

Runtime Lab

Q1

```
def search_q1(Y, n, x):  
    for i in range (0, n):  
        if Y[i] == x:  
            return i  
    return -1  
  
Y = ['apple', 'banana', 'mango', 'grapes', 'pineapple', 'durian']  
x = "pineapple"  
  
n = len(Y)  
result = search_q1(Y, n, x)  
if result == -1:  
    print("Element is not present in the list")  
else:  
    print("Element", x, "is present at index", result)
```

Given that we're ignoring constants, the time complexity will be the $\text{len}(Y)$ (which is 6), which in this case is Y .

Q2

```
def search_q2(X, item):  
    first = 0  
    last = len(X)-1  
    found = False  
    while first<=last and not found:  
        mid = (first + last)//2  
        if X[mid] == item:  
            found = True  
            print("The element item", item, "was found at index ", X.index(item))  
        else:  
            if item < X[mid]:  
                last = mid - 1  
            else:  
                first = mid + 1  
    return found
```

```
print(search_q2([10, 15, 35, 42, 60, 70, 82, 94], 60))
```

In the above script, the sample size is constantly halved. This is binary the time complexity will be $O(\log(8))$, or in the general case $O(\log(n))$.

Q3

```
test = 0
n = 10
for i in range(n):
    test = test + 1

for j in range(n):
    test = test - 1
```

We have 2 loops which are going over the same sample size, and since we're ignoring constants, this time complexity will be $O(n) + O(n)$, or in this case $O(10) + O(10)$.

Q4

```
i = n
while i > 0:
    k = 2 + 2
    i = i // 2
```

Time complexity will be $O(\log(n))$, given that the sample space is constantly halved.

Q5

```
mat = [[1, 2, 3], [1, 1, 1], [5, 7, 8]]
add = 0
for i in range(len(mat)):
    for j in range(len(mat[0])):
        add += mat[i][j]
print(add)
```

The time complexity for this script is $O(n^2)$, or in this case $O(9)$.

The reason is that we have a main loop and a nested loop. The main loop has 3 elements and the nested loop also has 3 elements (in this script at least). Thus $O(n^2)$.

Q6

```
def fibonacci(n):
    if n<2:
        return n
    return fibonacci(n-1) + fibonacci(n-2)

for n in range(2,12,2):
    print("Series sum for {} is {}".format(n, fibonacci(n)))
```

Due to recursion, the time complexity of the above script will be $O(2^n)$ (we're discounting the for loop since its linear or $O(n)$).