Chapter 8. Classification: Basic Concepts

- Classification: Basic Concepts
- Decision Tree Induction
- Bayes Classification Methods



- Linear Classifier
- Model Evaluation and Selection
- ☐ Techniques to Improve Classification Accuracy: Ensemble Methods
- Additional Concepts on Classification
- Summary

What Is Bayesian Classification?

- A statistical classifier
 - Perform probabilistic prediction (i.e., predict class membership probabilities)
- ☐ Foundation Based on Bayes' Theorem
- Performance

18 bay Munuy

- A simple Bayesian classifier, *naïve Bayesian classifier*, has comparable performance with decision tree and selected neural network classifiers
- Incremental
 - Each training example can incrementally increase/decrease the probability that a hypothesis is correct—prior knowledge can be combined with observed data
- Theoretical Standard
 - Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

Bayes' Theorem: Basics

Total probability Theorem:

$$p(B) = \sum_{i} p(B|A_i)p(A_i)$$

Bayes' Theorem:

orem:
$$p(H|X) = \frac{p(X|H)P(H)}{p(X)} \propto p(X|H)P(H)$$
posteriori probability likelihood prior probability

What we should choose

What we just see What we knew previously

X: a data sample ("evidence")

H: X belongs to class C

Prediction can be done based on Bayes' Theorem:

Classification is to derive the maximum posteriori

Naïve Bayes Classifier: Making a Naïve Assumption

- ☐ Practical difficulty of Naïve Bayes inference: It requires initial knowledge of many probabilities, which may not be available or involving significant computational cost
- A Naïve Special Case
 - Make an additional assumption to simplify the model, but achieve comparable performance.

attributes are conditionally independent (i.e., no dependence relation between attributes)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdot \cdots \cdot p(x_n|C_i)$$

Only need to count the class distribution w.r.t. features

Naïve Bayes Classifier: Categorical vs. Continuous Valued Features

□ If feature x_k is categorical, $p(x_k = v_k | C_i)$ is the # of tuples in C_i with $x_k = v_k$, divided by $|C_{i,D}|$ (# of tuples of C_i in D)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdot \cdots \cdot p(x_n|C_i)$$

 $\hfill \square$ If feature x_k is continuous-valued, $p(x_k=v_k|C_i)$ is usually computed based on Gaussian distribution with a mean μ and standard deviation σ

$$p(x_k = v_k | C_i) = N(x_k | \mu_{C_i}, \sigma_{C_i}) = \frac{1}{\sqrt{2\pi}\sigma_{C_i}} e^{-\frac{(x - \mu_{C_i})^2}{2\sigma^2}}$$

Naïve Bayes Classifier: Training Dataset

Class:

C1:buys_computer = 'yes'

C2:buys_computer = 'no'

Data to be classified:

X = (age <=30, Income = medium,

Student = yes, Credit_rating = Fair)

| | | 1 | T | | • |
|------|--------|---------|---------------|---------------|------------|
| age | income | student | credit_rating | buys_computer | |
| <=30 | high | no | fair | no | / |
| <=30 | high | no | excellent | no | |
| 3140 | high | no | fair | yes | |
| >40 | medium | no | fair | yes | |
| >40 | low | yes | fair | yes | 7 |
| >40 | low | yes | excellent | no | > 120ining |
| 3140 | low | yes | excellent | yes | Patn |
| <=30 | medium | no | fair | no | |
| <=30 | low | yes | fair | yes | |
| >40 | medium | yes | fair | yes | |
| <=30 | medium | yes | excellent | yes | |
| 3140 | medium | no | excellent | yes | |
| 3140 | high | yes | fair | yes | |
| >40 | medium | no | excellent | no | |

ρ(H^{-y} | X) = ? ρ(H^{-y} | X) = ? = ρ(X| H^{-y}) ρ(H^{-y}) - ²/₄

P(Hay = N \ conge . 41, student= yes) =

Naïve Bayes Classifier: An Example

```
P(C<sub>i</sub>): P(buys_computer = "yes") = 9/14 = 0.643
P(buys_computer = "no") = 5/14 = 0.357
```

 \square Compute $P(X|C_i)$ for each class

$$P(age = "<= 30" | buys_computer = "no") = 3/5 = 0.6$$

P(income = "medium" | buys_computer = "no") =
$$2/5 = 0.4$$

$$P(student = "yes" | buys_computer = "yes) = 6/9 = 0.667$$

P(student = "yes" | buys_computer = "no") =
$$1/5 = 0.2$$

| age | income | student | credit_rating | buys_computer |
|------|--------|---------|---------------|---------------|
| <=30 | high | no | fair | no |
| <=30 | high | no | excellent | no |
| 3140 | high | no | fair | yes |
| >40 | medium | no | fair | yes |
| >40 | low | yes | fair | yes |
| >40 | low | yes | excellent | no |
| 3140 | low | yes | excellent | yes |
| <=30 | medium | no | fair | no |
| <=30 | low | yes | fair | yes |
| >40 | medium | yes | fair | yes |
| <=30 | medium | yes | excellent | yes |
| 3140 | medium | no | excellent | yes |
| 3140 | high | yes | fair | yes |
| >40 | medium | no | excellent | no |

X = (age <= 30, income = medium, student = yes, credit_rating = fair)</p>

$$P(X|C_i)$$
: $P(X|buys_computer = "yes") = 0.222 x 0.444 x 0.667 x 0.667 = 0.044 $P(X|buys_computer = "no") = 0.6 x 0.4 x 0.2 x 0.4 = 0.019$$

$$P(X|C_i)*P(C_i): P(X|buys_computer = "yes") * P(buys_computer = "yes") = 0.028$$

 $P(X|buys_computer = "no") * P(buys_computer = "no") = 0.007$

Therefore, X belongs to class ("buys_computer = yes")

Lazy Learner: Instance-Based Methods

- Instance-based learning:
 - Store training examples and delay the processing ("lazy evaluation") until a new instance must be classified
- Typical approaches
 - <u>k-nearest neighbor approach</u>
 - Instances represented as points in a Euclidean space.
 - Locally weighted regression
 - Constructs local approximation
 - Case-based reasoning
 - Uses symbolic representations and knowledge-based inference

