# Homework 1

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I used for solving this exercise Matlab. For the distance I used euclidian distance. My clustering algorithm calculates for every Datavector the distances to every centroid and then checks which centroid is closed. The vector is add to the closest cluster. When all datavectors are put in a cluster the new cluster centroids are calculated.

My abort criterion is the change between the centroids. If they still change I will apply the algorithms again. Because of the computer accuracy I do not use 0, but  $10^{-15}$ . I also let the algorithm stop after 3 rounds, but it is already good enough after 2 rounds.

After the first round all data is clustered in cluster 2 and 3. I decided to let be the first centroid (-1000, -1000, -1000). Than it does not influence the result. The distances in the first round are to see in 1

	Ιa	belle 1: Di	star.	ices first	rou	ına
${ m cluster}$	1	$\operatorname{distance}$	to	cluster	$^{2}$	$_{ m dist}$

$\operatorname{distance\_to\_cluster\_2}$	$distance\_to\_cluster\_3$
3000,002694	$23000,\!00899$
5000,486525	15000,09671
13112,00189	6888,039561
4000,028178	$24000,\!00035$
$20,\!15113235$	20000,002
7500,000631	$27500,\!00685$
9000,088284	$11000,\!02773$
5000,212648	$25000,\!02102$
3000,000006	17000,00789
25000, 12893	$5000,\!409169$
5000,027278	$25000,\!00028$
2500,000209	$22500,\!00527$
4000,02221	24000,00046
3500,002355	$23500,\!00885$
15000,04597	$5000,\!051895$
7,034833476	$20000,\!01362$
$2200,\!477885$	$22200,\!02037$
$1500,\!016496$	$21500,\!01267$
7000,000319	13000,00815
7000,004581	$27000,\!0024$
	3000,002694 $5000,486525$ $13112,00189$ $4000,028178$ $20,15113235$ $7500,000631$ $9000,088284$ $5000,212648$ $3000,000006$ $25000,12893$ $5000,027278$ $2500,000209$ $4000,02221$ $3500,002355$ $15000,04597$ $7,034833476$ $2200,477885$ $1500,016496$ $7000,000319$

	Tabelle 2: centroid							
_3	$\operatorname{centroid}_{\_}$	$\operatorname{centroid}_2$	_ 1	$\operatorname{centroid}_{\underline{}}$				
12	231	7000	00	-100				
32	0,0005	$0,\!29309$	00	-100				
3		6	00	-100				

#### The new centroids are in 2

Tabelle 3: Distances second round

${\rm distance\_to\_cluster\_1}$	${\rm distance\_to\_cluster\_2}$	${\rm distance\_to\_cluster\_3}$
22116,19085	0	16112,00028
28758,56529	8000, 338507	8112,360556
36006, 45169	16112,00028	0
21365,89781	1000, 180514	$17112,\!01414$
$24510,\!81085$	3000,093366	$13112,\!02657$
18878,30691	4500,000119	20612,00039
32284,64122	$12000,\!0792$	4112,262067
$20652,\!19999$	$2000,\!613442$	$18112,\!0751$
$27003,\!89625$	6000,001337	10112,00244
47192,82789	28000, 12683	11888,32027
$20631,\!35796$	$2000,\!10364$	$18112,\!01496$
$22505,\!10872$	$500,\!0250381$	$15612,\!00206$
$21367,\!51278$	1000,147276	17112,01178
21734,0764	500,0000847	$16612,\!00027$
37765,65939	18000,04611	$1888,\!500752$
24496,12265	3000,001514	13112
22765,44019	$801,\!5423085$	15312,09033
$23287,\!55072$	1500,003029	14612
30483,445	10000,0018	6112,006626
19220,80594	4000,015673	20112,00478

#### And the centroids in 4

uoiu_i	centroid_2	centroid_o
-10000	7000	23112
-10000	$0,\!29309$	0,000532
-10000	6	3

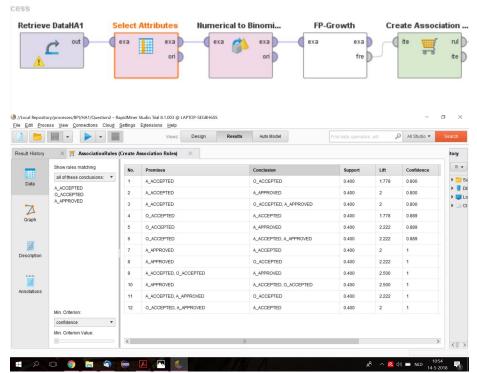
 $\begin{array}{ccc} & \text{Tabelle 5: Cluster 1} \\ \text{amount\_req} & \text{case\_duration} & \text{total\_activities} \end{array}$ 

Cluster 1 contains 5. Cluster 2 contains as in 6 Cluster 3 in 7

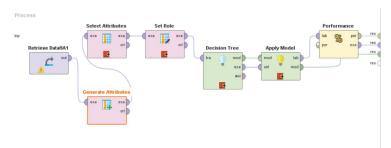
	Tabelle 6: Cluster 2	
$\operatorname{amount} \operatorname{req}$	${ m case\_duration}$ to	${ m tal\_activities}$
7000	0,29309	6
15000	28,43964	74
6000	0,048206	25
10000	12,95023	26
2500	0,021134	7
5000	29,51885	46
13000	$0,\!515625$	10
5000	7,612419	25
7500	$0,\!489861$	11
6000	6,503808	22
6500	0,002049	6
10000	0,000799	3
7800	$19,\!1099$	52
8500	0,000486	3
3000	6,955382	15

	Tabelle 7: Cluster	
$\operatorname{amount} \operatorname{req}$	$\operatorname{case\_duration}$	$total\_activities$
23112	0,000532	3
19000	19,78213	45
35000	19,74352	88
25000	$21{,}14506$	41
17000	0,01375	12

The process is built up like in the picture. First I selected the attributes I am assumed to consider (**Select Attributes**). Then the numerical values are translated to binomial values, because this is needed for the association rules. (**Numerical to Binomial**) RapidMiner expectes a FrequentItemSet for the **Create Association Rule**, so before I could use that I also had to use **FP-growth**.

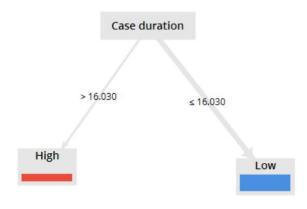


I would pick the rule  $\{A\_ACCEPTED, O\_ACCEPTED\} \Rightarrow \{A\_APPROVED\}$  and  $\{A\_APPROVED\} \Rightarrow \{A\_ACCEPTED, O\_ACCEPTED\}$ , because they have the highest lift, confidence and support. When you have a closer look you will see that the sets are probably of the rules have a back- and forth relationsip. Such that you can summarize it in one rule. Then you could look for the next best rules, where lift, support and confidence is the highest.



#### The process

first changes the numerical attribute TotalActivites to a nominal one by Generate Attributes and Select Attributes. The generating consideres the old TotalActivites and contains the rule that all data, where TotalActivites is lower or the same as 40 it should be assigned to "Low" otherwise "High". The Set Role gives the new attribute as label, so RapidMiner knows what should have be the outcome of the Decision Tree. Decision Tree generates the decision Tree. Then Apply Model for Performance checking. The output is then the model and the performance of the model on the data. The found decision tree is



#### If you check the Confusionmatrix

accuracy: 100.00%					
	true Low	true High	class precision		
pred. Low	14	0	100.00%		
pred. High	0	6	100.00%		
class recall	100.00%	100.00%			

you see, that this decision tree classifys the data perfectly. So you can predict

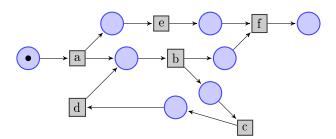
by just knowing the case duration the total activities. If the case duration is higher, than also the total activities are high. This seems to be logical, if you have to do a lot this takes most of the times longer and otherwise around, if you do not need long you mostly did not do a lot of different things in the time.

#### 1.

 $L1 = \left[ \langle a, b, e, f \rangle, \langle a, b, e, c, d, b, f \rangle, \langle a, b, c, e, d, b, f \rangle, \langle a, b, c, d, e, b, f \rangle, \langle a, e, b, c, d, b, f \rangle \right]$  The  $\alpha$ -Algorithm gives the following:

$$T_L = \{a, b, c, d, e, f\}$$
 
$$T_I = \{a\}$$
 
$$T_O = \{f\}$$

	a	b	$\mathbf{c}$	d	e	f
$\overline{\mathbf{a}}$	#	$\rightarrow$	#	#	→             #  -	#
b	←	#	$\rightarrow$	$\leftarrow$		$\rightarrow$
$\mathbf{c}$	#	$\leftarrow$	#	$\rightarrow$		#
d	#	$\rightarrow$	$\leftarrow$	#		#
e	←				#	$\rightarrow$
f	#	←	#	#	$\leftarrow$	#



#### 2.

$$L2 = \left[ \langle a, b, c, d \rangle, \langle a, c, b, d \rangle, \langle a, e, f, d \rangle, \langle a, e, g, d \rangle, \langle a, e, h, d \rangle \right]$$

The  $\alpha-$ Algorithm gives the following:

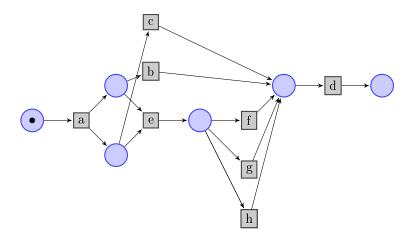
$$T_L = \{a, b, c, d, e, f, g, h\}$$

$$T_I = \{a\}$$

$$T_O = \{d\}$$

	a	b	c	d	e			
$\mathbf{a}$	#	$\rightarrow$	$\rightarrow$	#	$\rightarrow$	#	#	#
b	←	#		$\rightarrow$	#	#		
$^{\mathrm{c}}$	←		#	$\rightarrow$	#	#		#
d	#	→ # 	$\leftarrow$	#	#	$\leftarrow$	$\leftarrow$	$\leftarrow$
e	<i>₩</i>	#	#	#	#	$\rightarrow$	$\rightarrow$	$\rightarrow$
f	#	#	#	$\rightarrow$	$\leftarrow$	#	#	#
g	#	#	#	$\rightarrow$	$\leftarrow$	#	#	#
h	#	#	#	$\rightarrow$	$\leftarrow$	#	#	#

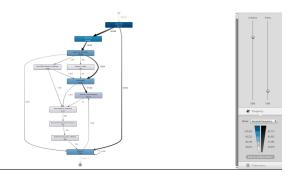
$$\begin{split} X_L &= \{(\{a\},\{b\}),(\{a\},\{c\}),(\{a\},\{e\}),(\{a\},\{b,e\}),(\{a\},\{c,e\}),(\{b\},\{c\}),(\{b\},d\}),(\{c\},\{b\}),\\ &\quad (\{c\},\{d\}),(\{e\},\{f\}),(\{e\},\{g\}),(\{e\},\{h\}),(\{g\},\{d\}),(\{h\},\{d\}),(\{f\},\{d\}),\\ &\quad (\{g,h\},\{d\}),(\{g,f\},\{d\}),(\{h,f\},\{d\}),(\{g,f,h\},\{d\})\} \\ Y_L &= \{(\{a\},\{b,e\}),(\{a\},\{c,e\}),(\{g,f,h\},\{d\})\} \end{split}$$



#### **a**)

The process has 15370 cases and 561470 events. Median number of events is 5 (and average number The average duration is 48.8 weeks.

#### **b**)



The loop tells us, that a part of all people had to pay at least two times. If you check the log data, you can see, that mostly it happens in the next 30 days. It happen 4306 and for 4014 cases. So there are cases, where it happens more than one time. You also can see, that it happens at most 14 times.

### **c**)



You can see that the distribution is going up and down a little bit, but there are 10 laces to see where more happens. Further in the end activity gets lower and the distance between the 6th and 7th lace is higher than between the others. It is always around the typical paydays, so probably a lot of people then have the money to pay the fine.

#### d)

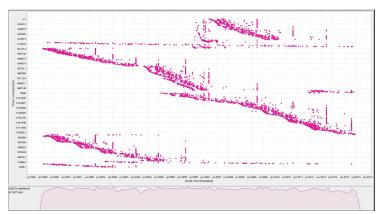
There are 231 variants. The third most frequent variant has 20385 instances. It just contains the behaviour create and send fine. Nothing more happens there.

#### $\mathbf{e})$

It is just possible to 43% or 56%. The average case duration shorts to 45.2 weeks and the median to 20.9weeks in both cases. So in average the cases are faster finished.

The median is the instance in the middel. So if you write down all instances sorted, it is the one in the middel. The average is the sum of all instances divided by the number of instances. The average can change a lot for big or extree small oultiers. The median shows more a real duration in the middle of all instance durations.

# f)



In the first dotted chart you see when which case is active.

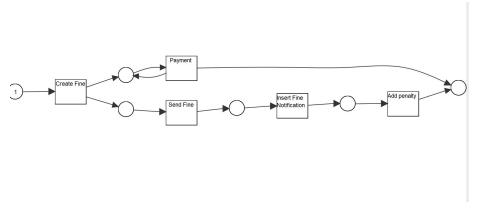
Question5fc.jpg

For interpreting the dot chart for the question c) I changed the y-axis to the event names so I can see when which events happening. I also zoomed in so I can see the months of the years. Now you can check better the dates of the peaks.

You can see that insert fine notification is strongly connected to the lashes to see in c). Also a little bit the send fine.

Payment happens close to always but still is a little bit bundled at the peaks. Furthermore I would say, that in disco it is more easy to see when peaks happen, but in prom better to see what is happen on the peak days.

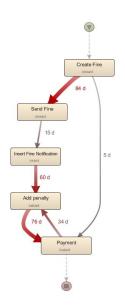
#### $\mathbf{g}$



If you apply the alpha-algoirthm on the not filtered data you can not see so clear, that in the resulting chart the payment can happen always and also infinite often. It sounds weird, because you do not expect someone paying before he gets the fine, but looking at the data it happens.

Also in the filtered version the people or pay after the fine is created or pay to late, so that they get a penalty.

h)





84days is the median for send fine. I chose the median, because then you get a better idea what happens most of the times. The mean is 85.1 days. What you also can see, is that after 60days always a penalty is added.