

Minimize

r

Subject to

Demand Volume:

$$\begin{aligned}x_{111} + x_{121} &= 3 \\x_{112} + x_{122} &= 4 \\x_{113} + x_{123} &= 5 \\x_{114} + x_{124} &= 6 \\x_{211} + x_{221} &= 5 \\x_{212} + x_{222} &= 6 \\x_{213} + x_{223} &= 7 \\x_{214} + x_{224} &= 8 \\x_{311} + x_{321} &= 7 \\x_{312} + x_{322} &= 8 \\x_{313} + x_{323} &= 9 \\x_{314} + x_{324} &= 10\end{aligned}$$

Capacity ST:

$$\begin{aligned}x_{111} + x_{112} + x_{113} + x_{114} - c_{11} &\leq 0 \\x_{121} + x_{122} + x_{123} + x_{124} - c_{12} &\leq 0 \\x_{211} + x_{212} + x_{213} + x_{214} - c_{21} &\leq 0 \\x_{221} + x_{222} + x_{223} + x_{224} - c_{22} &\leq 0 \\x_{311} + x_{312} + x_{313} + x_{314} - c_{31} &\leq 0 \\x_{321} + x_{322} + x_{323} + x_{324} - c_{32} &\leq 0\end{aligned}$$

Capacity TD:

$$\begin{aligned}x_{111} + x_{211} + x_{311} - d_{11} &\leq 0 \\x_{112} + x_{212} + x_{312} - d_{12} &\leq 0 \\x_{113} + x_{213} + x_{313} - d_{13} &\leq 0 \\x_{114} + x_{214} + x_{314} - d_{14} &\leq 0 \\x_{121} + x_{221} + x_{321} - d_{21} &\leq 0 \\x_{122} + x_{222} + x_{322} - d_{22} &\leq 0 \\x_{123} + x_{223} + x_{323} - d_{23} &\leq 0 \\x_{124} + x_{224} + x_{324} - d_{24} &\leq 0\end{aligned}$$

Transit nodes:

$$\begin{aligned}x_{111} + x_{211} + x_{311} + x_{112} + x_{212} + x_{312} + x_{113} + x_{213} + x_{313} + x_{114} + x_{214} + x_{314} - r &\leq 0 \\x_{121} + x_{221} + x_{321} + x_{122} + x_{222} + x_{322} + x_{123} + x_{223} + x_{323} + x_{124} + x_{224} + x_{324} - r &\leq 0\end{aligned}$$

Binary Variables:

$$\begin{aligned}u_{111} + u_{121} &= 2 \\u_{112} + u_{122} &= 2 \\u_{113} + u_{123} &= 2 \\u_{114} + u_{124} &= 2 \\u_{211} + u_{221} &= 2 \\u_{212} + u_{222} &= 2 \\u_{213} + u_{223} &= 2 \\u_{214} + u_{224} &= 2 \\u_{311} + u_{321} &= 2 \\u_{312} + u_{322} &= 2 \\u_{313} + u_{323} &= 2 \\u_{314} + u_{324} &= 2\end{aligned}$$

Demand Flow:

$$\begin{aligned}2 x_{111} - 3 u_{111} &= 0 \\2 x_{121} - 3 u_{121} &= 0 \\2 x_{112} - 4 u_{112} &= 0 \\2 x_{122} - 4 u_{122} &= 0 \\2 x_{113} - 5 u_{113} &= 0 \\2 x_{123} - 5 u_{123} &= 0 \\2 x_{114} - 6 u_{114} &= 0 \\2 x_{124} - 6 u_{124} &= 0 \\2 x_{211} - 5 u_{211} &= 0 \\2 x_{221} - 5 u_{221} &= 0 \\2 x_{212} - 6 u_{212} &= 0 \\2 x_{222} - 6 u_{222} &= 0 \\2 x_{213} - 7 u_{213} &= 0 \\2 x_{223} - 7 u_{223} &= 0 \\2 x_{214} - 8 u_{214} &= 0 \\2 x_{224} - 8 u_{224} &= 0 \\2 x_{311} - 7 u_{311} &= 0 \\2 x_{321} - 7 u_{321} &= 0 \\2 x_{312} - 8 u_{312} &= 0 \\2 x_{322} - 8 u_{322} &= 0 \\2 x_{313} - 9 u_{313} &= 0 \\2 x_{323} - 9 u_{323} &= 0 \\2 x_{314} - 10 u_{314} &= 0 \\2 x_{324} - 10 u_{324} &= 0\end{aligned}$$

Bounds

0 <= x111
0 <= x121
0 <= x112
0 <= x122
0 <= x113
0 <= x123
0 <= x211
0 <= x221
0 <= x212
0 <= x222
0 <= x213
0 <= x223
0 <= x311
0 <= x321
0 <= x312
0 <= x322
0 <= x313
0 <= x323
0 <= r

Binaries

u111
u112
u113
u114
u121
u122
u123
u124
u211
u212
u213
u214
u221
u222
u223
u224
u311
u312
u313
u314
u321
u322
u323
u324

End