数字逻辑



Number Systems

Decimal numbers

Binary numbers



Number Systems

Decimal numbers

$$5374_{10} = 5 \times 10^3 + 3 \times 10^2 + 7 \times 10^1 + 4 \times 10^0$$
five three seven four thousands hundreds tens ones

Binary numbers



Number Conversion

- Decimal to binary conversion:
 - Convert 10011₂ to decimal

- Decimal to binary conversion:
 - Convert 47₁₀ to binary

Number Conversion

- Decimal to binary conversion:
 - Convert 10011₂ to decimal
 - $-16\times1+8\times0+4\times0+2\times1+1\times1=19_{10}$

- Decimal to binary conversion:
 - Convert 47₁₀ to binary
 - $-32\times1+16\times0+8\times1+4\times1+2\times1+1\times1=101111_2$

Hexadecimal Numbers

Hex Digit	Decimal Equivalent	Binary Equivalent
0	0	
1	1	
2	2	
3	3	
4	4	
5	5	
6	6	
7	7	
8	8	
9	9	
A	10	
В	11	
С	12	
D	13	
Е	14	
F	15	

ONE

Hexadecimal Numbers

Hex Digit	Decimal Equivalent	Binary Equivalent
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
С	12	1100
D	13	1101
Е	14	1110
F	15	1111



Hexadecimal to Binary Conversion

- Hexadecimal to binary conversion:
 - Convert 4AF₁₆ (also written 0x4AF) to binary

- Hexadecimal to decimal conversion:
 - Convert 0x4AF to decimal



Hexadecimal to Binary Conversion

- Hexadecimal to binary conversion:
 - Convert 4AF₁₆ (also written 0x4AF) to binary
 - 0100 1010 1111₂

- Hexadecimal to decimal conversion:
 - Convert 4AF₁₆ to decimal
 - $16^2 \times 4 + 16^1 \times 10 + 16^0 \times 15 = 1199_{10}$



Bits, Bytes, Nibbles...

Bits

10010110
most least significant bit bit

Bytes & Nibbles

10010110 nibble

Bytes

CEBF9AD7

most least significant byte byte



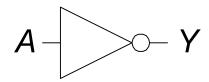
Logic Gates

- Perform logic functions:
 - inversion (NOT), AND, OR, NAND, NOR, etc.
- Single-input:
 - NOT gate, buffer
- Two-input:
 - AND, OR, XOR, NAND, NOR, XNOR
- Multiple-input



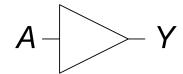
Single-Input Logic Gates

NOT



$$Y = \overline{A}$$

BUF



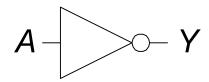
$$Y = A$$

A	Y
0	
1	



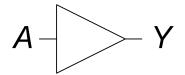
Single-Input Logic Gates

NOT



$$Y = \overline{A}$$

BUF



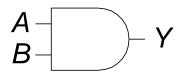
$$Y = A$$

Α	Y
0	0
1	1

ONE

Two-Input Logic Gates

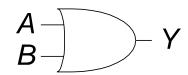
AND



$$Y = AB$$

Α	В	Y
0	0	
0	1	
1	0	
1	1	

OR



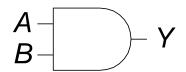
$$Y = A + B$$

A	В	Υ
0	0	
0	1	
1	0	
1	1	



Two-Input Logic Gates

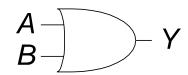
AND



$$Y = AB$$

Α	В	Y
0	0	0
0	1	0
1	0	0
1	1	1

OR

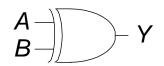


$$Y = A + B$$

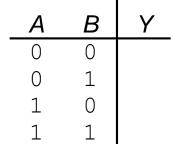
_A	В	Y
0	0	0
0	1	1
1	0	1
1	1	1

More Two-Input Logic Gates

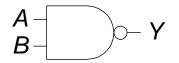
XOR



$$Y = A \oplus B$$



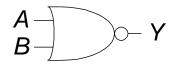
NAND



$$Y = \overline{AB}$$

Α	В	Υ
0	0	
0	1	
1	0	
1	1	

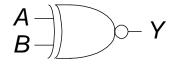
NOR



$$Y = \overline{A + B}$$

A	В	Y
0	0	
0	1	
1	0	
1	1	

XNOR

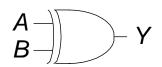


$$Y = \overline{A \oplus B}$$

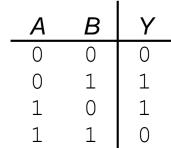
A	В	Y
0	0	
0	1	
1	0	
1	1	

More Two-Input Logic Gates

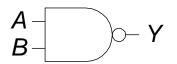
XOR



$$Y = A \oplus B$$



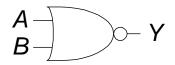
NAND



$$Y = \overline{AB}$$

Α	В	Y
0	0	1
0	1	1
1	0	1
1	1	0

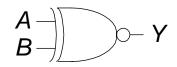
NOR



$$Y = \overline{A + B}$$

A	В	Υ
0	0	1
0	1	0
1	0	0
1	1	0

XNOR



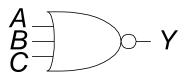
$$Y = \overline{A + B}$$

Α	В	Y
0	0	1
0	1	0
1	0	0
1	1	1

NE

Multiple-Input Logic Gates

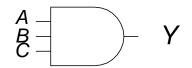
NOR3



$$Y = \overline{A + B + C}$$

Α	В	С	Y
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

AND3



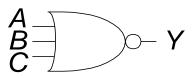
$$Y = ABC$$

A	В	С	Υ
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

NE

Multiple-Input Logic Gates

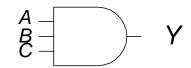
NOR3



$$Y = \overline{A + B + C}$$

A	В	С	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

AND3



$$Y = ABC$$

Α	В	С	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

• Multi-input XOR: Odd parity