $5 < 7$, we take/borrow from 6

So 6 becomes 5 and 5 becomes $5 + 8 = 13$

$$= 13 - 7$$

$$= 6_8$$

$$\begin{array}{r} 5 \quad 13 \\ 7 \quad 6 \quad 5 \end{array}$$

$$\begin{array}{r}
 5 13 \\
 7 6 5 \\
 - 3 7 7 \\
 \hline
 6
 \end{array}$$

Step-2: $5 - 7$

Here $5 < 7$, we take/borrow from 7

So 7 becomes 6 and 5 becomes $5 + 8 = 13$

$$= 13 - 7$$

$$= 6_8$$

$$\begin{array}{r}
 13 \\
 6 5 13 \\
 7 6 5 \\
 - 3 7 7 \\
 \hline
 6 6
 \end{array}$$

Step-3: $6 - 3$

Here $6 > 3$, so directly subtract it

$$= 6 - 3$$

$$= 3_8$$

$$\begin{array}{r}
 13 \\
 6 5 13 \\
 7 6 5
 \end{array}$$

$$\begin{array}{r} - 377 \\ \hline 366 \end{array}$$