

Answer: $A = 10100111$

$$\begin{array}{r}
 & \overset{11}{\text{ }} \overset{11}{\text{ }} \leftarrow \text{carry} \\
 B = & 11110110 \\
 + & \\
 \hline
 & \overset{1}{\text{ }} 1001\overset{1}{\text{ }} 1101 \\
 & \text{Discarded}
 \end{array}$$

8-bit

rubric : if the process is right, \Rightarrow math has ^{minor} 1 mistakes
 \hookrightarrow give 80%

give partial credit if math is half done.

Answer: $70 - 10 - 42$

70 in binary:

<u>Division</u>	<u>Quotient</u>	<u>Remainder</u>
$70/2$	35	0
$35/2$	17	1
$17/2$	8	1
$8/2$	4	0
$4/2$	2	0
$2/2$	1	0
$1/2$	0	1

so, 70 in binary = 1000110

70 in 8-bit binary = 01000110

10 in binary = 1010

10 in 8-bit binary = 00001010

-10 in binary:

2's complement of 10:
 1) flip the bits : $\begin{array}{r} 1 \\ 11110101 \\ 00000001 \\ \hline 11110110 \end{array}$
 2) Add 1

42 in binary:

<u>Division</u>	<u>Quotient</u>	<u>Remainder</u>
$42/2$	21	0
$21/2$	10	1
$10/2$	5	0
$5/2$	2	1
$2/2$	1	0
$1/2$	0	1

42 in binary = 101010

42 in 8-bit binary = 00101010

- 42 in binary:

2's complement of 42 : 00101010

1) flip the bits: 11010101

2) Add 1: $\begin{array}{r} 00000001 \\ + 11010101 \\ \hline 11010110 \end{array}$

$$\text{Now, } \underline{70 - 10} : = 70 + (-10)$$

$$\begin{array}{r} 1 & 1 \\ 70 & : 01000110 \\ -10 & : 11110110 (+) \\ \hline 100111100 \end{array}$$

8-bit

Discard

$$\text{Now: } (70 - 10) - 42 = (70 - 10) + (-42)$$

$$\begin{array}{r} 11111 \\ (70-10) : 00111100 \\ -42 : 11010110 (+) \\ \hline 10010010 \end{array}$$

8-bit

Discard

Now Answer is = 00010010

Convert it to decimal $\frac{1}{2}$

$$\begin{array}{r}
 10010 \\
 \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\
 1 \cdot 2^4 + 0 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 0 \cdot 2^0 \\
 = 16 + 0 + 0 + 2 + 0 \\
 = 18. \text{ (Answer)}
 \end{array}$$

Q4.

Answer:

$$\begin{array}{ccccccc} \underline{1101} & \underline{0011} & \underline{0111} & \underline{1101} & \underline{1100} & \underline{1111} & \underline{0001} \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ D & 3 & 7 & D & C & F & 1) \end{array}$$

Answers D37DCF1

$$\begin{aligned} A &= 1010 \\ B &= 1011 \\ C &= 1100 \\ D &= 1101 \\ E &= 1110 \\ F &= 1111 \end{aligned}$$

Q5: Approach - I
 - 90

Convert 90 to binary:

<u>Division</u>	<u>Quotient</u>	<u>Remainder</u>
$90/2$	45	0
$45/2$	22	1
$22/2$	11	0
$11/2$	5	1
$5/2$	2	1
$2/2$	1	0
$1/2$	0	1

90 in binary: 1011010

90 in 16-bit binary = 0000 0000 0101 1010

2's complement of 90:

1) Flip the bits: 1111 1111 1010 0101
 2) Add 1 : 0000 0000 0000 0001 (+)
1111 1111 1010 0110

Convert to Hex:

F F A 6

Answer: FFA6

Q5: Approach -2

Convert 90 to Hexadecimal:

Division	Quotient	Remainder
90/16	5	10 (A)
5/16	0	5

90 is in Hexadecimal = 5A

16-bit Hex of 90 = 005A

Hexadecimal 2's complement:

i) Subtract all digits from 15 (F)

$$\begin{array}{r} F F F F \\ 005A \text{ } (-) \\ \hline FFA5 \end{array}$$

z) Add 1 : $FFA5 + 1 = \underline{\underline{FFA6}}$ (Answer).

Q:6

Answer:

(a) The signed binary number is negative.
because most significant bit is 1.

first, perform a 2's complement on 11110101

$$\begin{array}{r} \text{1) Flip the bits - } 00001010 \\ \text{2) Add 1 } - \frac{00000001 (+)}{00001011} \end{array}$$

Now, Convert to decimal

$$\begin{array}{r} 1011 \\ 1*2^3 + 0*2^2 + 1*2^1 + 1*2^0 \\ 8 + 0 + 2 + 1 \end{array}$$

$$\text{Answer is } = \underline{\underline{-11}}$$

Q6

(b) 00110101

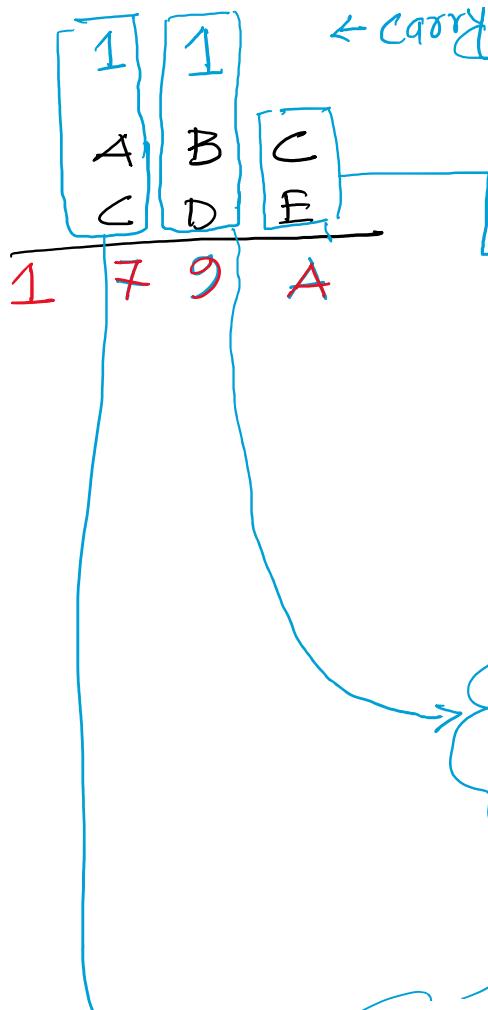
The signed number is positive, because most significant bit is 0.

convert the number into decimal.

$$\begin{array}{r} \underline{110101} \\ 1 \cdot 2^5 + 1 \cdot 2^4 + 0 \cdot 2^3 + 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 \\ 32 + 16 + 0 + 4 + 0 + 1 \\ = 53 \quad (\text{Answer}) \end{array}$$

$A = 10$
 $B = 11$
 $C = 12$
 $D = 13$
 $E = 14$
 $F = 15$

Q-7



$c = 12, e = 14, c + e = 12 + 14 = 26$

Now, $26/16 = 1$, remainder = 10
 $= A$
 result

$b = 11, d = 13, 1 + b + d = 1 + 11 + 13 = 25$

Now, $25/16 = 1$, remainder = 9
 carry
 result

$a = 10, c = 12, 1 + a + c = 1 + 10 + 12 = 23$

Now, $23/16 = 1$, remainder = 7
 carry

$(16 + 10 - 1) = 12 = C$

$(-1 + 9 - 1) = 7$

Answer = 127C

Q-8: the range of signed integers is -2^{n-1} to $+2^{n-1}-1$ where n is the number of bits.

so, for 5-bit storage range = -2^{5-1} to $+2^{5-1}-1$
or -2^4 to 2^4-1
or (-16 to 15)

so, -19 cannot be stored ~~is~~ correctly in 5-bit storage.

Q-9: smallest value can be stored in a n bit storage

$$-2^{n-1} = \text{for } 145\text{-bit, it is } -2^{-145-1} = -2^{144}$$

Q-10:

X	Y	Z	P
0	0	0	0
0	0	1	1 → $(\bar{x} \wedge \bar{y} \wedge z)$
0	1	0	1 → $(x \wedge \bar{y} \wedge \bar{z})$
0	1	1	1 → $(x \wedge y \wedge z)$
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

$$P = (\bar{x} \wedge \bar{y} \wedge z) \vee (x \wedge \bar{y} \wedge \bar{z}) \vee (x \wedge y \wedge z)$$

