

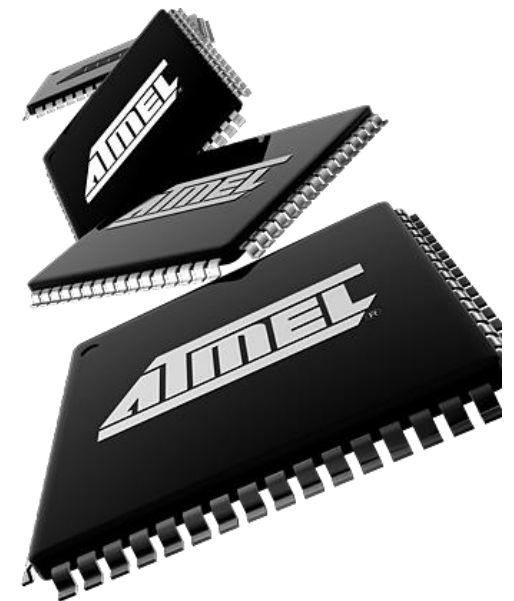
Principles and Applications of Microcontrollers

Yan-Fu Kuo

Dept. of Bio-industrial Mechatronics Engineering
National Taiwan University

Today:

- Pulse width modulation (PWM)

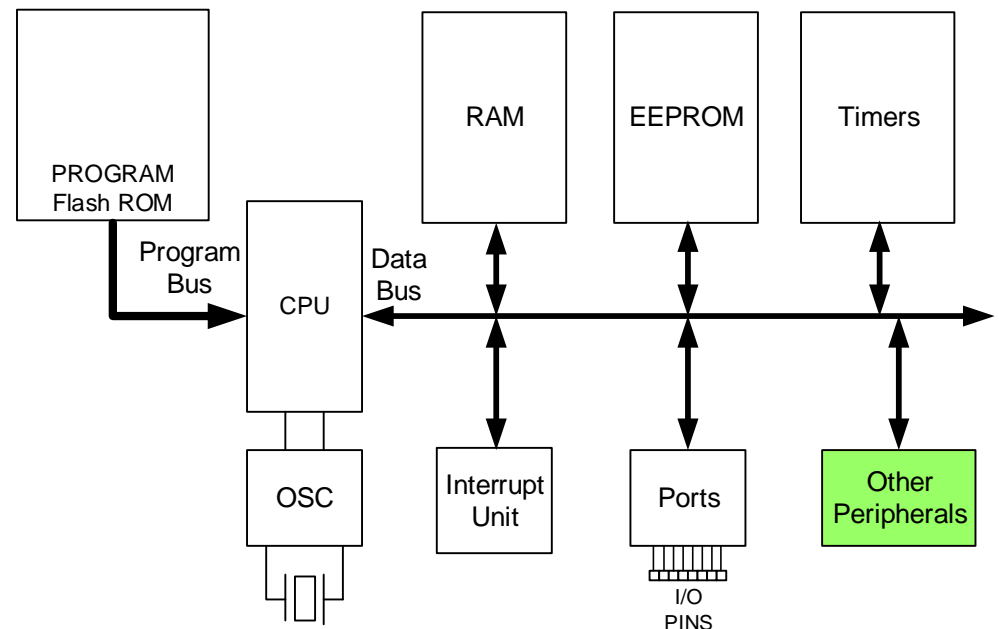


Outline

- Pulse width modulation (PWM)

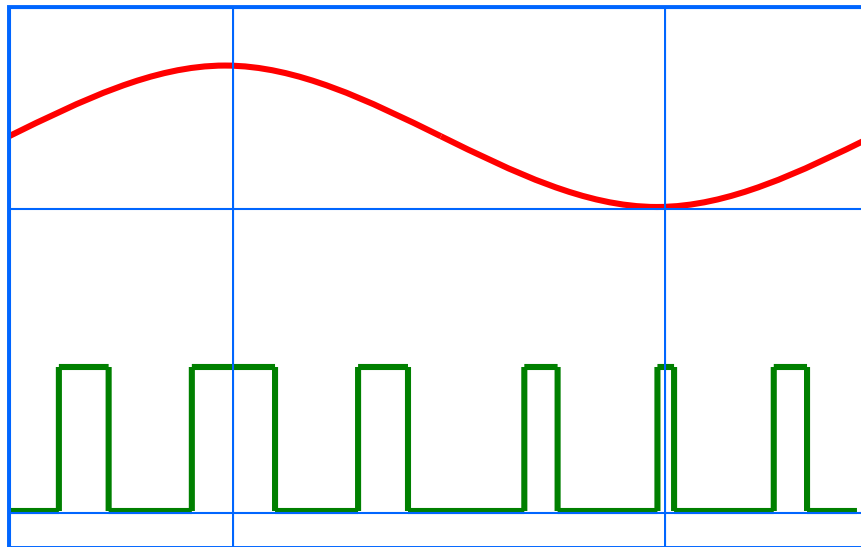
- What is PWM?
- AVR PWM pinout
- Fast PWM
- Phase correct PWM
- Square wave
- Duty cycle and frequency

- Getting started



Pulse Width Modulation

- An approach of approximating analog signal in the form of pulses (binary signal)



Analog Signal

Width Modulated Pulses

Advantages and Application

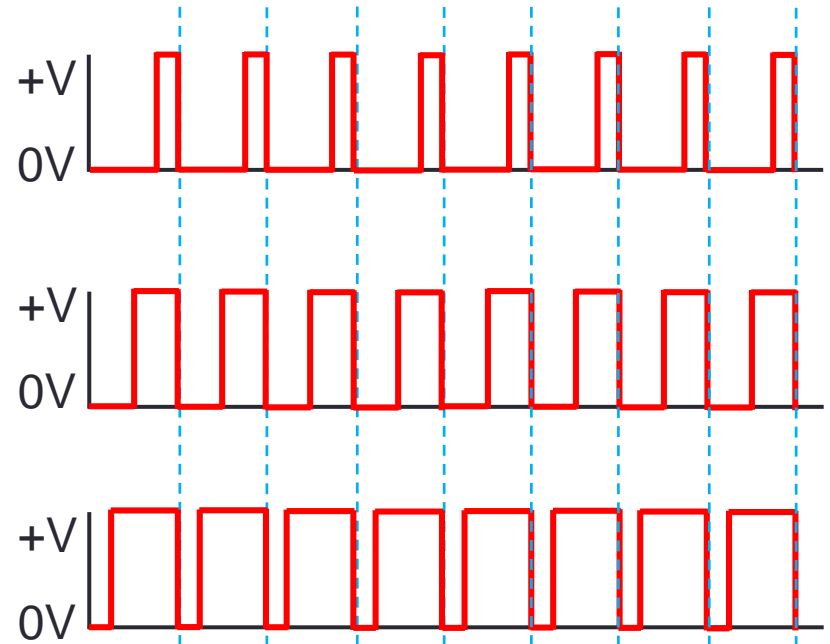
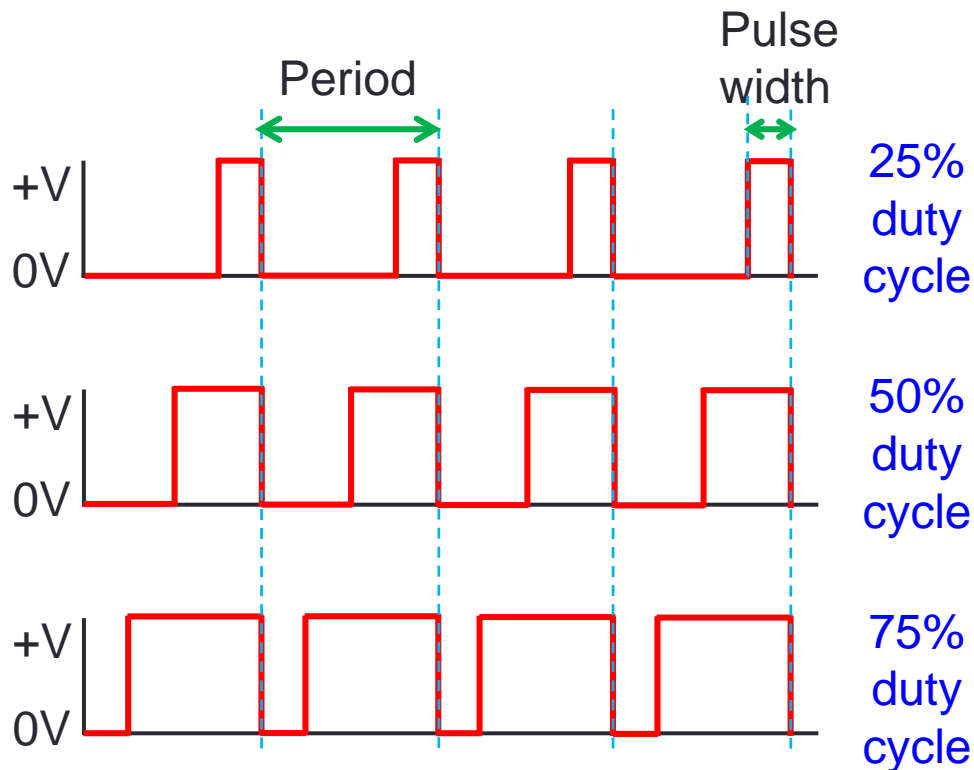
- Advantage:
 - Providing control on output power of a binary output device without changing hardware
 - Digital signal is resistant to noise
 - Less heat dissipated versus using resistors for intermediate voltage values
- Application:
 - Electric stove heater
 - Lamp dimmers
 - Voltage regulation – convert 12 volts to 5 volts by having a 41.7% duty cycle
 - Sound production

PWM Pinout

(PCINT14/RESET) PC6	1	28	PC5 (ADC5/SCL/PCINT13)
(PCINT16/RXD) PD0	2	27	PC4 (ADC4/SDA/PCINT12)
(PCINT17/TXD) PD1	3	26	PC3 (ADC3/PCINT11)
(PCINT18/INT0) PD2	4	25	PC2 (ADC2/PCINT10)
(PCINT19/ OC2B /INT1) PD3	5	24	PC1 (ADC1/PCINT9)
(PCINT20/XCK/T0) PD4	6	23	PC0 (ADC0/PCINT8)
VCC	7	22	GND
GND	8	21	AREF
(PCINT6/XTAL1/TOSC1) PB6	9	20	AVCC
(PCINT7/XTAL2/TOSC2) PB7	10	19	PB5 (SCK/PCINT5)
(PCINT21/ OC0B /T1) PD5	11	18	PB4 (MISO/PCINT4)
(PCINT22/ OC0A /AIN0) PD6	12	17	PB3 (MOSI/ OC2A /PCINT3)
(PCINT23/AIN1) PD7	13	16	PB2 (SS/ OC1B /PCINT2)
(PCINT0/CLKO/ICP1) PB0	14	15	PB1 (OC1A /PCINT1)

Factors to Consider

1. Frequency
2. Duty cycle = $\frac{\text{Pulse Width}}{\text{Period}}$



Outline (Cont'd)

- Pulse width modulation (PWM)
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50% duty cycle



75% duty cycle

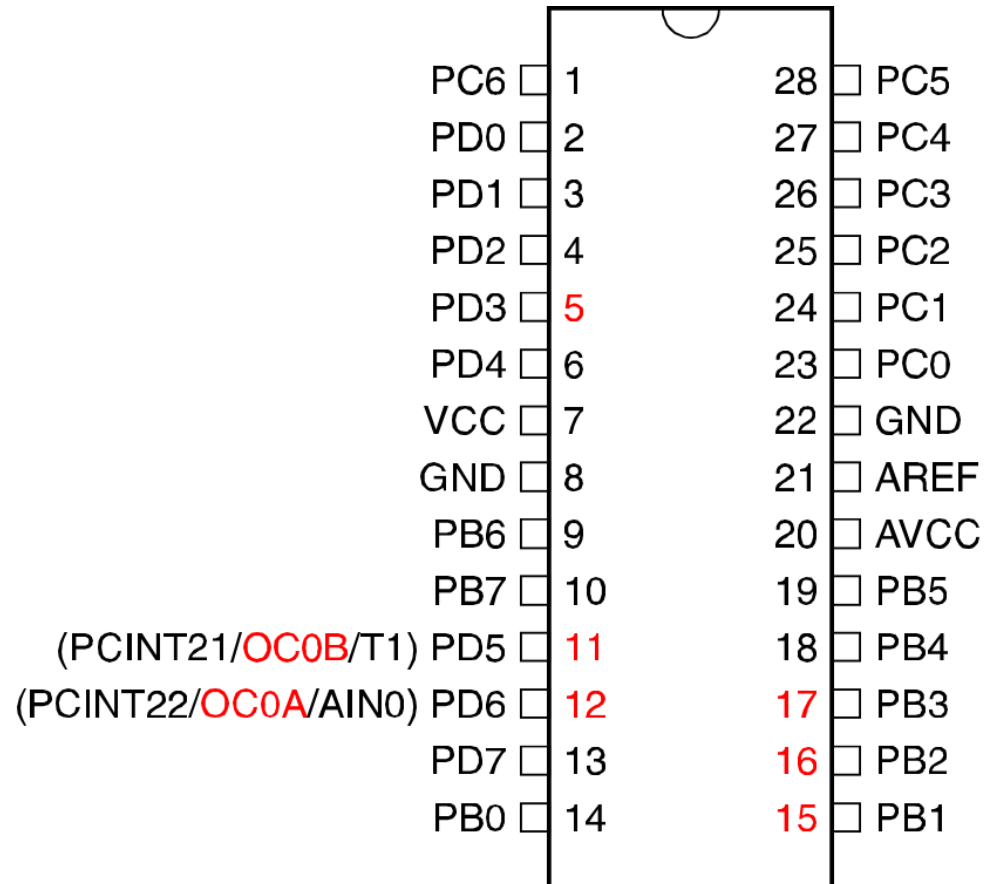
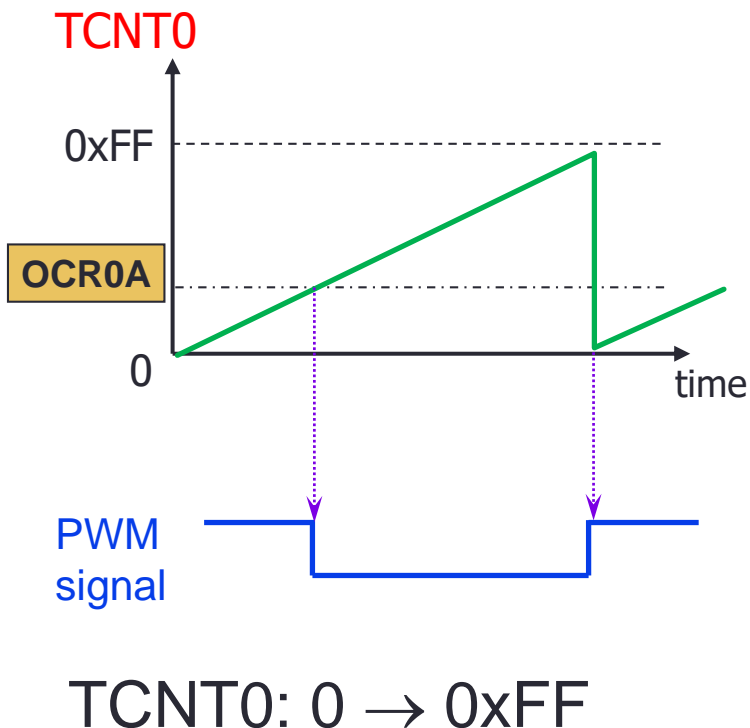


25% duty cycle

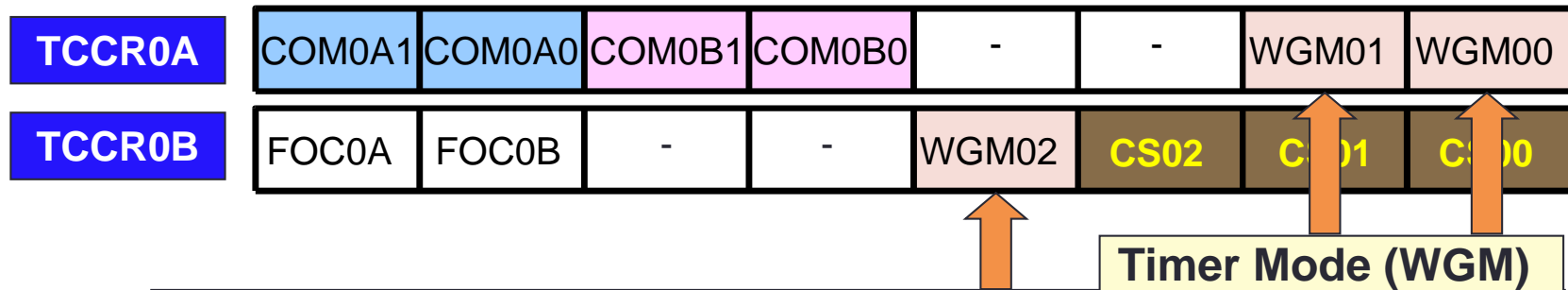


Fast PWM

- Timers are used to generate PWM signals
- OCR0A** determines the duty cycle



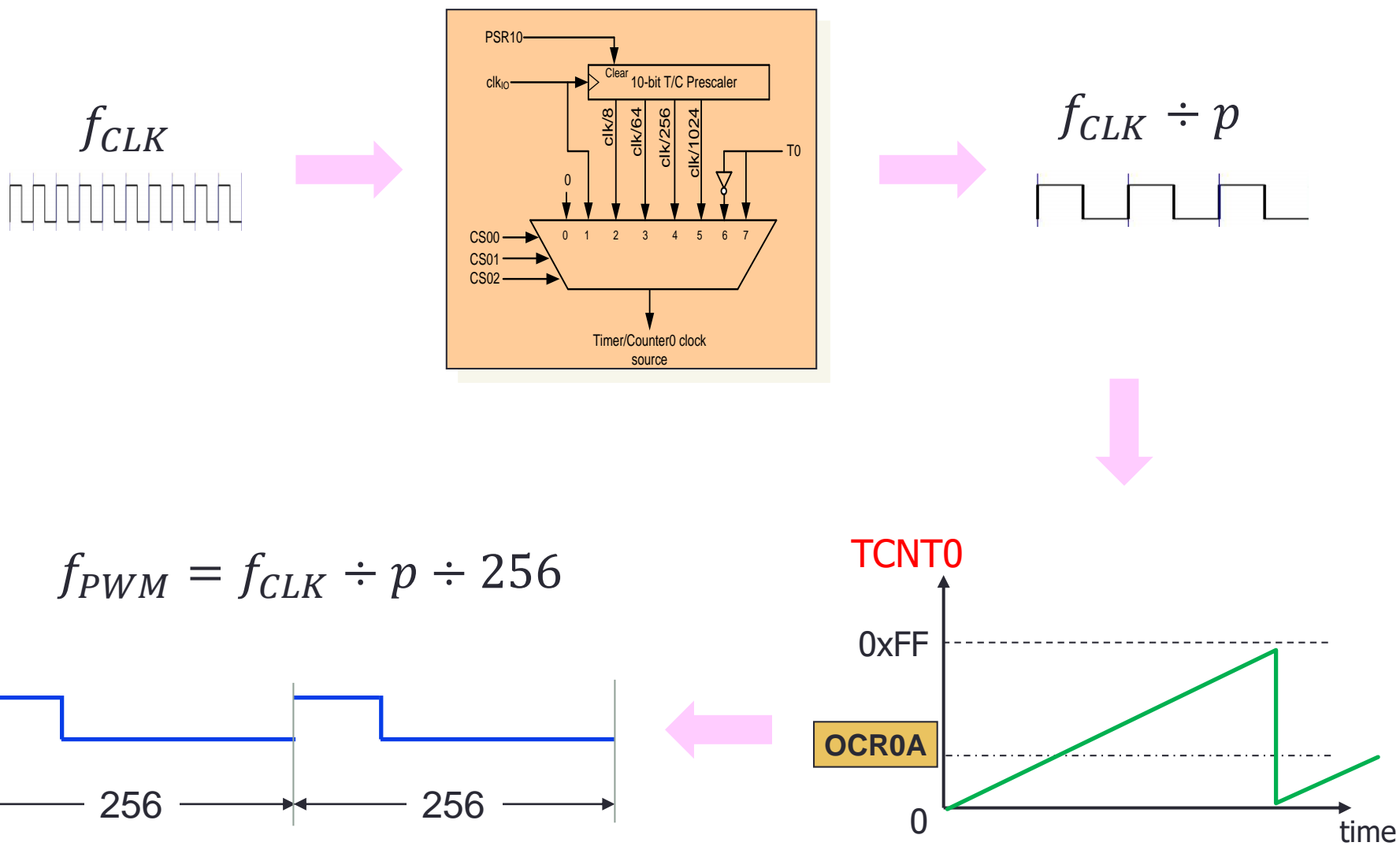
PWM Mode Control: TCCR0A/B



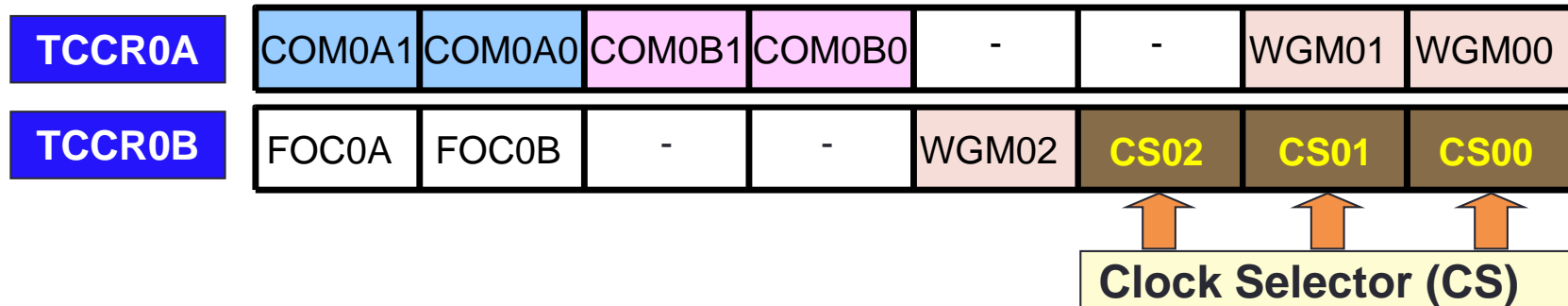
• Re

WGM02	WGM01	WGM00	Comment
0	0	0	Normal
0	0	1	Phase Correct PWM, top 0xFF
0	1	0	CTC (Clear Timer on Compare Match)
0	1	1	Fast PWM, top 0xFF
1	0	0	Reserved
1	0	1	Phase Correct PWM, top OCR0A
1	1	0	Reserved
1	1	1	Fast PWM, top OCR0A

Fast PWM Frequency



Review: Timer Prescaler Control (TCCR0A/B)

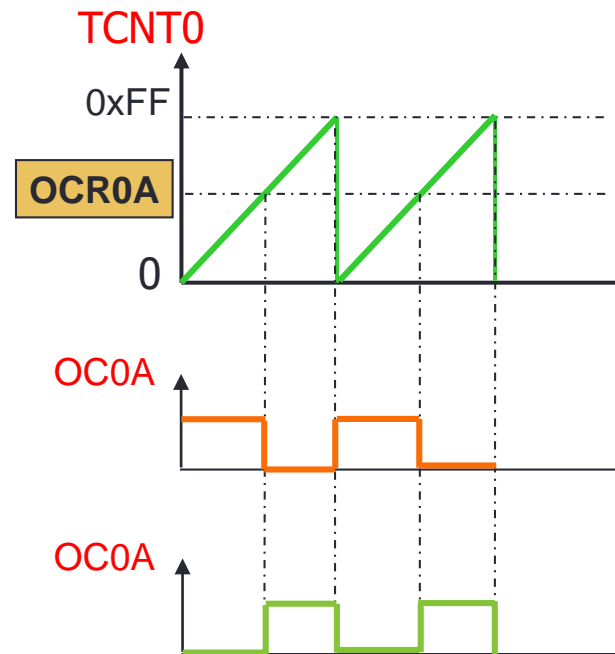
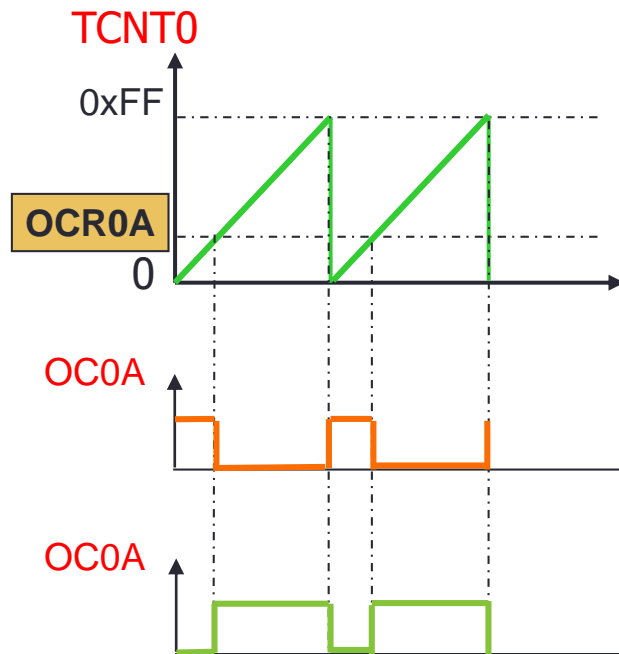


CS02	CS01	CS00	Comment
0	0	0	No clock source (Timer/Counter stopped)
0	0	1	clk (No Prescaling)
0	1	0	clk / 8
0	1	1	clk / 64
1	0	0	clk / 256
1	0	1	clk / 1024
1	1	0	External clock source on T0 pin. Clock on falling edge
1	1	1	External clock source on T0 pin. Clock on rising edge

Fast PWM Duty Cycle (OC0A)

- Non-inverted vs. inverted

PB7 ☐ 10
 (PCINT21/OC0B/T1) PD5 ☐ 11
 (PCINT22/OC0A/AIN0) PD6 ☐ 12
 PD7 ☐ 13



Non-inverted mode

$$\text{Duty cycle} = \frac{OCR0A + 1}{256} \times 100$$

Inverted mode

$$\text{Duty cycle} = \frac{255 - OCR0A}{256} \times 100$$

OC0A Invert Control: TCCR0A/B

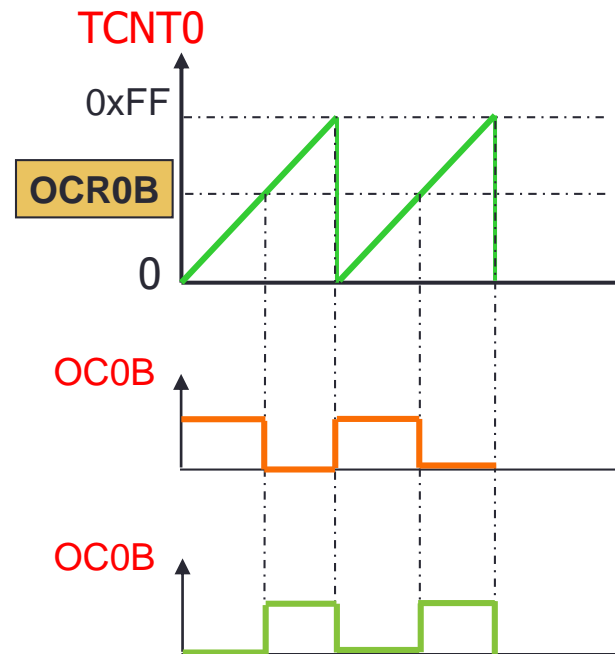
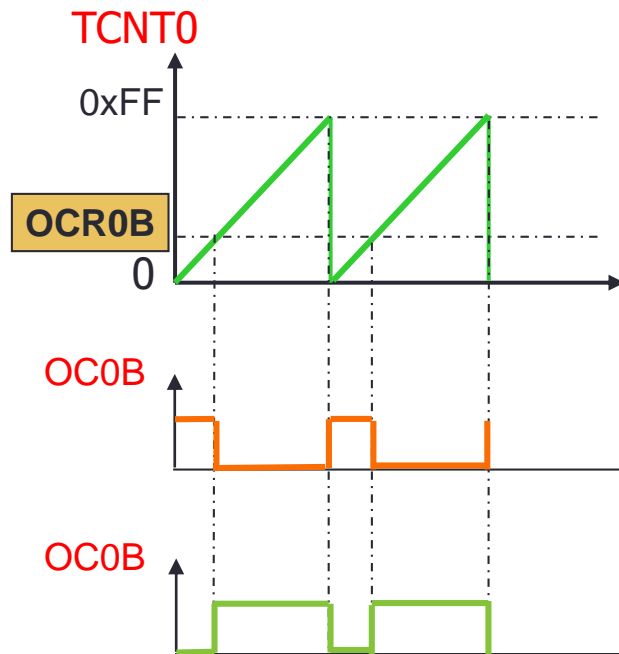
The diagram illustrates the configuration of the TCCR0A and TCCR0B registers for the Compare Output Mode. TCCR0A contains COM0A1, COM0A0, COM0B1, COM0B0, and WGM01. TCCR0B contains FOC0A, FOC0B, WGM02, CS02, CS01, and CS00. Orange arrows indicate that COM0A1 and COM0A0 in TCCR0A correspond to the COM0A1 and COM0A0 columns in the Compare Output Mode table.

COM0A1	COM0A0	Comment
0	0	PWM off
0	1	WGM02 = 0: PWM off WGM02 = 1: Toggle OC0A on compare match
1	0	PWM, non-inverted
1	1	PWM, inverted

Fast PWM Duty Cycle (OC0B)

- Non-inverted vs. inverted

PB7 ☐ 10
 (PCINT21/OC0B/T1) PD5 ☐ 11
 (PCINT22/OC0A/AIN0) PD6 ☐ 12
 PD7 ☐ 13



Non-inverted mode

$$\text{Duty cycle} = \frac{\text{OCR0B} + 1}{256} \times 100$$

Inverted mode

$$\text{Duty cycle} = \frac{255 - \text{OCR0B}}{256} \times 100$$

OC0B Invert Control: TCCR0A/B

TCCR0A

COM0A1COM0A0COM0B1COM0B0- -WGM01WGM00

TCCR0B

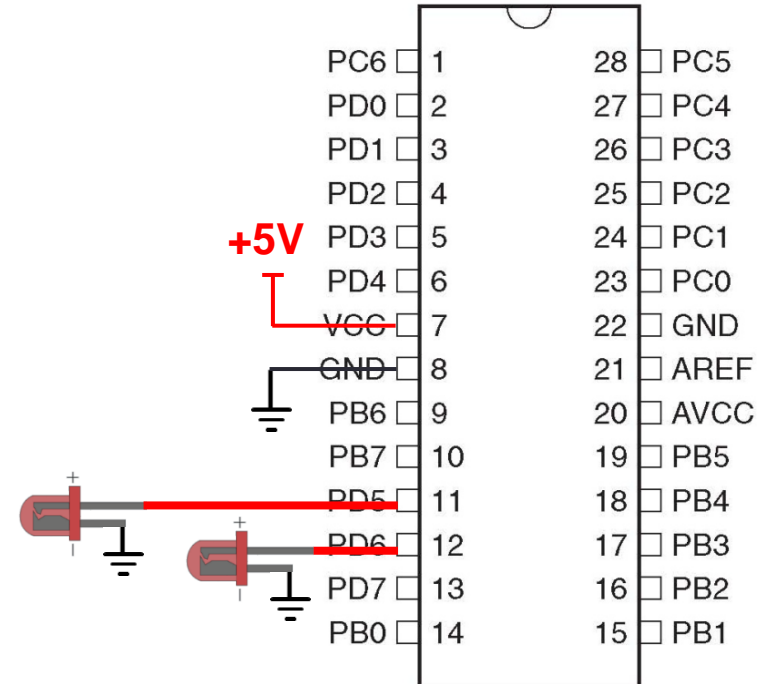
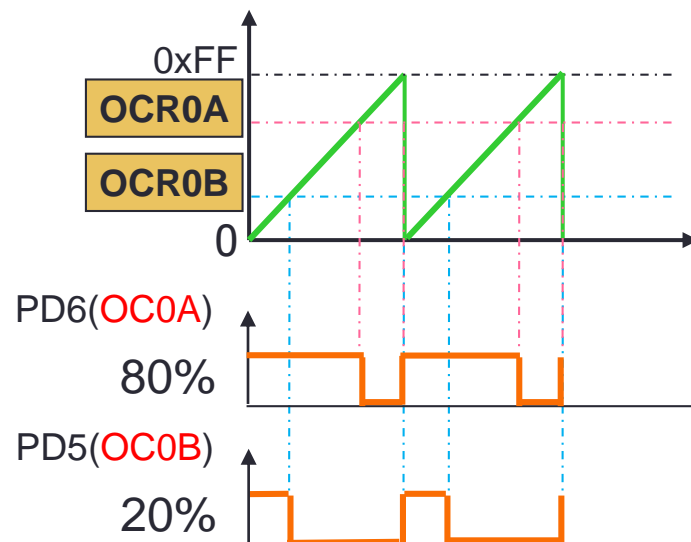
FOC0AFOC0B-WGM02CS02CS01CS00

Compare Output Mode

Fast PWM	COM0A1	COM0A0	Comment
	0	0	PWM off
	0	1	WGM02 = 0: PWM off WGM02 = 1: Toggle OC0B on compare match
	1	0	PWM, non-inverted
	1	1	PWM, inverted
Phase Correct PWM	COM0A1	COM0A0	Comment
	0	0	PWM off
	0	1	WGM02 = 0: PWM off WGM02 = 1: Toggle OC0B on compare match
	1	0	PWM, non-inverted
	1	1	PWM, inverted

Example: Fast PWM

- Suppose the MCU runs at 1Mhz
- Generate PWM waves using Timer0 (non-inverted)
- Output a wave of 80% duty cycle at PD6 (OC0A)
- Output a wave of 20% duty cycle at PD5 (OC0B)
- Prescaler factor $p = 1024$



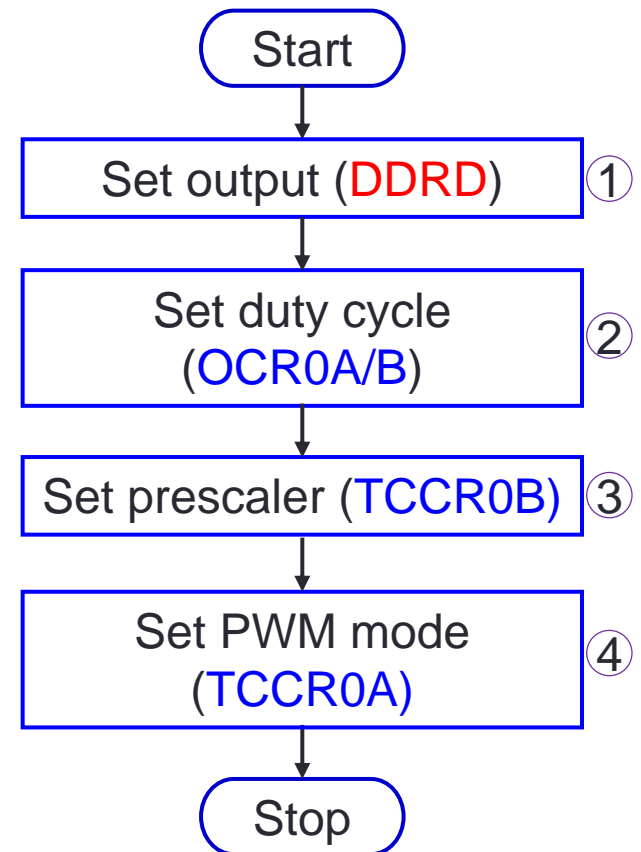
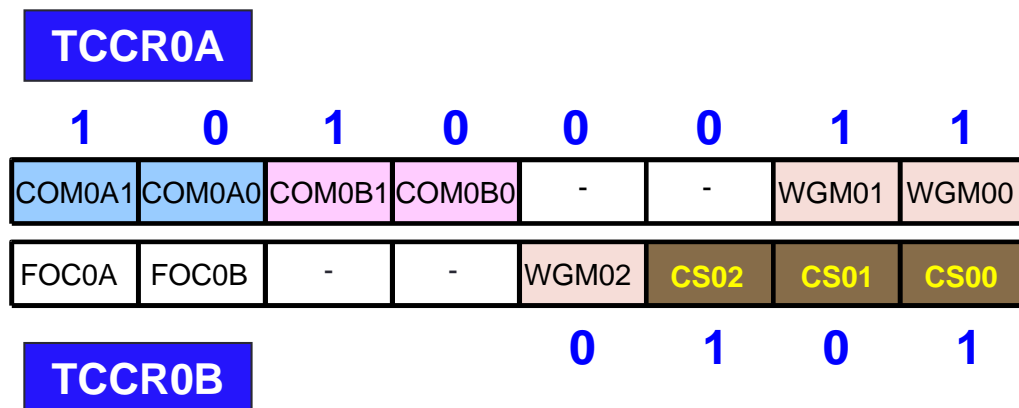
Flowchart (Fast PWM)

- What value do we set to the controller registers?

$$f_{PWM} = 10^6 \div 1024 \div 256 \approx 3.8 \text{ Hz}$$

$$\frac{OCR0A + 1}{256} \times 100 = 80 \Rightarrow OCR0A = 203$$

$$\frac{OCR0B + 1}{256} \times 100 = 20 \Rightarrow OCR0B = 50$$



Fast PWM at 3.8 Hz

```
#include <avr/io.h>

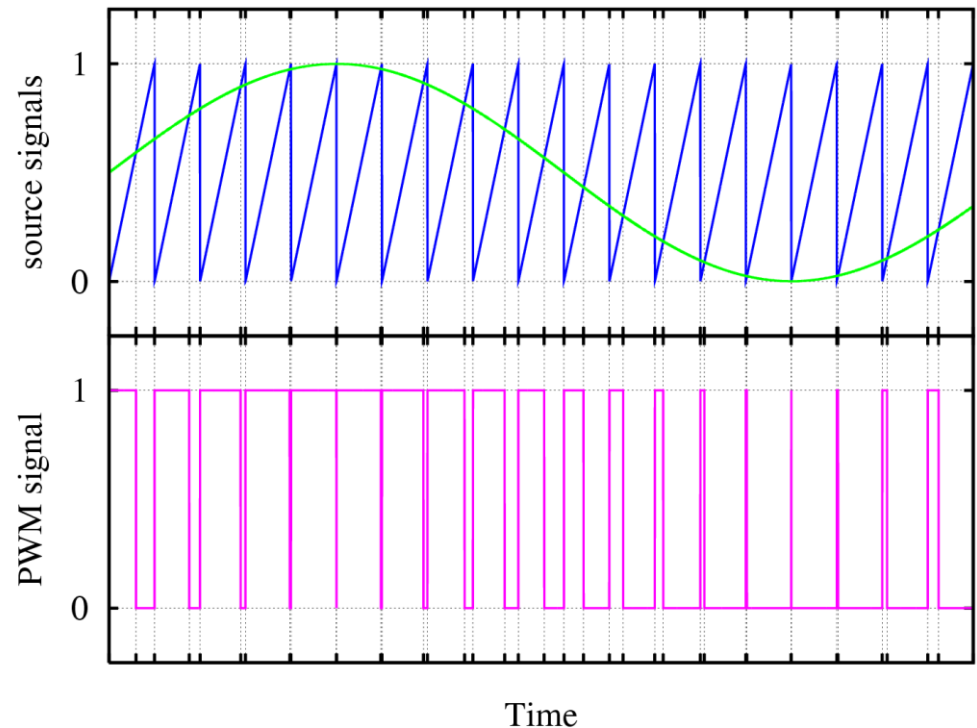
int main(void)
{
    CLKPR=(1<<CLKPCE) ;
    CLKPR=0b00000011;           // set clk to 1Mhz
    ① DDRD=0xFF;                 // PORTD as output
    ② OCR0A=203;                 // 80% duty cycle
    OCR0B=50;                    // 20% duty cycle
    ③ TCCR0A=0b10100011;        // fast PWM, non-inverted
    ④ TCCR0B=0b00000101;        // timer prescaler
}
```

Outline (Cont'd)

- Pulse width modulation (PWM)

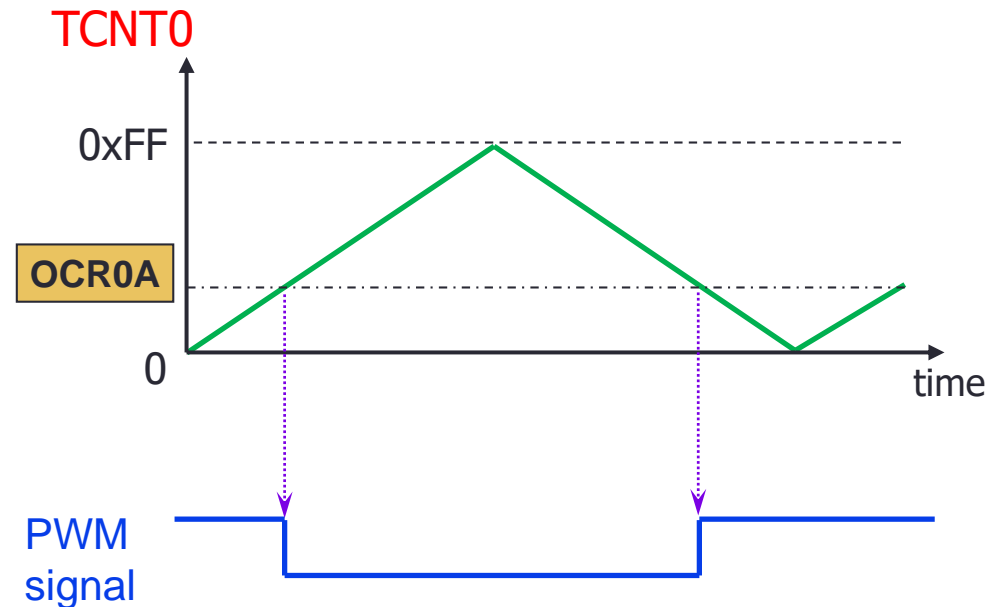
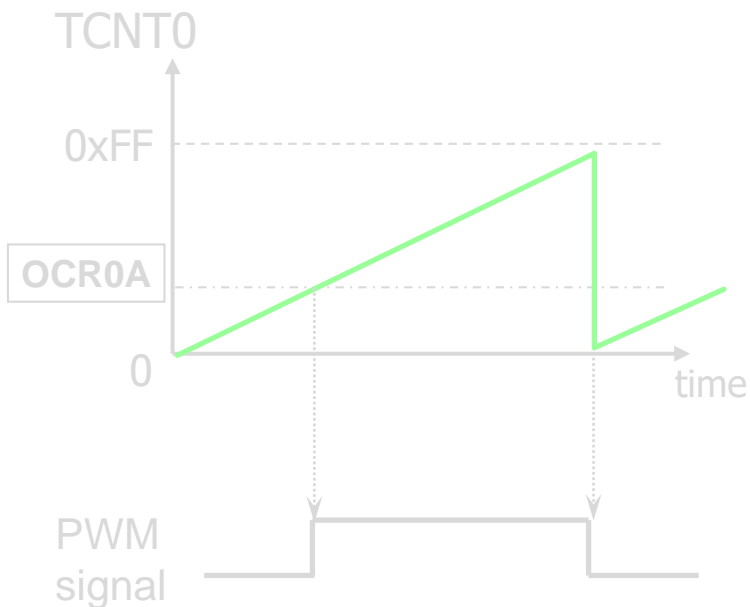
- What is PWM?
- AVR PWM pinout
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- Square wave
- Duty cycle and frequency

- Getting started



Phase Correct PWM

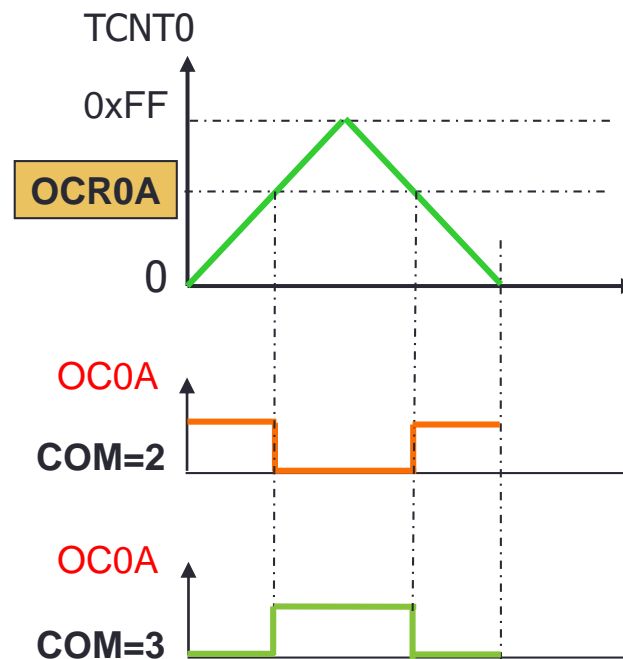
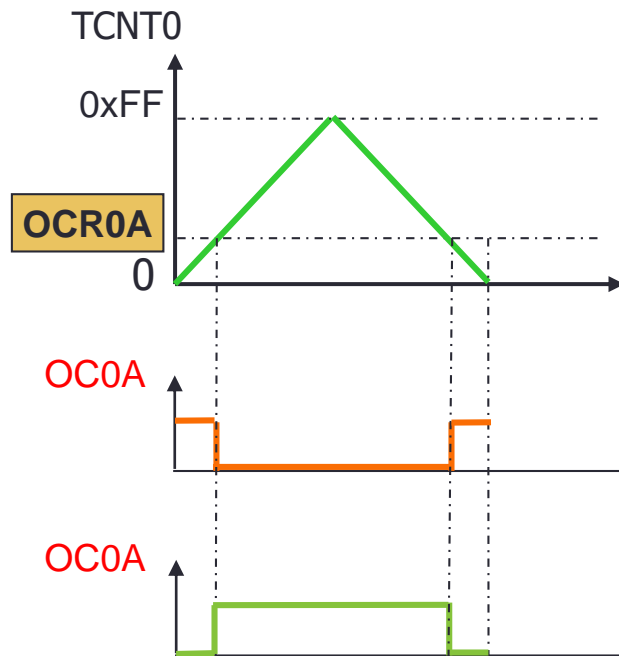
- Timers are used to generate PWM signals



TCNT0: 0 → 0xFF → 0

Phase Correct PWM Frequency and Duty Cycle

- $f_{PWM} = f_{CLK} \div p \div 510$ (p : scalar factor of the timer)
- Non-inverted vs. inverted



Non-inverted mode

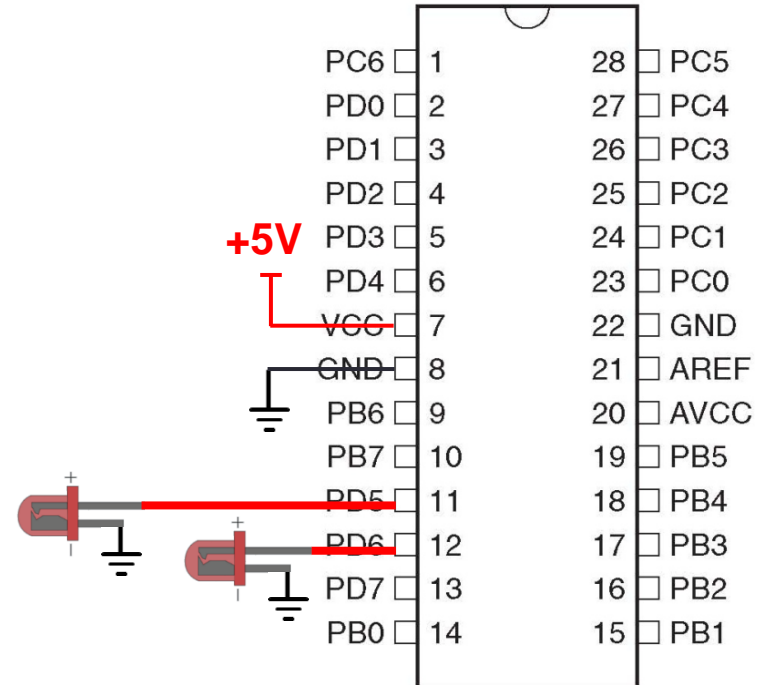
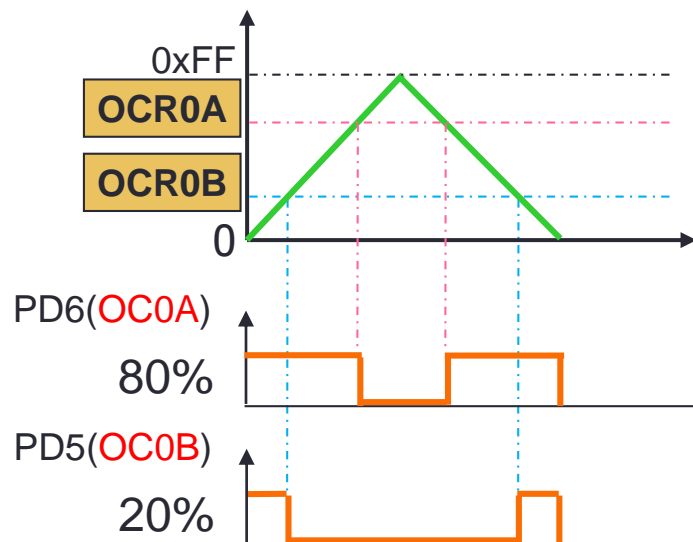
$$\text{Duty cycle} = \frac{OCR0A + 1}{255} \times 100$$

Inverted mode

$$\text{Duty cycle} = \frac{255 - OCR0A}{255} \times 100$$

Example: Phase Correct PWM

- Suppose the MCU runs at 1Mhz
- Generate PWM waves using Timer0 (non-inverted)
- Output a wave of 80% duty cycle at PD6 (OC0A)
- Output a wave of 20% duty cycle at PD5 (OC0B)
- Prescaler factor $p = 1024$



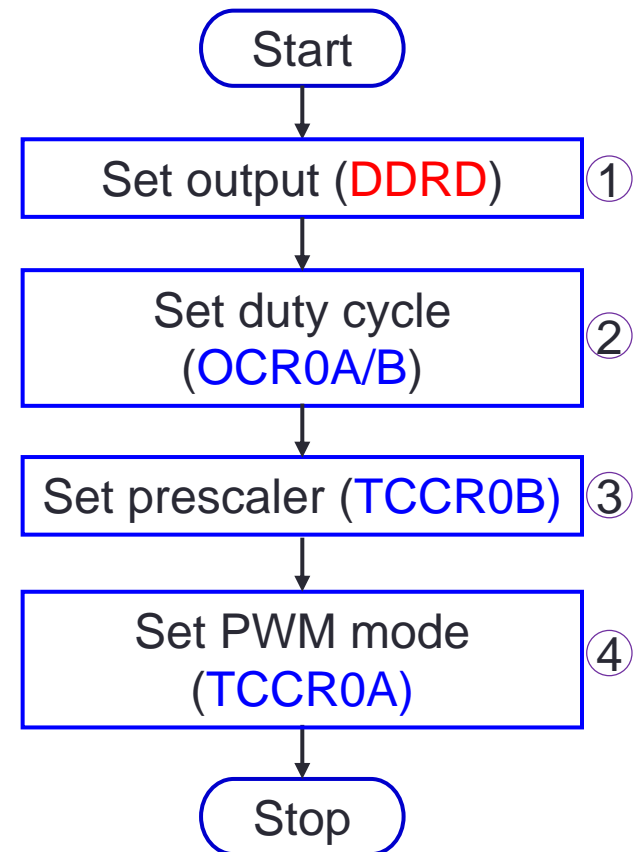
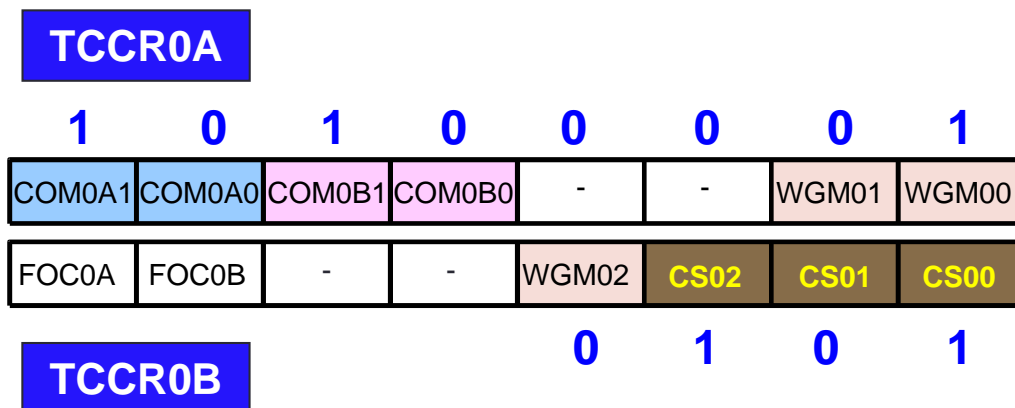
Flowchart (Phase Correct PWM)

- What value do we set the controller registers?

$$f_{PWM} = 10^6 \div 1024 \div 510 \approx 1.9 \text{ Hz}$$

$$\frac{OCR0A + 1}{255} \times 100 = 80 \Rightarrow OCR0A = 203$$

$$\frac{OCR0B + 1}{255} \times 100 = 20 \Rightarrow OCR0B = 50$$



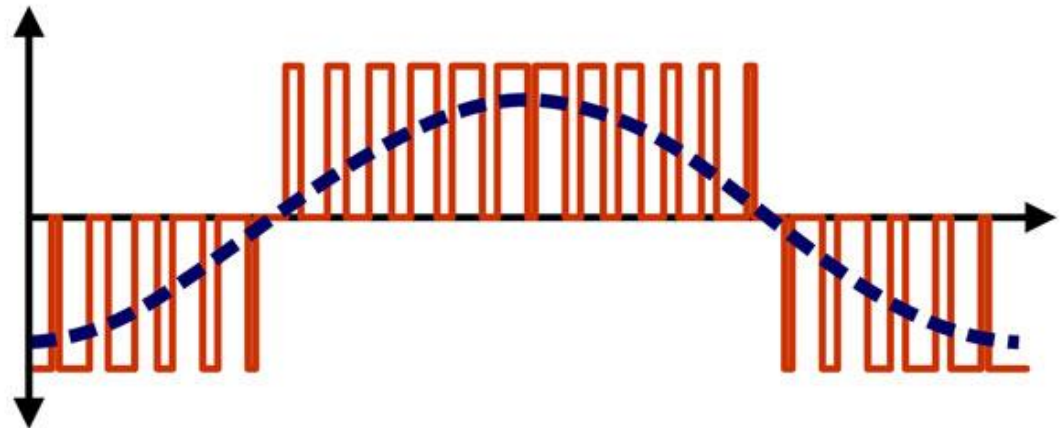
Phase Correct PWM at 1.9Hz

```
#include <avr/io.h>

int main(void)
{
    CLKPR=(1<<CLKPCE) ;
    CLKPR=0b00000011;           // set clk to 1Mhz
    ① DDRD=0xFF;                 // PORTD as output
    ② OCR0A=203;                 // 80% duty cycle
    OCR0B=50;                   // 20% duty cycle
    ③ TCCR0A=0b10100001;        // phase correct PWM
    ④ TCCR0B=0b00000101;        // timer prescaler
}
```


Outline (Cont'd)

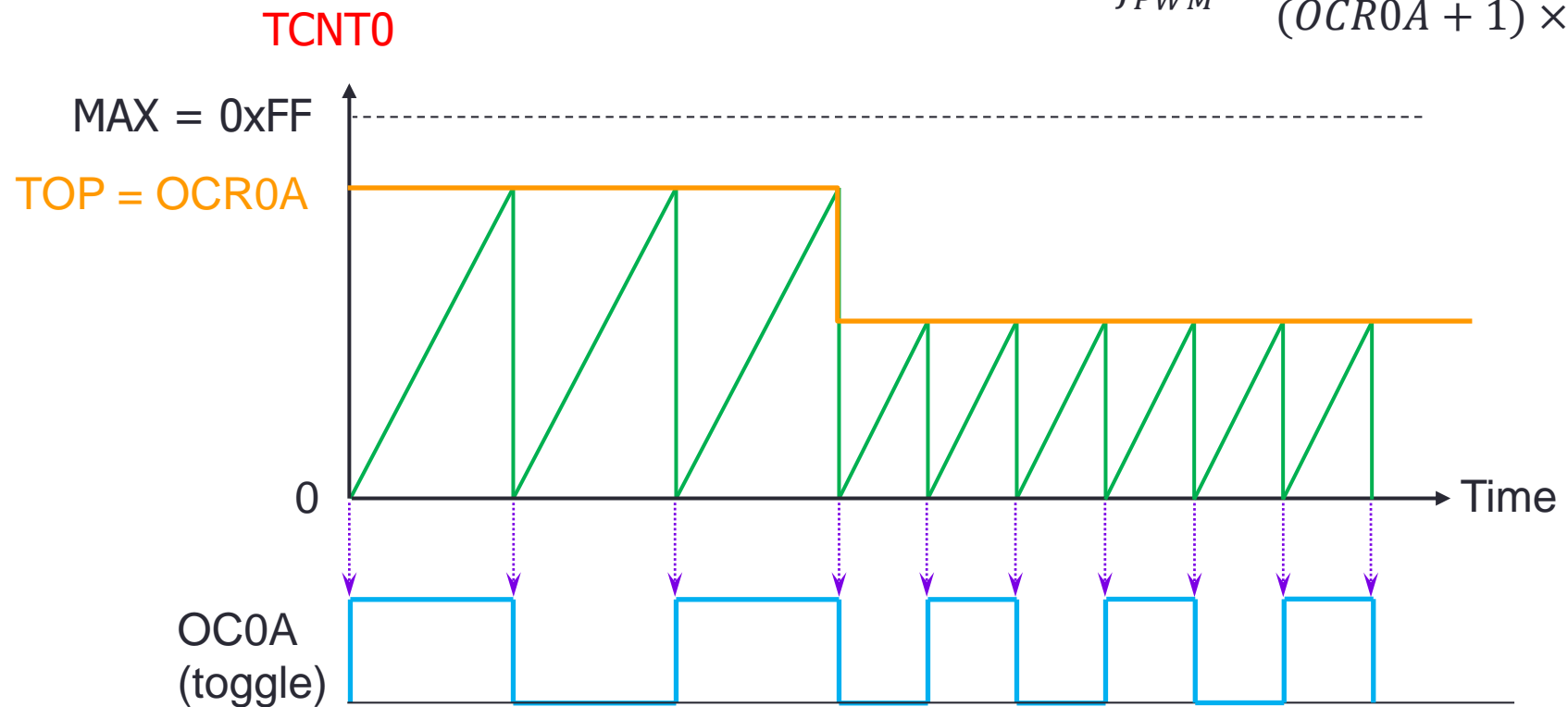
- Pulse width modulation (PWM)
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Square Wave with Frequency Control

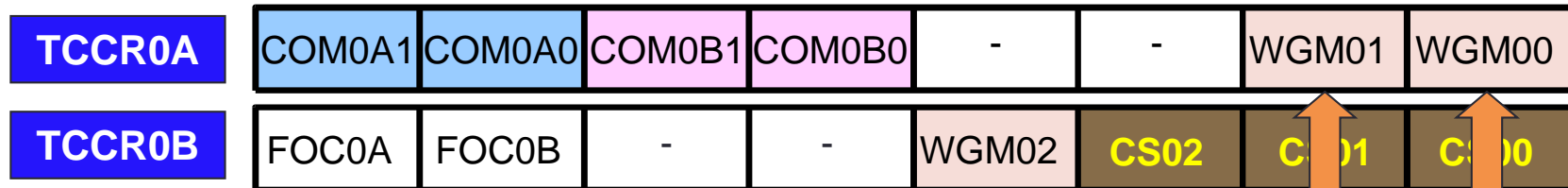
- Generate square waves with various frequencies

$$f_{PWM} = \frac{f_{CLK}}{(OCR0A + 1) \times p}$$



Note: duty cycle cannot be controlled in this mode!

Square Wave Frequency Control: Mode Setup

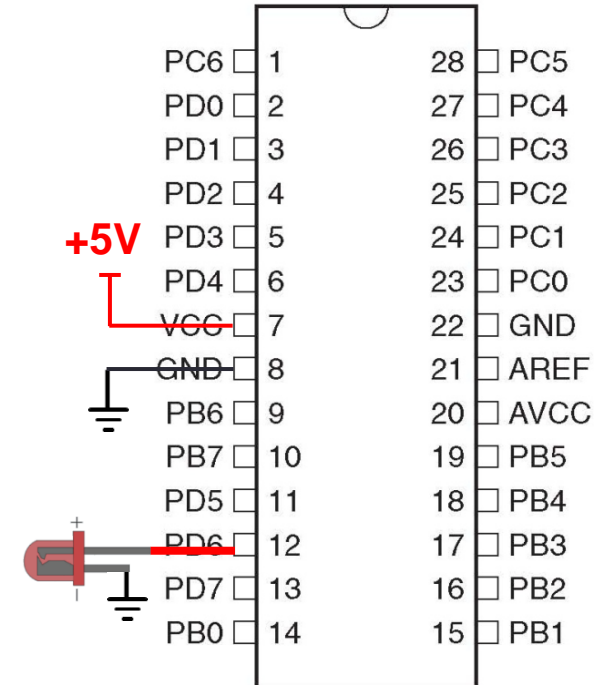
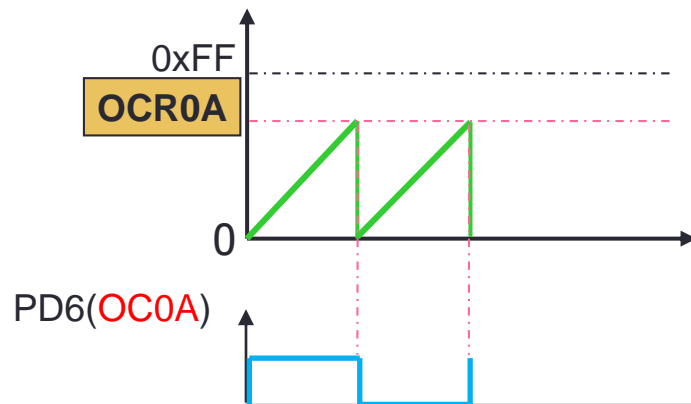


Timer Mode (WGM)			
WGM02	WGM01	WGM00	Comment
0	0	0	Normal
0	0	1	Phase Correct PWM, top 0xFF
0	1	0	CTC (Clear Timer on Compare Match)
0	1	1	Fast PWM, top 0xFF
1	0	0	Reserved
1	0	1	Phase Correct PWM, top OCR0A
1	1	0	Reserved
1	1	1	Fast PWM, top OCR0A

Square Wave Frequency Control: Toggle Setup

Example: Varying LED Flash Frequency

- Suppose the MCU runs at 1Mhz
- Generate square waves continuously using PWM
- Vary the OCR0A from 30 to 250 with an increment of 55
- Output the wave at PD6 (OC0A)
- Prescaler factor $p = 1024$

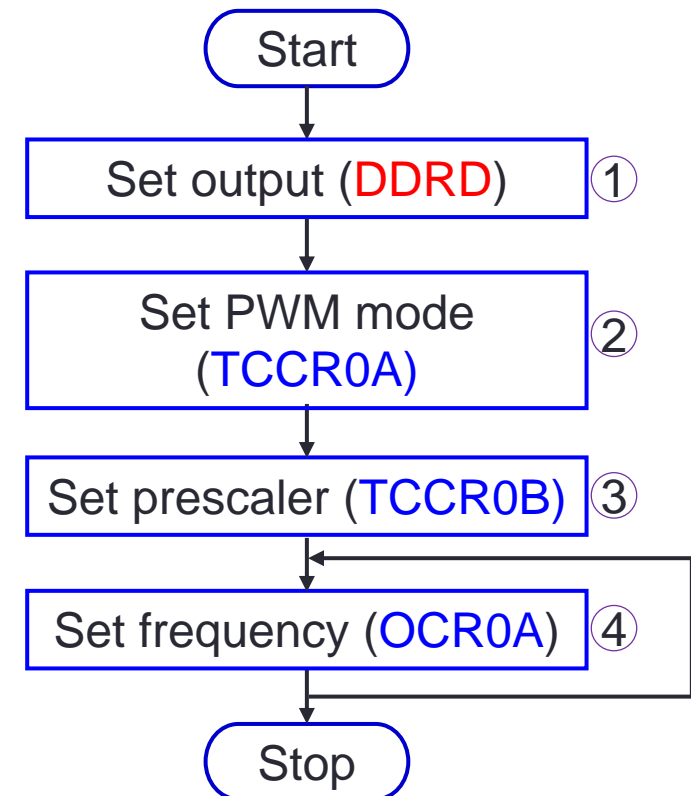
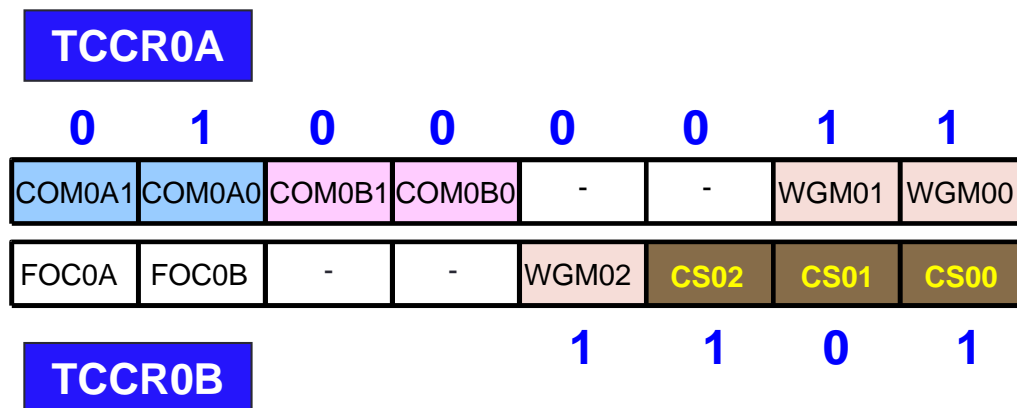


Flowchart (LED Flash)

$$f_{PWM} = \frac{10^6}{(30+1) \times 1024} \approx 31.5 \text{ Hz}$$

$$f_{PWM} = \frac{10^6}{(250+1) \times 1024} \approx 3.9 \text{ Hz}$$

- What value do we set the controller registers?



Varying LED Flash Frequency

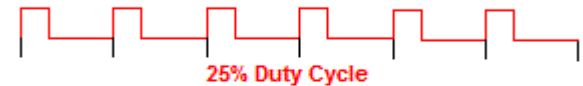
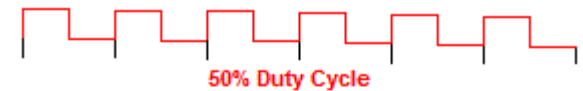
```
#define F_CPU 1000000UL
#include <avr/io.h>
#include <util/delay.h>

int main(void)
{
    CLKPR=(1<<CLKPCE) ;
    CLKPR=0b00000011;           // set clk to 1Mhz
    ① DDRD=0xFF;                 // PORTD as output
    ② TCCR0A=0b01000011;         // TOP OCR0A, toggle at TOP
    ③ TCCR0B=0b00001101;         // timer prescaler
    while (1){
        for (int i=30; i<=250; i=i+55){
            ④ OCR0A=i;
                _delay_ms(2000) ;
        }
    }
}
```

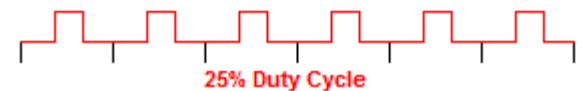
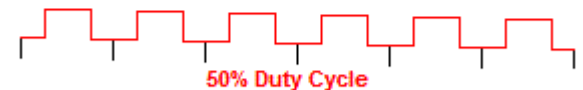
Outline (Cont'd)

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 - What is PWM?
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 - Fast PWM
 - Phase correct PWM
 - Square wave
 - Duty cycle and frequency control
- Getting started

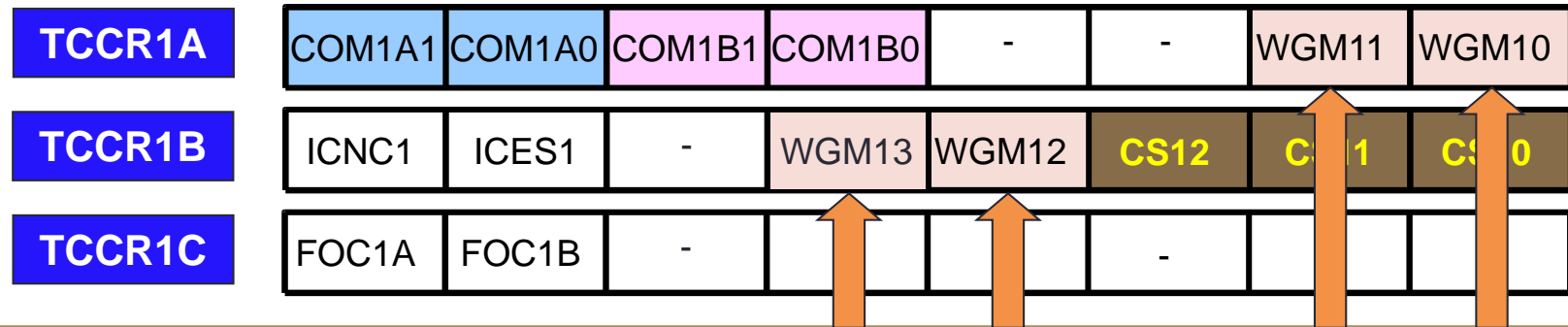
STANDARD PWM



Phase Correct PWM



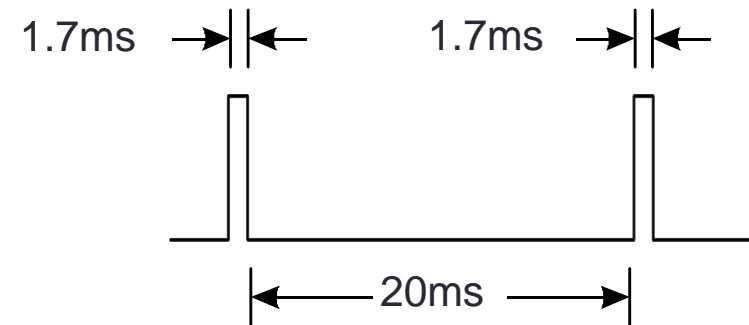
PWM Modes of Timer/Counter1



Mode	WGM 13	WGM 12	WGM 11	WGM 10	Timer/counter mode	TOP	Update of OCR1x at	TOV1 flag set on
0	0	0	0	0	Normal	0xFFFF	Immediate	MAX
1	0	0	0	1	PWM, Phase Correct, 8-bit	0x00FF	TOP	BOTTOM
2	0	0	1	0	PWM, Phase Correct, 9-bit	0x01FF	TOP	BOTTOM
3	0	0	1	1	PWM, Phase Correct, 10-bit	0x03FF	TOP	BOTTOM
4	0	1	0	0	CTC	OCR1A	Immediate	MAX
5	0	1	0	1	Fast PWM, 8-bit	0x00FF	BOTTOM	TOP
6	0	1	1	0	Fast PWM, 9-bit	0x01FF	BOTTOM	TOP
7	0	1	1	1	Fast PWM, 10-bit	0x03FF	BOTTOM	TOP
8	1	0	0	0	PWM, Phase and Frequency Correct	ICR1	BOTTOM	BOTTOM
9	1	0	0	1	PWM, Phase and Frequency Correct	OCR1A	BOTTOM	BOTTOM
10	1	0	1	0	PWM, Phase Correct	ICR1	TOP	BOTTOM
11	1	0	1	1	PWM, Phase Correct	OCR1A	TOP	BOTTOM
12	1	1	0	0	CTC	ICR1	Immediate	MAX
13	1	1	0	1	(Reserved)	—	—	—
14	1	1	1	0	Fast PWM	ICR1	BOTTOM	TOP
15	1	1	1	1	Fast PWM	OCR1A	BOTTOM	TOP

Example: 46Hz with 8% Duty Cycle

- Suppose the MCU runs at 1MHz
- Generate a wave as the figure (46Hz and 8% duty cycle)
- Use PWM of Timer1
- Prescaler factor $p = 1$



PC6	<input type="checkbox"/> 1	28	<input type="checkbox"/> PC5
PD0	<input type="checkbox"/> 2	27	<input type="checkbox"/> PC4
PD1	<input type="checkbox"/> 3	26	<input type="checkbox"/> PC3
PD2	<input type="checkbox"/> 4	25	<input type="checkbox"/> PC2
PD3	<input type="checkbox"/> 5	24	<input type="checkbox"/> PC1
PD4	<input type="checkbox"/> 6	23	<input type="checkbox"/> PC0
VCC	<input type="checkbox"/> 7	22	<input type="checkbox"/> GND
GND	<input type="checkbox"/> 8	21	<input type="checkbox"/> AREF
PB6	<input type="checkbox"/> 9	20	<input type="checkbox"/> AVCC
PB7	<input type="checkbox"/> 10	19	<input type="checkbox"/> PB5
PD5	<input type="checkbox"/> 11	18	<input type="checkbox"/> PB4
PD6	<input type="checkbox"/> 12	17	<input type="checkbox"/> PB3
PD7	<input type="checkbox"/> 13	16	<input type="checkbox"/> PB2
PB0	<input type="checkbox"/> 14	15	<input type="checkbox"/> PB1 (OC1A/PCINT1)

Example: 46Hz with 8% Duty Cycle (Cont'd)

• Strategy:

1. Mode 14 fast PWM
2. Set frequency using **ICR1**

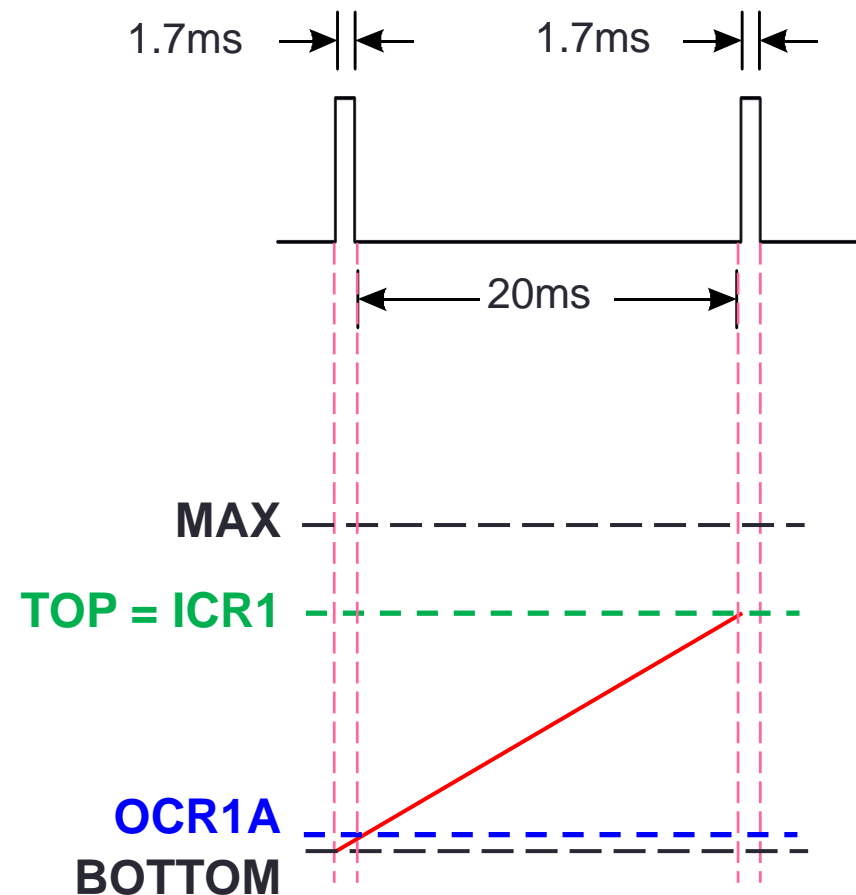
$$f = \frac{10^6}{\text{ICR1}} = 46$$

$$\Rightarrow \text{ICR1} = 21701$$

3. Set duty cycle using **OCR1A**

$$DC = \frac{1.7}{20+1.7} = \frac{\text{OCR1A}}{\text{ICR1}}$$

$$\Rightarrow \text{OCR1A} = 1700$$



OC1A Toggle Mode: TCCR0A

TCCR1A	COM1A1	COM1A0	COM1B1	COM1B0	-	-	WGM11	WGM10
TCCR1B	IC1C1	IC1S1	-	WGM13	WGM12	CS12	CS11	CS10
TCCR1C	FO1A	FO1B	-	-	-	Compare Output Mode		

Fast PWM	COM0A1	COM0A0	Comment
	1	0	Clear OC1A on compare match, Set OC1A at BOTTOM
	1	1	Set OC1A on compare match, Clear OC1A at BOTTOM
Phase Correct PWM	COM0A1	COM0A0	Comment
	1	0	Clear OC1A on compare match, Set OC1A at BOTTOM
	1	1	Set OC1A on compare match, Clear OC1A at BOTTOM

Note: the setup for OC1B is the same

46Hz with 8% Duty Cycle

	1	0	0	0	0	0	1	0
TCCR1A	COM1A1	COM1A0	COM1B1	COM1B0	-	-	WGM11	WGM10
	0	0	0	1	1	1	0	1
TCCR1B	ICNC1	ICES1	-	WGM13	WGM12	CS12	CS11	CS10

```

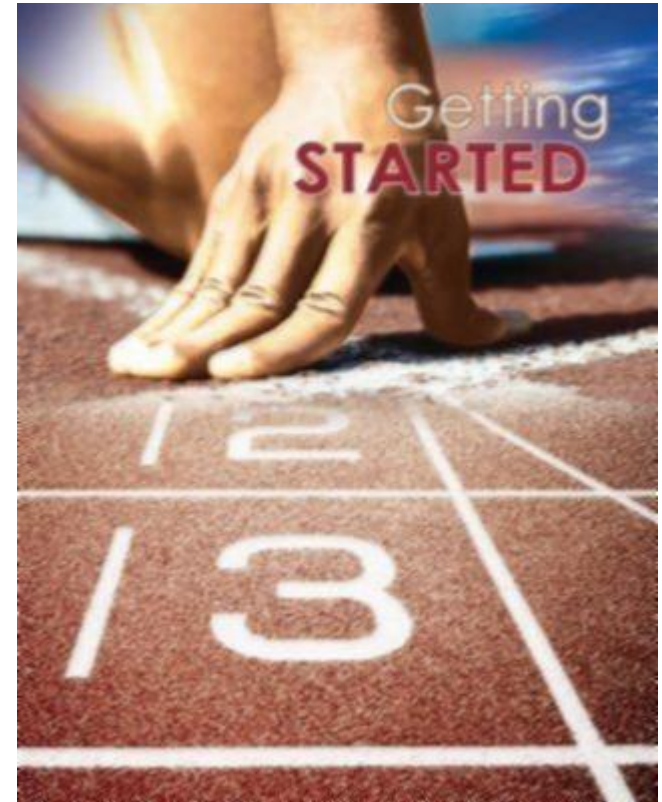
#include <avr/io.h>

int main(void)
{
    CLKPR=(1<<CLKPCE) ;
    CLKPR=0b00000011;           // set clk to 1Mhz
    DDRB=0xFF;                  // PORTB as output
    ICR1=21701;
    OCR1A=1700;
    TCCR1A=0b10000010;
    TCCR1B=0b00011001;
}

```

Outline (Cont'd)

- Pulse width modulation (PWM)
 - What is PWM?
 - AVR PWM pinout
 - PWM modes
- Getting started



Reference

- ATmega328P data sheet
- AVR 8-bit instruction set
- AVR131: Using the AVR's High-speed PWM
- M. A. Mazidi, S. Naimi, and S. Naimi, *The AVR Microcontroller and Embedded Systems: Using Assembly and C*, Prentice Hall, 2010