

# CSDS 313/413: Introduction to Data Analysis

## Homework 3: Pairwise Association

### Solutions

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## 1 Task 1: Association Between Genomic Variants

### 1.1 Part (a): Two Variables from p1a.csv

#### 1.1.1 Test Statistics and P-values

##### Mutual Information (MI)

- Observed MI value:
- Number of permutations (N):
- P-value:
- Selected significance level ( $\alpha$ ):
- Conclusion:

##### Jaccard Index (JI)

- Observed JI value:
- Number of permutations (N):
- P-value:
- Selected significance level ( $\alpha$ ):
- Conclusion:

##### Pearson's Chi-squared ( $\chi^2$ )

- Observed  $\chi^2$  value:
- Degrees of freedom:
- P-value:
- Selected significance level ( $\alpha$ ):
- Conclusion:

### **1.1.2 Analysis and Interpretation**

**Statistical Significance:**

**Strength of Association:**

**Agreement Between Statistics:**

**Explanation of Any Discrepancies:**

### **1.1.3 Visualization**

## **1.2 Part (b): 105 Variable Pairs from p1b.csv**

### **1.2.1 Test Statistics and P-values**

**Number of Permutations (N):**

**Selected Significance Level ( $\alpha$ ):**

**Multiple Hypothesis Correction Method:**

### **1.2.2 Results Summary**

**Mutual Information (MI)**

- Number of significantly associated pairs:
- List of significant pairs:

**Jaccard Index (JI)**

- Number of significantly associated pairs:
- List of significant pairs:

**Pearson's Chi-squared ( $\chi^2$ )**

- Number of significantly associated pairs:
- List of significant pairs:

### **1.2.3 Comparison of Statistics**

**Overlap Between Statistics:**

- MI and JI overlap:
- MI and  $\chi^2$  overlap:
- JI and  $\chi^2$  overlap:
- All three statistics overlap:

**Which Two Statistics Are Most Similar:**

**Preferred Test Statistic and Justification:**

**Impact of Using Only Preferred Statistic:**

#### **1.2.4 Visualizations**

## 2 Task 2: Association Between Continuous Variables

### 2.1 Part (a): Variable Pair from p2a.csv

#### 2.1.1 Test Statistics and P-value

Pearson Correlation ( $r_a$ ):

- Correlation coefficient:
- P-value ( $p_a$ ):
- Selected significance level ( $\alpha$ ):
- Sample size:

#### 2.1.2 Analysis and Interpretation

Statistical Significance:

Magnitude of Association:

Direction of Association:

#### 2.1.3 Visualization

### 2.2 Part (b): Comparison of p2a.csv and p2b.csv

#### 2.2.1 Test Statistics and P-value for p2b.csv

Pearson Correlation ( $r_b$ ):

- Correlation coefficient:
- P-value ( $p_b$ ):
- Selected significance level ( $\alpha$ ):
- Sample size:

#### 2.2.2 Comparison Analysis

Comparison of Correlations ( $r_a$  vs  $r_b$ ):

Stronger Association Based on Correlations:

Comparison of P-values ( $p_a$  vs  $p_b$ ):

Stronger Association Based on P-values:

Agreement Between Correlations and P-values:

**Explanation of Any Discrepancy:**

**Visual Assessment from Scatter Plots:**

**Agreement with Statistical Measures:**

### **2.2.3 Visualizations**

#### **2.3 Part (c): Comparison of p2a.csv and p2c.csv**

##### **2.3.1 Test Statistics and P-value for p2c.csv**

**Pearson Correlation ( $r_c$ ):**

- Correlation coefficient:
- P-value ( $p_c$ ):
- Selected significance level ( $\alpha$ ):
- Sample size:

##### **2.3.2 Comparison Analysis**

**Comparison of Correlations ( $r_a$  vs  $r_c$ ):**

**Stronger Association Based on Correlations:**

**Comparison of P-values ( $p_a$  vs  $p_c$ ):**

**Stronger Association Based on P-values:**

**Agreement Between Correlations and P-values:**

**Explanation of Any Discrepancy:**

**Visual Assessment from Scatter Plots:**

**Agreement with Statistical Measures:**

### **2.3.3 Visualizations**

### 3 Code Appendix