

WSKmaths — Useful mathematical definitions.

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This version 22nd March 2019

This package ensures that a number of useful mathematics packages are loaded, provides a number of useful theorem-like environments, and defines a number of significant mathematics macros. The concluding section offers a few general remarks about writing in L^AT_EX.

1 Packages

The mathematics packages loaded by this package are

- `amsmath`,
- `amsfonts`,
- `amsthm`,
- `framed`,
- `caption`,
- `xspace`.

It is worth looking at the documentation for `amsmath` (<ftp://ftp.ams.org/pub/tex/doc/amsmath/amslldoc.pdf>) and `amsthm` (<ftp://ftp.ams.org/pub/tex/doc/amscs/amsthdoc.pdf>); depending on your writing style, some constructions in these might save much time and effort.

2 Theorem-like environments

The package defines theorem-like environments as follows, all numbered consecutively as a whole:

- in theorem-style:
 - `thm` (theorems),
 - `prop` (propositions),
 - `lem` (lemmas),
 - `cor` (corollaries),
 - `exercise` (exercises);
- in separate styles:
 - `defn` (definitions, in definition style),
 - `rem` (remarks, in remark style).
 - `qn` (questions, in remark style).

Proofs should be enclosed in a `\begin{proof} ... \end{proof}` environment.

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3 Mathematical macros

It is convenient to replace commonly used mathematical constructions by L^AT_EX macros. This makes it easier to maintain notational consistency, and also it is then easier to change notation if (for example) it becomes apparent that notation clashes. The package defines these macros:

<code>\CFTP</code>	<ul style="list-style-type: none"> The Coupling from the Past algorithm is abbreviated by <i>CFTP</i>: use <code>\CFTP</code> (text mode). This and the following two textual macros do not save much typing, but facilitate textual consistency and coherent typographical style.
<code>\Ito</code>	<ul style="list-style-type: none"> For Itô (as in the Itô differential), use <code>\Ito</code> (text mode).
<code>\MCMC</code>	<ul style="list-style-type: none"> Abbreviate Markov chain Monte Carlo by <i>MCMC</i>: use <code>\MCMC</code> (text mode).
<code>\Borel</code>	<ul style="list-style-type: none"> Denote the Borel σ-algebra by \mathfrak{B}: use <code>\Borel</code>.
<code>\Expect</code>	<ul style="list-style-type: none"> Write $\mathbb{E}[X]$ for the expectation of the random variable X: use <code>\Expect{X}</code>. The enclosing square brackets will change size to encompass the argument. (For multi-line expectations, you'll have to do this the hard way, using <code>\mathbb{E}\Big[...\Big]</code>, or variants.)
<code>\Indicator</code>	<ul style="list-style-type: none"> Write $\mathbb{I}[A]$ for the indicator of the event A: use <code>\Indicator{A}</code>. The enclosing square brackets will change size to encompass the argument. Note that Williams (1991)'s notation $\mathbb{E}[X ; A]$ (<code>\Expect{X\;;\;A}</code>) is more concise and ultimately more readable than the equivalent $\mathbb{E}[X \mathbb{I}[A]]$. For conditional expectation use <code>\Expect{X\; \;Y}</code>.
<code>\Integers</code>	<ul style="list-style-type: none"> Denote the set of integers by \mathbb{Z}: write <code>\Integers</code>.
<code>\Hess</code>	<ul style="list-style-type: none"> Denote the Hessian (covariant second derivative) of a function f in directions U and V by $\text{Hess } f(U, V)$: use <code>\Hess f(U,V)</code>.
<code>\Law</code>	<ul style="list-style-type: none"> Write $\mathcal{L}(X)$ for the law of the random variable X: use <code>\Law{X}</code>.
<code>\Leb</code>	<ul style="list-style-type: none"> Write $\text{Leb}(A)$ for the Lebesgue measure of a set A: use <code>\Leb(A)</code>.
<code>\Numbers</code>	<ul style="list-style-type: none"> Denote the set of natural numbers by \mathbb{N}: use <code>\Numbers</code>.
<code>\Prob</code>	<ul style="list-style-type: none"> Write $\mathbb{P}[A]$ for the probability of the event A: use <code>\Prob{A}</code>. The enclosing square brackets will change size to encompass the argument. (For multi-line probabilities use <code>\mathbb{P}\Big[...\Big]</code> etc.) For conditional probability use <code>\Prob{A\; \;Y}</code>.
<code>\Rationals</code>	<ul style="list-style-type: none"> Denote the set of rational numbers by \mathbb{Q}: use <code>\Rationals</code>.
<code>\Reals</code>	<ul style="list-style-type: none"> Denote the set of real numbers by \mathbb{R}: use <code>\Reals</code>.
<code>\Var</code>	<ul style="list-style-type: none"> Write $\text{Var}[X]$ the variance of the random variable X: use <code>\Var{X}</code>. The enclosing square brackets will change size to encompass the argument.
<code>\Cov</code>	<ul style="list-style-type: none"> Write $\text{Cov}[X, Y]$ the covariance of the random variables X and Y: use <code>\Cov{X,Y}</code>. The enclosing square brackets will change size to encompass the argument.
<code>\ball</code>	<ul style="list-style-type: none"> The metric ball of centre x and radius r is denoted by $\text{ball}(x, r)$: use <code>\ball{x,r}</code>. In exposition one should always be clear about whether one means the open or the closed ball!
<code>\origin</code>	<ul style="list-style-type: none"> The origin of Euclidean space is denoted by \mathbf{o}: use <code>\origin</code>.
<code>\d</code>	<ul style="list-style-type: none"> Some publishers (eg Cambridge University Press) advise that the differential notation in the integral $\int f(x) \, dx$, or derivative $\frac{d}{dx}f(x)$ should use a specially defined symbol <code>\d</code>, as in <code>\int f(x) \, \d{x}</code> or <code>\tfrac{\d}{\d{x}}f(x)</code>. Note that this overloads an original L^AT_EX definition which uses <code>\d</code> to generate a dot below a symbol. Note also the use of a thin space <code>\,</code> before <code>\text{d}</code> in the definition of <code>\d</code>. This can clarify complicated expressions.

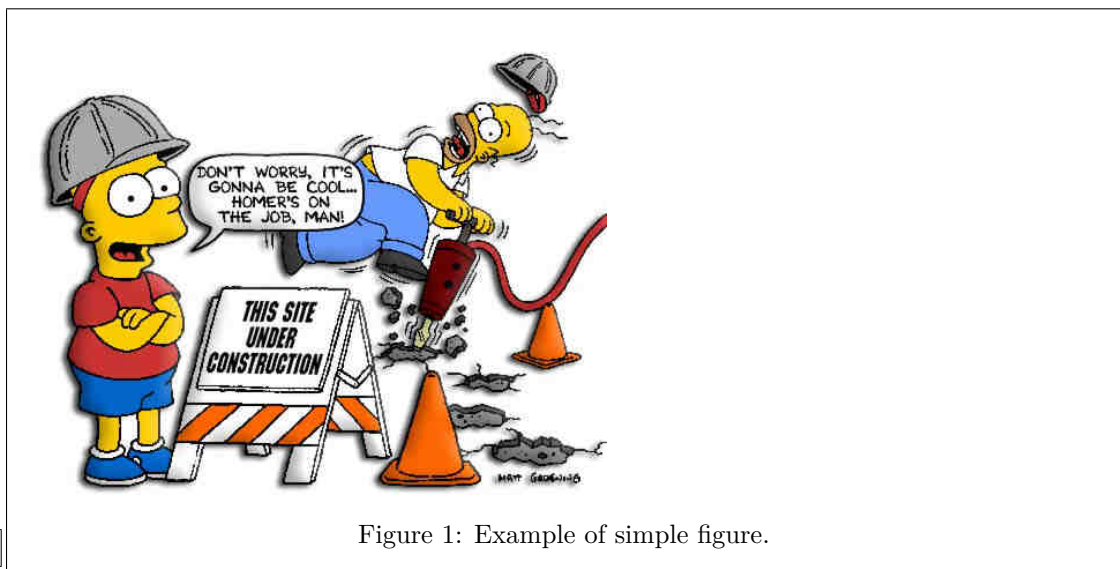


fig:homer

Figure 1: Example of simple figure.

\citet{Goos...}, (b) it is easy to copy-and-paste GoossensMittelbachSamarin-1994 from the .bib file entry (see below), (c) you can then easily and consistently identify the cited reference from the source as well as the PDF output.

The .bib file contains this entry in the following form:

```
@book{GoossensMittelbachSamarin-1994,
  author = {Goossens, Michel and Mittelbach, Frank and Samarin, Alexander},
  booktitle = {Human Factors},
  pages = {528},
  title = {{The LaTeX Companion}},
  publisher = {Addison-Wesley},
  address = {reading, Massachusetts},
  year = {1994}
}
```

I prefer to use \usepackage{natbib} with a name-date system (the default for natbib). This offers considerable flexibility, for example using \citep for a reference in parentheses (Goossens et al., 1994). See the natbib quick reference for more details: <http://merkel.zoneo.net/Latex/natbib.php>. I have modified \usepackage{showkeys} to \usepackage[notcite]{showkeys}, so as to avoid annotating citations with keys, redundant if one constructs citations as Authors-year.

It is beyond the scope of this note, but be aware that one can save huge amounts of time by using a bibliography manager such as Mendeley <http://www.mendeley.com/>. My set-up allows collection of references from the web using Zotero <https://www.zotero.org/> with a single click. These then transfer automatically to Mendeley. When dragged into a particular Mendeley group, they are stored in BIB_T_E_X form in various .bib files which can then be used directly by my various writing projects. Get this set up correctly, and you can then easily add references in final form as you are drafting the L_AT_E_X. Why might you want to do this? (a) Completing the bibliography is a tedious chore at the end of a writing project, but easily done bit-by-bit when writing; (b) A steadily increasing bibliography is a great motivator when writing!

Saving time and effort in all these ways makes mathematical writing much easier.

References

bachSamarin-1994

Michel Goossens, Frank Mittelbach, and Alexander Samarin. *The LaTeX Companion*. Addison-Wesley, reading, Massachusetts, 1994.

Williams-1991

David Williams. *Probability with martingales*. Cambridge Mathematical Textbooks. Cambridge University Press, Cambridge, 1991. ISBN 0-521-40455-X; 0-521-40605-6.

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Numbers written in *italic* refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in *roman* refer to the code lines where the entry is used.

B		G		N	
<code>\ball</code>	<i>2</i>	<code>\grad</code>	<i>3</i>	<code>\Numbers</code>	<i>2</i>
<code>\Borel</code>	<i>2</i>	H		O	
C		<code>\half</code>	<i>3</i>	<code>\origin</code>	<i>2</i>
<code>\CFTP</code>	<i>2</i>	<code>\Hess</code>	<i>2</i>	P	
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<code>\dist</code>	<i>3</i>	<code>\Ito</code>	<i>2</i>	<code>\Reals</code>	<i>2</i>
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F		M			
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