Pattern Creator

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Problem

- ➤ ECP limited to simple shapes
- ➤ Small file sizes required

Idea

- ➤ Draw arbitrary geometrical shapes
- > Shapes represented as parametrizations of closed curves
- ➤ Use low amount of rectangles to fill the shapes
- ➤ Implement as an easy to use Python package

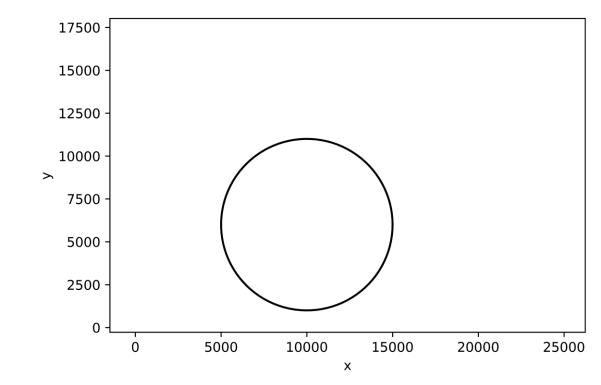
Definition of shapes

Parametrization of a **closed** curve $\vec{x}(t)$

Example:

$$\vec{x}_{\text{Circle}}(t) = \begin{pmatrix} x_0 + r \cdot \cos(2\pi t) \\ y_0 + r \cdot \sin(2\pi t) \end{pmatrix}$$

with $t \in [0, 1)$.

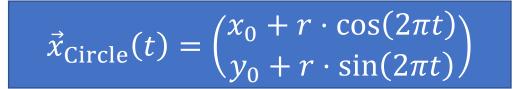


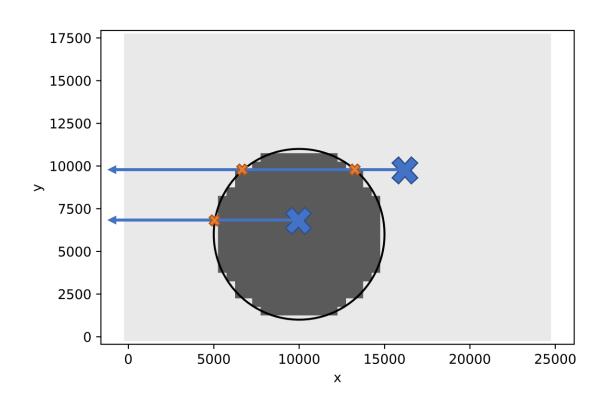
Translation of the shape into pixels

- ➤ Black / White image
- ➤ Pixel as the smallest possible rectangle
- $\triangleright 1 \rightarrow \text{pixel is part of a shape, } 0 \rightarrow \text{pixel is not part of a shape}$

Raycasting method

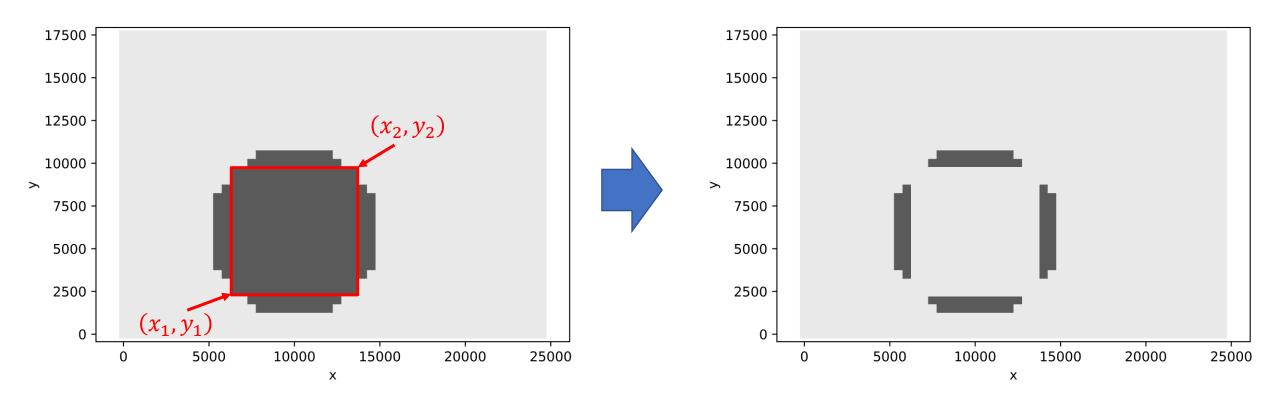
- Check for each pixel $\vec{p}=(x,\ y)$, if a ray going from $(x,\ y)$ to $(-\infty,y)$ intersects $\vec{x}(t)$ and odd (even) amount of times
- ➤Odd (even) → Pixel is (not) inside of the shape





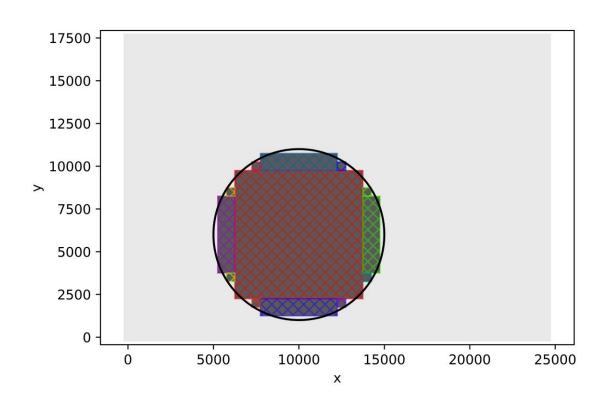
Grouping pixels into larger rectangles

- Find the largest rectangle that fits into the shape in the image
- Save coordinates of two opposite corners (x_1, y_1, x_2, y_2)
- > Remove the found rectangle from the image
- **≻**Repeat



Grouping pixels into larger rectangles

- ➤ Repeat until no pixel is left
- ➤ Convert rectangle corner coordinates into ECP code





ECP .pat code

RECT 6250, 2250, 13750, 9750

RECT 5250, 3750, 6250, 8250

RECT 7750, 1250, 12250, 2250

RECT 7750, 9750, 12250, 10750

RECT 13750, 3750, 14750, 8250

RECT 5750, 3250, 6250, 3750

RECT 5750, 8250, 6250, 8750

RECT 7250, 1750, 7750, 2250

RECT 7250, 9750, 7750, 10250

RECT 12250, 1750, 12750, 2250

RECT 12250, 9750, 12750, 10250

RECT 13750, 3250, 14250, 3750

RECT 13750, 8250, 14250, 8750

More complicated shapes

- ➤ Combination of multiple curves
- ➤ Overlap is automatically supported
- ➤ Higher resolution with fast computation time

➤ Short code:

```
from generate_pattern import Pattern, circle, ellipse
from math import pi

pattern = Pattern(3e4, 2.5e4, 250)
pattern.add_parametrized_shape(circle, 8e3, 18e3, 3e3)
pattern.add_parametrized_shape(ellipse, 1.5e4, 1.1e4, 0.4e4, 1e4, 90 / 180 * pi)
pattern.add_parametrized_shape(ellipse, 8e3, 14e3, 0.15e4, 0.4e4, -40 / 180 * pi)
pattern.add_parametrized_shape(ellipse, 5e3, 17e3, 0.1e4, 0.3e4, 90 / 180 * pi)
pattern.add_parametrized_shape(ellipse, 17e3, 6e3, 1e3, 3e3, 0 / 180 * pi)
pattern.add_parametrized_shape(ellipse, 14e3, 4e3, 1.2e3, 3e3, 90 / 180 * pi)
pattern.add_parametrized_shape(ellipse, 22e3, 11e3, 2.2e3, 5e3, -50 / 180 * pi)
pattern.visualize()
print(pattern.export_pattern())
```

