

## **Midterm Project**

### **Calculation And Simulation Of A Golf Ball's Trajectory**

1. A golf ball moves according to the parametric functions

$$x = 32t$$

$$y = 42t - 4.9t^2$$

where horizontal distance  $x$  and altitude  $y$  are in meters, and time  $t$  in seconds, and where air resistance to the movement is not taken into account.

- a) Determine the initial velocity (both magnitude and direction) of the ball. (5%)
- b) Calculate both the maximum altitude  $y_{\max}$  and maximum horizontal distance  $x_{\max}$  that the ball can reach, and the time for the ball to reach  $x_{\max}$ . (10%)

2. If air resistance is taken into account to some extent for the horizontal movement but ignored for the vertical movement, as is reflected in the following parametric functions

$$x = 32t - 0.1t^2$$

$$y = 42t - 4.9t^2$$

- a) Determine the maximum altitude  $y_{\max}$  and maximum horizontal distance  $x_{\max}$  that the ball can reach. (5%)

- b) Calculate both the velocity and acceleration (both magnitude and direction) of the ball at the moment hitting ground (assuming level terrain). (5%)

3. Demonstration — Write a program using a language of your choice to simulate the ball's trajectory in both conditions: when air resistance is considered and when is not. (50%)

4. Demonstration — At the time of demonstration you will be provided with another set of parametric functions. You will run the same program to demonstrate the trajectory of the movement. (25%)

### **Note**

- a) Solutions to Q1 and Q2, which include necessary calculation processes, are required to be submitted as paper work. The paper work is due Oct. 18.
- b) Demonstration to be carried out on Oct. 18. Code submittal not required.