

Ejemplo

$Z = a + 2b$

s.a.

r1:  $a + 3b \leq 15$        $a+3b+h1=15$   
r2:  $2a + b \leq 12$        $2a+b+h2=12$   
r3:  $a \geq 0$   
r4:  $b \geq 0$

Maximizar

	a	b	h1	h2		
h1	1	3	1	0	15	5
h2	2	1	0	1	12	12
Zj	-1	-2	0	0	0	

1/3h1	b	1/3	1	1/3	0	5	15
-b+h2	h2	1	2/3	0	- 1/3	1	7
2b+Zj	Zj	- 1/3	0	2/3	0	10	
-1/3a+b	b	0	1	2/5	- 1/5	3	3/5
3/5h2	a	1	0	- 1/5	3/5	4	1/5
1/3a+Zj	Zj	0	0	3/5	1/5	11	2/5

a=	4	1/5
b=	3	3/5
h1=	0	
h2=	0	
Zj=	11	2/5

Minimizar

	a	b	h1	h2		
h1	1	3	1	0	15	5
h2	2	1	0	1	12	12
Zj	1	2	0	0	0	

a=	0
b=	0
h1=	15
h2=	12
Zj=	0

1.  $Z = a + 3b$

s.a.

r1:  $2a + b \leq 50$

r2:  $a + 2b \leq 60$

r3:  $a \geq 0$

r4:  $b \geq 0$

$2a + b + h_1 = 50$

$a + 2b + h_2 = 60$

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Maximizar

	a	b	h1	h2		
h1	2	1	1	0	50	50
h2	1	2	0	1	60	30
Zj	-1	-3	0	0	0	

-1b+h1	h1	1.5	0	1	-0.5	20
1/2h2	b	0.5	1	0	0.5	30
3b+Zj	Zj	0.5	0	0	1.5	90

a=	0
b=	30
h1=	20
h2=	0
Zj=	90

$2a + b + h_1 = 50$	50
$a + 2b + h_2 = 60$	60

Minimizar

	a	b	h1	h2		
h1	2	1	1	0	50	50
h2	1	2	0	1	60	30
Zj	1	3	0	0	0	

a=	0
b=	0
h1=	50
h2=	30
Zj=	0

2.  $Z = 4x + y$

s.a.

r1:  $x + y \geq 8$

r2:  $2x + 2y \leq 35$

r3:  $x \leq 6$

r4:  $x \geq 0$

r5:  $y \geq 0$

$-x - y + h1 = -8$

$2x + 2y + h2 = 35$

$x + h3 = 6$

Maximizar

	x	y	h1	h2	h3		
h1	-1	-1	1	0	0	-8	8
h2	2	2	0	1	0	35	17.5
h3	1	0	0	0	1	6	6
Zj	-4	-1	0	0	0	0	0

1x+h1	h1	0	-1	1	0	1	-2	2
-2x+h2	h2	0	2	0	1	-2	23	11.5
	x	1	0	0	0	1	6	#(DIV/0)!
4x+Zj	Zj	0	-1	0	0	4	24	-24

	y	0	1	-1	0	-1	2	-2
-2y+h2	h2	0	0	2	1	0	19	9.5
	x	1	0	0	0	1	6	#(DIV/0)!
1y+Zj	Zj	0	0	-1	0	3	26	-26

1h1+y	y	0	1	0	0.5	-1	11.5
	h1	0	0	1	0.5	0	9.5
	x	1	0	0	0	1	6
1h1+Zj	Zj	0	0	0	0.5	3	35.5

x=	6	-x-y+h1=-8	-8
y=	11.5	2x+2y+h2=35	35
h1=	9.5	x+h3=6	6
h2=	0		
h3=	0		
Zj=	35.5		

Minimizar

	x	y	h1	h2	h3		
h1	-1	-1	1	0	0	-8	
h2	2	2	0	1	0	35	
h3	1	0	0	0	1	6	
Zj	4	1	0	0	0	0	

x=	0
y=	0
h1=	-8
h2=	35
h3=	6
Zj=	0

3.  $Z = \frac{1}{4}x + \frac{1}{3}y$

s.a.

r1:  $2x + 3y \leq 30$

r2:  $7x + y \leq 49$

r3:  $x - y \leq 15$

r4:  $x \geq 0$

r5:  $y \geq 0$

$2x+3y+h1=30$

$7x+y+h2=49$

$x-y+h3=15$

Maximizar

	x	y	h1	h2	h3		
h1	2	3	1	0	0	30	10
h2	7	1	0	1	0	49	49
h3	1	-1	0	0	1	15	-15
Zj	-0.25	-0.33333333	0	0	0	0	
y	2/3	1	1/3	0	0	10	15
-1y+h2	6 1/3	0	- 1/3	1	0	39	6.15789474
1y+h3	1 2/3	0	1/3	0	1	25	15
1/3y+Zj	- 1/36	0	1/9	0	0	3 1/3	
-2/3x+y	0	1	7/19	- 2/19	0	5 17/19	
x	1	0	- 1/19	3/19	0	6 3/19	
-5/3x+h3	0	0	8/19	- 5/19	1	14 14/19	
1/36x+Zj	0	0	25/228	1/228	0	3 115/228	

x=	6	3/19
y=	5	17/19
h1=	0	
h2=	0	
h3=	14	14/19
Zj=	3 115/228	

$2x+3y+h1=30$

$30$

$7x+y+h2=49$

$49$

$x-y+h3=15$

$15$

Minimizar

	x	y	h1	h2	h3	
h1	2	3	1	0	0	30
h2	7	1	0	1	0	49
h3	1	-1	0	0	1	15
Zj	0.25	0.33333333	0	0	0	0

x=	0
y=	0
h1=	30
h2=	49
h3=	15
Zj=	0

4.  $Z = 7m + 2n$

s.a.

- r1:  $4m + n \leq 16$   
r2:  $m + 5n \leq 30$   
r3:  $m \leq n - 12$   
r4:  $m \geq 0$   
r5:  $n \geq 0$

$4m + n + h1 = 16$   
 $m + 5n + h2 = 30$   
 $m - n + h3 = -12$

Maximizar

	m	n	h1	h2	h3	
h1	4	1	1	0	0	16
h2	1	5	0	1	0	30
h3	1	-1	0	0	1	-12
Zj	-7	-2	0	0	0	0
m	1	1/4	1/4	0	0	4
-1m+h2	0	4 3/4	- 1/4	1	0	26
-1m+h3	0	-1 1/4	- 1/4	0	1	-16
7m+Zj	0	- 1/4	1 3/4	0	0	28
-1/4n+m	0	0	5/19	- 1/19	0	2 12/19
5/4n+h3	0	0	- 6/19	5/19	1	-9 3/19
1/4n+Zj	0	0	1 14/19	1/19	0	29 7/19

m=	2 12/19
n=	5 9/19
h1=	0
h2=	0
h3=	-9 3/19
Zj=	29 7/19

$4m + n + h1 = 16$   
 $m + 5n + h2 = 30$   
 $m - n + h3 = -12$

Minimizar

	m	n	h1	h2	h3	
h1	4	1	1	0	0	16
h2	1	5	0	1	0	30
h3	1	-1	0	0	1	-12
Zj	7	2	0	0	0	0

m=	0
n=	0
h1=	16
h2=	30
h3=	-12
Zj=	0

5.  $Z = 3x - 5y$

s.t.

r1:  $3x + 2y \leq 25$

r2:  $x \leq 5$

r3:  $4x \leq 36 - 3y$

r4:  $x \geq -4$

r5:  $y \geq 2$

$3x + 2y + h1 = 25$

$x + h2 = 5$

$4x + 3y + h3 = 36$

$-4x + h4 = -4$

$-y + h5 = 2$

Maximize

	x	y	h1	h2	h3	h4	h5		
h1	3	2	1	0	0	0	0	25	8.33333333
h2	1	0	0	1	0	0	0	5	5
h3	4	3	0	0	1	0	0	36	9
h4	-4	0	0	0	0	1	0	4	-1
h5	0	-1	0	0	0	0	1	-2	#(DIV/0)
Zj	-3	5	0	0	0	0	0	0	

$-3x + h1$

$x$

$h3$

$4x + h4$

$h5$

$3x + Zj$

x	5	$3x + 2y + h1 = 25$	25
y	0	$x + h2 = 5$	5
h1	10	$4x + 3y + h3 = 36$	36
h2	0	$-4x + h4 = -4$	4
h3	16	$-y + h5 = 2$	-2
h4	24		
h5	-2		
Zj	15		

Minimize

	x	y	h1	h2	h3	h4	h5		
h1	3	2	1	0	0	0	0	25	12.5
h2	1	0	0	1	0	0	0	5	#(DIV/0)
h3	4	3	0	0	1	0	0	36	12
h4	-4	0	0	0	0	1	0	4	#(DIV/0)
h5	0	-1	0	0	0	0	1	-2	2
Zj	3	-5	0	0	0	0	0	0	

$-2y + h1$

$h2$

$h3$

$h4$

$h5$

$5y + Zj$

h1	0.33333333	0	1	0	-0.66666667	0	0	1
h2	1	0	0	1	0	0	0	5
h3	1.33333333	0	0	0	0.33333333	0	1	10
h4	-4	0	0	0	0	1	0	4
y	1.33333333	1	0	0	0.33333333	0	0	12
h5 + Zj	Zj	9.66666667	0	0	0	1.66666667	0	60

x	0	$3x + 2y + h1 = 25$	25
y	12	$x + h2 = 5$	5
h1	1	$4x + 3y + h3 = 36$	36
h2	5	$-4x + h4 = -4$	4
h3	0	$-y + h5 = 2$	-2
h4	4		
h5	10		
Zj	60		