

Ten \leftrightarrow Square: A Non-Standard Universe

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What if physics was based on different rules?

What if the distance of a point to the origin wasn't given by

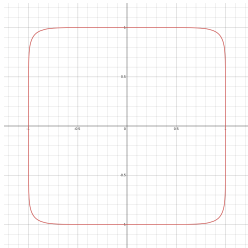
$$d = \sqrt{x^2 + y^2}$$

What if the distance of a point to the origin was given instead by

$$d = \sqrt[10]{x^{10} + y^{10}}$$

In such a universe, everything would likely behave differently. But how differently? Could one even imagine it? Could we make sense of it if we see it?

Here is what a "circle" would look like



Its area can be approximated using a Taylor series:

$$4 \int_0^1 \sqrt{1 - x^{10}} dx = 4 \left(1 - \sum_{n=1}^{\infty} \binom{1/10}{n} (-x)^{10n} \right) \approx 3.9429449613$$

In such a universe, π could be defined to be equal to that area.

However, if π is defined to be the ratio of the circumference to the diameter, we reach a contradiction. π would be equal to 3.7887. The number π doesn't have the same properties in such a universe as these two definition to not agree on the same value.

How would the universe look?

Would stars form? If so, what would they look like?

The physics

Gravity: $\mathbf{F}_g = -\frac{Gm_1m_2}{||\mathbf{r}||^2}\hat{\mathbf{r}}$

Friction: $\mathbf{F}_f = -\beta\dot{\mathbf{r}}$

(Heuristic) Collision force: $\mathbf{F}_c = \frac{Am_1m_2}{||\mathbf{r}||^3}\hat{\mathbf{r}}$

But $||(r_1, r_2)|| = (r_1^{10} + r_2^{10})^{\frac{1}{10}}!$

Positions and velocities calculated by Euler Integration.

-An invisible body at the center of the simulation keeps everything in the view area

Implementation: avoiding value explosions

Computing powers of 10 creates extremely large values which computers can't capture.

Computing tenth powers is extremely slow.

Solution: A pre-computed look up table with high-precision floats.

$$(x^{10} + y^{10})^{\frac{1}{10}} = d \quad (1)$$

$$\implies x \left[1 + \left(\frac{y}{x} \right)^{10} \right]^{\frac{1}{10}} = d \quad (2)$$

$$L(r) = (1 + r^{10})^{\frac{1}{10}} \quad (3)$$

$$a := \max(x, y) \quad b := \min(x, y) \quad (4)$$

$$|a| \cdot L\left(\left|\frac{b}{a}\right|\right) = d \quad (5)$$

Implementation: Optimizing an N-body simulation

An N-body simulation involves the computation of N^2 forces. With thousands of bodies this number gets large.

Solution: hardware acceleration using WebGPU. N^2 threads can compute forces in parallel for an $O(1)$ time complexity. A few more passes sums them to get acceleration.

The simulation

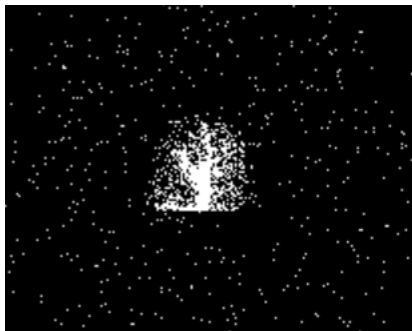


Figure: A forming star

Click here to check out the simulation!