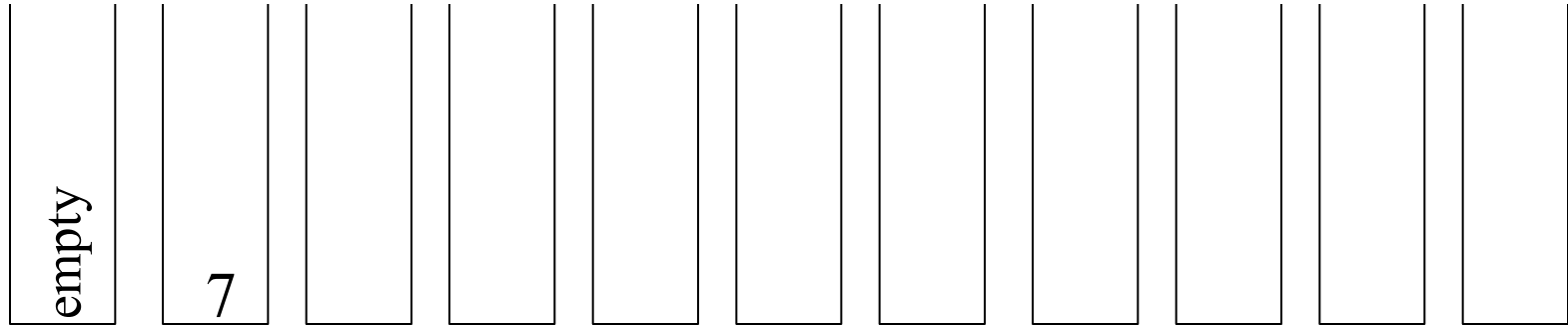
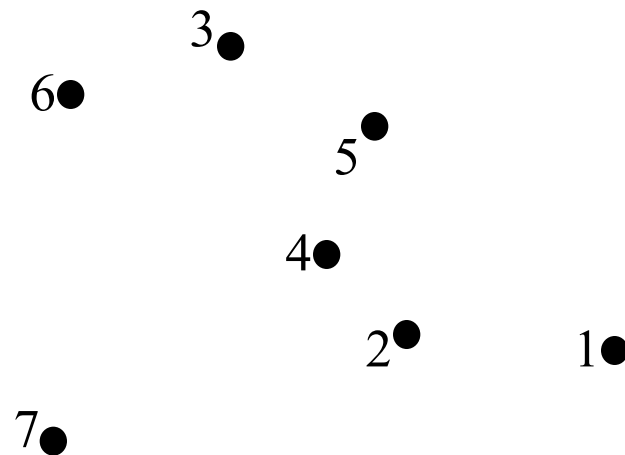


2. For Graham's scan finding convex hull of the point set given below:

- Give the sorted sequence of points for Graham scan \_\_\_\_\_
- Show the content of the stack after each change



- Give the convex hull of this point set \_\_\_\_\_



3. Below given a point set in the **rectilinear** metric (the height/width of any cell=1) where the closest pair of points should be found using divide and conquer. Show

- the first partition of the point set (draw a line)

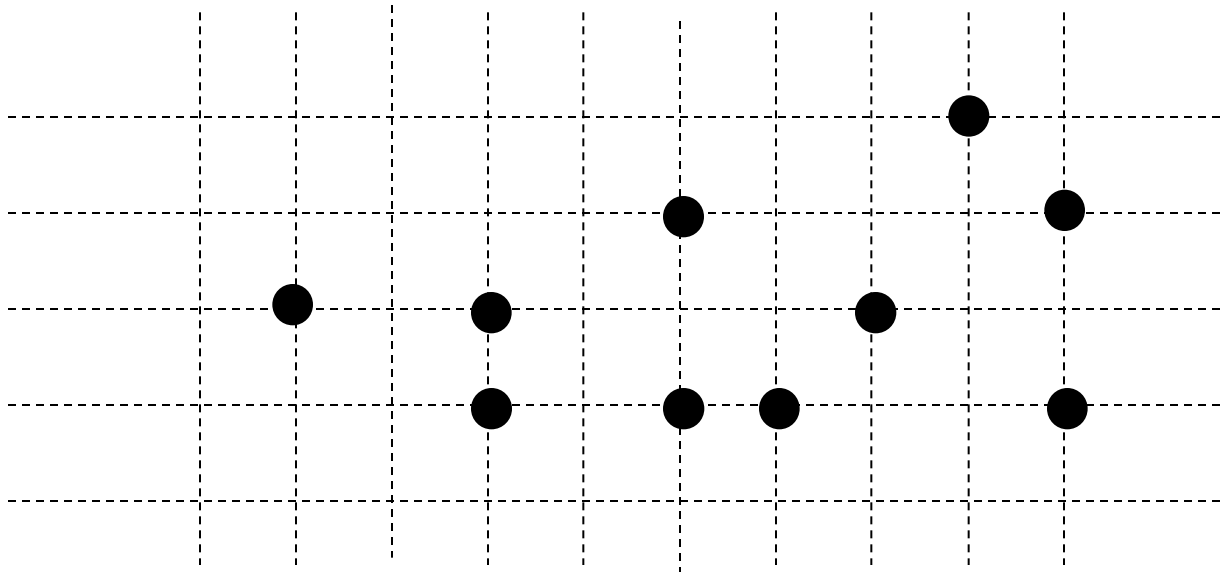
- the closest pair in the left part (connect solid),  $\delta_{\text{left}} = \underline{\hspace{2cm}}$ ,

and the right part (connect solid),  $\delta_{\text{right}} = \underline{\hspace{2cm}}$

- the middle strip (shade)

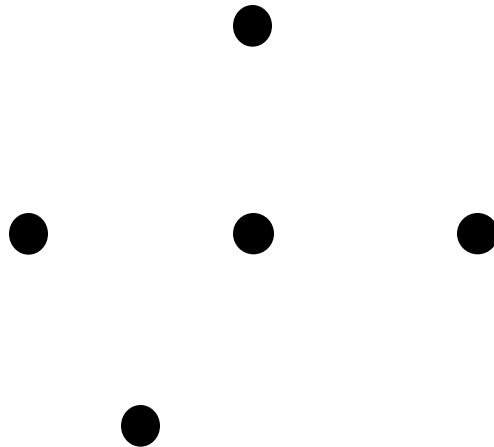
- pairs in the middle strip for which distances should be computed (connect dashed)

- closest pair in the middle strip (connect solid)



4. Below given a point set in the **Euclidean** metric. Draw

- Voronoi regions (dashed edges)
- Voronoi graph / Delanau triangulation (solid edges)
- minimum spanning tree (double edges)

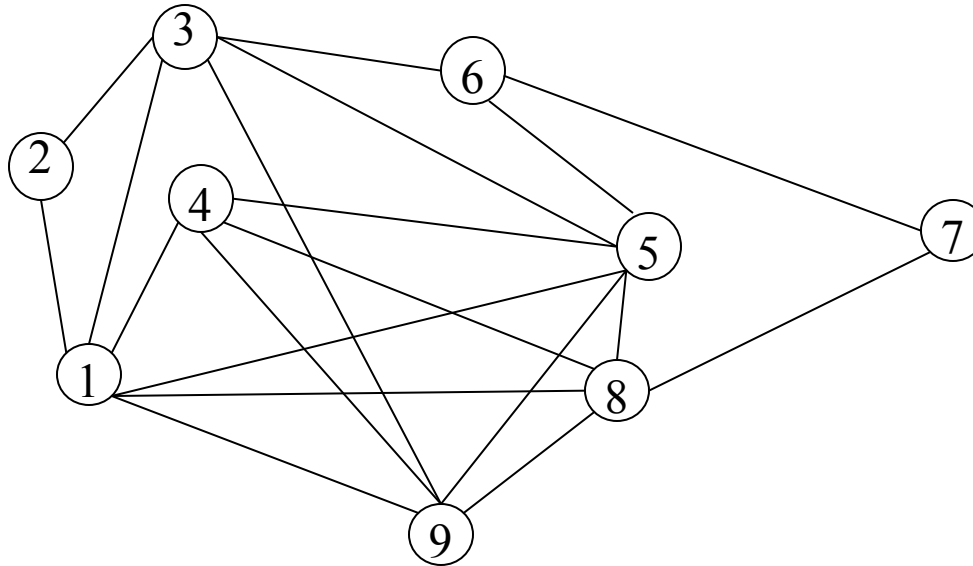


6. In the following graph find

- Maximum Independent Set \_\_\_\_\_

- Minimum Vertex Cover \_\_\_\_\_

- Maximum Clique \_\_\_\_\_



7. For the 3-CNF

$$f = (x' + y + z) \& (x + y' + z') \& (x + y + z') \& (x' + y' + z) \& (x' + y + z') \& (x + y + z)$$

- give 0-1 assignment to variables such that  $f=1$  \_\_\_\_\_
- give 0-1 assignment to variables such that  $f=0$  \_\_\_\_\_
- Draw the corresponding graph and mark the maximum independent set

8. Prove, that the Steiner Tree problem, (finding shortest tree connecting  $n$  points in the plane) is in class NP

a) Optimization formulation

b) Decision formulation

c) Polynomial-size certificate

d) Polynomial time verification algorithm