Week 14 - Dimensionality Reduction

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CarreFour Marketing - Dimensionality Reduction

Defining The Question

Specifying the Question

- 1. This section of the project entails reducing your dataset to a low dimensional dataset using the t-SNE algorithm or PCA.
- 2. You will be required to perform your analysis and provide insights gained from your analysis.

Metric of success

- Importing the data
- Cleaning the data
- performing a thorough EDA
- Performing Dimensionality Reduction

Data relevance

The data has been provided by the supermarket itself

Understanding the context

You are a Data analyst at Carrefour Kenya and are currently undertaking a project that will inform the marketing department on the most relevant marketing strategies that will result in the highest no. of sales (total price including tax). Your project has been divided into four parts where you'll explore a recent marketing dataset by performing various unsupervised learning techniques and later providing recommendations based on your insights.

Experimental design

The experimental design will involve the following steps:

- Dealing with missing values.
- Dropping variables of low variance.
- Use of decision trees to tackle missing values, outliers and identifying significant variables.
- Use of random forest to select a smaller subset of input features.
- Using the Pearson correlation matrix to identify and later drop variables with high correlation.
- Performing backward feature elimination.
- Performing factor analysis to group high correlated variables.
- Using Principal Component Analysis (PCA).

Reading The Data

```
# Importing Libraries
library (tidyr)
library(naniar)
library (ggplot2)
library (e1071)
library (corrplot)
## corrplot 0.92 loaded
library(factoextra)
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library(NbClust)
library(superml)
## Loading required package: R6
#installing packages
library(data.table)
#Loading the dataset
df <- fread("http://bit.ly/CarreFourDataset")</pre>
```

Checking The Data

```
# Preview the data head(df)
```

```
Invoice ID Branch Customer type Gender
                                                       Product line Unit price
## 1: 750-67-8428
                               Member Female
                                                  Health and beauty
                                                                         74.69
                      Α
## 2: 226-31-3081
                      С
                               Normal Female Electronic accessories
                                                                         15.28
## 3: 631-41-3108
                      Α
                               Normal
                                       Male
                                                 Home and lifestyle
                                                                         46.33
## 4: 123-19-1176
                      Α
                               Member
                                        Male
                                                  Health and beauty
                                                                         58.22
## 5: 373-73-7910
                                                  Sports and travel
                                                                         86.31
                      Α
                               Normal
                                        Male
## 6: 699-14-3026
                               Normal
                                        Male Electronic accessories
                                                                         85.39
##
     Quantity
                  Tax
                           Date Time
                                          Payment
                                                    cogs gross margin percentage
## 1:
            7 26.1415 1/5/2019 13:08
                                          Ewallet 522.83
                                                                        4.761905
## 2:
            5 3.8200 3/8/2019 10:29
                                             Cash 76.40
                                                                        4.761905
## 3:
            7 16.2155 3/3/2019 13:23 Credit card 324.31
                                                                        4.761905
## 4:
            8 23.2880 1/27/2019 20:33
                                          Ewallet 465.76
                                                                        4.761905
## 5:
            7 30.2085 2/8/2019 10:37
                                          Ewallet 604.17
                                                                        4.761905
## 6:
            7 29.8865 3/25/2019 18:30
                                          Ewallet 597.73
                                                                        4.761905
##
     gross income Rating
                            Total
## 1:
          26.1415
                     9.1 548.9715
## 2:
           3.8200
                     9.6 80.2200
```

```
## 3:
           16.2155
                      7.4 340.5255
## 4:
           23.2880
                      8.4 489.0480
                      5.3 634.3785
## 5:
           30.2085
## 6:
           29.8865
                      4.1 627.6165
# Preview the data
tail(df)
       Invoice ID Branch Customer type Gender
                                                          Product line Unit price
```

```
## 1: 652-49-6720
                                Member Female Electronic accessories
                                                                            60.95
                       С
## 2: 233-67-5758
                                                    Health and beauty
                                                                            40.35
                                Normal
                                          Male
## 3: 303-96-2227
                                                                            97.38
                       В
                                Normal Female
                                                   Home and lifestyle
## 4: 727-02-1313
                       Α
                                Member
                                          Male
                                                   Food and beverages
                                                                            31.84
## 5: 347-56-2442
                                          Male
                                                   Home and lifestyle
                                Normal
                                                                            65.82
## 6: 849-09-3807
                                Member Female
                                                  Fashion accessories
                                                                            88.34
##
      Quantity
                   Tax
                            Date Time Payment
                                                  cogs gross margin percentage
## 1:
             1 3.0475 2/18/2019 11:40 Ewallet 60.95
                                                                      4.761905
## 2:
             1 2.0175 1/29/2019 13:46 Ewallet 40.35
                                                                      4.761905
## 3:
            10 48.6900 3/2/2019 17:16 Ewallet 973.80
                                                                      4.761905
             1 1.5920 2/9/2019 13:22
## 4:
                                           Cash 31.84
                                                                      4.761905
## 5:
             1 3.2910 2/22/2019 15:33
                                           Cash 65.82
                                                                      4.761905
## 6:
             7 30.9190 2/18/2019 13:28
                                           Cash 618.38
                                                                      4.761905
##
      gross income Rating
                              Total
## 1:
            3.0475
                      5.9
                            63.9975
## 2:
            2.0175
                      6.2
                            42.3675
## 3:
           48.6900
                      4.4 1022.4900
## 4:
            1.5920
                      7.7
                            33.4320
## 5:
            3.2910
                      4.1
                            69.1110
## 6:
           30.9190
                      6.6 649.2990
```

Dimensionanity of the data dim(df)

[1] 1000 16

The dataframe has 1000 rows and 16 columns

Tidying The Dataset

```
# check the column names
colnames(df)
```

```
[1] "Invoice ID"
                                   "Branch"
##
    [3] "Customer type"
                                    "Gender"
   [5] "Product line"
##
                                    "Unit price"
   [7] "Quantity"
                                    "Tax"
  [9] "Date"
                                   "Time"
##
## [11] "Payment"
                                    "cogs"
## [13] "gross margin percentage" "gross income"
## [15] "Rating"
                                    "Total"
```

```
\# standardize column names with standard naming convention ie lowercase and replace spaces with '_ '
# replace the spaces with underscores using qsub() function
names(df) <- gsub(" ","_", names(df))</pre>
# The column names have a mixture of uppercase and lowercase charachers we should correct that and
#make all the characters lowercase.
names(df) <- tolower(names(df))</pre>
# Confirmation
colnames(df)
## [1] "invoice_id"
                                 "branch"
   [3] "customer_type"
                                 "gender"
##
## [5] "product_line"
                                 "unit_price"
## [7] "quantity"
                                 "tax"
## [9] "date"
                                 "time"
## [11] "payment"
                                 "cogs"
## [13] "gross_margin_percentage" "gross_income"
## [15] "rating"
                                 "total"
# Let us find the datatypes of the data
## Classes 'data.table' and 'data.frame': 1000 obs. of 16 variables:
                                   "750-67-8428" "226-31-3081" "631-41-3108" "123-19-1176" ...
## $ invoice_id
                           : chr
                           : chr
                                   "A" "C" "A" "A" ...
## $ branch
## $ customer_type
                        : chr "Member" "Normal" "Normal" "Member" ...
                           : chr "Female" "Female" "Male" "Male" ...
## $ gender
## $ product_line
                                   "Health and beauty" "Electronic accessories" "Home and lifestyle" "
                            : chr
                           : num 74.7 15.3 46.3 58.2 86.3 ...
## $ unit_price
                           : int 75787761023...
## $ quantity
## $ tax
                           : num 26.14 3.82 16.22 23.29 30.21 ...
## $ date
                                   "1/5/2019" "3/8/2019" "3/3/2019" "1/27/2019" ...
                            : chr
                           : chr "13:08" "10:29" "13:23" "20:33" ...
## $ time
## $ payment
                           : chr "Ewallet" "Cash" "Credit card" "Ewallet" ...
## $ cogs
                                   522.8 76.4 324.3 465.8 604.2 ...
                            : num
## $ gross_margin_percentage: num
                                   4.76 4.76 4.76 4.76 4.76 ...
## $ gross_income : num 26.14 3.82 16.22 23.29 30.21 ...
                            : num 9.1 9.6 7.4 8.4 5.3 4.1 5.8 8 7.2 5.9 ...
## $ rating
                            : num 549 80.2 340.5 489 634.4 ...
## $ total
## - attr(*, ".internal.selfref")=<externalptr>
The dataset has character, integer and numerical datatypes Time and date are in the incorrect format
# Change date to date format
df$date <- as.Date(df$date, "%m/%d/%Y")</pre>
# Change time to time format
df$time <- as.ITime(df$time)</pre>
```

head(df)

```
invoice_id branch customer_type gender
                                                          product_line unit_price
##
## 1: 750-67-8428
                       Α
                                Member Female
                                                    Health and beauty
                                                                            74.69
## 2: 226-31-3081
                       C
                                 Normal Female Electronic accessories
                                                                            15.28
## 3: 631-41-3108
                                                                            46.33
                       Α
                                 Normal
                                          Male
                                                   Home and lifestyle
## 4: 123-19-1176
                       Α
                                 Member
                                          Male
                                                    Health and beauty
                                                                            58.22
## 5: 373-73-7910
                       Α
                                 Normal
                                          Male
                                                    Sports and travel
                                                                            86.31
## 6: 699-14-3026
                       С
                                 Normal
                                          Male Electronic accessories
                                                                            85.39
##
      quantity
                   tax
                              date
                                       time
                                                payment
                                                           cogs
## 1:
             7 26.1415 2019-01-05 13:08:00
                                                Ewallet 522.83
## 2:
             5 3.8200 2019-03-08 10:29:00
                                                   Cash 76.40
## 3:
             7 16.2155 2019-03-03 13:23:00 Credit card 324.31
             8 23.2880 2019-01-27 20:33:00
                                                Ewallet 465.76
## 4:
## 5:
             7 30.2085 2019-02-08 10:37:00
                                                Ewallet 604.17
             7 29.8865 2019-03-25 18:30:00
## 6:
                                                Ewallet 597.73
##
      gross_margin_percentage gross_income rating
                                                      total
## 1:
                     4.761905
                                    26.1415
                                               9.1 548.9715
## 2:
                                               9.6 80.2200
                     4.761905
                                     3.8200
## 3:
                     4.761905
                                    16.2155
                                               7.4 340.5255
## 4:
                     4.761905
                                    23.2880
                                               8.4 489.0480
## 5:
                     4.761905
                                    30.2085
                                               5.3 634.3785
## 6:
                     4.761905
                                    29.8865
                                               4.1 627.6165
```

#Finding the total number of missing values in each column colSums(is.na(df))

```
branch
##
                  invoice_id
                                                                     customer_type
##
##
                      gender
                                           product_line
                                                                        unit_price
##
                            0
                                                       0
##
                    quantity
                                                     tax
                                                                               date
##
                            0
                                                       0
                                                                                   0
##
                         time
                                                payment
                                                                               cogs
##
                            0
                                                       0
                                                                                   0
##
   gross_margin_percentage
                                           gross_income
                                                                             rating
##
                            0
                                                       0
                                                                                   0
##
                        total
##
                            0
```

There are no missing values in the dataset

```
# Cheking for duplicates
df_dup <- df[duplicated(df),]
df_dup</pre>
```

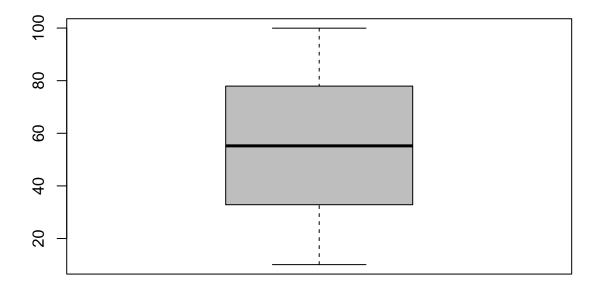
Empty data.table (0 rows and 16 cols): invoice_id,branch,customer_type,gender,product_line,unit_pric

There is no duplicate data in this dataset

Checking for outliers

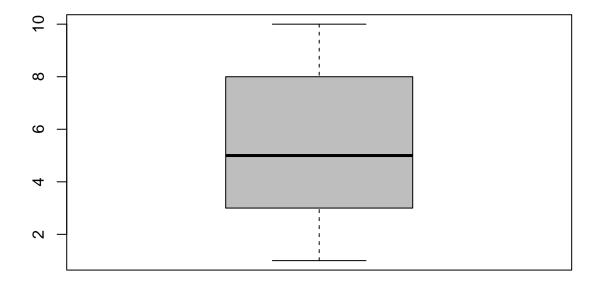
```
# Plotting boxplots to check for outliers
boxplot(df$unit_price,col='grey', main = 'Unit Price')
```

Unit Price



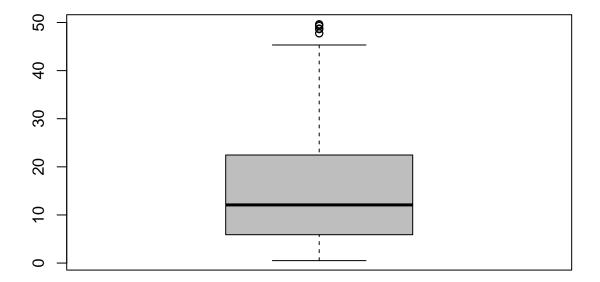
boxplot(df\$quantity,col='grey', main = 'Quantity Boxplot')

Quantity Boxplot

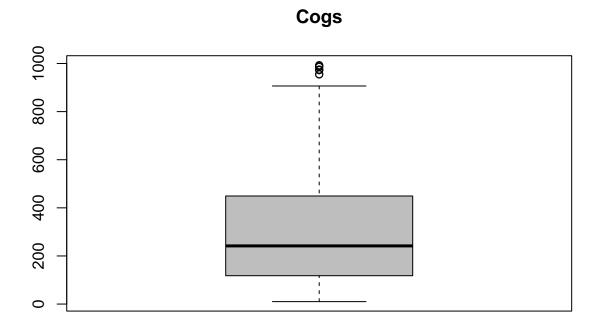


boxplot(df\$tax,col='grey', main = 'Tax')



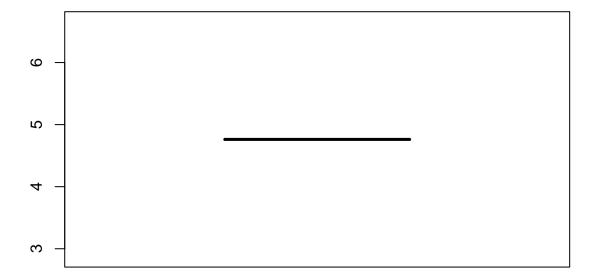


boxplot(df\$cogs,col='grey', main = 'Cogs')



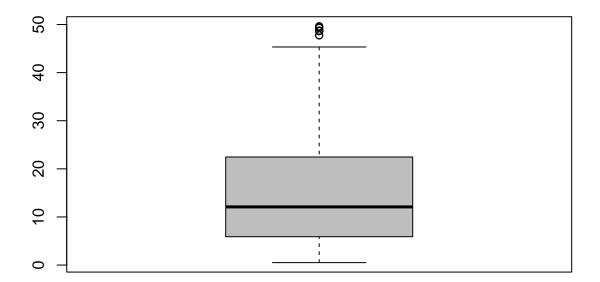
boxplot(df\$gross_margin_percentage,col='grey', main = 'Gross Margin Percentage')

Gross Margin Percentage



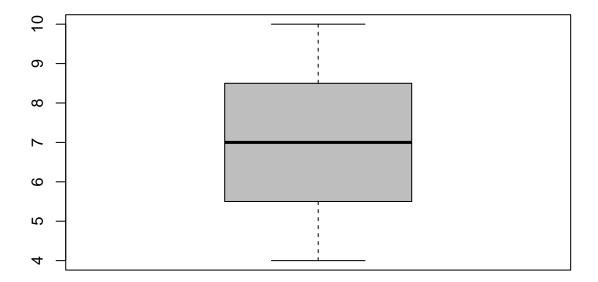
```
boxplot(df$gross_income,col='grey', main = 'Gross Income')
```

Gross Income



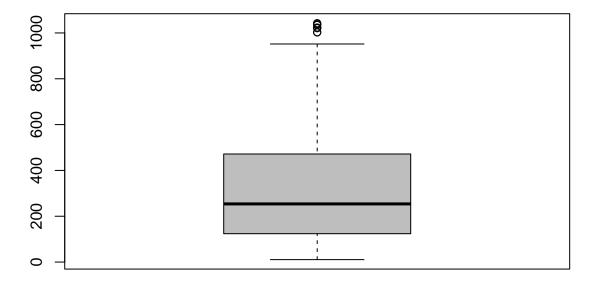
boxplot(df\$rating,col='grey', main = 'Rating')

Rating



boxplot(df\$total,col='grey', main = 'Total')

Total

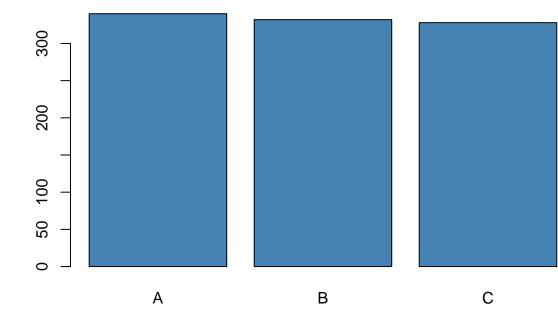


Tax, Cogs, Gross Income, Total has some outliers but we will leave them because they are actual representation of the data

Exploratory Data Analysis

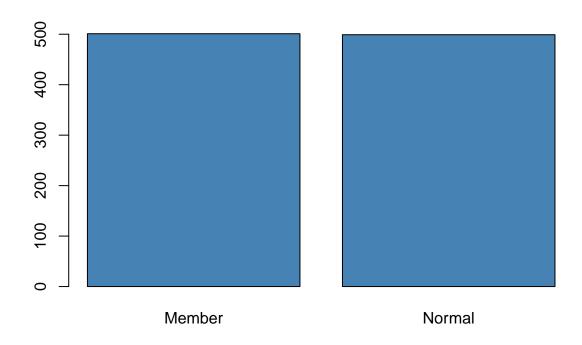
Univariate Analysis

```
# Frequency of categorical columns
#Branch , customer_type, Gender, productline , payment
branch <- table(df$branch)
barplot(branch, col = "steelblue")</pre>
```

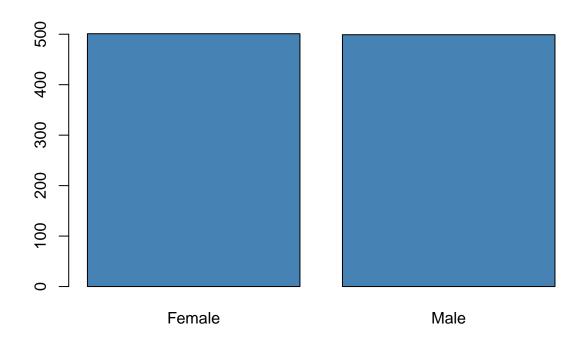


Categorical Variables

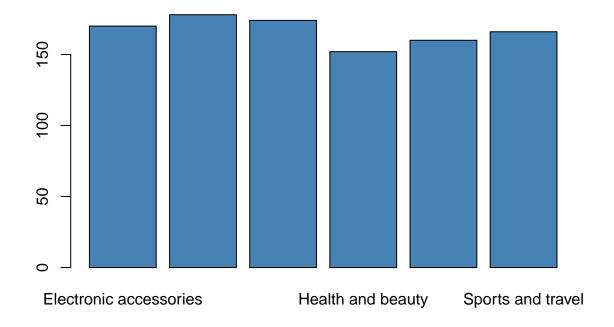
```
customer_type_freq <- table (df$customer_type)
barplot(customer_type_freq, col = "steelblue")</pre>
```



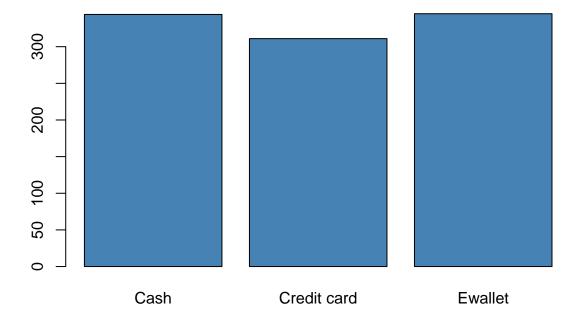
```
gender <- table(df$gender)
barplot(gender, col = "steelblue")</pre>
```



```
product_line <- table(df$product_line)
barplot(product_line, col = "steelblue")</pre>
```

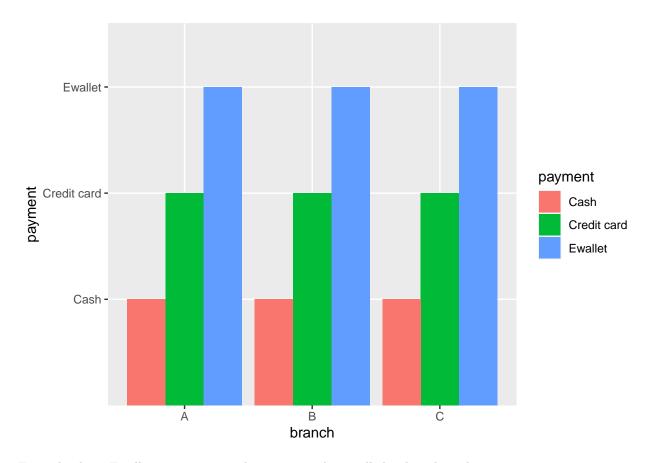


```
payment <- table(df$payment)
barplot(payment, col = "steelblue")</pre>
```



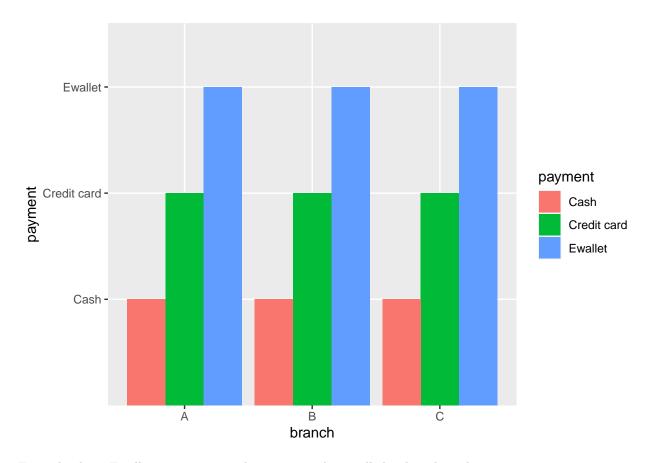
From the bar plots above we can conclude that: - The data is collected on Branches A, B and C equally. - The information collected was half from the members and half from the normal customers. - The gender was equally balances in the data. - Slightly More people paid their bills with E wallet and cash rather than Credit card

```
ggplot(df, aes(fill=payment, y= payment, x=branch)) +
   geom_bar(position="dodge", stat="identity")
```



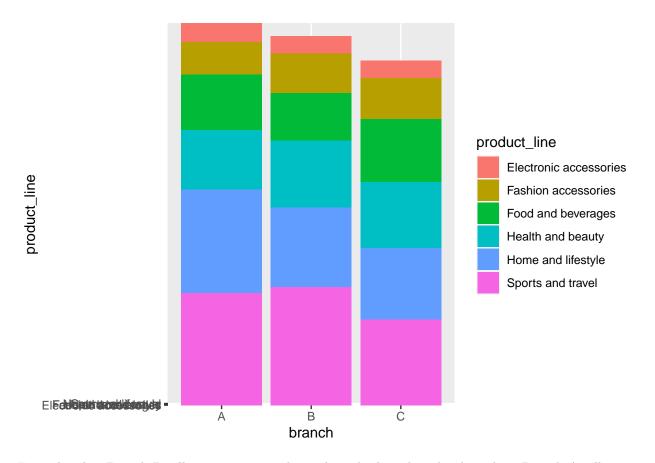
From the data, Ewallet payments are the most popular in all the three branches.

```
ggplot(df, aes(fill=payment, y= payment, x=branch)) +
   geom_bar(position="dodge", stat="identity")
```



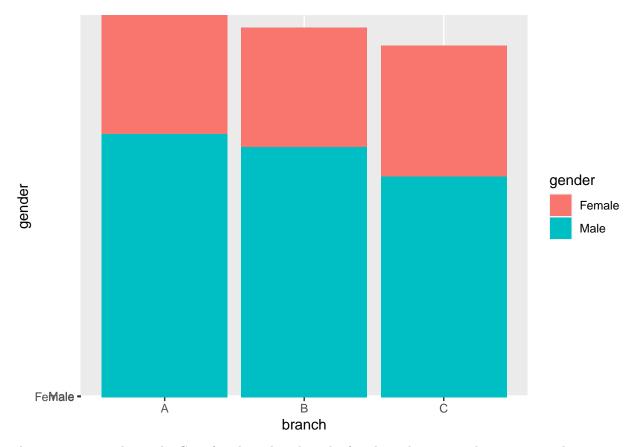
From the data, Ewallet payments are the most popular in all the three branches.

```
ggplot(df, aes(fill=product_line, y= product_line, x=branch)) +
   geom_bar(position="stack", stat="identity")
```



From the plot, Branch B sells more sports and travel goods than the other branches. Branch A sells more home and lifestyle goods than the other branches. Therefore, the marketing team should stack these branches with the product with which they sell more.

```
ggplot(df, aes(fill=gender, y= gender, x=branch)) +
    geom_bar(position="stack", stat="identity")
```



There are more males in the Carrefour branches than the females. This is not what many people assume as many people erroneously think that there are usually more females doing shopping.

Measures of central tendency for the numerical columns

```
# numerical columns.
num_col <- unlist(lapply(df, is.numeric))
df_num <- subset(df, select = num_col)
head (df_num)</pre>
```

```
##
      unit_price quantity
                                               cogs gross_margin_percentage
                               tax
                                        time
## 1:
           74.69
                         7 26.1415 13:08:00 522.83
                                                                    4.761905
## 2:
           15.28
                         5 3.8200 10:29:00 76.40
                                                                    4.761905
## 3:
           46.33
                         7 16.2155 13:23:00 324.31
                                                                    4.761905
           58.22
                         8 23.2880 20:33:00 465.76
## 4:
                                                                    4.761905
## 5:
           86.31
                         7 30.2085 10:37:00 604.17
                                                                    4.761905
## 6:
           85.39
                         7 29.8865 18:30:00 597.73
                                                                    4.761905
##
      gross_income rating
                              total
           26.1415
## 1:
                       9.1 548.9715
## 2:
            3.8200
                       9.6 80.2200
                       7.4 340.5255
## 3:
           16.2155
           23.2880
                       8.4 489.0480
## 4:
## 5:
           30.2085
                       5.3 634.3785
                       4.1 627.6165
## 6:
           29.8865
```

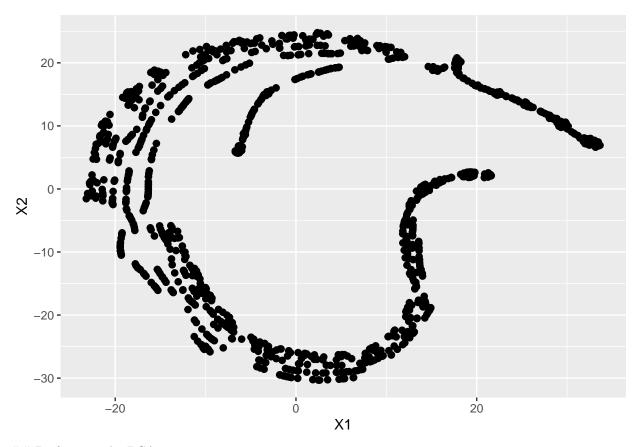
```
#Getting the measures of dispersion in the numerical columns.
summary_stats <- data.frame(</pre>
 Mean = apply(df_num, 2, mean),
 Median = apply(df_num, 2, median),
 Min = apply(df_num, 2, min),
 Max = apply(df_num, 2, max))
summary_stats
##
                                               Median
                                                                Min
                                                                              Max
                                    Mean
                                                                       99.960000
## unit_price
                               55.672130
                                            55.230000
                                                          10.080000
                                             5.000000
                                                          1.000000
                                                                       10.000000
## quantity
                               5.510000
## tax
                               15.379369
                                            12.088000
                                                           0.508500
                                                                       49.650000
## time
                           55481.880000 55140.000000 36000.000000 75540.000000
## cogs
                              307.587380 241.760000
                                                          10.170000 993.000000
## gross_margin_percentage
                               4.761905
                                             4.761905
                                                           4.761905
                                                                        4.761905
## gross_income
                               15.379369
                                            12.088000
                                                           0.508500
                                                                       49.650000
## rating
                                6.972700
                                             7.000000
                                                           4.000000
                                                                       10.000000
## total
                              322.966749
                                           253.848000
                                                          10.678500 1042.650000
# Define the function
getmode <- function(v) {</pre>
 uniqv <- unique(v)</pre>
  uniqv[which.max(tabulate(match(v, uniqv)))]
}
# Mode
mode.unit_price <- getmode(df$unit_price)</pre>
mode.unit_price
## [1] 83.77
mode.quantity <- getmode(df$quantity)</pre>
mode.quantity
## [1] 10
mode.tax <- getmode(df$tax)</pre>
mode.tax
## [1] 39.48
mode.cogs <- getmode(df$cogs)</pre>
mode.cogs
## [1] 789.6
mode.gross_income <- getmode(df$gross_income)</pre>
mode.gross_income
```

[1] 39.48

```
mode.rating <- getmode(df$rating)</pre>
mode.rating
## [1] 6
mode.total <- getmode(df$total)</pre>
mode.total
## [1] 829.08
# Label Encoder
#Branch , customer_type, Gender, productline , payment
lbl <- LabelEncoder$new()</pre>
lbl$fit(df$branch)
df$branch <- lbl$fit_transform(df$branch)</pre>
lbl$fit(df$customer type)
df$customer_type <- lbl$fit_transform(df$customer_type)</pre>
lbl$fit(df$gender)
df$gender <- lbl$fit_transform(df$gender)</pre>
lbl$fit(df$product_line)
df$product_line <- lbl$fit_transform(df$product_line)</pre>
lbl$fit(df$payment)
df$payment <- lbl$fit_transform(df$payment)</pre>
str(df)
## Classes 'data.table' and 'data.frame': 1000 obs. of 16 variables:
## $ invoice_id : chr "750-67-8428" "226-31-3081" "631-41-3108" "123-19-1176" ...
## $ branch
                           : num 0 1 0 0 0 1 0 1 0 2 ...
## $ customer_type
                          : num 0 1 1 0 1 1 0 1 0 0 ...
## $ gender
                            : num 0 0 1 1 1 1 0 0 0 0 ...
                           : num 0 1 2 0 3 1 1 2 0 4 ...
## $ product_line
## $ unit_price
                           : num 74.7 15.3 46.3 58.2 86.3 ...
## $ quantity
                           : int 75787761023...
                           : num 26.14 3.82 16.22 23.29 30.21 ...
## $ tax
                           : Date, format: "2019-01-05" "2019-03-08" ...
## $ date
## $ time
                           : 'ITime' int 13:08:00 10:29:00 13:23:00 20:33:00 10:37:00 18:30:00 14:36
## $ payment
                            : num 0 1 2 0 0 0 0 0 2 2 ...
                           : num 522.8 76.4 324.3 465.8 604.2 ...
## $ cogs
## $ gross_margin_percentage: num 4.76 4.76 4.76 4.76 4.76 ...
## $ gross_income
                     : num 26.14 3.82 16.22 23.29 30.21 ...
## $ rating
                            : num 9.1 9.6 7.4 8.4 5.3 4.1 5.8 8 7.2 5.9 ...
                            : num 549 80.2 340.5 489 634.4 ...
## $ total
## - attr(*, ".internal.selfref")=<externalptr>
# Since the gross margin percentage has only one value we can drop the column.
table(df$gross_margin_percentage)
##
## 4.761904762
##
         1000
```

```
df$gross_margin_percentage <- NULL</pre>
# Drop the categorcal columns
df$invoice_id <- NULL</pre>
df$date <- NULL
df$time <- NULL
# Separate the data
df.x <- df[ , 1:11]
df.y <- df[, 12]
head(df.x)
     branch customer_type gender product_line unit_price quantity
                                                                 tax payment
## 1: 0
                       0
                             0
                                         0
                                                74.69
                                                            7 26.1415
                                                           5 3.8200
## 2:
                       1
                             0
                                                15.28
                                                                           1
         1
                                         1
                                                46.33
                                                           7 16.2155
## 3:
        0
                       1
                             1
                                         2
                                                                           2
## 4:
                       0
                                         0
                                                58.22
                                                           8 23.2880
                                                                           0
         0
        0
## 5:
                       1
                             1
                                        3
                                                86.31
                                                           7 30.2085
                                                                           0
                                                85.39
## 6:
         1
                       1
                                                           7 29.8865
##
     cogs gross_income rating
## 1: 522.83 26.1415 9.1
                          9.6
## 2: 76.40
                3.8200
## 3: 324.31
               16.2155 7.4
## 4: 465.76
                23.2880 8.4
## 5: 604.17
                30.2085
                          5.3
## 6: 597.73
                29.8865
                          4.1
head(df.y)
##
        total
## 1: 548.9715
## 2: 80.2200
## 3: 340.5255
## 4: 489.0480
## 5: 634.3785
## 6: 627.6165
# perform tsne
library(Rtsne)
tsne = Rtsne(df.x, dims = 2, perplexity = 30)
#visualize TSNE
df.tsne = data.frame(tsne$Y)
```

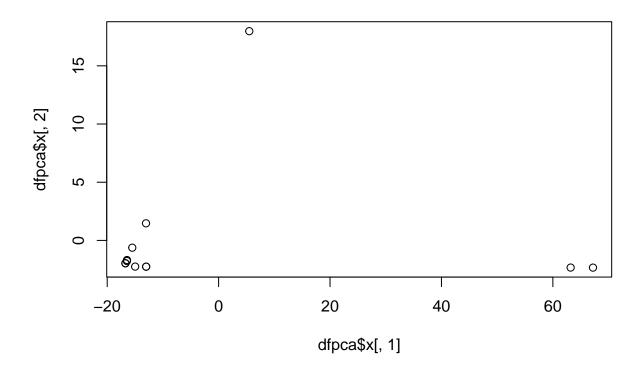
ggplot(df.tsne, aes(x=X1, y=X2)) + geom_point(size=2)



Performing the PCA

```
# Run the PCA on the df
dfpca <- prcomp(t(df),center = TRUE, scale=TRUE)
## plot pc1 and pc2
plot(dfpca$x[,1], dfpca$x[,2], main = "PCA1 & PCA2 values")</pre>
```

PCA1 & PCA2 values

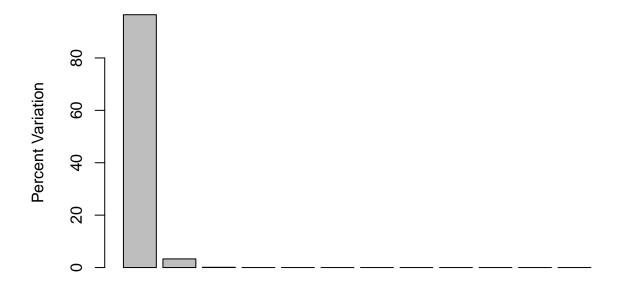


```
# Lets get a summary of the pca
summary (dfpca)
## Importance of components:
##
                              PC1
                                       PC2
                                               PC3
                                                       PC4
                                                               PC5
                                                                        PC6
                                                                                PC7
                          31.0616 5.76498 1.21319 0.50237 0.29831 0.23451 0.20497
## Standard deviation
## Proportion of Variance 0.9648 0.03323 0.00147 0.00025 0.00009 0.00005 0.00004
## Cumulative Proportion
                           0.9648 0.99806 0.99953 0.99978 0.99987 0.99993 0.99997
##
                              PC8
                                       PC9
                                                PC10
                                                          PC11
## Standard deviation
                          0.14119 0.09579 2.638e-14 1.965e-15 6.211e-17
## Proportion of Variance 0.00002 0.00001 0.000e+00 0.000e+00 0.000e+00
## Cumulative Proportion 0.99999 1.00000 1.000e+00 1.000e+00 1.000e+00
## make a scree plot
pca.var <- dfpca$sdev^2</pre>
```

barplot(pca.var.per, main="Scree Plot", xlab="Principal Component", ylab="Percent Variation")

pca.var.per <- round(pca.var/sum(pca.var)*100, 1)</pre>

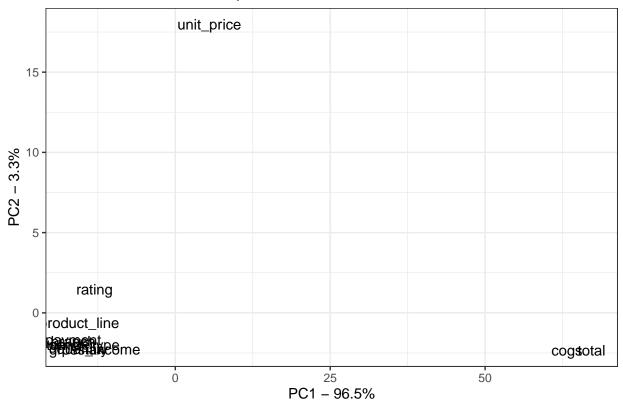
Scree Plot



Principal Component

```
## plot that shows the PCs and the variation:
pca.data <- data.frame(Sample=rownames(dfpca$x),</pre>
                       X=dfpca$x[,1],
                       Y=dfpca$x[,2])
pca.data
##
                        Sample
                                         Х
## branch
                        branch -16.460925 -1.774218
## customer_type customer_type -16.728657 -1.974943
## gender
                        gender -16.727800 -1.955175
## product_line
                  product_line -15.501089 -0.625429
## unit_price
                    unit_price
                                 5.501295 17.977265
## quantity
                      quantity -14.979897 -2.249242
## tax
                           tax -13.006234 -2.255524
## payment
                       payment -16.446861 -1.686001
## cogs
                          cogs 63.189817 -2.333115
## gross_income
                  gross_income -13.006234 -2.255524
## rating
                        rating -13.033551 1.469104
## total
                         total 67.200135 -2.337199
ggplot(data=pca.data, aes(x=X, y=Y, label=Sample)) +
  geom_text() +
  xlab(paste("PC1 - ", pca.var.per[1], "%", sep="")) +
  ylab(paste("PC2 - ", pca.var.per[2], "%", sep="")) +
  theme bw() +
  ggtitle("Customer Data PCA Graph")
```

Customer Data PCA Graph



PC1 explains 96.5% of the total variance, which means that nearly 96% of the information in the dataset (11 variables) can be encapsulated by just that one Principal Component. PC2 explains 3.3% of the variance. etc

library(ggbiplot)

- ## Loading required package: plyr
- ## Loading required package: scales
- ## Loading required package: grid

ggbiplot (prcomp(df))

