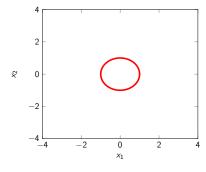
Numerieke technieken en optimalisatie

Jochen Schütz

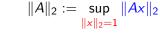


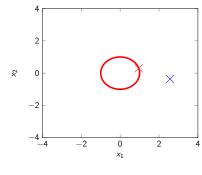
$$||A||_2 := \sup_{||x||_2 = 1} ||Ax||_2$$





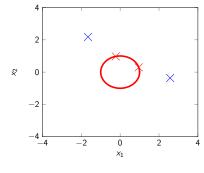
UHASSELT





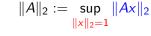


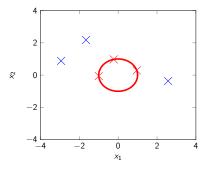






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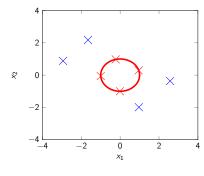




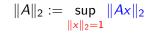


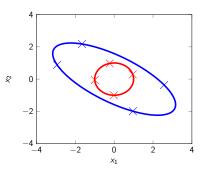
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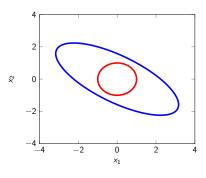




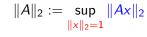


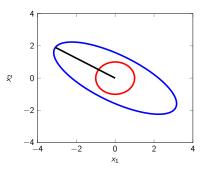














Belangrijke matrix normen

$$||A||_{\infty} = \max_{i} \sum_{j=1}^{n} |a_{ij}|.$$
 $||A||_{1} = \max_{j} \sum_{i=1}^{n} |a_{ij}|.$

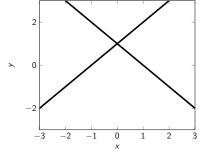
$$\|A\|_1 = \max_j \sum_{i=1} |a_{ij}|.$$

 $\|A\|_2 = \sqrt{\lambda_{max}(A^T A)}.$

(spectraal norm)

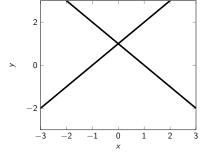


$$x + y = 1$$
$$-x + y = 1$$



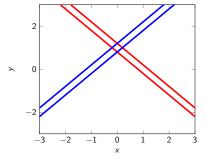


$$x + y = 1 \pm \varepsilon$$
$$-x + y = 1 \pm \varepsilon$$



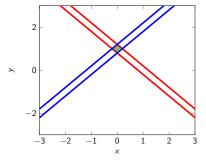


$$x + y = 1 \pm \varepsilon$$
$$-x + y = 1 \pm \varepsilon$$





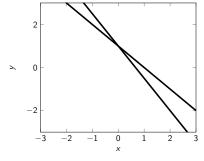
$$x + y = 1 \pm \varepsilon$$
$$-x + y = 1 \pm \varepsilon$$





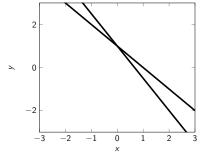
$$x + y = 1$$

$$\frac{3}{2}x + y = 1$$

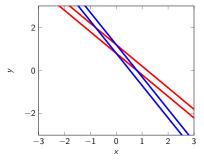




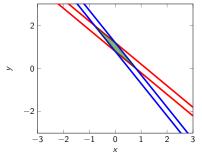
$$x + y = 1 \pm \varepsilon$$
$$\frac{3}{2}x + y = 1 \pm \varepsilon$$



$$x + y = 1 \pm \varepsilon$$
$$\frac{3}{2}x + y = 1 \pm \varepsilon$$

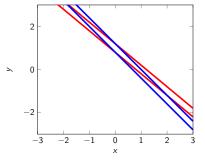


$$x + y = 1 \pm \varepsilon$$
$$\frac{3}{2}x + y = 1 \pm \varepsilon$$



$$x + y = 1 \pm \varepsilon$$

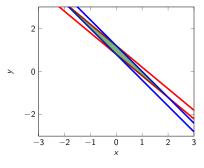
$$\frac{6}{5}x + y = 1 \pm \varepsilon$$





$$x + y = 1 \pm \varepsilon$$

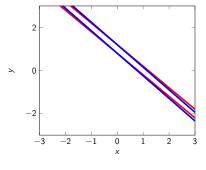
$$\frac{6}{5}x + y = 1 \pm \varepsilon$$





$$x + y = 1 \pm \varepsilon$$

$$\frac{22}{21}x + y = 1 \pm \varepsilon$$



$$x + y = 1 \pm \varepsilon$$

$$\frac{22}{21}x + y = 1 \pm \varepsilon$$

