



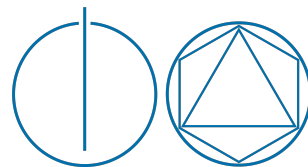
FAKULTÄT FÜR INFORMATIK

TECHNISCHE UNIVERSITÄT MÜNCHEN

Interdisciplinary Project in Mathematics

Random Generation of Tangrams

Wiebke Köpp





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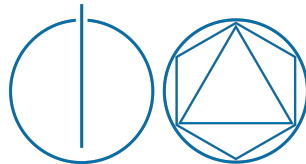
TECHNISCHE UNIVERSITÄT MÜNCHEN

Interdisciplinary Project in Mathematics

Random Generation of Tangrams

Zufällige Generierung von Tangrams

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I assure the single handed composition of this interdisciplinary project in mathematics is only supported by declared resources.

Munich, March 31, 2015

Wiebke Köpp

Acknowledgments

Kurzfassung

Abstract

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1 Introduction

1.1 Section

Citation testiing

1.1.1 Subsection

See Figure 1.1.



Figure 1.1: An example for a figure.

1.2 Section

See Table 1.1, Figure 1.2, Figure 1.3, Figure 1.4.

Table 1.1: An example for a simple table.

A	B	C	D
1	2	1	2
2	3	2	3

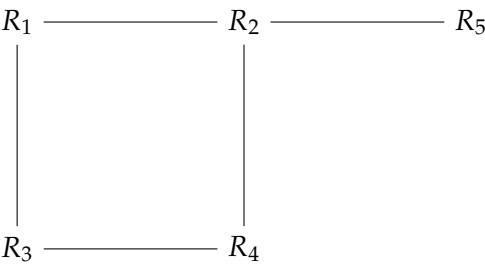


Figure 1.2: An example for a simple drawing.

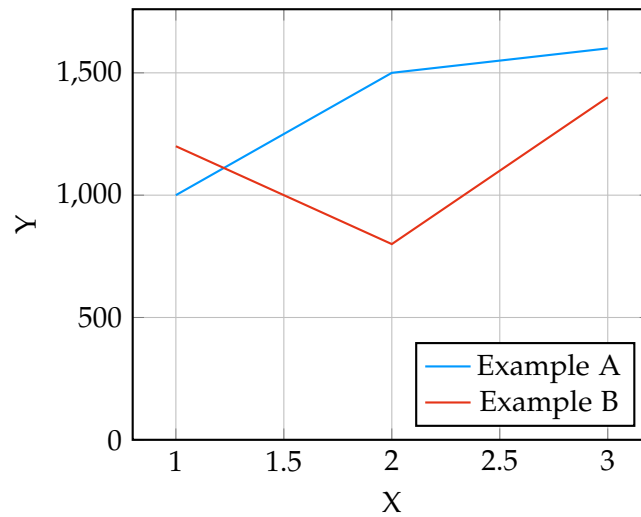


Figure 1.3: An example for a simple plot.

```
SELECT * FROM tbl WHERE tbl.str = "str"
```

Figure 1.4: An example for a source code listing.

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1.1 Example table 3

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