

**Connectivity Detection**

Q: Given a graph  $G_1$ , determine if there is a path between node 2 and 3.  
A: The answer is yes.

**Hamilton Path**

Q: Given a graph  $G_2$ , is there a path visits every node exactly once.  
A: No.

**Shortest Path**

Q: Given a graph  $G_1$ , find the shortest path between node 2 and 3.  
A: The path is 2,0,4,3.

**Cycle Detection**

Q: Given a graph  $G_1$ , determine if there is a graph cycle.  
A: No cycle in the graph.

**Bipartite Matching**

Q: Given a graph  $G_2$ , whether node 1 is connective to node 4.  
A: Yes.

**Degree Computing**

Q: Given a graph  $G_1$ , compute the degree of node 4.  
A: The degree is 3.

$G_1$

```
Graph[name="G1"]{
  node_list=[0, 1, 2, 3, 4, 5];
  edge_list=[
    (0 <-> 1)[weight=1],
    (0 <-> 2)[weight=3],
    ...
  ];
}
```

$G_2$

```
Graph[name="G2"]{
  node_list=[0, 1, 2, 3, 4, 5];
  edge_list=[
    (0 <-> 2), (0 <-> 5),
    (1 <-> 2), (1 <-> 3),
    ...
  ];
}
```

**Link Prediction**

Q: Given a graph  $G_3$ , predict the relation between "James Cameron" and "Canada".  
A: place\_of\_birth.

**Question Answering**

Q: Given a graph  $G_3$ , answer the question: what's the birthday of the film TITANIC's director?  
A: 1954.

**Relevance Inspection**

Q: Given a graph  $G_3$ , whether the following passage is relevant to the graph. "James ...".  
A: Yes, it's relevant.

**Graph  $G_3$**

```
Graph[name="G3"]{
  entity_list = [
    "James Cameron", "Ontario", ... ],
  triple_list = [
    ("James Cameron" -> "Ontario")[
      relation="born in"
    ], ... ],
}
```

**Graph  $G_4$**

```
Graph[name="G4"]{
  entity_list = [
    "User1", "User2", ... ],
  triple_list = [
    ("User1" -> "Item1")[score="good"],
    ... ],
    "User1".review = "The film ...",
    ...
  ];
}
```

**Caption Generation**

Q: Given a graph  $G_3$ , generate a caption to describe the graph.  
A: James Cameron ...

**Node Classification**

Q: Given a graph  $G_3$ , classify the node "Canada".  
A: country\_name.

**Collaboration Filtering**

Q: Given a graph  $G_4$ , what's the user3's review preference towards item1?  
A: It's 🍌.

Definition: Given a graph, understand the structure and answer the question about connectivity, cycle, hamilton path, bipartite matching, shortest path and degree.

Graph Structure Modeling  
(Graph2Text)

Graph Language Modeling  
(Graph2Text)

Definition: Given a graph, understand the graph semantic and answer the question about caption, QA, node classification, link prediction, relevance and collaboration.

Definition: Given a passage, understand the instruction and question, and then generate a graph to satisfy the semantics or structures.

Graph Generation Modeling  
(Text2Graph)

Graph Thought Modeling  
(Text2Graph2Text)

Definition: Given a reasoning question, think step by step: 1) find a topic entity, 2) then generate a graph that express the thinking process, 3) finally output the answer.

**Knowledge Graph Generation**

Q: Given the following passage, generate a knowledge graph to express the semantics: "James Cameron is a Canadian filmmaker born in Ontario in 1954. He directed popular movies such as Titanic and Avatar."  
A: The graph is shown in the follow:

```
Graph[name="Knowledge-Graph"]{
  entity_list = ["James Cameron", "Ontario", ... ],
  triple_list = [("James Cameron" -> "Ontario")[
    relation="born in"], ... ],
}
```

**Structure Graph Generation**

Q: Given the follow description, generate a graph to release the structure. "In an undirected graph, the nodes are from 0 to 6, (i, w, j) means an edge with a weight w. All edges are: (3, 5, 5), (0, 2, 1), (0, 1, 6), (2, 3, 4), (5, 1, 6), (2, 3, 3), (1, 1, 6) and (1, 4, 6)."  
A: The graph is shown in the follow:

```
Graph[name="Structure-Graph"]{
  node_list = [0, 1, 2, 3, 4, 5, 6],
  edge_list = [
    (0 -> 1)[weight=2], (0 -> 6)[weight=1], ... ],
}
```

**Commonsense & Factual Reasoning**

Q: What's the birth country of Avatar's director?  
A: To answer this question, we first find the topic entity is "Avatar". Then, we construct a knowledge subgraph of the topic entity, the graph is:

```
Graph[name="thought-Graph"]{
  entity_list = ["James Cameron", "Avatar", ... ],
  triple_list = [("Avatar" -> "James Cameron")[
    relation="director"], ... ],
}
```

Based on the graph, we can find a reasoning path that (Avatar, director, James Cameron, born in, Ontario, country, Canada). So the answer is Canada.

**Arithmetical & Logical Reasoning**

Q: Roger had 16 dollars. For his birthday he got 28 more dollars but spent 25 on a new game. How much money does he have now?  
A: To answer this question, we first find the topic entity is "Roger". Then, we construct a graph:

```
Graph[name="thought-Graph"]{
  entity_list = ["Roger", "16 dollars", ... ],
  triple_list = [("Roger" -> "16 dollars")[
    relation="first has"], ... ],
}
```

Based on the graph, we can find a reasoning path that (Roger, first has, 16 dollars, add, 28 dollars, minus, 25 dollars). So the answer is 19 dollars.