

Forces and Moments on Bevel Gears

Introduction

This model simulates a pair of straight conical bevel gears. The gears are modeled as rigid. A transient analysis is performed to compute the forces and moments at the center of the fixed gear. This model is built using the gears functionality in the Multibody Dynamics interface in COMSOL Multiphysics.

The data for this model is taken from Ref. 1. The results of the analysis are compared with the results given in the reference.

Model Definition

The model geometry is shown in Figure 1. It has three components: wheel, pinion, and a rigid bar. Both the wheel and pinion are modeled as bevel gears. The wheel is fixed on its location. The pinion is mounted on a rigid bar through a hinge joint. The rigid bar is hinged at a point lying on the axis of the wheel.

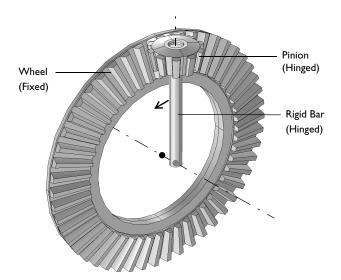


Figure 1: Model geometry. The wheel center, the hinge location of rigid bar, and the axis of both the gears are also shown.

MODEL PARAMETERS

The properties of the wheel and pinion are given in the table below:

TABLE I: GEAR PROPERTIES

PROPERTIES		WHEEL	PINION
Number of teeth	n	50	10
Pitch diameter	$d_{ m p}$	100 mm	20 mm
Pressure angle	α	20°	20°
Cone angle	γ	78.7°	11.3°
Center of rotation	\mathbf{x}_{c}	(0, 0, 0) mm	(0, -10, 50) mm
Axis of rotation	\mathbf{e}_{g}	(0, -1, 0)	(0, 0, -1)

The pinion is hinged to the rigid bar about the its own axis. The rigid bar is hinged to the ground about the wheel axis. The center of this hinge joint is (0, 10 mm, 0).

CONSTRAINTS AND LOADS

- The wheel is fixed to the ground.
- The rigid bar is given a rotation of 1 rad.
- A resisting torque of 10 N·m is applied at the joint between pinion and the rigid bar.

Results and Discussion

The comparison of the computed results with the solution presented in Ref. 1 is given in the tables below:

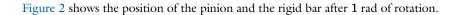
TABLE 2: CONTACT FORCE AND REACTION FORCES

	FC	FX	FY	FZ
Computed values (in N)	1064.2	600.32	356.92	802.94
Reference values (in N)	1064	600.35	356.9	802.9

TABLE 3: REACTION MOMENTS

	мх	MY	MZ
Computed values (in N·m)	-9.642	50	-15.017
Reference values (in N·m)	-9.641	50	-15.016

It can be seen that the computed values of the forces and moments are in the very close agreement with the reference values. The units and the coordinate system are different in the reference model. Hence reference results are adjusted appropriately before using them for the comparison.



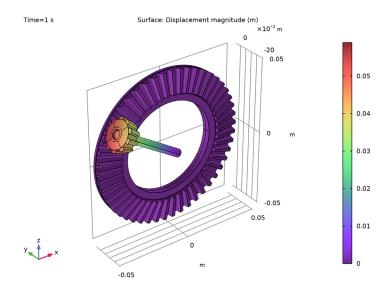


Figure 2: Displacement of the pinion and the rigid bar after 1 rad of rotation.

Figure 3 and Figure 4 show the reaction forces and moments at the wheel center. The forces and moments are plotted for various positions of the pinion.

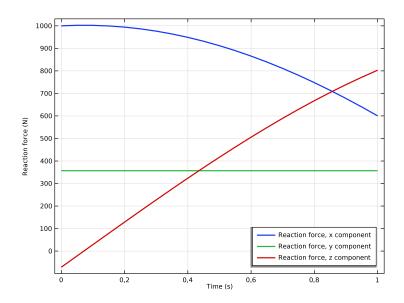


Figure 3: Reaction forces at the center of the wheel.

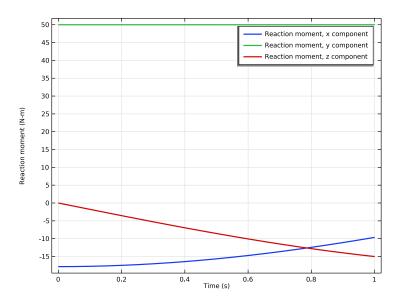


Figure 4: Reaction moments at the center of the wheel.

Notes About the COMSOL Implementation

- To build a gear geometry, you can import a gear part from the Parts Library and customize it by changing its input parameters. Alternatively, you can also create an equivalent disc or cone to represent the gear.
- All the gears are assumed rigid. The elasticity of a gear mesh can be included on **Gear** Pair nodes using the Gear Elasticity subnode.
- All the Gear Pair nodes are assumed ideal and frictionless. You can add Transmission Error, Backlash, or Friction subnodes when required.
- To constraint the motion of a gear, you can use Prescribed Displacement/Rotation or Fixed Constraint subnodes. Alternatively, you can mount the gears on a shaft or on the ground through various **loint** nodes.
- The contact force on a Gear Pair is computed using Weak constraints or Penalty method. By default, the contact force computation is turned off. Use the weak constraints method for more accurate contact forces; however, you can, preferably, switch to the penalty method for large rigid body systems.

References

1. A. Cardona, "Three-Dimensional Gears Modeling in Multibody Systems Analysis," International Journal for Numerical Methods in Engineering, vol. 40, pp. 357-381, 1997.

Application Library path: Multibody Dynamics Module/Verification Examples/ bevel gear pair

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics>Multibody Dynamics (mbd).

- 3 Click Add.
- 4 Click \Longrightarrow Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click **Done**.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file bevel_gear_pair_parameters.txt.

PART LIBRARIES

- I In the Home toolbar, click Windows and choose Part Libraries.
- 2 In the Part Libraries window, select Multibody Dynamics Module>3D>External Gears> bevel gear in the tree.
- 3 Click Add to Geometry.

GEOMETRY I

Bevel Gear I (pil)

- I In the Home toolbar, click **Build All**.
 - To customize the gear geometry, enter the gear parameters in the input parameters of the part.
- 2 In the Model Builder window, under Component I (compl)>Geometry I click Bevel Gear I (pil).
- 3 In the Settings window for Part Instance, locate the Input Parameters section.
- **4** In the table, enter the following settings:

Name	Expression	Value	Description
n	n1	50	Number of teeth
dp	dp1	0.1 m	Pitch diameter
alpha	alpha	20 °	Pressure angle
gamma	gamma1	78.7 °	Cone angle

Name	Expression	Value	Description
adr	0.75	0.75	Addendum to module ratio
tfr	0	0	Tip fillet radius to pitch diameter ratio (Set 0 for no fillet)
rfr	0	0	Root fillet radius to pitch diameter ratio (Set 0 for no fillet)
dhr	0.6	0.6	Hole diameter to pitch diameter ratio (Set 0 for no hole)
wgr	0.03	0.03	Gear width to pitch diameter ratio
Isr	0	0	Shaft length to pitch diameter ratio (Set 0 for no shaft)
xc	xcx1	0 m	Gear center, x coordinate
yc	xcy1	0 m	Gear center, y coordinate
zc	xcz1	0 m	Gear center, z coordinate
egx	ex1	0	Gear axis, x component
egy	ey1	-1	Gear axis, y component
egz	ez1	0	Gear axis, z component

Bevel Gear 2 (pi2)

- I In the **Geometry** toolbar, click Parts and choose **Bevel Gear**.
- 2 In the Settings window for Part Instance, locate the Input Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
n	n2	10	Number of teeth
dp	dp2	0.02 m	Pitch diameter
alpha	alpha	20 °	Pressure angle
gamma	gamma2	11.3 °	Cone angle
adr	0.3	0.3	Addendum to module ratio
htr	3	3	Tooth height to addendum ratio
tfr	0	0	Tip fillet radius to pitch diameter ratio (Set 0 for no fillet)
rfr	0	0	Root fillet radius to pitch diameter ratio (Set 0 for no fillet)

Name	Expression	Value	Description
wgr	0.4	0.4	Gear width to pitch diameter ratio
wbr	0.1	0.1	Back cone width to gear width ratio
wcr	0	0	Collar width to gear width ratio (Set 0 for no collar)
lsr	0	0	Shaft length to pitch diameter ratio (Set 0 for no shaft)
xc	xcx2	0 m	Gear center, x coordinate
yc	xcy2	-0.01 m	Gear center, y coordinate
zc	xcz2	0.05 m	Gear center, z coordinate
egx	ex2	0	Gear axis, x component
egy	ey2	0	Gear axis, y component
egz	ez2	-1	Gear axis, z component
th	360/(2*n2)[deg]	18 °	Mesh alignment angle

Cylinder I (cyll)

- I In the Geometry toolbar, click Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type dp2/8.
- 4 In the Height text field, type dp1/2.
- **5** Locate the **Position** section. In the **x** text field, type xcx2.
- 6 In the y text field, type xcy2.
- 7 In the z text field, type xcz2.
- 8 Locate the Axis section. From the Axis type list, choose Cartesian.
- 9 In the z text field, type -1.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Clear the Create pairs check box.
- 5 In the Geometry toolbar, click **Build All**.

MULTIBODY DYNAMICS (MBD)

Add two Bevel Gear nodes and specify all the properties of gears. For the automated creation of Bevel Gear nodes from geometry parts, use Automated Model Setup section of Multibody Dynamics node.

- I In the Model Builder window, under Component I (compl) click Multibody Dynamics (mbd).
- 2 In the Settings window for Multibody Dynamics, click Physics Node Generation in the upper-right corner of the Automated Model Setup section. From the menu, choose Create Gears.

Bevel Gear 1

- I In the Model Builder window, expand the Gears node, then click Bevel Gear I.
- 2 In the Settings window for Bevel Gear, locate the Density section.
- 3 From the p list, choose User defined.

Fixed Constraint I

- I In the Physics toolbar, click **Attributes** and choose **Fixed Constraint**.
- 2 In the Settings window for Fixed Constraint, click to expand the Reaction Force Settings section.
- 3 Select the Evaluate reaction forces check box.

Bevel Gear 2

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd)> Gears click Bevel Gear 2.
- 2 In the Settings window for Bevel Gear, locate the Density section.
- **3** From the ρ list, choose **User defined**.

Now add a **Gear Pair** node to connect the two bevel gears.

Gear Pair I

- I In the Physics toolbar, click A Global and choose Gear Pair.
- 2 In the Settings window for Gear Pair, locate the Gear Selection section.
- 3 From the Wheel list, choose Bevel Gear 1.
- 4 From the Pinion list, choose Bevel Gear 2.
- **5** Locate the **Contact Force Computation** section. From the list, choose Computed using weak constraints.

Rigid Material: Bar

- I In the Physics toolbar, click **Domains** and choose Rigid Material.
- 2 Select Domain 5 only.
- 3 In the Settings window for Rigid Material, type Rigid Material: Bar in the Label text field.
- **4** Locate the **Density** section. From the ρ list, choose **User defined**.

Hinge Joint 1

- I In the Physics toolbar, click **Global** and choose Hinge Joint.
- 2 In the Settings window for Hinge Joint, locate the Attachment Selection section.
- 3 From the Source list, choose Rigid Material: Bar.
- 4 From the Destination list, choose Bevel Gear 2.
- 5 Locate the Center of Joint section. From the list, choose Centroid of selected entities.
- **6** From the **Entity level** list, choose **Point**.

Center of Joint: Point 1

- I In the Model Builder window, click Center of Joint: Point 1.
- 2 In the Settings window for Center of Joint: Point, locate the Point Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 648, 650 in the Selection text field.
- 5 Click OK.

Hinge Joint 1

- I In the Model Builder window, click Hinge Joint 1.
- 2 In the Settings window for Hinge Joint, locate the Axis of Joint section.
- **3** Specify the \mathbf{e}_0 vector as

0 x 0 y 1 z

Apply an external torque on this joint.

Applied Force and Moment I

- I In the Physics toolbar, click 🕞 Attributes and choose Applied Force and Moment.
- 2 In the Settings window for Applied Force and Moment, locate the Applied On section.
- **3** From the list, choose **Joint**.

4 Locate the Applied Force and Moment section. In the M text field, type M_b.

Hinge Joint 2

- I In the Physics toolbar, click A Global and choose Hinge Joint.
- 2 In the Settings window for Hinge Joint, locate the Attachment Selection section.
- 3 From the Source list, choose Fixed.
- 4 From the Destination list, choose Rigid Material: Bar.
- 5 Locate the Center of Joint section. From the Entity level list, choose Point.

Center of Joint: Point 1

- I In the Model Builder window, click Center of Joint: Point I.
- 2 In the Settings window for Center of Joint: Point, locate the Point Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 647, 649 in the Selection text field.
- 5 Click OK.

Hinge Joint 2

- I In the Model Builder window, click Hinge Joint 2.
- 2 In the Settings window for Hinge Joint, locate the Axis of Joint section.
- **3** Specify the \mathbf{e}_0 vector as

0	x
1	у
0	z

Prescribed Motion I

- I In the Physics toolbar, click 💂 Attributes and choose Prescribed Motion.
- 2 In the Settings window for Prescribed Motion, locate the Prescribed Rotational Motion section.
- 3 In the θ_p text field, type -th_b*t[1/s].

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Fine**.

STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0,0.05,1).
- 4 In the Home toolbar, click **Compute**.

RESULTS

Displacement (mbd)

- I In the **Displacement (mbd)** toolbar, click **Plot**.
- 2 Click the Zoom Extents button in the Graphics toolbar.

Evaluate the contact force, reaction force, and the reaction moment at the center of the fixed bevel gear.

Global Evaluation 1

- I In the Results toolbar, click (8.5) Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- **3** From the **Time selection** list, choose **Last**.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Gear pairs>Gear Pair I> mbd.grp1.Fc - Force at contact point - N.
- 5 Click **= Evaluate**.

Global Evaluation 2

- I In the Results toolbar, click (8.5) Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- 3 From the Time selection list, choose Last.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction force - N>mbd.bvgl.RFx - Reaction force, x component.
- 5 Click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction force - N>mbd.bvgI.RFy - Reaction force, y component.

- 6 Click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction force - N>mbd.bvgI.RFz - Reaction force, z component.
- 7 Click ▼ next to **= Evaluate**, then choose **New Table**.

Global Evaluation 3

- I In the Results toolbar, click (8.5) Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- **3** From the **Time selection** list, choose **Last**.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction moment - N·m>mbd.bvgl.RMx - Reaction moment, x component.
- 5 Click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction moment - N·m>mbd.bvgl.RMy - Reaction moment, y component.
- **6** Click **Add Expression** in the upper-right corner of the **Expressions** section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction moment - N·m>mbd.bvgl.RMz - Reaction moment, z component.
- 7 Click ▼ next to **= Evaluate**, then choose **New Table**.

Use the following instructions to plot the time variation of reaction forces and reaction moments as shown in Figure 3 and Figure 4 respectively.

Reaction forces

- I In the Results toolbar, click \(\subseteq ID Plot Group. \)
- 2 In the Settings window for ID Plot Group, type Reaction forces in the Label text field.

Global I

- I Right-click Reaction forces and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Bevel gears>Bevel Gear I>Reaction force - N>mbd.bvgI.RFx -Reaction force, x component.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction force - N>mbd.bvgl.RFy - Reaction force, y component.

- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction force N>mbd.bvgl.RFz Reaction force, z component.
- 5 Click to expand the Coloring and Style section. From the Width list, choose 2.

Reaction forces

- I In the Model Builder window, click Reaction forces.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- **3** From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section.
- **5** Select the **y-axis label** check box. In the associated text field, type Reaction force (N).
- 6 Locate the Legend section. From the Position list, choose Lower right.
- 7 In the Reaction forces toolbar, click **Plot**.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Reaction moments

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Reaction moments in the Label text field.

Global I

- I Right-click Reaction moments and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Bevel gears>Bevel Gear I>Reaction moment N·m>mbd.bvgl.RMx Reaction moment, x component.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction moment N·m>mbd.bvgl.RMy Reaction moment, y component.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Bevel gears>Bevel Gear I> Reaction moment N·m>mbd.bvgl.RMz Reaction moment, z component.
- **5** Locate the Coloring and Style section. From the Width list, choose **2**.

Reaction moments

- I In the Model Builder window, click Reaction moments.
- 2 In the Settings window for ID Plot Group, locate the Title section.

- **3** From the **Title type** list, choose **None**.
- 4 Locate the **Plot Settings** section.
- 5 Select the y-axis label check box. In the associated text field, type Reaction moment
- **6** In the **Reaction moments** toolbar, click **Plot**.
- 7 Click the Zoom Extents button in the Graphics toolbar.

Modify the default velocity plot to show the gears and use it to create an animation.

Gears

- I In the Model Builder window, expand the Results>Velocity (mbd) node, then click Velocity (mbd).
- 2 In the Settings window for 3D Plot Group, type Gears in the Label text field.

Arrow Line

- I In the Model Builder window, under Results>Gears right-click Arrow Line and choose Delete.
- 2 Click Yes to confirm.

Volume

- I In the Model Builder window, under Results>Gears click Volume.
- 2 In the Settings window for Volume, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Aurora Aurora Australis in the tree.
- 5 Click OK.

Volume

- I In the Model Builder window, click Volume.
- 2 In the Gears toolbar, click Plot.

Animation I

- I In the Results toolbar, click Animation and choose Player.
- 2 In the Settings window for Animation, locate the Scene section.
- **3** From the **Subject** list, choose **Gears**.