The Essence of Reactive Programming

A Theoretical Approach

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ABSTRACT

n the last few years the *** of Reactive Programming has gained much traction in the developer's community, especially with the general trend for programming languages to embrace functional programming and the shifting of today's applications towards an asynchronous approach to modeling data. The goal of this work is to shed some light to the sea of more or less informed opinions regarding what the meaning of Reactive Programming is thorough the use of Mathematics...

DEDICATION AND ACKNOWLEDGEMENTS

"Well, here at last, dear friends, on the shores of the Sea comes the end of our fellowship in Middle-earth. Go in peace! I will not say: do not weep, for not all tears are an evil."

> — J.R.R Tolkien, The Return of the King

H ere goes the dedication.

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INTRODUCTION

"Lasciate ogne speranza, voi ch'intrate." — Dante Alighieri, Divina Commedia

With the evolution of technologies brought in by the new millennium and the exponential growth of Internet-based services targeting millions of users all over the world, the Software Engineers' community has been continuously tested by an ever growing number of challenges related to management of increasingly large amounts of user data ^[6].

This phenomena is commonly referred to as Big Data. A very popular 2001 research report^[10] by analyst Doug Laney, proposes a definition of big data based on its three defining characteristics:

- *Volume*: the quantity of data applications have to deal with, ranging from small e.g. locally maintained Databases to large e.g. distributed File Systems replicated among data centers.
- *Variety*: the type and structure of data, ranging from classic SQL-structured data sets to more diversified and unstructured ones such as text, images, audio and video.
- *Velocity*: the speed at which data is generated, establishing the difference between pull-based systems, where data is synchronously pulled by the consumer, and push-based systems, more suited for handling real-time data by asynchronously pushing it to its clients.

Each of these traits directly influences the way programming languages, APIs and databases are designed today. The increasing volume calls for a declarative approach to data handling as opposed to an imperative one, resulting in the developer's focus shifting from how to compute something to what it is to be computed in the first place ^[5]. The diversification of data, on the other hand, is the main drive for the research and development of noSQL approaches to data storage. Lastly, the increase in velocity fuels the need for event-driven, push-based models of computation that can better manage the high throughput of incoming data ^[11].

In this context, the concept of *reactive programming* has gained much traction in the developer's community as a paradigm well-suited for the development of asynchronous event-driven applications ^[2]. Unfortunately, reactive programming has been at the center of much discussion, if not confusion, with regards to its definition, properties and principles that identify it ^[12].

The goal of our work is to use mathematics as a tool to analyze today's commercial reactive libraries and understand how they relate to the theoretical concept of reactive programming. We are going to do so by utilizing concepts and ideas from functional programming and category theory with the purpose of deriving the reactive types, and will subsequently continue with the development of a reference reactive library which builds upon the previously derived theoretical foundations.

Contributions

To the best of our knowledge, we are not aware of any previous work which analyses reactive programming from a theoretical point of view or derives its types and interfaces though the use of mathematics.

The most known attempt at defining reactive programming is the Reactive Manifesto ^[?], a document that tries to describe reactive systems in terms of design principles and conceptual architecture. Although certainly insightful, we feel the document targets a more managing-focused audience as opposed to software developers and engineers.

Our work, on the other hand, aims at providing types and interfaces that describe the real essence of the reactive paradigm, aiding engineers that wish to use or develop reactive libraries in understanding and taking more informed decisions in the matter.

Overview

Chapter 2 starts with ... bla bla bla

Write overview

Notation & Conventions

In the exposition of our work we will make use of Haskell as the reference language. This decision is motivated by the language's strong connection with mathematics as well as it's clean syntax.

All the code presented in this report, a minimal complete theoretical implementation and a full blown library implementation of a reactive library can be found at the associated code repository on Github ().

Github link

CHAPTER

REACTIVE PROGRAMMING

The cold winds are rising in the North... Brace yourselves, winter is coming.

— George R.R. Martin,

A Game of Thrones

In this chapter we are going to introduce the concept of reactive programming and motivate it's importance and relevance with regards to modern applications and the type of problems developers have to face nowadays. We are then going to introduce the most popular commercial libraries that claim to solve the reactive problem, with the purpose of giving the reader some context for our discussion and motivating the need for a mathematical formalization that abstracts over the class of problems these implementations set out to address.

1.1 The Essence of Reactive Programs

The use of the term reactive program in scientific literature is dated back to the mid-sixties ^[1]. A relevant and insightful definition was given by G. Berry in 1991 ^[3] as he describes reactive programs in relation to their dual counterparts, interactive programs:

"Interactive programs interact at their own speed with users or with other programs; from a user point of view, a time-sharing system is interactive. Reactive programs also

maintain a continuous interaction with their environment, but at a speed which is determined by the environment, not by the program itself."

Interactive programs concretize the idea of a pull-based model of computation, where the program - the consumer in this case - has control over the speed at which data will be requested and handled. A perfect example of an interactive program is a control-flow structure such as a for-loop iterating over a collection of data: the program is in control of the speed at which data is retrieved from the containing collection and will request the next element only after it is done handling the current one.

Reactive programs, on the contrary, embody the idea of a push-based - or event-driven - model of computation, where the speed at which the program interacts with the environment is determined by the environment rather than the program itself. In other words, it is now the producer of the data - i.e. the environment - who determines the speed at which events will occur whilst the program's role reduces to that of a silent observer that will react upon receiving events. Standard example of such systems are GUI applications dealing with various events originating from user input - e.g. mouse clicks, keyboard button presses - and programs dealing with stock market, social media or any other kind of asynchronous updates.

1.2 Why Reactive Programming Matters

Considering the definition and examples of reactive programs we analyzed in the previous section, let's now try to formalize the class of problems the reactive programming paradigm is specifically well-suited for.

The table below provides a collection of types offered by common programming languages for handling data, parameterized over two variables: the size of the data, either one or multiple values, and the way data is handled, either by synchronous or asynchronous computations ^[13].

	One	Many
Sync	a	Iterable a
Async	Future a	Reactive Programming

The first row shows that synchronous functions come in two flavors: classic functions that return a single value of type a and functions that produce a collection of results of type a, abstracted through the Iterable a interface (See section 2.1). These types of functions embody the standard imperative, pull-based approach to programming, where a call to a function/method synchronously blocks until a result is produced.

Moving on to the second row, we encounter Future a , an interface representing an asynchronous computation that, at a certain point in the future, will result in a value of type a . Futures are generally created by supplying two callbacks together with the asynchronous computation, one to be executed in case of success and the other one in case of error.

Programming languages, however, are not as well equipped when it comes to handling asynchronous computations resulting in multiple values - i.e. push-based collections. The issue lies in the fact that the program's control flow is dictated by the environment rather than the program itself - i.e. inversion of control -, making it very hard to model such problems with commonly known control structures, which are optimized for sequential models of computation. Traditional solutions typically involve developers manually trying to compose callbacks by explicitly writing CPS (continuation passing style) code [13], resulting in what it's commonly referred to as *Callback Hell* [4].

The aforementioned class of problems reflects the definition of reactive programs we analyzed in the previous section, where the environment asynchronously - i.e. at its own speed - pushes multiple events to the program. The reactive programming paradigm sets out to provide interfaces and abstractions to facilitate the modeling of such problems as push-based collections.

However, interfaces are only as good as the implementations that back them up. In the next section we are going to discuss and analyze various APIs and libraries that claim to embody the reactive paradigm, motivating our need for a mathematical formalization to aid in unifying these different approaches under a single set of interfaces, eliminating doubts and confusion when it comes to the essence of reactive programming.

1.3 Reactive Programming in the Real World

Talk about FRP, Reactive Streams, Rx and other stuff. CIte survey paper Claim that Observable is dual of Iterator in order to justify the why.

1.3.1 Reactive Extensions

1.3.2 Reactive Streams

Try to define itself as reactive programming, mathematics prove the claim wrong, they implement asynchronous iterables. This does not make them useless, yet they are not a good solution for the problem we are trying to solve.

Probably put the derivation of Reactive Streams in the appendix, it's not really the focus, I guess.

1.3.3 Functional Reactive Programming

Much researched topic, beautiful in theory, yet based on continuous time, un-achievable with computers where time is inherently discrete. Connel Elliot, the inventor of FRP, says that commercial implementations are far from the original theory and do not really represent the essence of FRP

2

INTO THE RABBIT HOLE: Deriving the Observable

"It was much pleasanter at home," thought poor Alice, "when one wasn't always growing larger and smaller, and being ordered about by mice and rabbits. I almost wish I hadn't gone down the rabbit-hole – and yet – and yet – ..."

— Lewis Carol,
Alice in Wonderland

As we saw in Chapter 1, the Iterable interface embodies the idea of a pull-based model of computation and is the commonly adopted solution to dealing with synchronous computations resulting in multiple values. In this chapter we are going to formalize the intuition that there exists a duality relation between interactive and reactive programs, as well as between pull and push models of computations, by deriving the Observable interface starting from its dual counterpart, the Iterable.

The derivation that follows will require the use of a number mathematical concepts such as *categorical duality, continuations, (co)products, (un)currying, covariance, contravariance* and *functors.* We suggest the reader to get familiar with these topics before diving into the derivation. An accessible introduction to each can be found in Appendix A.

2.1 Iterables

An Iterable is a programming interface which enables the user to traverse a collection of data, abstracting over the underlying implementation ^[7].

The interface and semantics of Iterable s were first introduced by the Gang of Four though their Iterator pattern^[7]; today's most used programming languages introduce the Iterable as the root interface for standard pull collections APIs - exposing concrete implementations such as maps, sets, indexed sequences and so on.

The Iterable interface is generally fixed across programming languages, with the exception of naming conventions - C# and related languages call it IEnumerable - and slight differences in the types, as we can see from the following definitions.

```
-- Java Iterable
   class Iterable a where
       getIterator :: () -> IO (Iterator a)
   class Iterator a where
       hasNext :: () -> Bool
       next :: () -> IO a
8
10
   -- C# IEnumerable
   class IEnumerable a where
       getEnumerator :: () -> IO (IEnumerator a)
13
14
  class IEnumerator a where
       moveNext :: () -> IO Bool
16
       current :: () -> a
17
```

Although the essence of the pattern is preserved by both definitions, we claim that the C# version more clearly and accurately reflects the way side effects play a role in the usage of the interface: moveNext contains all the side effects of traversing the underlying collection and retrieving the next value while current can inspect the retrieved value multiple times in a pure way. The Java version, on the other hand, embeds the side effect in the next function, making it impossible to inspect the current value multiple times. For this reason and without loss of generality, we will make use of the

C# definition - modulo naming conventions - in the reminder of the discussion:

```
class Iterable a where
getIterator :: () -> IO (Iterator a)

class Iterator a where
moveNext :: () -> IO Bool
current :: () -> a
```

2.2 The Essence of Iterables

The first step in deriving the Observable is to simplify our Iterable definition to a type that reflects its very essence; we are gonna do this by stripping the interface presented in the previous section of all the unnecessary operational features that only clutter our definition.

Let's start by taking a closer look at the Iterator interface; we can observe that the definition of the functions moveNext and current is equivalent to a single function which returns either a value - analogous to a moveNext call returning true and a subsequent invocation to current - or nothing - analogous to a call to moveNext returning false.

Before we formalize this observation with a proper type, let us notice another effect that is hidden in the current definition of moveNext and not made explicit by the its type: the possibility for an exception to be thrown by the function's body.

By merging these considerations with the notion of coproducts and Haskell's Either and Maybe type, we obtain the following definition.

```
class Iterable a where
getIterator :: () -> IO (Iterator a)
class Iterator a where
moveNext :: () -> IO (Either SomeException (Maybe a))
```

Note how, theoretically, <code>getIterator</code> could also throw an exception. We assume here, without loss of generality, that the function will never throw and will always be able to return an <code>Iterator</code> instance.

The next step is to forget about class instances and express our interfaces as simple types.

```
type Iterable a = () -> IO (Iterator a)
type Iterator a = () -> IO (Either Exception (Maybe a))
```

At this point, we want to put aside the operational concerns regarding exceptions and termination and assume the Iterator function will always return a value of type a.

```
type Iterable a = () -> IO (() -> IO a)
type Iterator a = () -> IO a
```

We have now reached a point where no simplification is possible anymore. The obtained types reflect the essence of the Iterator patter: an Iterable is, theoretically, a function which, when invoked, produces an Iterator and an Iterator is itself a function producing a value of type a as a side effect.

When looking at the Iterator type from an object oriented perspective, the reader should notice a strict similarity to a *getter* function - i.e. a lazy producer of values: iterators are, in fact, nothing more than getters of values of type a . The Iterable, on the other hand, is a function that enables the user to get an Iterator, i.e. a getter of a getter of a.

This correspondence will turn out to be very insightful later on in our discussion, where we will observe that <code>Observable</code> is nothing more that a setter of setters, another instance of duality in our formalization.

When looking at the relation between the Iterator type and its base component, a, we can observe how they are bound by a covariance relation:

$$\frac{A <: B}{(() \to A) <: (() \to B)}$$

The intuition can be easily understood when we think of an iterable as a soft-drink vending machine, i.e. a function which, whenever called, will give back a soft-drink:

$$\frac{Coke <: SoftDrink}{(() \rightarrow Coke) <: (() \rightarrow SoftDrink)}$$

If coke is a subtype of soft-drink, then whenever I am asked for a soft-drink vending machine, I can

hand out a coke vending machine without incurring in any troubles with the person who asked, as that machine will correctly provide soft drinks whenever prompted for one.

With Iterable being a getter itself, it should be clear how covariance plays the same role as with Iterator.

To formally prove the intuition of a covariant relation, we instantiate the <code>Iterable</code> / <code>Iterator</code> types to a covariant <code>Functor</code> .

```
{-
3
        Using a simplified syntax, hiding IO and Haskell's newtypes,
4
        in order to clearly show the idea:
5
6
        iterator :: () \rightarrow a
7
        iterable :: () -> () -> a
8
        fmapi :: (a \rightarrow b) \rightarrow (() \rightarrow a) \rightarrow () \rightarrow b
10
                                     ia = () \rightarrow f (ia ())
       fmapi
                        f
11
12
        fmapii :: (a \rightarrow b) \rightarrow (() \rightarrow () \rightarrow a) \rightarrow () \rightarrow b
13
                                     iia = () \rightarrow fmapi f (iia ())
       fmapii f
14
   -}
15
16
   newtype Iterator a = Iterator { runIterator :: () -> IO a }
17
   newtype Iterable a = Iterable { getIterator :: () -> IO (Iterator a) }
18
19
   instance Functor Iterator where
20
        fmap f ia = Iterator $ \_ -> liftM f (runIterator ia ())
21
22
   instance Functor Iterable where
23
        fmap f iia = Iterable $ \_ -> liftM (fmap f) (getIterator iia ())
24
```

We will see in the next section how these concepts are relevant in expressing and motivating the duality between Iterables and Observables.

2.3 Applying Duality

By now, the reader should be somehow familiar with the concept of duality, as it has appeared many times throughout our discussion in concepts such as pull and push models of computation or interactive and reactive programs. Duality is, in fact, a very important general theme that has manifestations in almost every area of mathematics [8] (See Appendice A for an introductory discussion on the topic).

Starting from the fact that the Iterable interface embodies the idea of interactive programming, let's use the principle of duality to derive the Observable interface and see how it relates to the concept of reactive programming. In practice, this translates to the simple task of flipping the function arrows in the Iterable interface, taking us from a function resulting in a value of type a to one accepting an a.

Note how the side effects are bound to function application rather than values, hence their flipped position in the Observable type.

The reader acquainted with functional programming will easily see the resemblance between the Observable type and a CPS function (See Appendice A).

```
cont :: (a -> r ) -> r
cont :: (a -> IO ()) -> IO ()
```

It is clear how an <code>Observable</code> is nothing more than a CPS function where the result type <code>r</code> is instantiated to <code>IO</code> () . To convince ourselves of this equivalence, let's think about the definition of a CPS function, i.e. a suspended computation which, given another function - the continuation - as argument, will produce its final result. This definition suits perfectly the idea behind <code>Observable</code> discussed in Section 1.3.1: a function which will do nothing - i.e. is suspended - until it is subscribed to by an <code>Observer</code> .

A continuation, on the other hand, represents the future of the computation, a function from an intermediate result to the final result $^{[14]}$; in the context of <code>Observable</code> s, the continuation represents the <code>Observer</code>, a function specifying what will happen to a value produced by the <code>Observable</code>, whenever it will become available, that is, whenever it will be pushed into the <code>Observer</code>. Since a continuation can be called multiple times within the surrounding CPS context, it is easy to see how this mathematical concept allows us to deal with multiple values produced at different times in the future.

In the previous section we have discussed many properties associated with Iterable s. Let's analyze now how these properties translate under dualisation and how they affect our new derived interface, the Observable.

First, moving from the observation that an Iterable is a getter of a getter, we can observe that the Observable plays exactly the opposite role, that is, a setter of a setter. The type Observer :: a -> IO () represents, in fact, the essence of a setter function, whereas the Observable consists in nothing more than the simple task of applying the observer function to itself, producing a setter of setters.

While the discussion about Iterable 's covariance was quite intuitive, things get a little bit more complicated when analyzing Observable s. Let's start by informally introducing the notion of positivity and negativity of types: we can interpret a function of type f:: a -> b as a way for us to produce a value of type b. In this context, b is considered to be positive with respect to the type a -> b. On the other hand, in order to apply the function, we are going to need a value of type a, which we will need to get from somewhere else; a is therefore considered to be negative w.r.t. the function type, as the function introduces a need for this value in order to produce a result. The point of this distinction is that positive type variables introduce a covariant relation between base and function type whereas negative type variables introduce a contravariant relation.

Analyzing Iterable within this framework is easy, the Iterator function contains a single type parameter found in a positive position, therefore resulting in a covariant relation; being the Iterable the result of applying the Iterator function to itself, we again result in a covariant relation w.r.t. the type parameter a.

The Observer function, on the contrary, introduces a need for a value of type a, resulting in a con-

travariant relation w.r.t. a . Again, the Observable function is the result of applying Observer to itself; surprisingly, this results in a being in a positive position. The intuition is easily understood by thinking about the rules of arithmetic multiplication: a is in negative position w.r.t. the Observer function, whereas the Observer is in negative position w.r.t. the Observable . This leads to a being negated twice, ultimately resulting in a positive position within the Observable function.

```
:: a \rightarrow b
         = -a \rightarrow +b
         :: (a \rightarrow b) \rightarrow c
          = -(-a -> +b) -> +c
          = (+a -> -b) -> +c
8
   observer
       :: a -> ()
         = -a \rightarrow ()
13
   observable
14
        :: ( a -> ()) -> ()
15
          = -(-a -> ()) -> ()
16
          = (+a -> ()) -> ()
17
```

Before we formalize this claim, let's convince ourselves that Observable s effectively produces a value of type a by looking at an example:

```
randomValueObs :: Observable Int
randomValueObs = Observable $ \observer -> do
int <- randomRIO (1, 10)
observer int</pre>
```

It is clear from this implementation that randomValueObs indeed produces a value of type Int, whereas the Observer introduces a need for such value in order to be applied. For more details on the positivity and negativity of functions and type variables, see [15] [9].

Just as we did with Iterable/Iterator, we can formally prove the covariant and contravariant re-

lations between Observable/Observer and their base type a by instantiating them to Functor and Contravariant - i.e. Cofunctor - respectively.

```
newtype Observer a = Observer { onNext :: a -> IO () }

newtype Observable a = Observable { subscribe :: Observer a -> IO () }

instance Contravariant Observer where

contramap f ob = Observer $ onNext ob . f

instance Functor Observable where

fmap f ooa = Observable $ subscribe ooa . contramap f
```

2.4 Termination and Error Handling

We began this chapter by progressively simplifying the Iterable 's interface in order to derive a type that would theoretically represent its very essence. One of the most important steps was setting aside concerns regarding termination an error handling of a collection. We are now going to reshape our reactive interfaces in order to address these concerns and appropriately describe the potential side effects directly in the types.

Informally, an Observable stream might not only produce one or more values, but it might gracefully terminate at a certain point in time or throw an exception and abruptly terminate whilst processing values. A more appropriate type for Observer is then the following:

Just as with Iterable, the introduction of Either SomeException allows us to express that the Observer can handle unexpected exceptions, while the Maybe reflects the possibility for a stream to end and propagate no more values.

Unfortunately, this type is very hard to read as well as understand for someone new to the topic. Looking at the matter from a functionality point of view, what we really need is for our CPS function - i.e. the Observable - to accept two additional continuations, one dealing with completion and one with exceptions. We can achieve this by first noticing that our type is nothing more than a coproduct - the same that we introduced previously for Iterable - of three base types:

a + SomeException + () . By utilizing the notion of product - the dual of coproduct - we can split the function handling the initial type into three different ones. This brings us to the final version of our reactive interfaces for push-base collections¹

The Observable is now a special version of a CPS function accepting three continuation functions - embedded inside the Observer -, one for each effect an Observable can propagate: value, termination or exception.

2.5 Observables are Continuations

Throughout our discussion, we have mentioned multiple times the connection between Observable and CPS functions. In this section we are going to explore this matter and see how we these two concepts are effectively the same thing.

We are going to start from the notion that Observable is, at its essence, nothing more than a setter of setters, the result of applying the Observer function to itself. We can than express the Observer as a function (!) ² that negates its type argument and results in a side-effectful computation.

```
!a :: a -> IO ()
```

¹The two definitions are equivalent also from an implementation point of view, the first simulating the second though the use of pattern matching.

²Regard the code used in this explaination as pseudo-Haskell.

When we apply the function to itself - i.e. substitute a for !a - we obtain our first definition of Observable, a CPS function that instantiates the result to IO ().

```
!!a :: (a -> IO ()) -> IO ()
```

As we have seen in the previous section, this definition is not expressive enough when we want to make explicit all the effects that are involved when dealing with push-base collections. It is therefore necessary to deviate from the standard definition of continuation and replace the inner application of (!) with a new function (?), whose type embed the involved effects:

```
?a :: Either Error (Maybe a) -> IO () -- termiantion and error handling
2 !?a :: (Either Error (Maybe a) -> IO ()) -> IO ()
```

Note how this definition is equivalent to the one used in the previous section, where we used the notion of products to unwrap the (?) function into three different ones, each addressing one of the possible effects.

Finally, we can now translate this pseudo-code into real Haskell, proving the equivalence between Observable and CPS functions. We are going to do so with the help of Haskell's continuation monad transformer, a construct which allows to stack the functionality of the continuation monad on top of other monads. With it, we can define the Observable as a continuation transformer producing an empty result in the IO monad.

```
5 -- Event a = Either SomeException (Maybe a)
6 data Event a = OnNext a | OnError SomeException | OnCompleted
7 deriving Show
8
9 type Observer a = Event a -> IO ()
10 type Observable a = ContT () IO (Event a)
11
12 newObservable :: (Observer a -> IO ()) -> Observable a
13 newObservable = ContT
14
15 subscribe :: Observable a -> Observer a -> IO ()
16 subscribe = runContT
```

The code above uses a slightly different approach to expressing the three types of side effects an Observer has to deal with. Insead of using Either and Maybe from Haskell's libraries, we utilize our own custom datatype Event, a coproduct of values of type a + SomeException + (); although the two definitions are equivalent in every aspect, the adopted one offers more clarity in terms of code readability.

At this point we have all the necessary tools to create and run an Observable.

```
obs = newObservable $ \observer ->
       do observer (OnNext 1)
19
          observer (OnNext 2)
          observer OnCompleted
21
22
  main :: IO ()
  main = subscribe obs print
   output>
       OnNext 1
       OnNext 1
29
      OnCompleted
30
   -}
31
```

Notice how, being a continuation, an Observable only pushes values once subscribed to and acts as a suspended computation otherwise.

The code above, being a toy example, fails to show some fundamental properties associated with this new interface; in particular, it fails to show how Observable s can actually handle asynchronous sources of data. The following snippet of code contains a more realistic and meaningful example of an Observable handling keyboard presses, asynchronous events by nature: whenever the user presses a key, an event containing the corresponding character is propagated to the Observer and will eventually be printed on the command line. It is worth noticing how our basic implementation of Observable based on continuations works just as well as a full blown one in terms of its core capability of handling asynchronous data.

```
obs :: Observable Char
   obs = newObservable $ \observer -> do
18
       keyboardCallback $= Just (\c p -> observer (OnNext c))
19
20
   display :: DisplayCallback
21
   display = do
22
     clear [ ColorBuffer ]
23
     flush
24
25
   main :: IO ()
26
   main = do
27
     (_progName, _args) <- getArgsAndInitialize</pre>
28
     _window <- createWindow "Observable Keyboard"</pre>
29
     subscribe obs (print . show)
30
     displayCallback $= display
31
     mainLoop
```

This example brings us to the following observation: Observable s are capable of handling asynchronous data sources, yet the means by which the data is handled are not asynchronous by default. This is a common misconception and source of much confusion among the community: the Observable interface is not opinionated w.r.t. concurrency and therefore, by default, synchronously handles it's incoming data, blocking the next incoming events whilst processing the current one. This behavior is not fixed though: as we will see in Chapter 3, it is possible to make use of Scheduler s to orthogonally introduce concurrency in our reactive systems, altering the control flow of the data processing allowing the user to dispatch the work to other threads.

At this point in the discussion we have arrived to a working implementation of a push based collection purely derived from mathematical and categorical concepts such as duality and continuations. In spite of being very insightful for theoretical discussions on the properties and relations of Observable and the continuation monad, this implementation of the reactive types is impractical in the context of a full fledged API. In the next Chapter we will take the necessary steps to build the bridge between theory and practice, providing a reference implementation of Observable more adapt to be utilized in real world applications.

For a full implementation of a Reactive Library based on the ideas presented in this section, aimed at highlighting the strong connection between <code>Observable</code> and other already existing functional structures from which it composes, see Appendice B.

3

OUT OF THE RABBIT HOLE: Towards a usable API

TBD
— Lewis Carol,
Alice in Wonderland

So far we focused our analysis on the essence of the Observable interface, setting aside the many operational concerns that would come up when trying to implement these concepts into a usable, commercial API. In this chapter we are going to build the bridge between our theoretical definition of Observable and a concrete and usable implementation of a reactive library, to which we will refer to as Rx.

In the remained of the discussion, we are going to introduce the *Reactive Contract*, a set of assumptions on the reactive types our library is going to build upon, *Schedulers*, which will allow us to bring concurrency into our reactive equation, *Subscriptions*, used to implement a mechanism for premature stream cancellation and, finally, *Operators*, the means that will make our reactive streams composable.

For the sake of clarity and completeness, the following set of interfaces represents the starting point for our discussion:¹

¹ subscribe has been renamed to _subscribe in order to both avoid naming conflicts later on in the discussion and reflect the fact that it should not be used from the outside.

It is worth noting that even though the Observable's theoretical foundations lie in the realm of functional programming, the road to make it usable is full of obstacles that are often better tackled using imperative programming features such as state. As much as I personally prefer a functional and pure approach to programming, I will favor, in the rest of the discussion, the solution that most clearly and easily solves the problem, be that functional of imperative.

3.1 The Reactive Contract

- Remember best effort cancellation.

3.2 Concurrency with Schedulers

At the end of Section 2.5 we discussed how Observable s, by default, handle data by means of a synchronous pipeline, blocking the processing of successive elements via the call stack. It is worth mentioning again how this synchronous processing does not affect the ability of Observable s to handle asynchronous data.

However, this synchronous behavior might not always be the best solution, especially in real world applications, where we might want to have a thread dedicated to listening to incoming events and one which processes them. Enter the Scheduler interface, an orthogonal [?] structure w.r.t. Observable which allows us to introduce concurrency into our reactive equation.

Scheduler's allow us to to alter the control flow of the data processing within an observable expression, introducing a way to dispatch the work of any number of operators to be executed within the specified context, e.g. a new thread.

The Scheduler interface looks like the following ².

²The interface presented in this section is the result of a simplification of the actual one, which involves Subscription s. We will discuss the impact of Subscription s on Schedulers in the next section; suffices to know

Scheduler's expose two functions which are essentially equal, modulo arbitrary delays in time. Both of these functions take an IO action as input and dispatch it to the appropriate execution context, producing a side effect.

To better understand Scheduler s, let us present the implementation of one of them, the newThread scheduler, which allows us to dispatch action to a new, dedicated thread.

```
newThread :: IO Scheduler
   newThread = do
37
       ch <- newTChanIO
38
       tid <- forkIO $ forever $ do
39
           join $ atomically $ readTChan ch
40
           yield
41
       return $ Scheduler (schedule_ch) (scheduleDelay_ch)
42
           where
43
               schedule_ ch io = atomically $ writeTChan ch io
                scheduleDelay_ ch delay io = do
45
                    threadDelay $ toMicroSeconds delay
46
                    atomically $ writeTChan ch io
47
```

The newThread function gives us a side effectful way of creating a Scheduler by generating a new execution context - i.e. a new thread - and setting up the necessary tools for safe communication with it. The Scheduler functions we are provided, on the other hand, simply write the input IO action to the channel and return, effectively dispatching the execution of those actions to the new thread.

Up to this point we haven't mentioned Observable s at all. This is the reason why we previously claimed that Scheduler and Observable are connected by an orthogonal relationship: the two in-

that the version presented here has no negative effects w.r.t the generality of our discussion.

terfaces are independent from one another, yet, when used together within an observable expression, they provide the user with greater expressive power w.r.t. concurrency.

The only thing missing now is a way for us to combine the functionality of these two interfaces: observeOn and subscribeOn are the operators that will aid us on this task. The former will allow us to dispatch any call to an observer continuation on to the specified execution context, whereas the latter will allow us to control the concurrency of the Observable subscribe function.

For the sake of completeness and understandability, the following snippet contains a simple implementation of the <code>observeOn</code> operator together with a sample usage.

```
observeOn :: Observable a -> IO Scheduler -> Observable a
   observeOn o sched = Observable $ \obr -> do
       s <- sched
51
       subscribe o (f s obr)
52
           where
               f s downstream = Observer
                                    = void . _schedule s . onNext downstream
                    {
                       onNext
55
                                    = void . _schedule s . onError downstream
                        onError
56
                        onCompleted = void . _schedule s $ onCompleted downstream
57
                   }
58
```

```
obs = Observable $ \obr ->
       do onNext obr 1
61
           onNext obr 2
62
           onNext obr 3
63
           onCompleted obr
64
65
   obr :: Observer Int
   obr = Observer on oe oc
       where
68
            on v = do
69
                tid <- myThreadId</pre>
70
                print (show tid ++ ": " ++ show v)
71
            oe = print . show
72
            oc = print "Completed"
73
74
   main :: IO ()
75
   main = do
76
       hSetBuffering stdout LineBuffering
77
       subscribe obs' obr
78
       tid <- myThreadId</pre>
79
       putStrLn $ "MainThreadId: " ++ show tid
80
       where
81
            obs' = obs 'rxmap' (+1) 'observeOn' newThread 'rxmap' (+10)
82
            rxmap = flip fmap
83
84
85
   output>
86
       ThreadId 2: 12
87
       ThreadId 2: 13
88
       ThreadId 2: 14
89
       Completed
90
       MainThreadId: 1
91
92
```

3.2.1 A note on the concept of time

Our discussion on push-based collections so far has not once mentioned the concept of time. This might appear strange, especially to the reader familiar with Functional Reactive Programming, where functions over continuous time are at the foundations of the theory. As we mentioned in Section 1.3.3, this dependency on continuous time comes at a great cost: commercial FRP libraries fail to successfully implement the concepts found in the theory as they cannot avoid simulating continuous time and approximating functions operating over it, being this concept inherently discrete in the context of computers.

Rx, on the other hand, completely sheds the notion of time from the notion of reactivity ^[?], shifting its focus, with the help of Scheduler s, to concurrency instead. Time still plays a role, although indirect, within the library: events are processed in the order they happen, and operators make such order is maintained, ultimately handing over to the user a stream of time-ordered events. See Section 3.1 for a broader discussion on this matter.

3.2.2 Impact on Operators

Previously we discussed how introducing concurrency is an orthogonal concept w.r.t. our reactive library. This statement is only partly true and falls short of its promises when we are dealing with combiner operators (see Section 3.4) such as (>=) or combineLatest. These operators will not work at their full potential in a synchronous setting, due to the fact that subscribing to a stream will consume it entirely - or forever process, in the case of an infinite stream - before allowing the operator to subscribe to a different one, effectively making interleaving of events impossible.

The problem is gracefully solved with the introduction of Scheduler s, which, by allowing for Observable s to be executed on different contexts, indirectly make it possible for interleaving to happen and for combiner operators to work at their full potential. This comes at a - even though small - cost, which motivates our claim of partial orthogonality: the internal state of a combiner operator needs to be synchronized and carefully handled as, with the introduction of concurrency, it can now be modified from different execution contexts.

3.3 Subscriptions

⁻ now purely practical concern: stop stream while processing from anywhere, tell observable I dont want to observe anymore, i.e. the observer is done. - what is it: IO action/s | in theory can be seen as readerT, the subscription is always the same one, but you can add stuff to it. - who does it belong to: the observer, you get one for each subscribe. - how does it work: call unsubscribe, best effort stop work - impact on operators: a need for children -> now you can free resources - impact on schedulers:

kill the thread - write that it only works now that we have schedulers - edge enforcement - subject + takeuntil - why cannot be monoid, we need remove

With schedulers, we are now able to handle observable streams from different execution contexts. The next step is to add a mechanism that will allow us to stop a stream from anywhere in our program, whenever we don't require it's data - i.e. a mechanism to tell the Observable that one of it's Observer s is not interested in receiving events anymore. We are going to do so by augmenting our informal definition of Observable from section 2.5 with a new function (%), which incorporates the notion of a cancellation mechanism through the Subscription datatype:

```
%a :: a -> IO Subscription
%?a :: (Either SomeException (Maybe a) -> IO ()) -> IO Subscription
```

With this change, each execution of the Observable function now returns a Subscription, a means for the user to prematurely terminate the processing of the stream.

We discussed in the previous section how schedulers effectively boost the expressive power of our reactive expressions by introducing concurrency and interleaving among events originating from different streams. Introducing a cancellation mechanism, on the other hand, is a purely practical concern: although very useful from a practical perspective, especially in the context of resource management, it doesn't impact expressive power from a reactive point of view.

The first step in designing this new feature is to understand how the already existing interfaces will be affected by the newly introduced one; we just saw how the _subscribe function should now return an action resulting in an instance of type Subscription. The next question is the following: to whom does a Subscription belongs to? The key observation in addressing this question is that an Observable can be subscribed to by multiple Observer s; our goal is to provide a mechanism that will allow for a fine-grained control over which Observer is supposed to stop receiving events. The answer is then straightforward: the notion of subscription is tight to that of observer. The following snippet incorporates this notion:

```
$a :: (Subscription, Either SomeException (Maybe a) -> IO ())

%$a :: (Subscription, Either SomeException (Maybe a) -> IO ())

-> IO Subscription
```

Let's quickly summarize what we have discussed so far: a subscription is some object which will allow us to prematurely stop observing a specific stream; since any stream can be subscribed to by multiple observers, we need to associate subscriptions to observers as opposed to observables. Lastly, a subscription is returned every time an observer is subscribed to a stream through the __subscribe function. The following modifications to our reactive interfaces reflect these ideas:

```
newtype Observable a = Observable
       { _subscribe :: Observer a -> IO Subscription
       }
15
   data Observer a = Observer
16
       { onNext :: a -> IO ()
17
       , onError :: SomeException -> IO ()
18
       , onCompleted :: IO ()
19
        subscription :: Subscription
20
       }
21
```

do not subscribe an observer to 2 different streams

So far we have talked a lot about Subscription s, yet we haven't clarified what the type really looks like. The general idea is to have Subscription record the state of the Observer w.r.t. the Observable it is subscribed to - be that subscribed or unsubscribed. This can be easily achieved with a variable _isUnsubscribed :: IORef Bool initialized to False, indicating that the associated Observer is initially not unsubscribed.

From a practical point of view, it is useful to augment Subscription with some additional functionality. The following code shows a definition of Subscription which incorporates an IO () action to be executed at unsubscription time. This is particularly useful when we want to associate resource cleanup actions to the termination - be that forced or natural - of a stream observation.

```
data Subscription = Subscription
{    _isUnsubscribed :: IORef Bool
}
, onUnsubscribe :: IO ()
}
```

We will see, later on, how we can further augment this interface in order to incorporate additional functionality useful for internal operator coordination as well as management of schedulers.

It's now time to introduce the two functions at the hearth of the whole cancellation mechanism: unsubscribe will take care of modifying the state carried by the Subscription - i.e. setting _isUnsubscribed to False - whereas subscribe will act as a proxy for the _subscribe function from Observable, calling it with a special Observer which will prevent events from propagating to the downstream once the Subscription has been unsubscribed. Note how, for this mechanism to work, it is necessary the two Observer s to share the same Subscription.

```
subscribe :: Observable a -> Observer a -> IO Subscription
   subscribe obs obr = do
72
       _subscribe obs $ Observer on' oe' oc' s
73
       where
74
                 = subscription obr
75
                 = ifSubscribed $ onCompleted obr >> unsubscribe s
           oc'
76
           on' a = ifSubscribed $ onNext obr a
77
           oe' e = ifSubscribed $ finally (onError obr e) (unsubscribe s)
78
           ifSubscribed a = isUnsubscribed s >>= flip unless a
79
80
   unsubscribe :: Subscription -> IO ()
81
   unsubscribe s = do
82
       writeIORef (_isUnsubscribed s) True
83
       onUnsubscribe s
```

So, what is a Subscription then? Conceptually, it could be a simple boolean recording whether an Observer is unsubscribed from the stream. In practice it is useful to augment it with some additional information. First of all, Subscription's can be used for resource cleanup at the termination - either forced or natural - of a stream. It is therefore useful to associate an IO () action to the datatype, which will represent the computation to be executed once the stream is unsubscribed from. Another improvement is making the type recursive, i.e. allowing Subscription's to contain, add and remove children subscriptions. This will be extremely useful for internal coordination of operators such as (>=) and for resource management in the context of schedulers - more on this in the next sub-subsections.

We could just chain IO actions, but then we cant remove, which can lead to stack overflow with huge thunks in flatmap.

Talk about the best effort in canceling work and eventual consistency with the contract.

```
data Subscription = Subscription

{ onUnsubscribe :: IO ()

, _isUnsubscribed :: IORef Bool

, subscriptions :: IORef [Subscription]

}
```

As a design decision, when unsubscribe is called on an observable subscription, the observable sequence will make a best effort attempt to stop all outstanding work. This means that any queued work that has not been started will not start. Any work that is already in progress might still complete as it is not always safe to abort work that is in progress. Results from this work will not be signaled to any previously subscribed observer instances.

Motivation for children subscriptions: some operators will create inner observables and therefore will need to unsubscribe from them when the outer observable is unsubscribed from.

On why using Cont () (StateT Subscription IO) (Event a) wouldn't work: it would be perfect in order to thread Subscriptions throughout execution making it usable inside operators, since the call to the continuation would return a state which would then be sequenced by »=. This method fails with schedulers, in particular newThread since the state of the action executed on the new thread would be disconnected from the threading mentioned above. The other thread would get a state but it would not know what to do with it and would not have any ways to connect it to the original one passed by the subscribe. Another way is to use mapStateT to map the IO action that will result from the state to an action on the other thread. Again, this method won't work,

On the motivation for a Subscription: it is needed so the user can cancel work at any time. This implies that a scheduler is used. If this is not the case the subscription will be returned synchronously after the execution of the whole stream. It will therefore be already unsubscribed and calling unsubscribe will be a NoOp. In the case that we actually use schedulers then we can unsubscribe from anywhere in our program.

Now the question is the following: can we reproduce the behaviour of unsubscribe with operators so that we can eliminate subscriptions altogether? That is, we can hide them to the outside and use them only inside the stream, we still need them but we don't necessarily need to return them when we subscribe. The behavious can be easily replaced by the use of takeUntil(Observable a) where we pass in a subject that will be signaled when we want to stop the stream. The takeUntil operator fires events from the upstream up until the point in which we signal the subject, then stops the stream and unsubscribes.

With this approach we seemingly lose one thing, i.e. the ability to specify what happens at unsubscription time; this functionality can simply be regained by a subscribe function that takes the unsubscribe action as a parameter and runs it when the stream is unsubscribed.

3.4 Operators

The first thing we want to re-introduce is handling exceptions and termination of a stream. Where an Iterable can return a value, terminate or throw an exception when we ask for a value, and Observable, being it's dual, can produce one or more values, terminate or throw an exception when it is subscribed to.

A more appropriate type for our interface is then the following.

```
type Observer a = Either SomeException (Maybe a) -> IO ()
type Observable a = ContT () IO (Observer a)
```

Remove this Event shit and move to the custom type directly? Not sure, I like the discussion on bind.

Now, this code is not exactly the definition of readable; let's apply some good design skills to make it more pleasant to the eye without changing it's meaning.

```
-- datatype representing Either SomeException (Maybe a)

data Event a =

OnNext a

OnError SomeException

OnCompleted

type Observer a = Event a -> IO ()

type Observable a = ContT () IO (Event a)
```

Although this might not look like a big change, it greatly influences the design of our API. We are, in fact, changing our instantiation of the continuation monad to an input type that is not a anymore, but Event a. On the other hand, out type variable for Observable is still a. This is not an issue

per se, but it has one big consequence: the flatmap function that we inherit from the continuation monad is not the one that we want to expose from out API anymore. The types differ like so.

```
-- bind inherited from the Continuation monad

(>>=) :: Observable a -> (Event a -> Observable b) -> Observable b

-- bind that we would like to expose from our API

flatmap :: Observable a -> (a -> Observable b) -> Observable b
```

This has many implications, first of all, we are gonna need to implement flatmap by ourselves.. see todo below...

It has now come the time to move away from an implementation of Observable as a type synonym. We have already seen how the current implementation using Event a does not allow for a correspondence between >= operations; this will only create confusion in the future. The next step is then to define our own observable tybe, which will clearly be really similar to the Continuation monad and subsequently prove that it is itself a monad.

With this implementation we have eliminated the materialisation of the event types. The Observer is now not a single function from Event a -> IO () but a collection of 3 continuations that will be used inside the observable depending on the type of the event. It is clear that this implementation of Observable has not changed in functionality from the previous one using the Continuation Monad, it has just dematerialized the 3 types of events in 3 functions which handle them.

The next step is to make Observable a monad

```
instance Monad Observable where
    return a = observable (\obr -> onNext obr a)
    o >>= f = ...
```

The return function is the exact same as in the continuation monad, with the only difference that we have now 3 continuations to chose from instead of a single one.

Bind, on the other hand, is completely different from the Cont monad implementation; in this case ...

finish the discussion

The only thing left to do now is to prove the monad laws to show that Observable really is a monad.

```
19 -- Monad Laws

20 -- return a >>= k = k a

21 -- m >>= return = m

22 -- m >>= (x -> k x >>= h) = (m >>= k) >>= h
```

We mentioned before how the bind from Cont differs from our in the Observable. Below I will show that in this implementation it corresponds to a function lift that ...

Talk about lift = »= in Cont.

By using lift we can transform streams and implement operators...

Modify keyboard press example from before to handle errors and termination. Point to later discussion regarding the rx contract, since now we can detect termination and errors but there is no guarantee that nothing will come after we receive them, i.e. that we abide the contract.

Todo list

Write overview	2
Github link	2
Probably put the derivation of Reactive Streams in the appendix, it's not really the focus, I guess	7
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APPENDIX A

egins an appendix

- A.1 Categorical Duality
- A.2 Continuations
- A.3 (Co)Products
- A.4 (Un)Currying
- A.5 (Covariance & Contravariance
- A.6 Functors

APPENDIX

APPENDIX B

B egins an appendix
Formal RX Implementation

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