

Stacks and Queues



What is a Stack

A stack is a data structure that consists of `Nodes`. Each `Node` references the next Node in the stack, but does not reference its previous.

Common terminology for a stack is

1. *Push* – Nodes or items that are put into the stack are *pushed*
2. *Pop* – Nodes or items that are removed from the stack are *popped*. When you attempt to `pop` an empty stack an exception will be raised.
3. *Top* – This is the top of the stack.
4. *Peek* – When you `peek` you will view the value of the `top` Node in the stack. When you attempt to `peek` an empty stack an exception will be raised.
5. *IsEmpty* – returns true when stack is empty otherwise returns false.

Stacks follow these concepts:

FILO

First In Last Out

This means that the first item added in the stack will be the last item popped out of the stack.

LIFO

Last In First Out

This means that the last item added to the stack will be the first item popped out of the stack.

Stack Visualization

Here's an example of what a stack looks like. As you can see, the topmost item is denoted as the `top`. When you push something to the stack, it becomes the new `top`. When you pop something from the stack, you pop the current `top` and set the next `top` as `top.next`.



Push $O(1)$

Pushing a Node onto a stack will always be an `O(1)` operation. This is because it takes the same amount of time no matter how many Nodes (`n`) you have in the stack.

When adding a Node, you `push` it into the stack by assigning it as the new top, with its `next` property equal to the original `top`.

Let's walk through the steps:

1. First, you should have the Node that you want to add. Here is an example of a Node that we want to add to the stack.
2. Next, you need to assign the `next` property of `Node 5` to reference the same Node that `top` is referencing: `Node 4`
3. Technically at this point, your new Node is added to your stack, but there is no indication that it is the first Node in the stack. To make this happen, you have to re-assign our reference `top` to the newly added Node, `Node 5`.
4. Congratulations! You completed a successful `push` of `Node 5` onto the stack.

Here is the pseudocode to `push` a value onto a stack:

```
ALGORITHM push(value)
// INPUT <-- value to add, wrapped in Node internally
// OUTPUT <-- none
node = new Node(value)
node.next <-- Top
top <-- Node
```

Pop O(1)

Popping a Node off a stack is the action of removing a Node from the top. When conducting a `pop`, the `top` Node will be re-assigned to the Node that lives below and the `top` Node is returned to the user.

Typically, you would check `isEmpty` before conducting a `pop`. This will ensure that an exception is not raised. Alternately, you can wrap the call in a try/catch block.

Let's try and `pop` off `Node 5` from the stack. Here is a visual of the current state of our stack:

1. The first step of removing **Node 5** from the stack is to create a reference named **temp** that points to the same Node that **top** points to.
2. Once you have created the new reference type, you now need to re-assign **top** to the value that the **next** property is referencing. In our visual, we can see that the **next** property is pointing to **Node 4**. We will re-assign **top** to be **Node 4**.
3. We can now remove **Node 5** safely without it affecting the rest of the stack. Before we do that though you may want to make sure that you clear out the **next** property in your current **temp** reference. This will ensure that no further references to **Node 4** are floating around the heap. This will allow our garbage collector to cleanly and safely dispose of the Nodes correctly.
4. Finally, we return the value of the **temp** Node that was just popped off.

Here is the pseudocode for a **pop**

```
ALGORITHM pop()  
// INPUT <-- No input  
// OUTPUT <-- value of top Node in stack  
// EXCEPTION if stack is empty  
  
Node temp <-- top  
top <-- top.next  
temp.next <-- null  
return temp.value
```

Peek O(1)

When conducting a **peek**, you will only be inspecting the **top** Node of the stack.

Typically, you would check **isEmpty** before conducting a **peek**. This will ensure that an exception is not raised. Alternately, you can wrap the call in a try/catch block.

Here is the pseudocode for a **peek**

```
ALGORITHM peek()  
// INPUT <-- none  
// OUTPUT <-- value of top Node in stack  
// EXCEPTION if stack is empty
```

```
return top.value
```

We do not re-assign the `next` property when we `peek` because we want to keep the reference to the next Node in the stack. This will allow the `top` to stay the top until we decide to `pop`.

IsEmpty O(1)

Here is the pseudocode for `isEmpty`

```
ALGORITHM isEmpty()  
// INPUT <-- none  
// OUTPUT <-- boolean  
  
return top = NULL
```

What is a Queue

Common terminology for a queue is

1. *Enqueue* - Nodes or items that are added to the queue.
2. *Dequeue* - Nodes or items that are removed from the queue. If called when the queue is empty an exception will be raised.
3. *Front* - This is the front/first Node of the queue.
4. *Rear* - This is the rear/last Node of the queue.
5. *Peek* - When you `peek` you will view the value of the `front` Node in the queue. If called when the queue is empty an exception will be raised.
6. *IsEmpty* - returns true when queue is empty otherwise returns false.

Queues follow these concepts:

FIFO

First **I**n **F**irst **O**ut

This means that the first item in the queue will be the first item out of the queue.

LILO

Last **I**n **L**ast **O**ut

This means that the last item in the queue will be the last item out of the queue.

Queue Visualization

Here is what a `Queue` looks like:





Enqueue O(1)

When you add an item to a queue, you use the `enqueue` action. This is done with an `O(1)` operation in time because it does not matter how many other items live in the queue (`n`); it takes the same amount of time to perform the operation.

Let's walk through the process of adding a Node to a queue:



1. First, we should change the `next` property of `Node 4` to point to the Node we are adding. In our case with the visual below, we will be re-assigning `Node 4`'s `.next` to `Node 5`. The only way we have access to `Node 4` is through our reference `rear`. Following the rules of reference types, this means that we must change `rear.next` to `Node 5`. 
2. After we have set the `next` property, we can re-assign the `rear` reference to point to `Node 5`. By doing this, it allows us to keep a reference of where the `rear` is, and we can continue to `enqueue` Nodes into the queue as needed. 
3. Congratulations! You have just successfully added a Node to a queue by activating the `enqueue` action.

Code

Here is the pseudocode for the `enqueue` method:

```
ALGORITHM enqueue(value)
// INPUT <-- value to add to queue (will be wrapped in Node internally)
// OUTPUT <-- none
node = new Node(value)
rear.next <-- node
rear <-- node
```

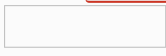
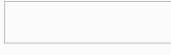

Dequeue O(1)

When you remove an item from a queue, you use the `dequeue` action. This is done

with an `O(1)` operation in time because it doesn't matter how many other items are in the queue, you are always just removing the `front` Node of the queue.

Typically, you would check `isEmpty` before conducting a `dequeue`. This will ensure that an exception is not raised. Alternately, you can wrap the call in a try/catch block.

Let's walk through the process of removing a Node from a queue.

1. The first thing you want to do is create a temporary reference type named `temp` and have it point to the same Node that `front` is pointing too. This means that `temp` will point to `Node 1`. 
2. Next, you want to re-assign `front` to the `next` value that the Node `front` is referencing. In our visual, this would be `Node 2`. 
3. Now that we have moved `front` to the second Node in line, we can next re-assign the `next` property on the `temp` Node to null. We do this because we want to make sure that all the proper Nodes clear any unnecessary references for the garbage collector to come in later and clean up. 
4. Finally, we return the value of the `temp` Node that was just removed.
5. Congratulations! You have just successfully completed a `dequeue` action on a queue!

Code

Here is the pseudocode for the `dequeue` method:

```
ALGORITHM dequeue()  
// INPUT <-- none  
// OUTPUT <-- value of the removed Node  
// EXCEPTION if queue is empty  
  
Node temp <-- front  
front <-- front.next  
temp.next <-- null  
  
return temp.value
```

Peek O(1)

When conducting a `peek`, you will only be inspecting the `front` Node of the queue.

Typically, you want to check `isEmpty` before conducting a `peek`. This will ensure

that an exception is not raised. Alternately, you can wrap the call in a try/catch block.

Code

Here is the pseudocode for a `peek`

```
ALGORITHM peek()  
// INPUT <-- none  
// OUTPUT <-- value of the front Node in Queue  
// EXCEPTION if Queue is empty  
  
return front.value
```

We do not re-assign the `next` property when we `peek` because we want to keep the reference to the next Node in the queue. This will allow the `front` to stay in the front until we decide to `dequeue`

IsEmpty O(1)

Here is the pseudocode for `isEmpty`

```
ALGORITHM isEmpty()  
// INPUT <-- none  
// OUTPUT <-- boolean  
  
return front = NULL
```