Homework 1

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Question 1

I used for solving this exercise Matlab. My code you can see here:

```
_{1} \; \mathrm{amount\_req} \; = \; [7000 \, , \; 15000 \, , \; 23112 \, , \; 6000 \, , \; 10000 \, , 2500 \, ,
                          5000, 13000, 35000, 5000, 7500, 6000, 6500, 25000, 10000, 7800, 8500, 17000, 3000];
 _{2} case duration =
                         [0.29309, 28.43964, 0.000532, 0.048206, 12.95023, 0.021134, 19.78213, 29.51885, 0.51888, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.021134, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02114, 0.02144, 0.02144, 0.02144, 0.02144, 0.02144, 0.02144, 0.0214
 _3 total_activities =
                         [6,74,3,25,26,7,45,46,10,88,25,11,22,6,41,3,52,3,12,15];
  c1 = [50000, 1.5, 6];
          c2 = [310000, 0.7, 10];
          c3 = [30000, 4, 26];
          clust1x = [];
 clust1y = [];
clust1z = [];
c l u s t 2 x = [];
        \operatorname{clust} 2y = [];
        \operatorname{clust} 2z = [];
       clust3x = [];
clust3y = [];
          clust3z = [];
        change = 100000;
       k = 0;
           while change > 10^-15
                            for i = 1:length (amount req)
                                             distc1(i) = distance([amount req(i), case duration
                                                           (i), total_activities(i)], c1);
```

```
distc2(i) = distance([amount req(i), case duration
22
                (i), total activities (i), c2);
            distc3(i) = distance([amount req(i), case duration
23
                (i), total activities (i), c3);
24
25
             if (\operatorname{distc1}(i) = \min([\operatorname{distc1}(i), \operatorname{distc2}(i), \operatorname{distc3}(
                i)]))
                 clust1x = [clust1x, amount req(i)];
27
                               clustly, case duration(i);
                 clust1y = 1
                 clust1z = [clust1z, total activities(i)];
29
             elseif(distc2(i)) = min([distc1(i), distc2(i),
30
                distc3(i)]))
                 clust2x =
                               clust2x, amount req(i);
31
                 clust2y = [
                               clust2y, case duration(i);
32
                 c l u s t 2 z = [
                               clust2z , total activities(i);
33
             else
34
                 clust3x = [
                               clust3x , amount req(i);
35
                 clust3y =
                               clust3y , case duration(i);
                 clust3z = [clust3z, total activities(i)];
37
            end
       end
       clnew = centroid ([clust1x; clust1y; clust1z]);
       c2new = centroid([clust2x; clust2y; clust2z]);
41
       c3new = centroid([clust3x; clust3y; clust3z]);
42
        change = distance(c1, c1new) + distance(c2, c2new) +
43
            distance (c3, c3new);
        c1 = c1 \text{new};
44
        c2 = c2 new;
45
        c3 = c3 new;
       k = k + 1;
47
       namen = { 'distance_to_cluster 1','
           distance to cluster_2', 'distance_to_cluster_3'};
       T = table(distc1', distc2', distc3', 'VariableNames',
49
           namen);
        filename = 'Question1.xlsx';
50
        writetable (T, filename, 'Sheet', k, 'Range', 'A1')
51
       namen2 = { 'centroid_1', 'centroid_2', 'centroid_3'};
T = table(c1',c2',c3', 'VariableNames',namen2);
5.3
        filename = 'Question1centroids.xlsx';
        writetable (T, filename, 'Sheet', k, 'Range', 'A1')
   end
   c1
57
   c\,2
   c3
59
60
```

```
k
61
       namen3 = { 'amount req', 'case duration', '
63
           total activities'};
       T = table(clust1x', clust1y', clust1z', 'VariableNames',
64
           namen3);
       filename = 'Question1cluster1.xlsx';
65
       writetable (T, filename, 'Sheet', 1, 'Range', 'A1')
67
       namen4 = { 'amount req', 'case duration', '
           total activities'};
       T = table(clust2x', clust2y', clust2z', 'VariableNames',
69
           namen4);
       filename = 'Question1cluster2.xlsx';
70
       writetable (T, filename, 'Sheet', 1, 'Range', 'A1')
       namen5 = { 'amount_req', 'case_duration', '
72
           total activities'};
       T = table(clust3x', clust3y', clust3z', 'VariableNames',
73
           namen5);
       filename = 'Question1cluster3.xlsx';
74
       writetable (T, filename, 'Sheet', 1, 'Range', 'A1')
75
```

The functions used I does not write down them here. 'distance' calculates the euclidian distance and centroid sums up all vectors and divides by the number of vectors.

My clustering algorithm now calculates for every Datavector the distances to every centroid and then checks which centroid is closed. The vector is add to the cluster. When all datavectors are put in a cluster the new cluster centroids are calculated.

My abort criterion is the change between the centroids. If they still change I will apply the algorithms again. Because of the computer accuracy I do not use 0, but 10^{-15} . The algorithm finds after two rounds already good enough clusters.

The distances in the first round are to see in 1

The new centroids are in 2

And the centroids in 4 The next round the distances are in 3

Cluster1 contains 5

Cluster 2 contains as in 6

Cluster 3 in 7

Tabelle 1: Distances first round			
$distance_to_cluster_1$	$\operatorname{distance_to_cluster_2}$		
0	4	20	
68	64	48	
3	7	23	
19	15	1	
20	16	0	
1	3	19	
39	35	19	
40	36	20	
4	0	16	
82	78	62	
19	15	1	
5	1	15	
16	12	4	
0	4	20	
35	31	15	
3	7	23	
46	42	26	
3	7	23	
6	2	14	
9	5	11	

Tabelle 2: centroid					
$\operatorname{centroid}_{_}$	_ 1	$\operatorname{centroid}_2$	$\operatorname{centroid}_3$		
70	00	13000	15000		
0,293	09	$0,\!515625$	$28,\!43964$		
	6	10	74		

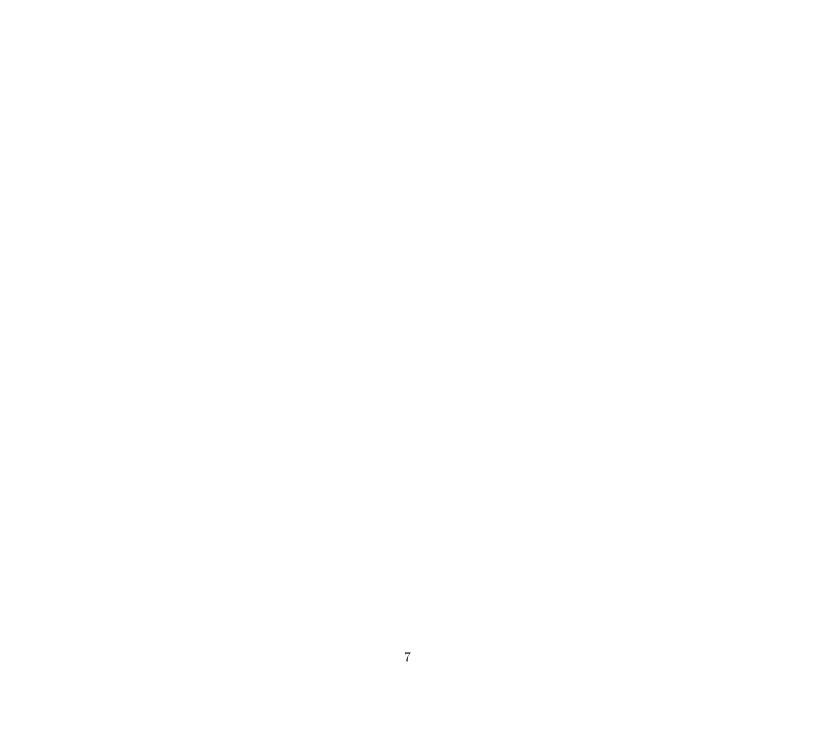
Tabelle 3: Distances second round				
$\operatorname{distance_to_cluster_1}$	${ m distance_to_cluster_2}$	${ m distance_to_cluster_3}$		
0	4	68		
68	64	0		
3	7	71		
19	15	49		
20	16	48		
1	3	67		
39	35	29		
40	36	28		
4	0	64		
82	78	14		
19	15	49		
5	1	63		
16	12	52		
0	4	68		
35	31	33		
3	7	71		
46	42	22		
3	7	71		
6	2	62		
9	5	59		

Tabelle 4:	centroids sec	ond round
$\operatorname{centroid} _1$	$\operatorname{centroid}_2$	$\operatorname{centroid}_3$
7000	13000	15000
0,29309	$0,\!515625$	$28,\!43964$
6	10	74

	Tabelle 5: Clust	er 1
$\operatorname{amount} \operatorname{req}$	${ m case_duration}$	$total_activities$
7000	0,29309	6
23112	0,000532	3
2500	0,021134	7
6500	0,002049	6
10000	0,000799	3
8500	0,000486	3
7000	0,29309	6
23112	0,000532	3
2500	0,021134	7
6500	0,002049	6
10000	0,000799	3
8500	0,000486	3

	Tabelle 6: Cluster	• 2
$\mathrm{amount} _\mathrm{req}$	$\operatorname{case_duration}$	total_activities
13000	$0,\!515625$	10
7500	$0,\!489861$	11
17000	0,01375	12
3000	6,955382	15
6000	0,048206	25
10000	12,95023	26
13000	$0,\!515625$	10
5000	7,612419	25
7500	0,489861	11
6000	6,503808	22
25000	21,14506	41
17000	0,01375	12
3000	6.955382	15

	Tabelle 7: cluster	3
$\operatorname{amount} \operatorname{req}$	$\operatorname{case_duration}$	total_activities
15000	28,43964	74
6000	0,048206	25
10000	12,95023	26
19000	19,78213	45
5000	29,51885	46
35000	19,74352	88
5000	7,612419	25
6000	6,503808	22
25000	$21{,}14506$	41
7800	$19,\!1099$	52
15000	28,43964	74
19000	19,78213	45
5000	29,51885	46
35000	19,74352	88
7800	19,1099	52



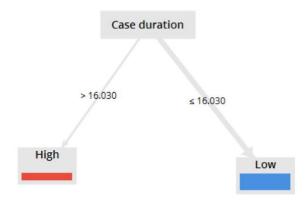
Question 2



I would pick the rule $\{A_ACCEPTED, O_ACCEPTED\} \Rightarrow \{A_APPROVED\}$ and $\{A_APPROVED\} \Rightarrow \{A_ACCEPTED, O_ACCEPTED\}$, because they have the highest lift, confidence and support. When you have a closer look you will see that the sets are probably logical equivalent. Always pick the rule with the best lift, confidence and support.

Question 3

The found decision tree is



If you check the Confusionmatrix

accuracy: 100.00%				
	true Low	true High	class precision	
pred. Low	14	0	100.00%	
pred. High	0	6	100.00%	
class recall	100.00%	100.00%		

you see, that this decision tree classifys the data perfectly. So you can predict by just knowing the case duration the total activities. If the case duration is higher, than also the total activities are high. This seems to be logical, if you have to do a lot this takes most of the times longer and otherwise around, if you do not need long you mostly did not do a lot of different things in the time.

Question 4

1.

$$L1 = [\langle a, b, e, f \rangle, \langle a, b, e, c, d, b, f \rangle, \langle a, b, c, e, d, b, f \rangle, \langle a, b, c, d, e, b, f \rangle, \langle a, e, b, c, d, b, f \rangle]$$

The $\alpha-$ Algorithm gives the following:

$$T_L = \{a, b, c, d, e, f\}$$

$$T_I = \{a\}$$

$$T_O = \{f\}$$

	a	b	\mathbf{c}	$^{\mathrm{d}}$	e	f
a	#	\rightarrow	#	#	\rightarrow	#
b	#	#	\rightarrow	#		\rightarrow
\mathbf{c}	#	#	#	\rightarrow		#
d	#	\rightarrow	#	#		#
e	#				#	\rightarrow
f	#	\leftarrow	#	#	→	\leftarrow

$$X_L = \{(\{a\}, \{b\}), (\{a\}, \{e\}), (\{b\}, \{c\}), (\{b\}, \{f\}), (\{c\}, \{d\}), (\{b\}, \{c, f\}), (\{d\}, \{b\}), (\{e\}, \{f\}), (\{a, d\}, \{b\})\}\}\}$$

$$Y_L = \{(\{a\}, \{e\}), (\{b\}, \{c, f\}), (\{b\}, \{f\}), (\{c\}, \{d\}), (\{e\}, \{f\}), (\{a, d\}, \{b\})\}\}$$

